

## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission



Intensities and Quantitative Analysis, the 3-Step Model-Valence levels

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

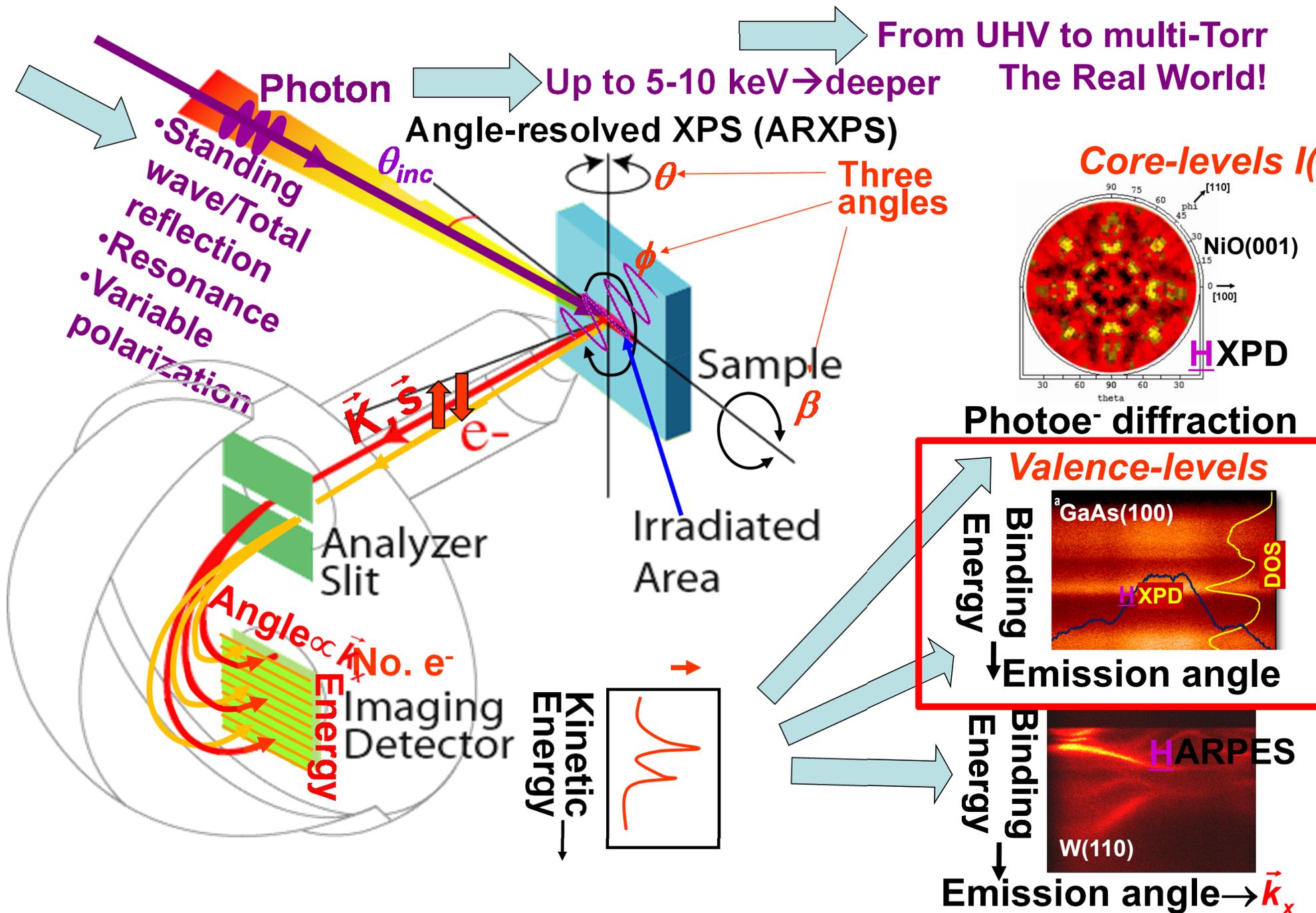
Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

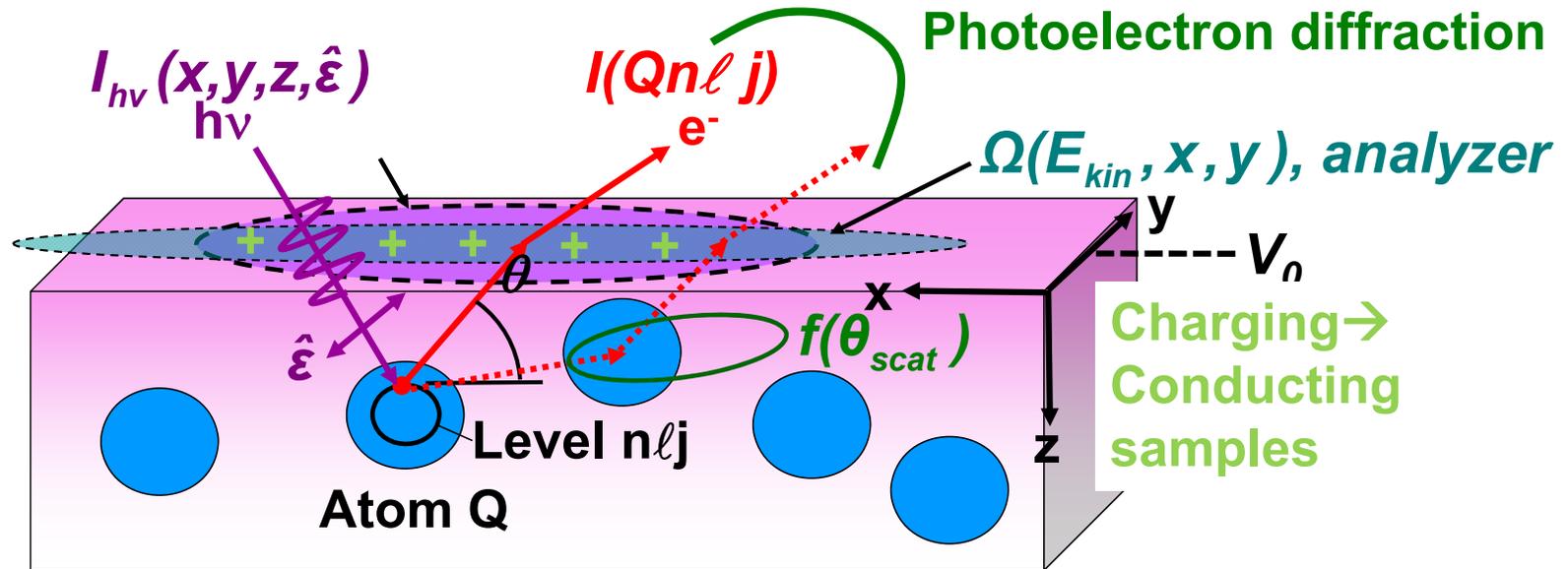
Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

# X-ray photoemission: some key elements



# ATOMIC (CORE) PHOTOELECTRON INTENSITIES: THE "FOUR-STEP" MODEL



$$I(Qn\ell j) = \int_0^\infty I_{hv}(x,y,z,\hat{\epsilon}) \rho_Q(x,y,z) \frac{d\sigma_{Qn\ell j}(h\nu, \hat{\epsilon})}{d\Omega} \exp\left[-\frac{z}{\Lambda_e(E_{kin}) \sin \theta}\right] \Omega(E_{kin}, x, y) dx dy dz$$

Non-dipole effects\* and resonant interchannel#

$I_{hv}(x,y,z,\hat{\epsilon}) =$  x-ray flux,  $\hat{\epsilon}$  = polarization

$\rho_Q(x,y,z) =$  density of atoms Q  $\rightarrow$  quantitative analysis

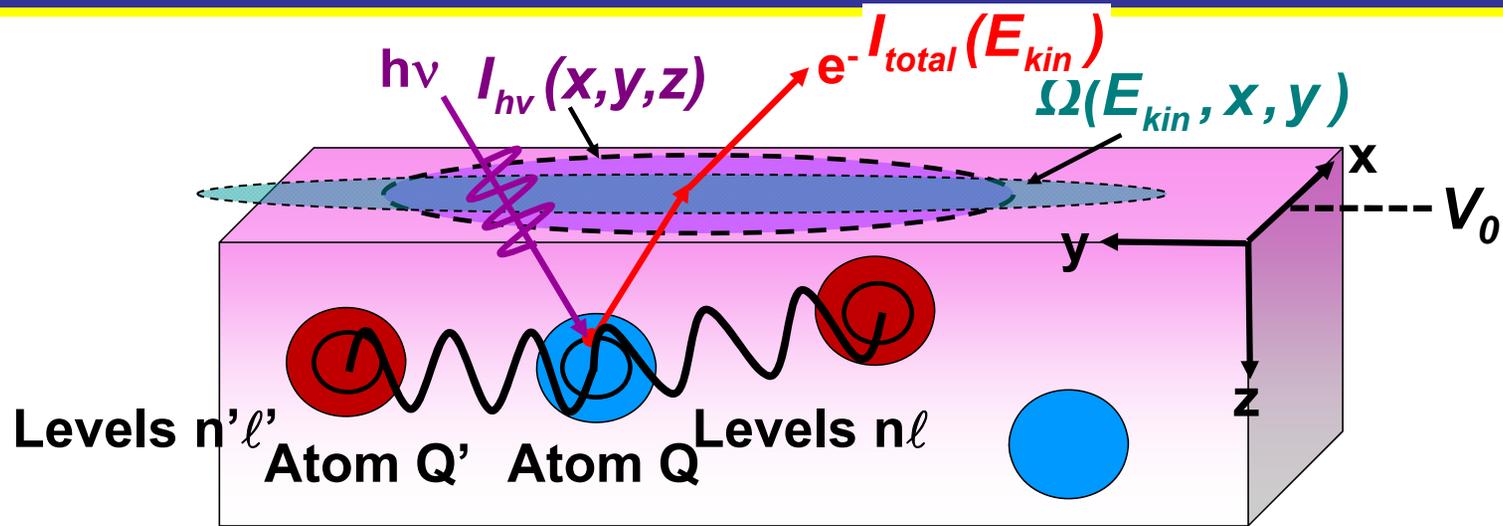
$\frac{d\sigma_{Qn\ell j}(h\nu, \hat{\epsilon})}{d\Omega} =$  energy-dependent differential photoelectric cross section for subshell  $Qn\ell j$

$\Lambda_e(E_{kin}) =$  energy-dependent inelastic attenuation length + elastic scattering:  $f(\theta_{scat})$

$\rightarrow$  Effective Attenuation Length (EAD)  $\rightarrow$  Mean Emission Depth (MED)

$\Omega(E_{kin}, x, y) =$  energy-dependent analyzer acceptance solid angle = transmission function

$V_0 =$  inner potential



For a given subshell:

$$I(E_{kin}, Qn\ell) =$$

$$C' \int_0^{\infty} I_{hv}(x, y, z) \rho_{Qn\ell}(E_b, x, y, z) \frac{d\sigma_{Qn\ell}(hv)}{d\Omega} \exp\left[-\frac{z}{\Lambda_e(E_{kin}) \sin\theta}\right] \Omega(E_{kin}, x, y) dx dy dz$$

$I_{hv}(x, y, z)$  = x-ray flux

$\rho_{Qn\ell}(E_b, x, y, z)$  = density of states, projected onto  $Qn\ell$  character

$\frac{d\sigma_{Qn\ell}(hv)}{d\Omega}$  = energy-dependent differential photoelectric cross section for subshell  $Qn\ell$

$\Lambda_e(E_{kin})$  = energy-dependent inelastic attenuation length

→ Mean Emission Depth

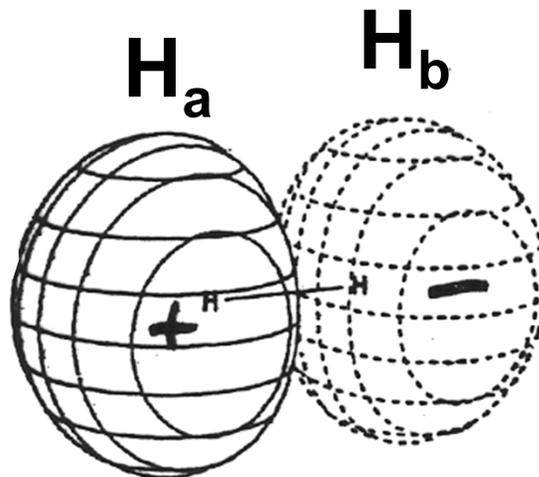
$\Omega(E_{kin}, x, y)$  = energy-dependent spectrometer acceptance solid angle

For the total VB intensity:

$$I_{total}(E_{kin}) = \sum_{Qn\ell} I(E_{kin}, Qn\ell)$$

1. Hydrogen

Symmetry:  $D_{\infty h}$

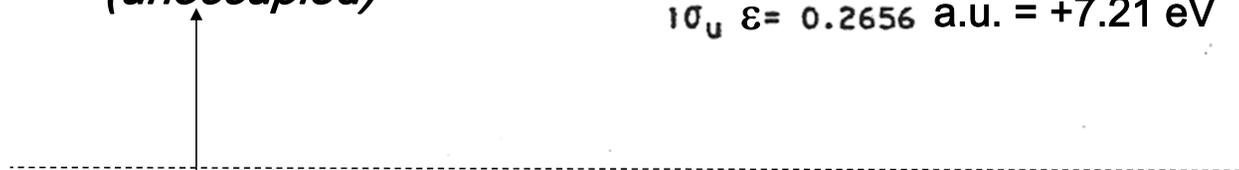


Anti-Bonding

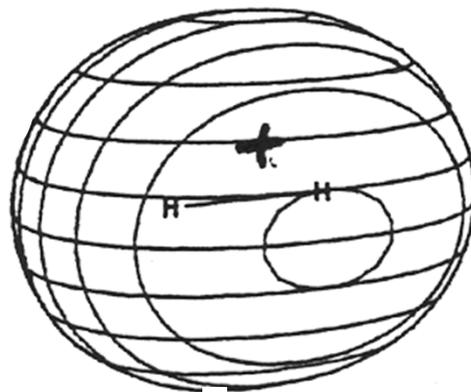
$$\varphi_{\text{anti}}^{\text{MO}} \cong \varphi_{1s_a} - \varphi_{1s_b}$$

$$1\sigma_u \quad \varepsilon = 0.2656 \text{ a.u.} = +7.21 \text{ eV}$$

$\varepsilon$  positive  
(unoccupied)



$\varepsilon$  negative  
(occupied)



Bonding

$$\varphi_{\text{bonding}}^{\text{MO}} \cong \varphi_{1s_a} + \varphi_{1s_b}$$

$$1\sigma_g \quad \varepsilon = -0.5944 \text{ a.u.} = -16.16 \text{ eV}$$

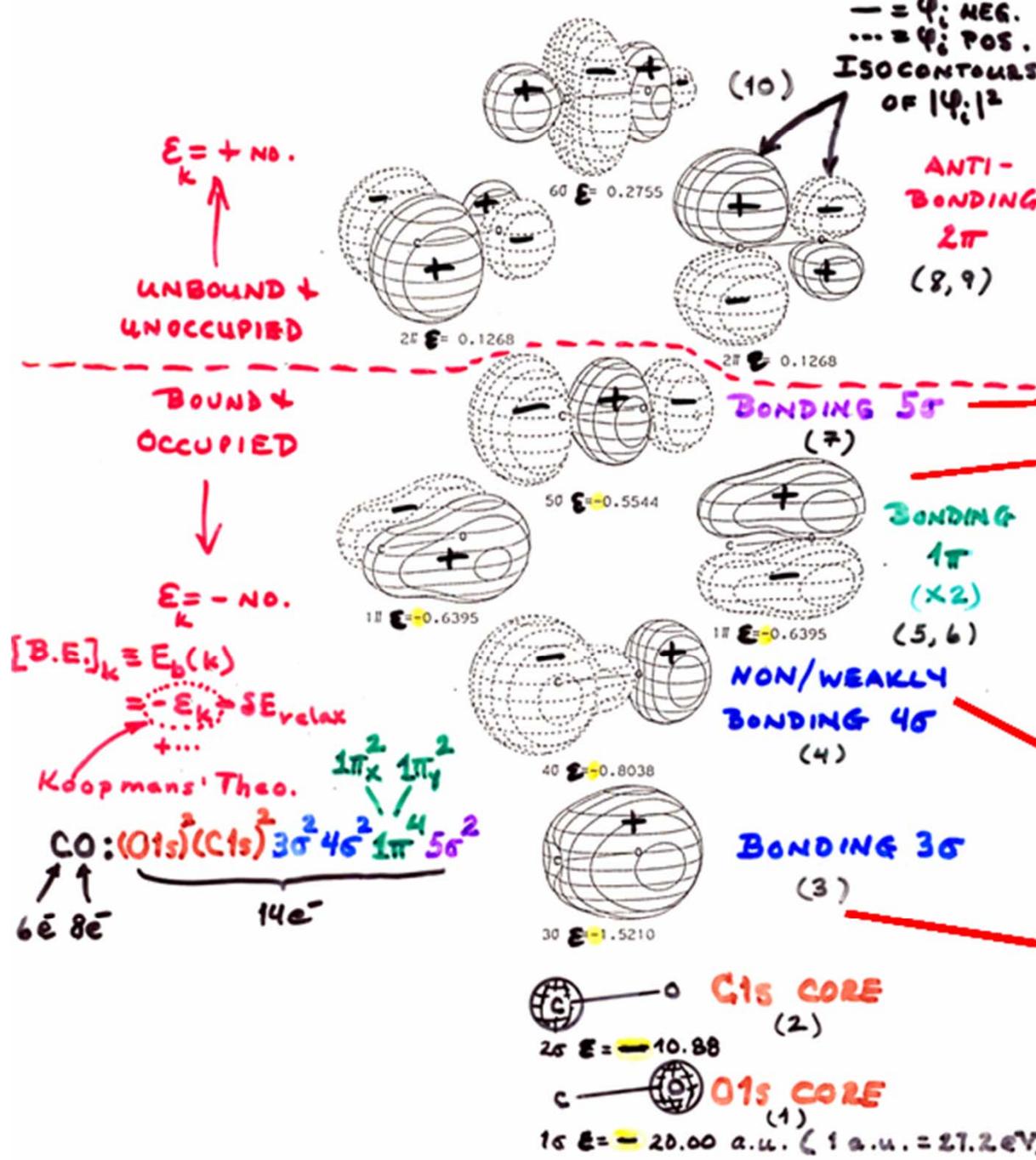
(Compare - 13.61 for H atom 1s)

# The electrons in carbon monoxide

15. Carbon Monoxide

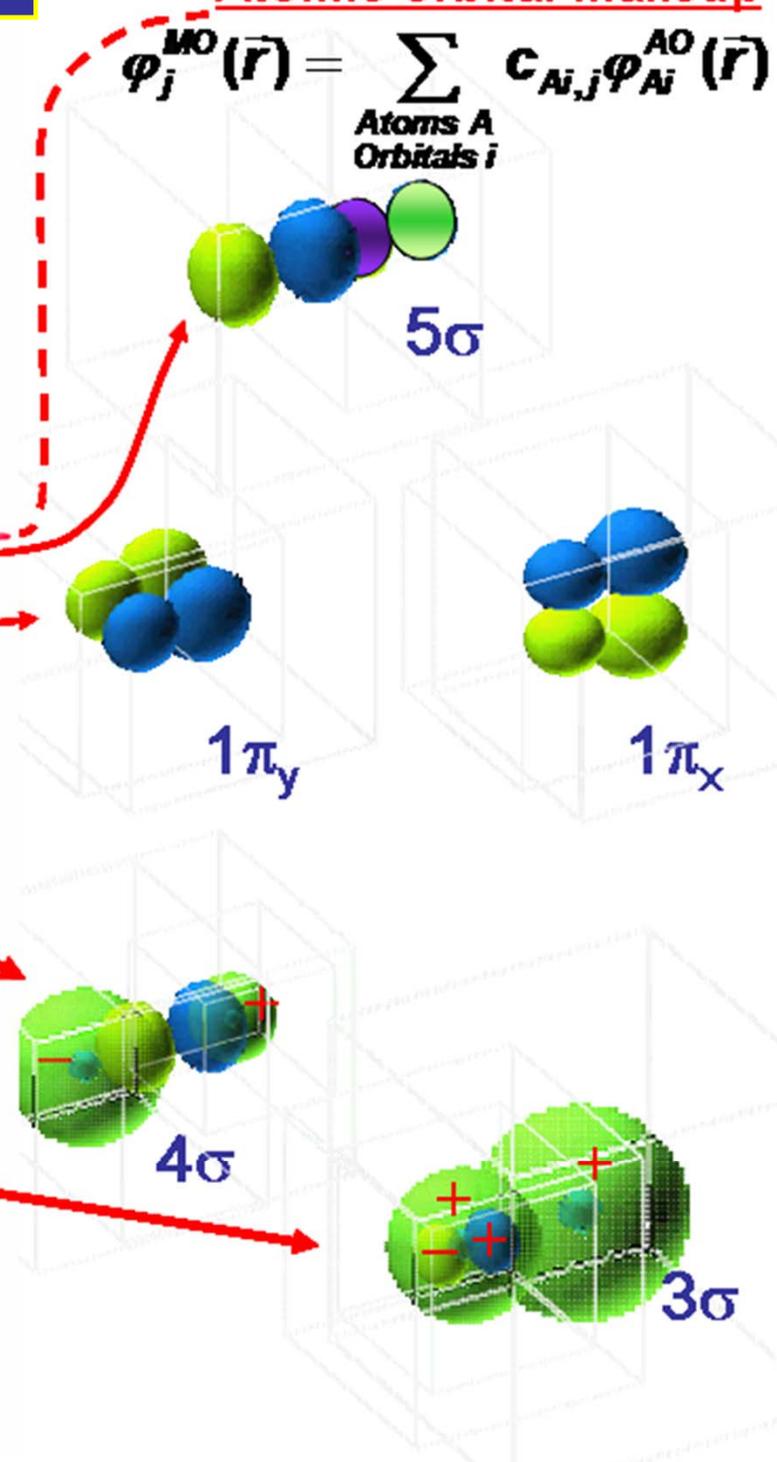
Symmetry:  $C_{\infty v}$

--- =  $\psi_i$ : NEG.  
 ... =  $\psi_i$ : POS.  
**ISOCONTOURS OF  $|\psi_i|^2$**



## Atomic orbital makeup

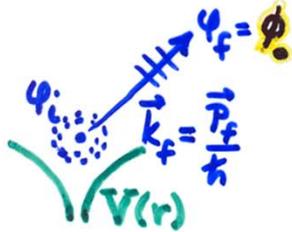
$$\psi_j^{MO}(\vec{r}) = \sum_{\text{Atoms } A} c_{Ai,j} \psi_{Ai}^{AO}(\vec{r})$$



# Photoelectron emission: basic matrix elements and selection rules

• ATOMIC-LIKE (LOCALIZED) STATES  $\Rightarrow$  CORE:

$$\psi_i(\vec{r}) = \psi_{n_i, l_i, m_i}(\vec{r}, \theta, \phi) = R_{n_i, l_i}(r) Y_{l_i, m_i}(\theta, \phi)$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f)$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f, m_f}^*(\theta_i, \phi_i) Y_{l_f, m_f}(\theta_f, \phi_f) R_{E_f, l_f}(r)$$

PHASE SHIFT OF  $l_f$  WAVE IN  $V(r)$

DIPOLE APPROX.: INT.  $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2$

EQUIVALENT WITHIN CONSTANT FACTOR



- $\Delta l = l_f - l_i = \pm 1$   
TWO CHANNELS
- $\Delta m = m_f - m_i = 0, \pm 1$   
LINEAR POLARIZ.
- $\Delta m = \pm 1$ , CIRCULAR POLARIZATION

• BLOCH-FUNCTION (DELOCALIZED) STATES  $\Rightarrow$  VALENCE:

$$\psi_i(\vec{r}) = u_{\vec{k}_i}(\vec{r}) e^{i\vec{k}_i \cdot \vec{r}}$$

$$\psi_f(\vec{r}) = u_{\vec{k}_f}(\vec{r}) e^{i\vec{k}_f \cdot \vec{r}}; E_f = \frac{p_f^2}{2m} = \frac{\hbar^2 k_f^2}{2m}$$

USUALLY NEGLIG.



$$|\langle \psi_f | \hat{E} \cdot \vec{p} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{p} | \psi_i \rangle|^2 \Rightarrow \Delta \vec{k} = \vec{k}_f - \vec{k}_i = \vec{k}_{ph} + \vec{k}_{phonon}$$

$$= \vec{g}_{BULK} \text{ (OR } \vec{g}_{SURF})$$

"DIRECT" TRANSITIONS

BUT LATTICE VIBRATIONS  $\Rightarrow$  SUM OVER  $\vec{k}_{PHONON}$   
 $\Rightarrow$  FRACTION DIRECT  $\approx$  DEBYE-WALLER FACTOR  
 $= \exp[-g^2 \bar{u}^2]$

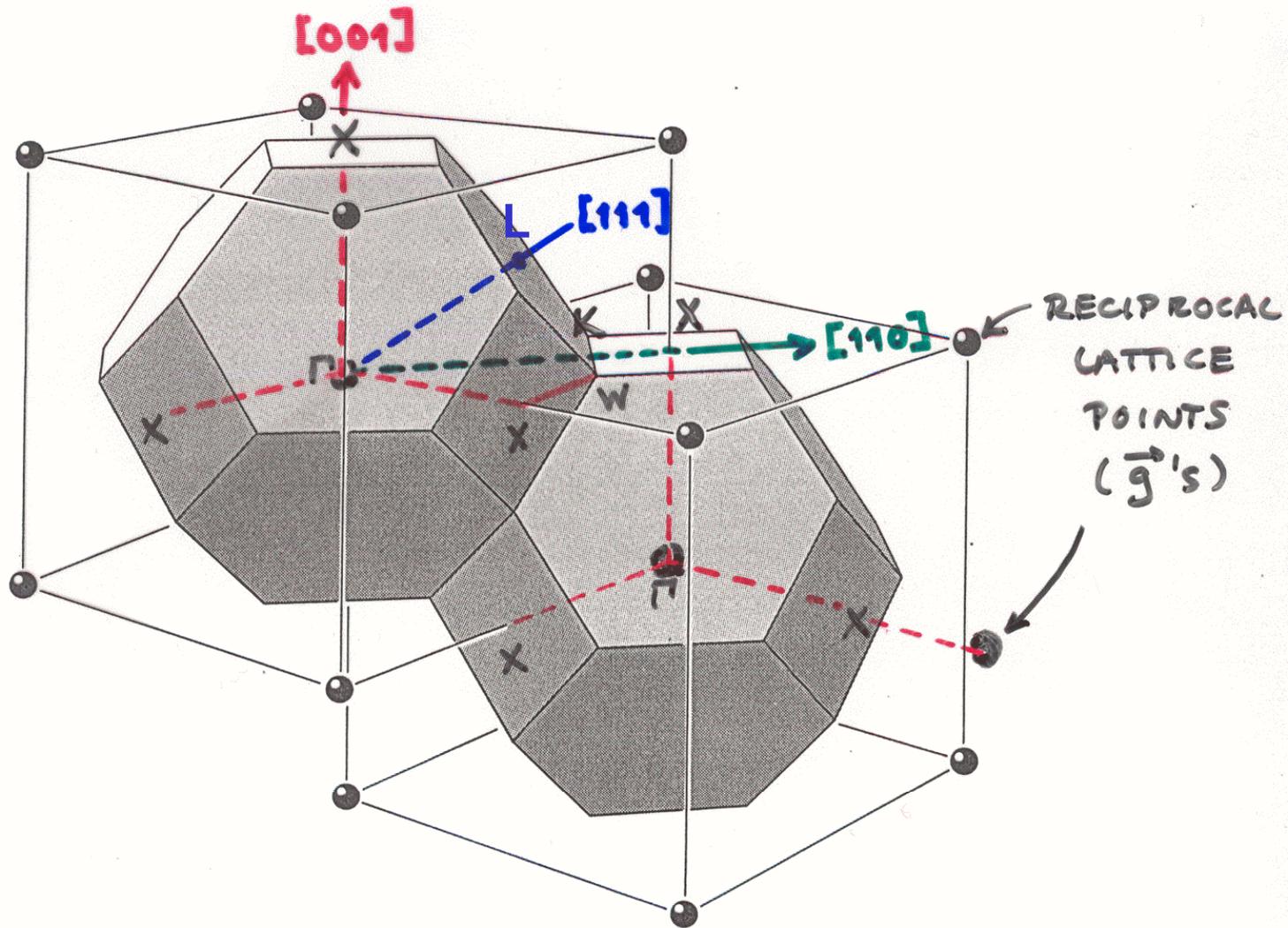


Figure 28 Brillouin zones of the face-centered cubic lattice. The cells are in reciprocal space, and the reciprocal lattice is body-centered, as drawn.

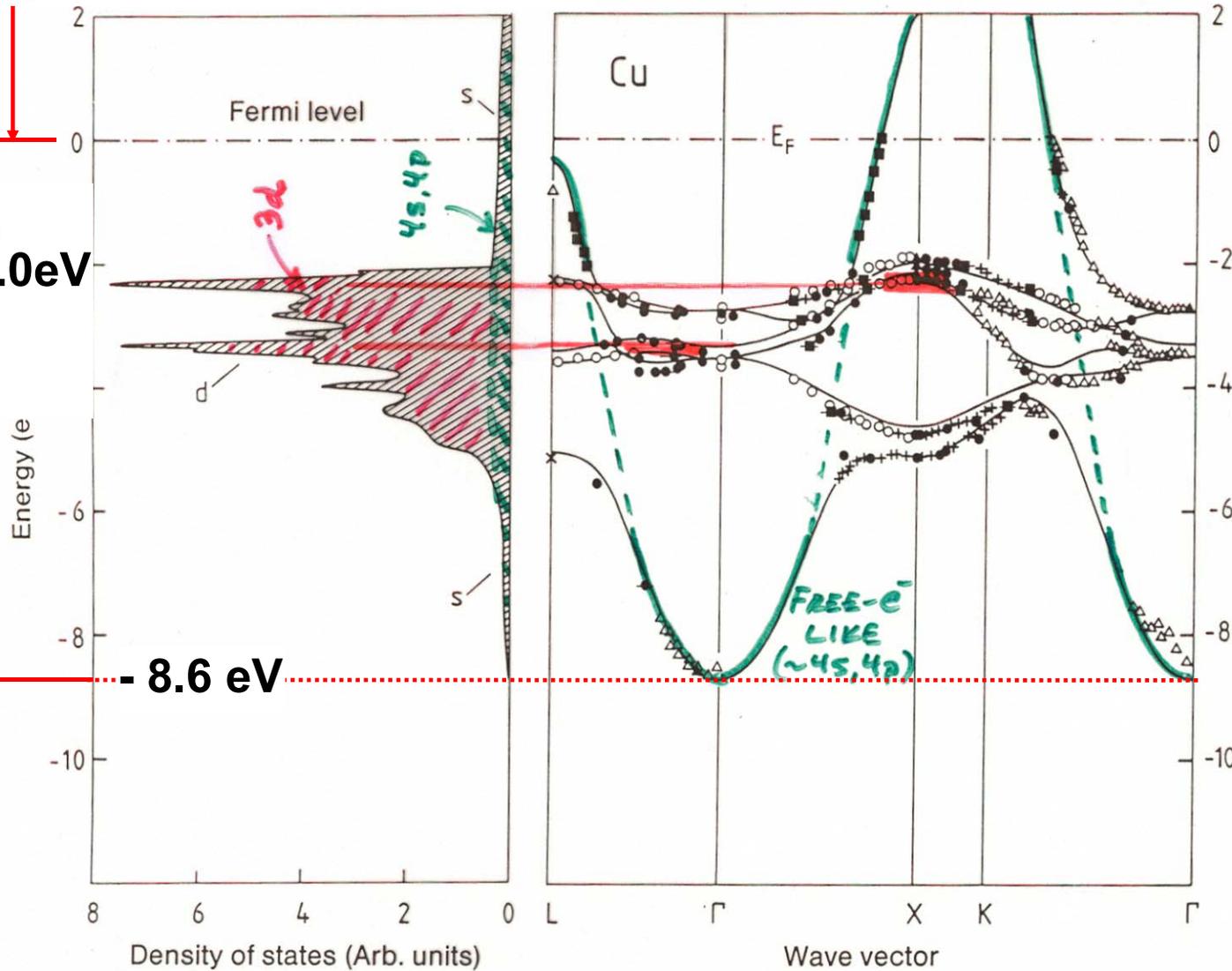
— STACKING OF fcc BRILLOUIN ZONES —

Vacuum level

# The electronic structure of a transition metal—fcc Cu

$\phi_{Cu} = 4.4 \text{ eV} = \text{work function}$

$V_{0,Cu} = 13.0 \text{ eV}$



Cu  $1s^2 \dots 3d^{10} 4s^1$   
ELECTRONIC BANDS  
+ DENSITY OF STATE!

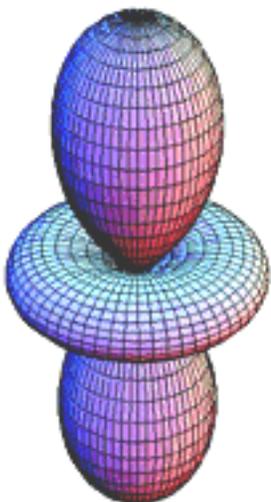
} MIXING  
} 3d LIKE  
} MIXING

Experimental points from angle-resolved photoelectron spectroscopy (more later)

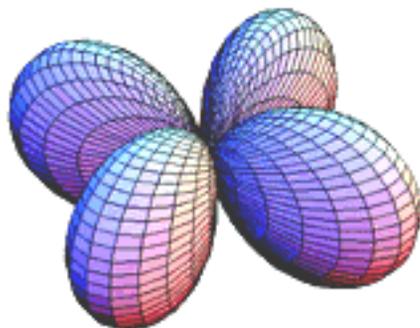
Fig. 7.12. Bandstructure  $E(k)$  for copper along directions of high crystal symmetry (right). The experimental data were measured by various authors and were presented collectively by Courths and Hüfner [7.4]. The full lines showing the calculated energy bands and the density of states (left) are from [7.5]. The experimental data agree very well, not only among themselves, but also with the calculation

And the d orbitals are not equivalent in different bonding environments:

$e_g$

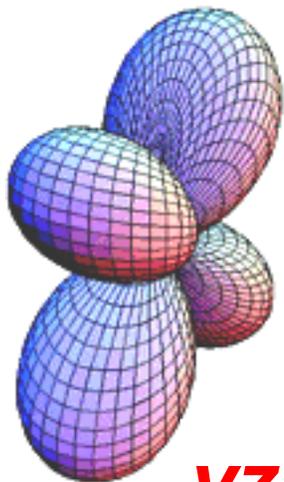


$3z^2-r^2$

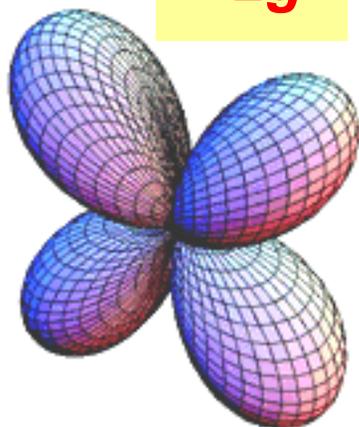


$x^2-y^2$

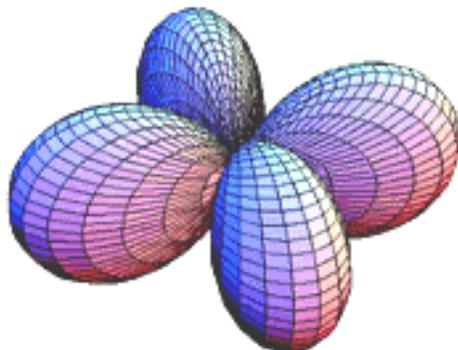
$t_{2g}$



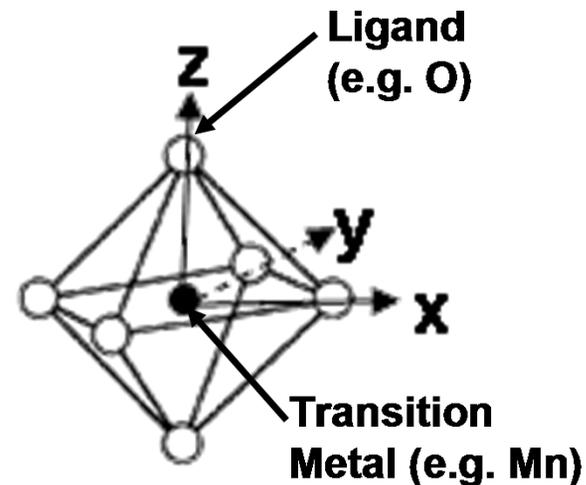
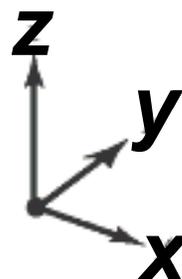
$yz$



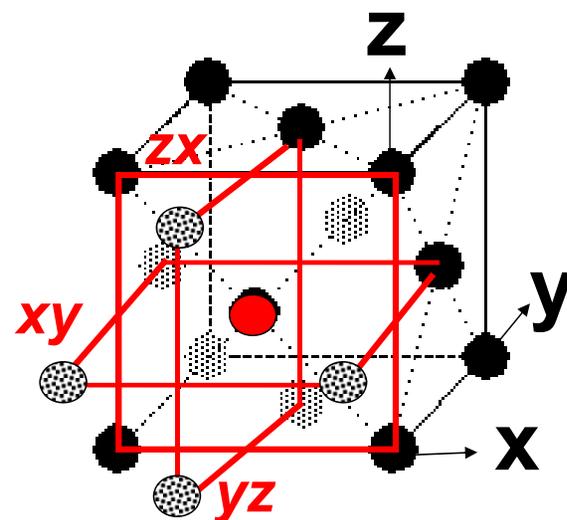
$zx$



$xy$

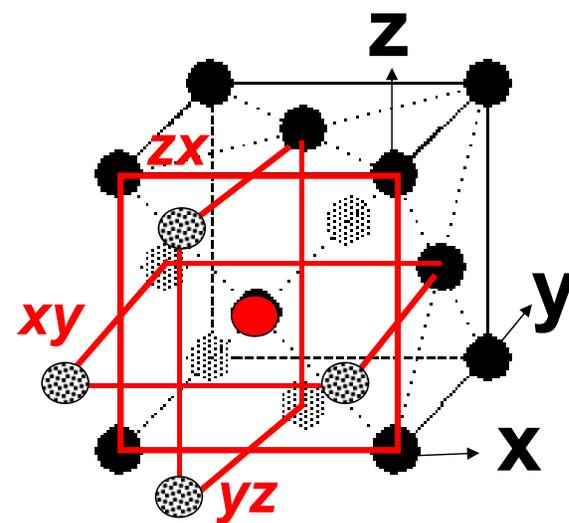
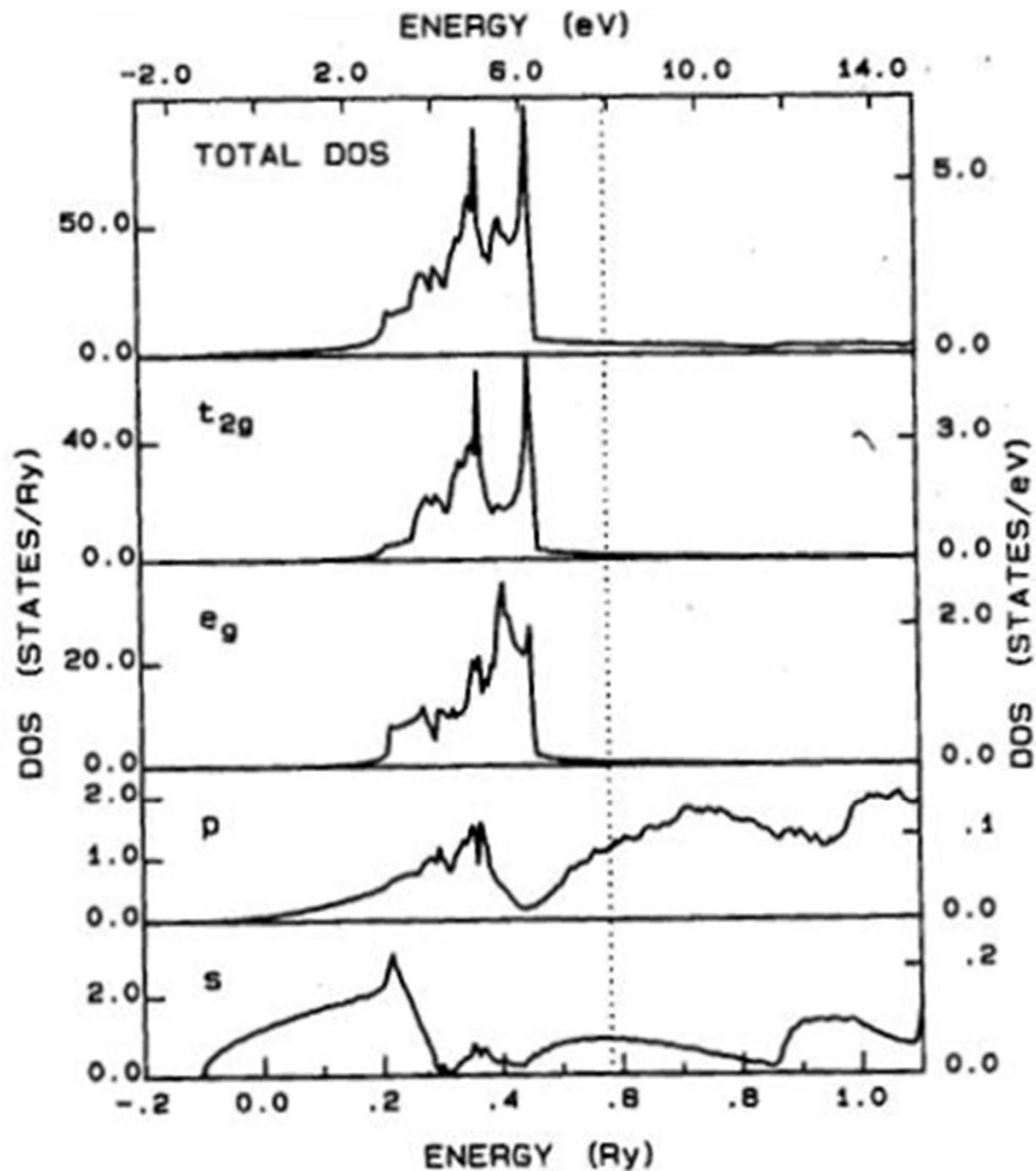


$e_g$  and  $t_{2g}$  not equivalent in octahedral (cubic) environment



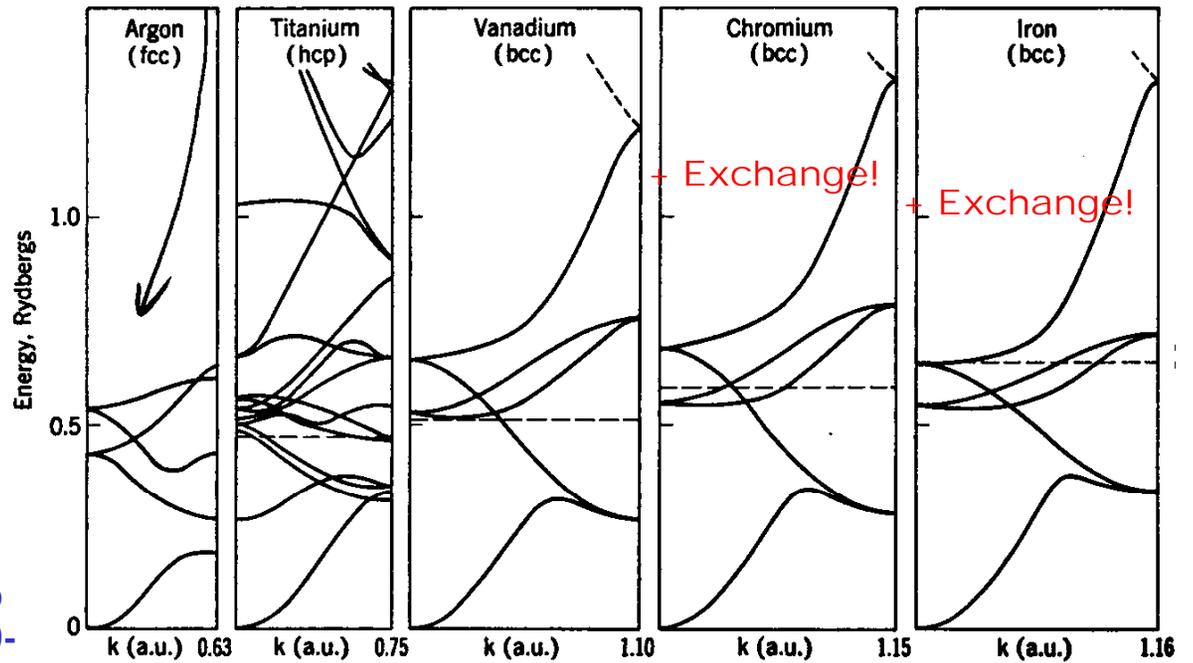
Face-centered cubic—  
12 nearest neighbors

# Copper densities of states-total and by orbital type:



The electronic structures of the 3d transition metals—  
 ≈ “rigid-band model”

3s<sup>2</sup>3p<sup>6</sup> filled + 3d,4s CB 3d<sup>2</sup>4s<sup>2</sup> 3d<sup>3</sup>4s<sup>2</sup> 3d<sup>4</sup>4s<sup>1</sup> 3d<sup>6</sup>4s<sup>2</sup>



+ Flat “core-like” Ar 3s, 3p bands at ~-1.0-1.5 Rydbergs

3d<sup>7</sup>4s<sup>2</sup> 3d<sup>8</sup>4s<sup>2</sup> 3d<sup>10</sup>4s<sup>1</sup> 3d<sup>10</sup>4s<sup>2</sup>

Ti <sup>22</sup>	V <sup>23</sup>	Cr <sup>24</sup>	Mn <sup>25</sup>	Fe <sup>26</sup>	Co <sup>27</sup>	Ni <sup>28</sup>	Cu <sup>29</sup>	Zn <sup>30</sup>
3d <sup>2</sup>	3d <sup>3</sup>	3d <sup>5</sup>	3d <sup>5</sup>	3d <sup>6</sup>	3d <sup>7</sup>	3d <sup>8</sup>	3d <sup>10</sup>	3d <sup>10</sup>
4s <sup>2</sup>	4s <sup>2</sup>	4s	4s <sup>2</sup>	4s <sup>2</sup>	4s <sup>2</sup>	4s <sup>2</sup>	4s	4s <sup>2</sup>

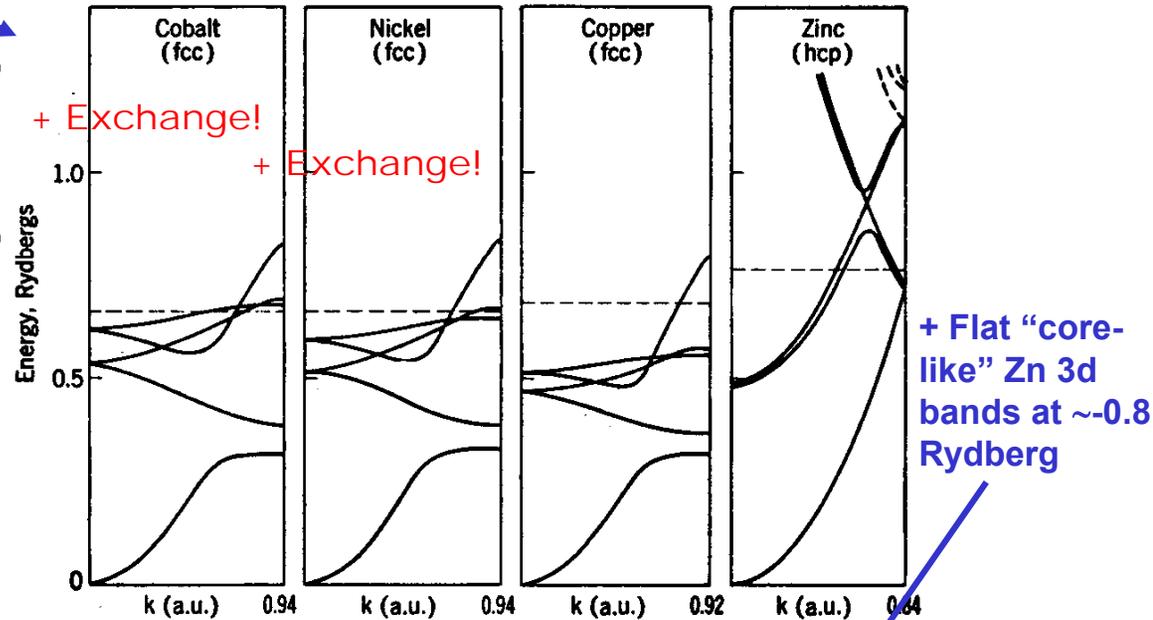


Fig. 10-20. Energy bands of 3d transition elements, along a single direction, from Mattheiss.

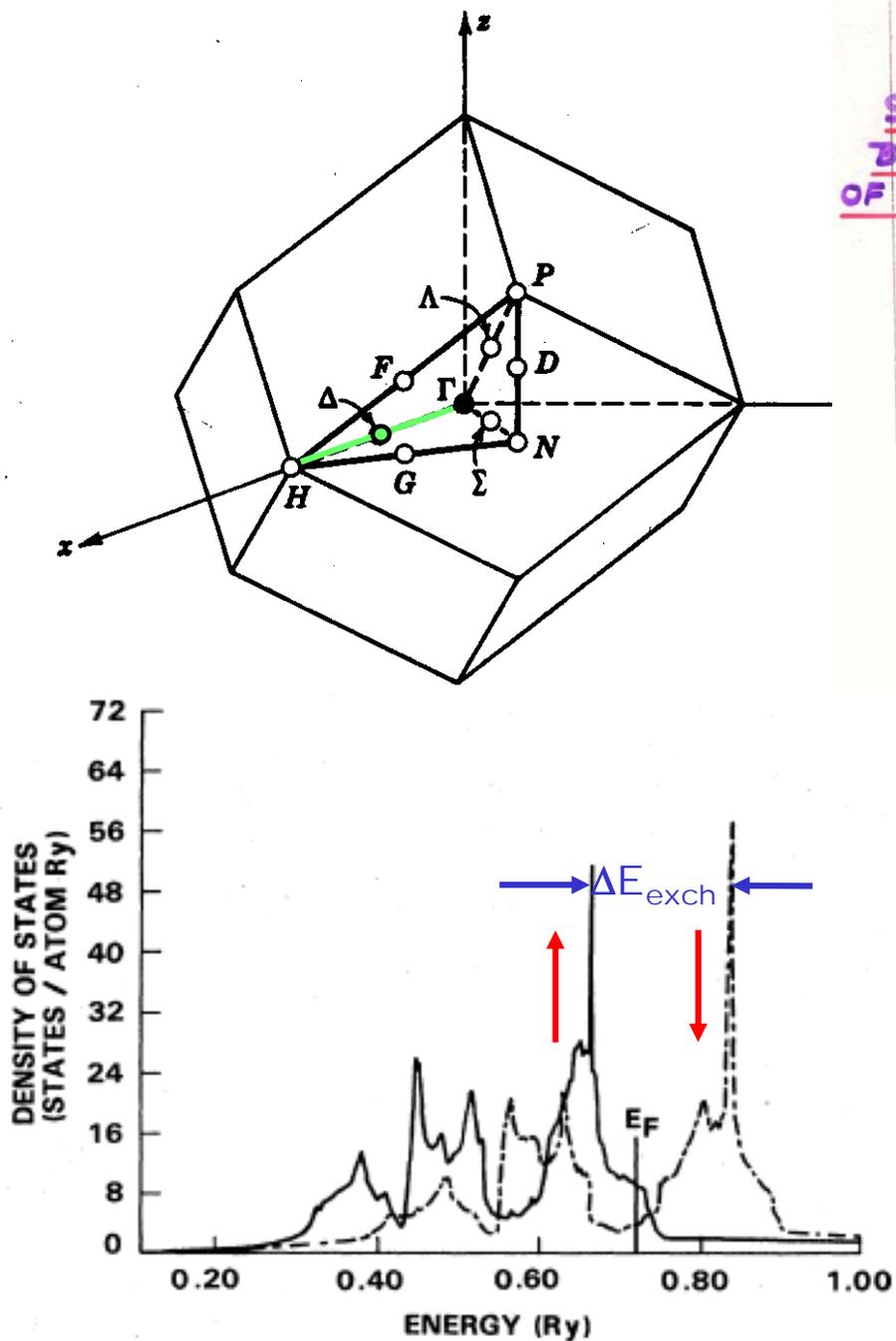
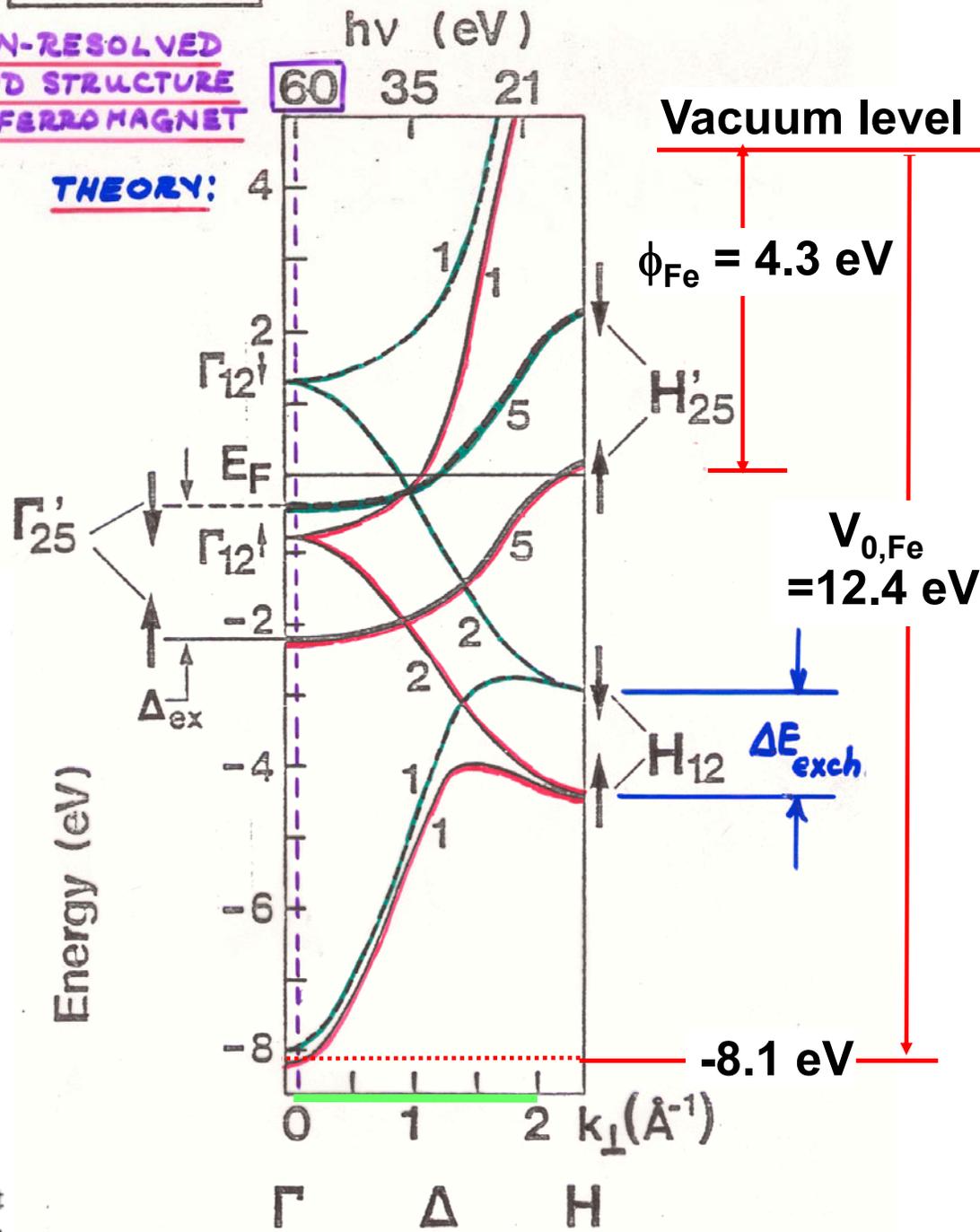


FIG. 4. Density of states at the equilibrium lattice constant of Fe for majority- (solid line) and minority- (broken line) spin states.

Hathaway et al., Phys. Rev. B 31, 7603 ('85)

**Fe (001)**  
SPIN-RESOLVED BAND STRUCTURE OF A FERROMAGNET

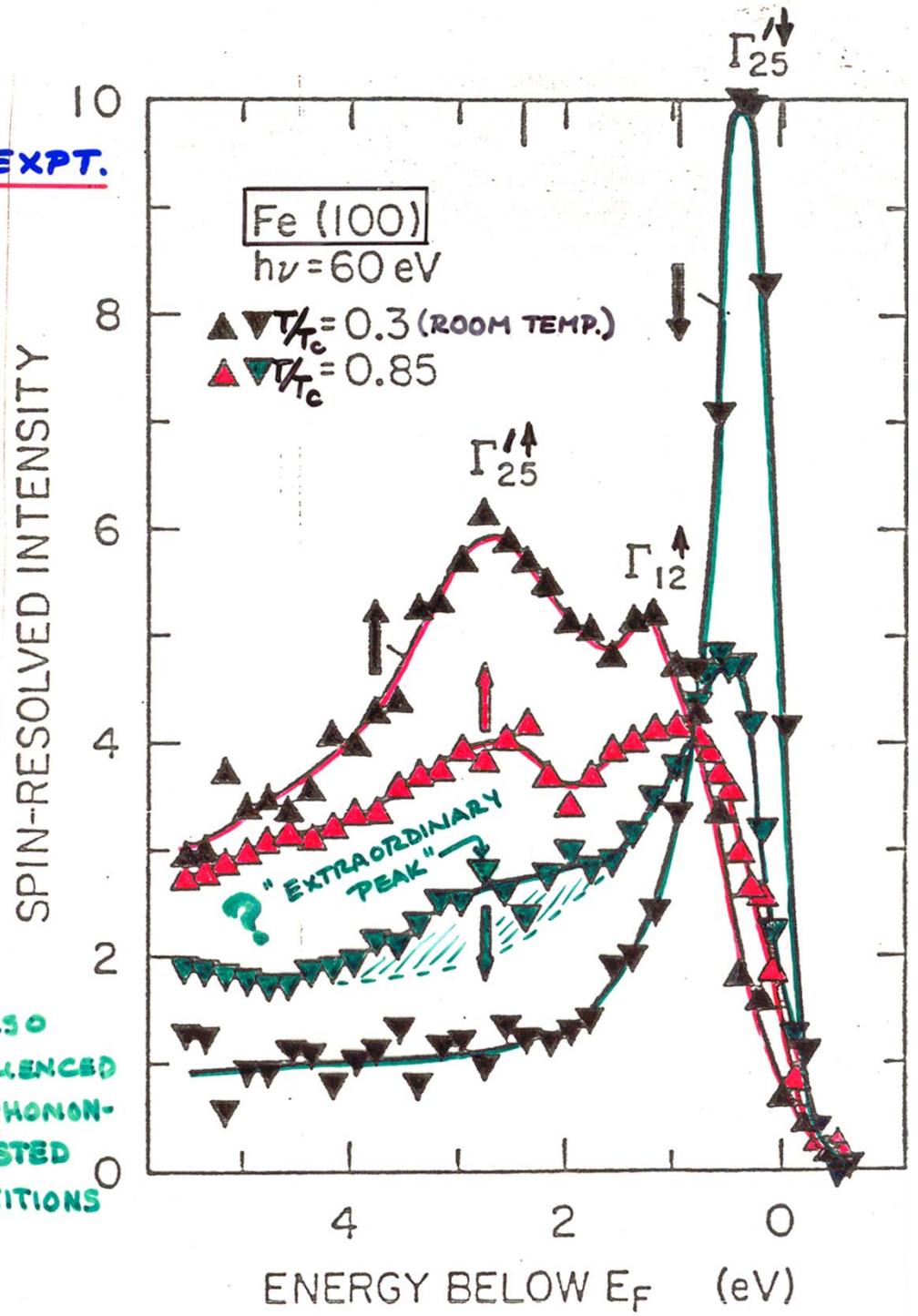


E. KISKER ET AL., PHYS. REV. B  
 31, 329 (1985)

Fe: ANGLE AND SPIN-RESOLVED SPECTRA AT  $\Gamma$  POINT

EXPT.

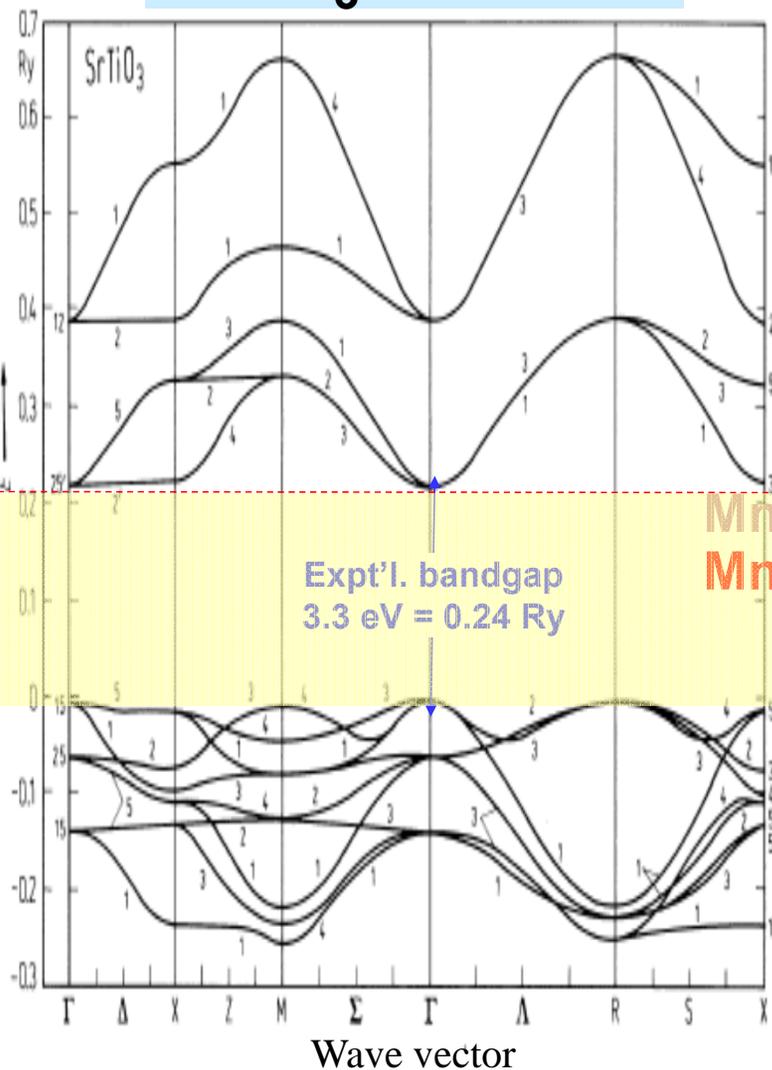
? ALSO INFLUENCED BY PHONON-ASSISTED TRANSITIONS



E. KISKER ET AL., PHYS. REV. B  
 31, 329 (1985)

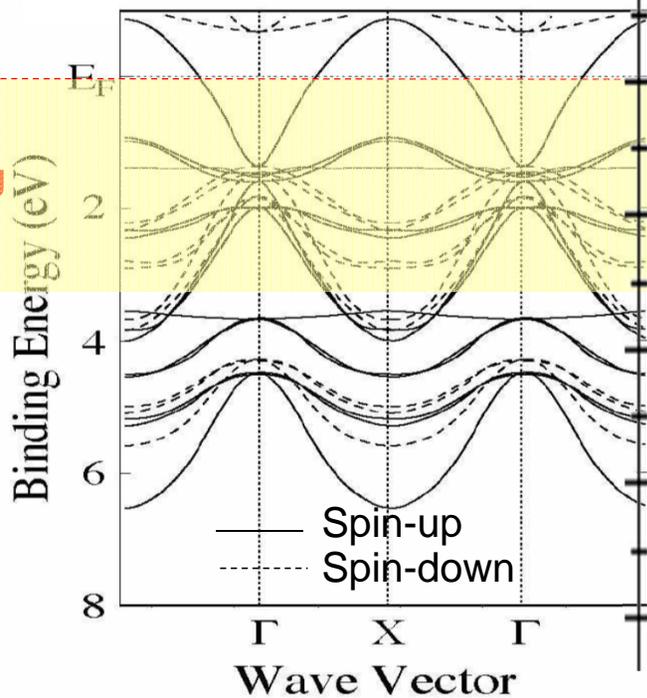
# SrTiO<sub>3</sub> and La<sub>0.67</sub>Sr<sub>0.33</sub>MnO<sub>3</sub> band structures and DOS

## SrTiO<sub>3</sub>-insulator



Mattheiss, PRB 6, 4718 (1972)

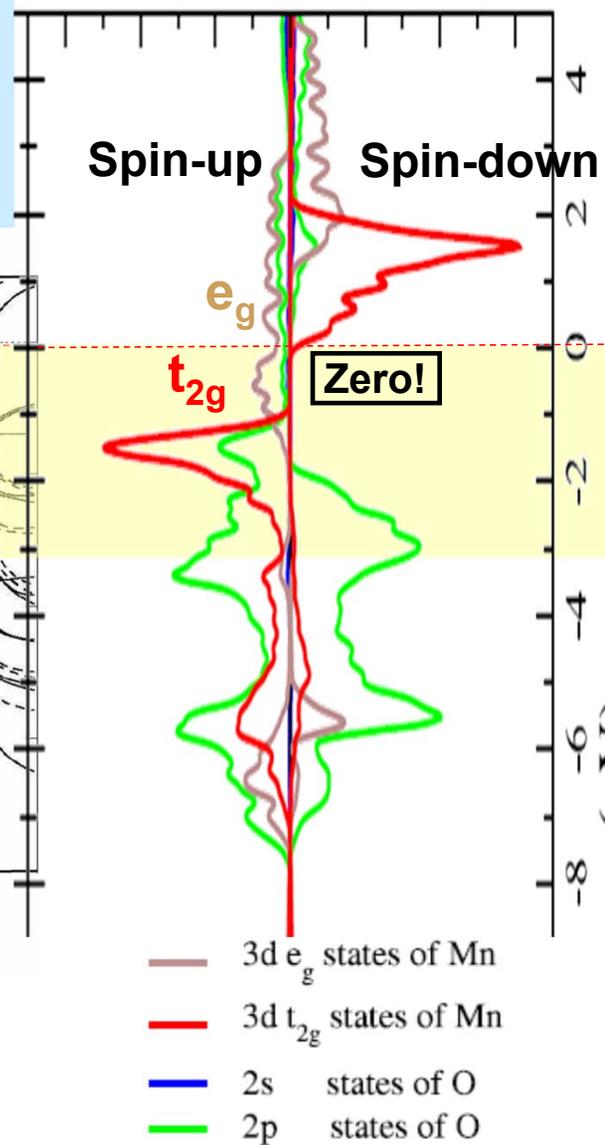
## La<sub>0.67</sub>Sr<sub>0.33</sub>MnO<sub>3</sub>- Half-Metallic Ferromagnetic metal

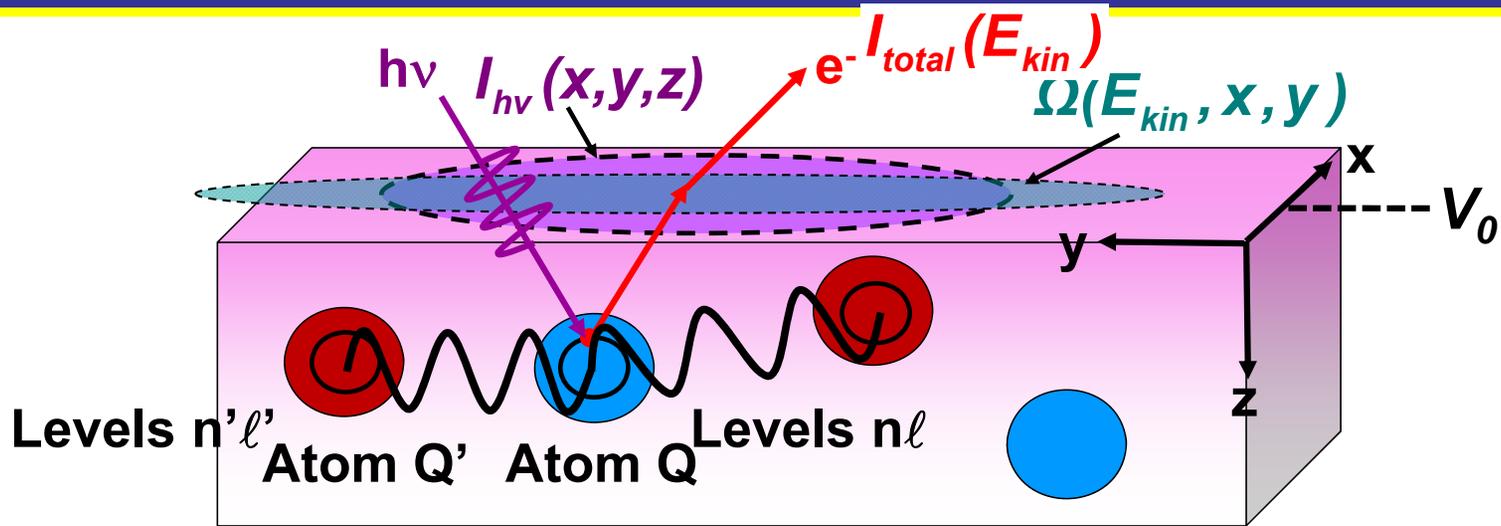


Chikamatsu et al.,  
PRB 73, 195105 (2006)

Zheng, Binggeli, J. Phys.  
Cond. Matt. 21, 115602 (2009)

## Projected DOSs





For a given subshell:

$$I(E_{kin}, Qn\ell) =$$

$$C' \int_0^{\infty} I_{hv}(x, y, z) \rho_{Qn\ell}(E_b, x, y, z) \frac{d\sigma_{Qn\ell}(hv)}{d\Omega} \exp\left[-\frac{z}{\Lambda_e(E_{kin}) \sin\theta}\right] \Omega(E_{kin}, x, y) dx dy dz$$

$I_{hv}(x, y, z)$  = x-ray flux

$\rho_{Qn\ell}(E_b, x, y, z)$  = density of states, projected onto  $Qn\ell$  character

$\frac{d\sigma_{Qn\ell}(hv)}{d\Omega}$  = energy-dependent differential photoelectric cross section for subshell  $Qn\ell$

$\Lambda_e(E_{kin})$  = energy-dependent inelastic attenuation length

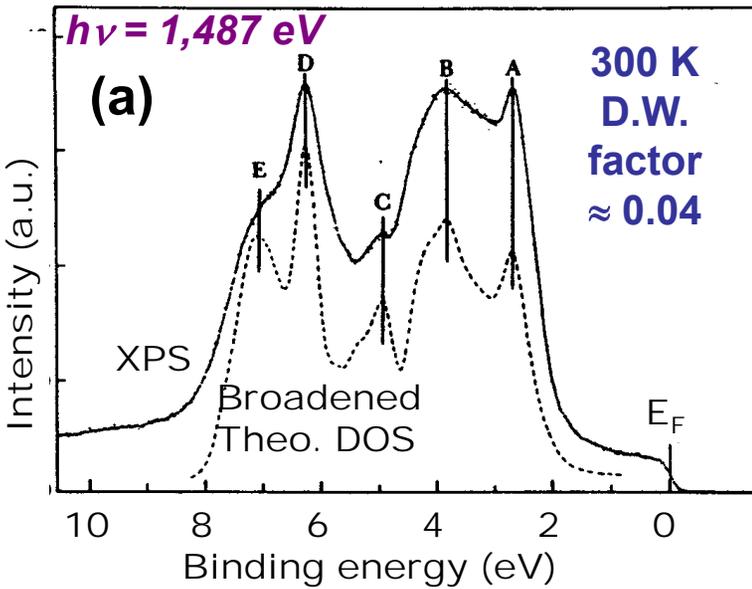
→ Mean Emission Depth

$\Omega(E_{kin}, x, y)$  = energy-dependent spectrometer acceptance solid angle

For the total VB intensity:

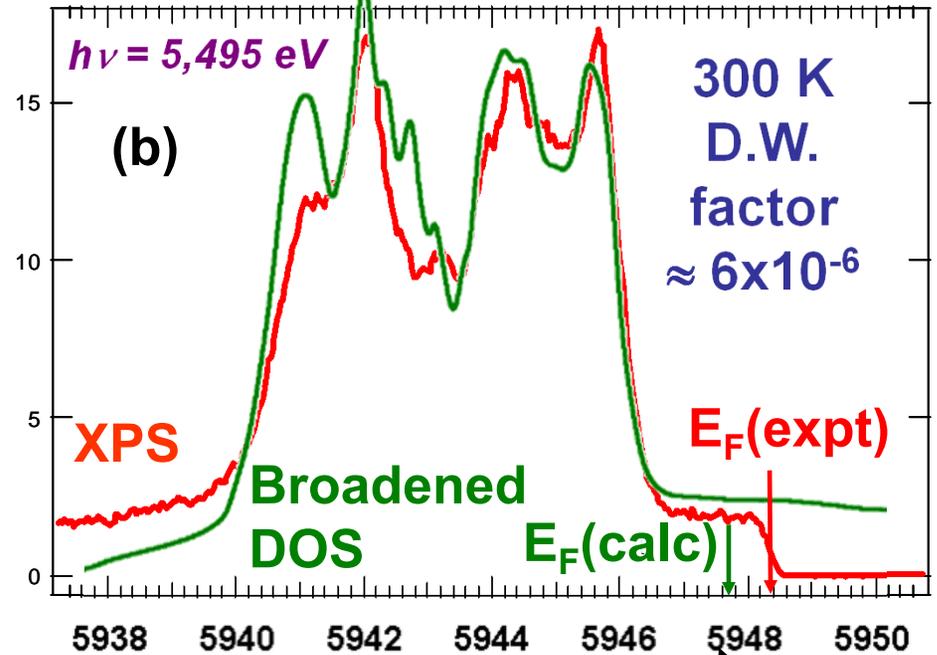
$$I_{total}(E_{kin}) = \sum_{Qn\ell} I(E_{kin}, Qn\ell)$$

# Gold Valence Spectrum

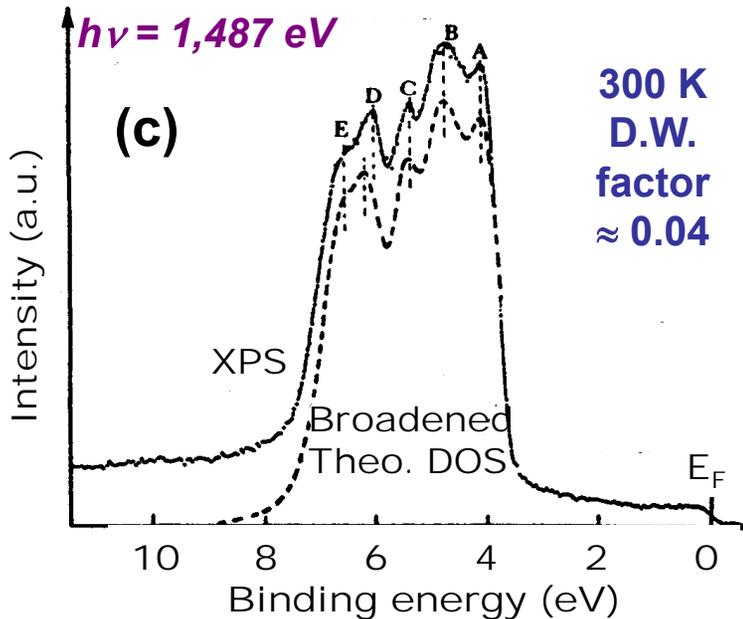


## Valence spectra in the XPS Limit

# Gold Valence Spectrum



# Silver Valence Spectrum

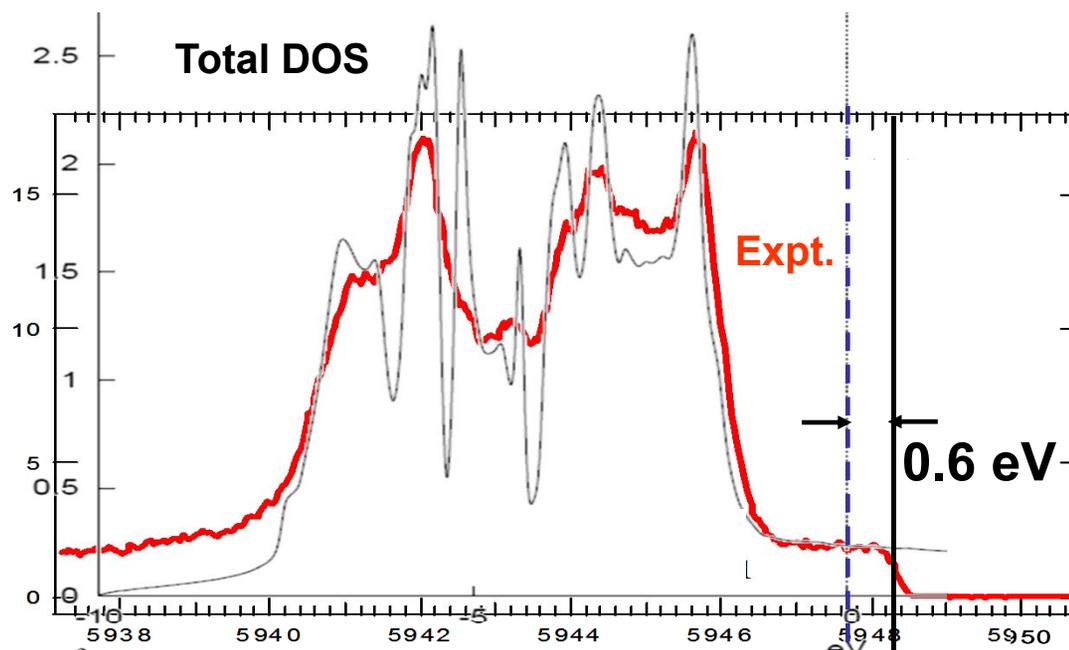


**Au subshell photoelectric cross section ratios:**  
**Au6s/Au5d = 0.012 at 1.5 keV**  
**Au6s/Au5d = 0.028 at 6 keV**  
**→6s weak but more imp. at 6 keV x 2.5x**

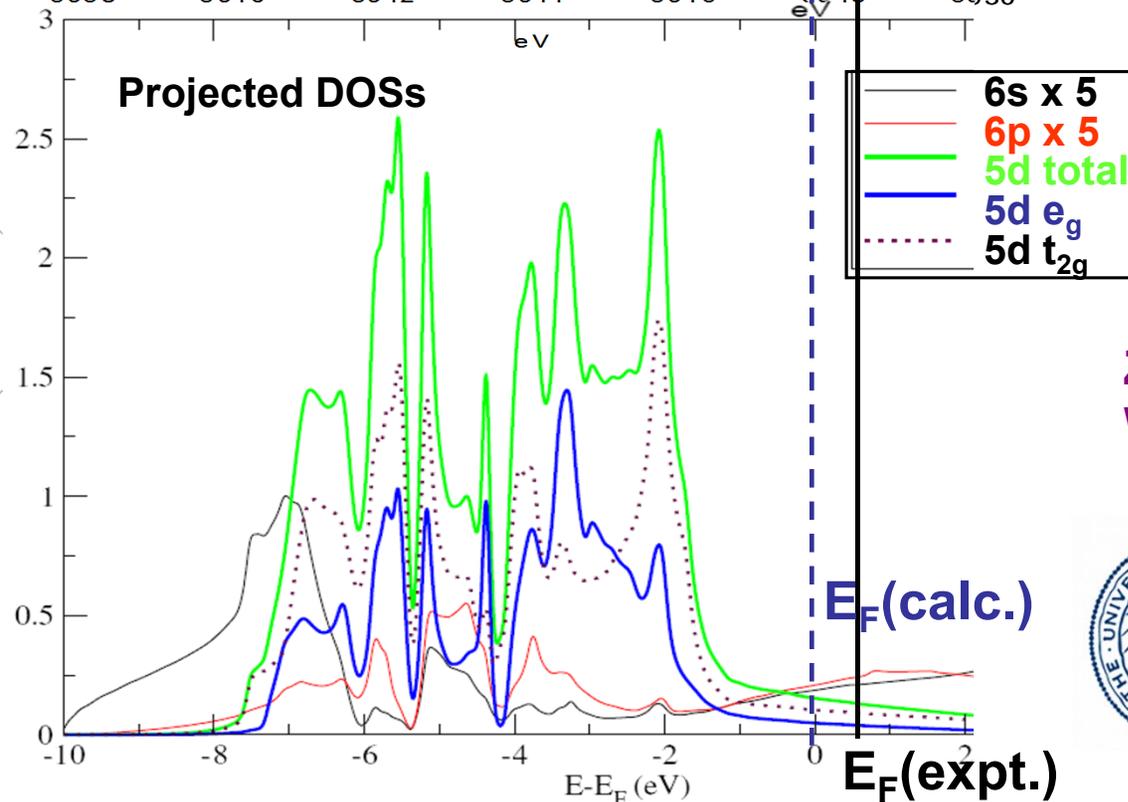
**Screening/  
 self-energy  
 correction**

**In the XPS  
Limit—  
Comparison to  
theoretical  
DOSs**

**Au subshell  
photoelectric cross  
section ratios:  
Au6s/Au5d = 0.012  
at 1.5 keV and 0.028  
at 6 keV → 6s more  
imp. at 6 keV x 2.5x**



Takata et al.,  
SPring8 @  
5.495 keV

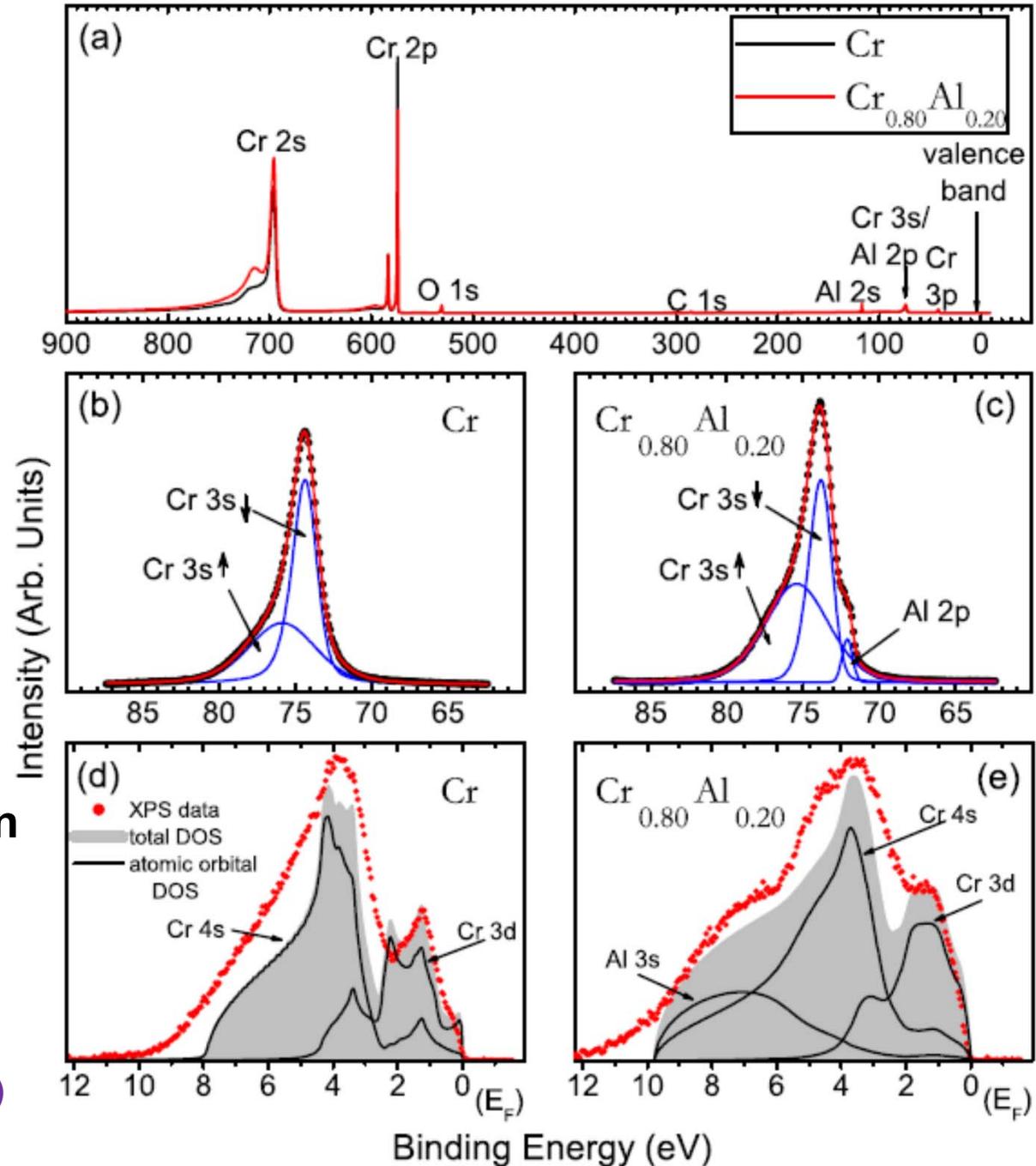


Z. Yin  
W.E. Pickett



# Hard x-ray photoemission from Cr and $\text{Cr}_{0.80}\text{Al}_{0.20}$

$h\nu = 5956 \text{ eV}$



Experiment vs cross-section weighted projected densities of states

Gray et al., PRL 105, 236404 (2010)

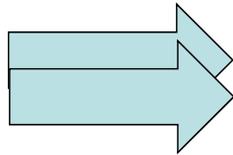
## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**



Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## **Valence-Level Photoemission**

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## **Some New Directions**

Photoemission with Hard X-Rays (throughout lectures)

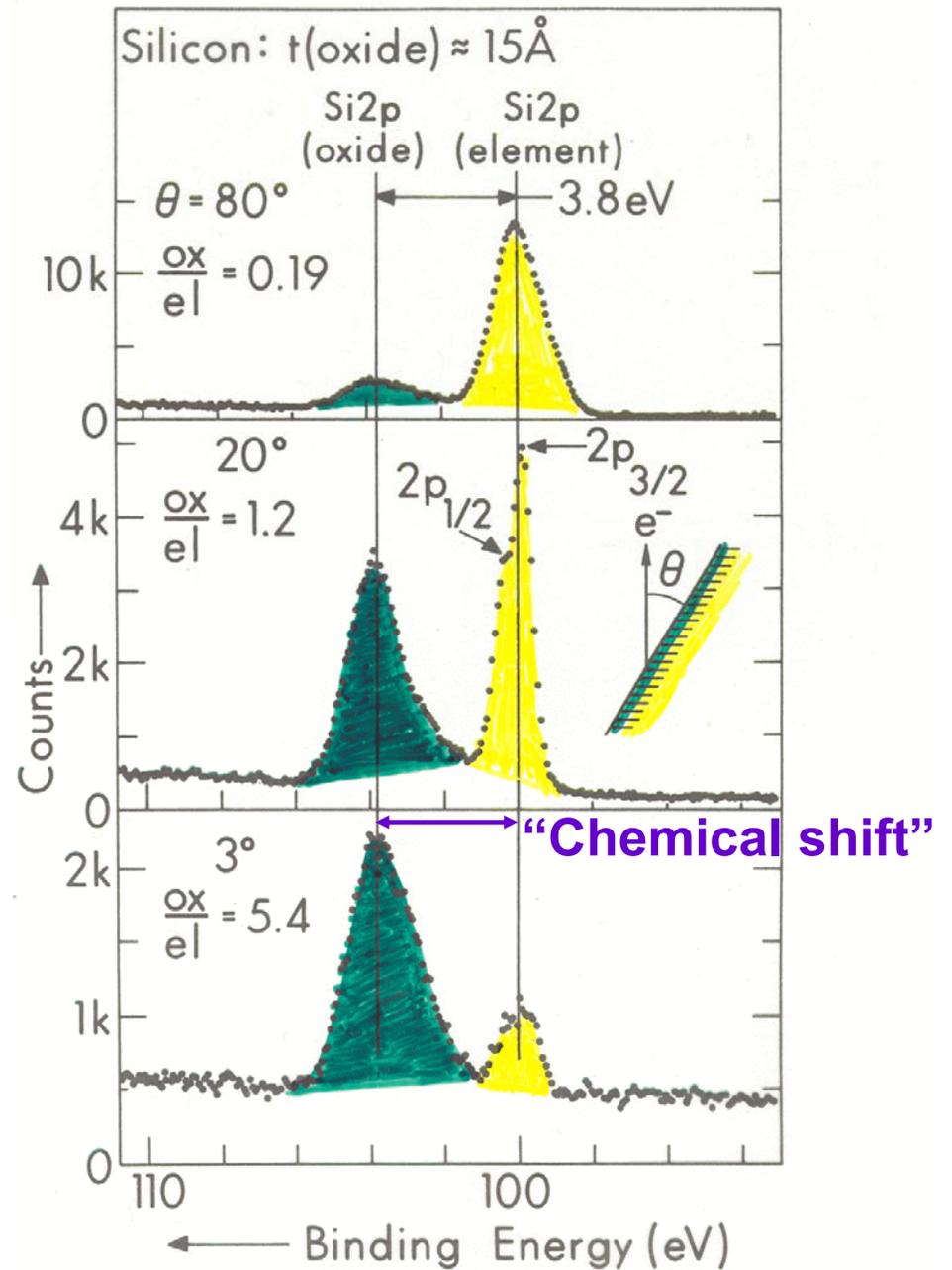
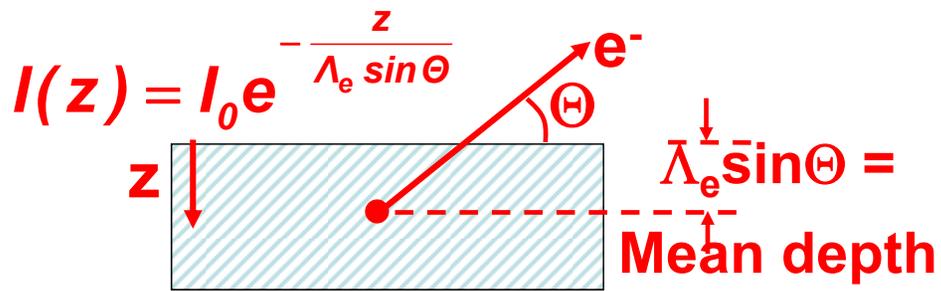
Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

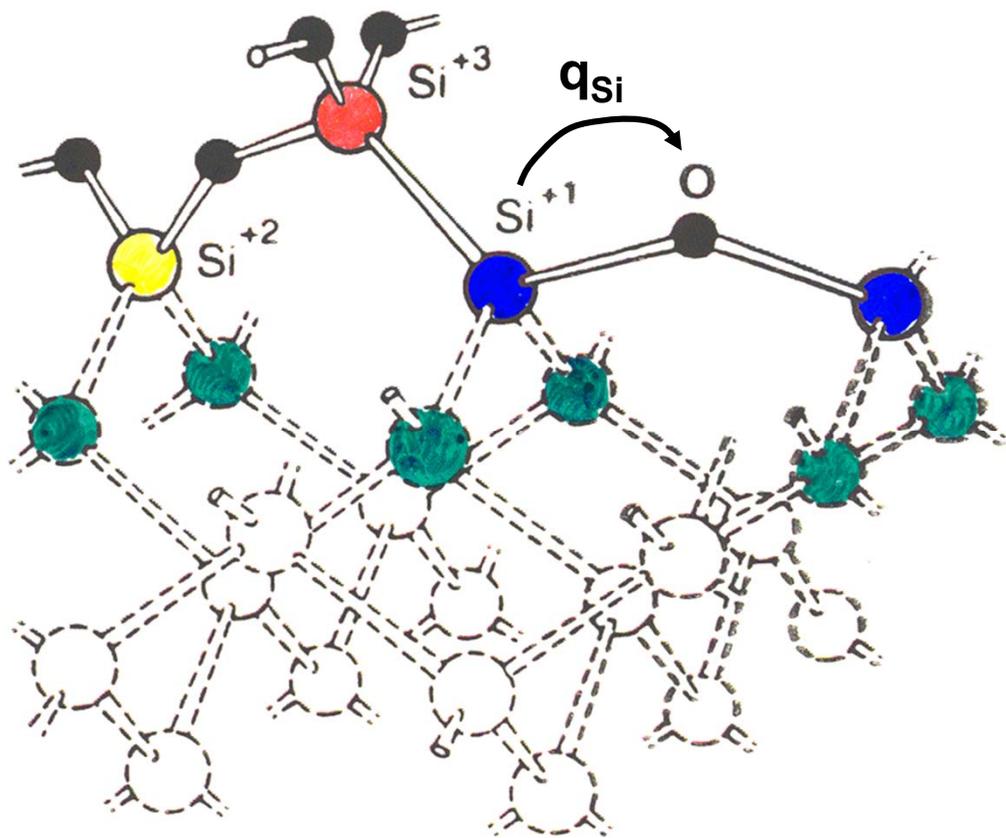
Temporal Resolution

# Enhancing surface sensitivity at grazing exit angles



# Chemical shifts:

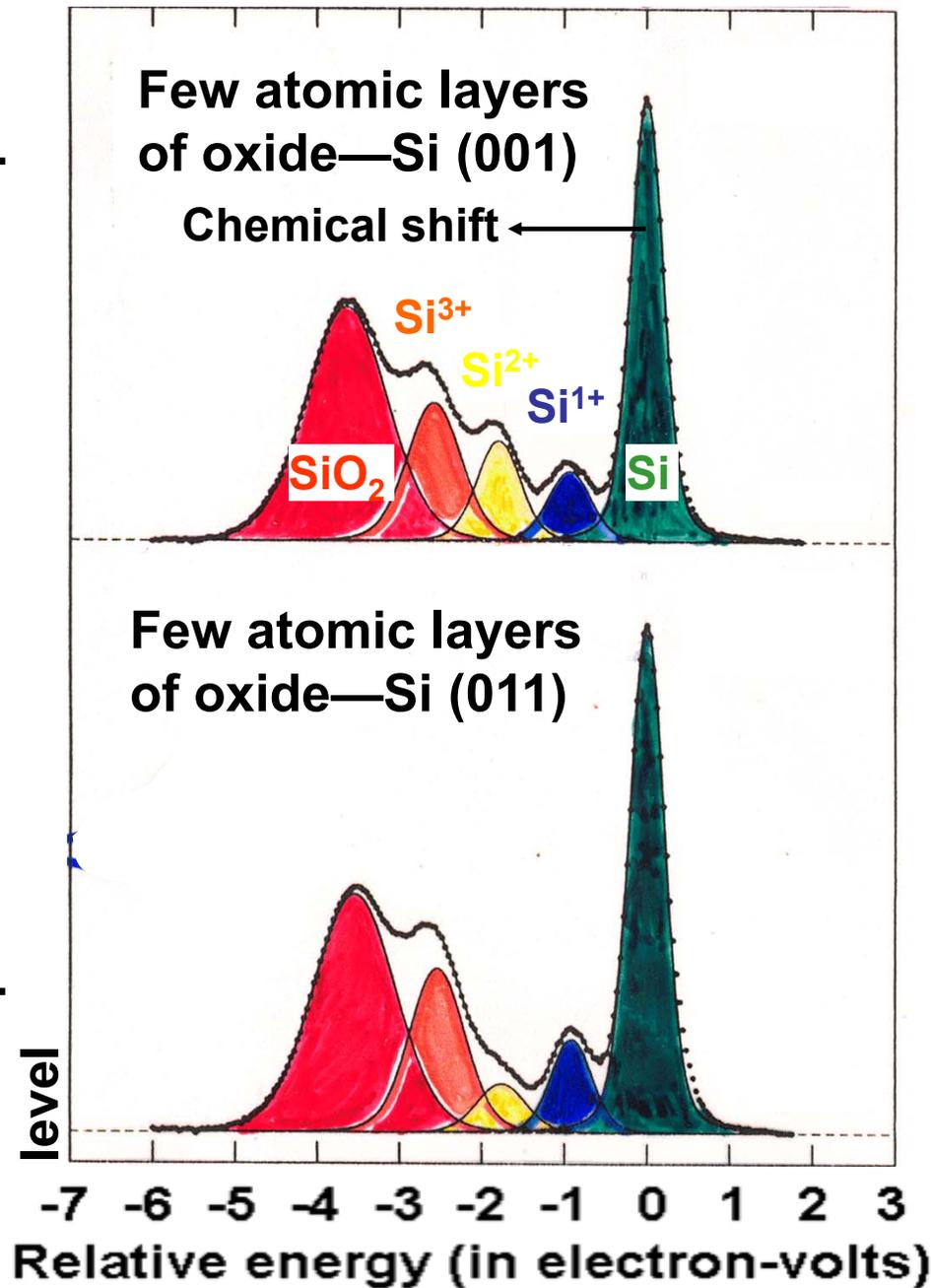
## Looking into the silicon dioxide layer with photoelectron spectroscopy



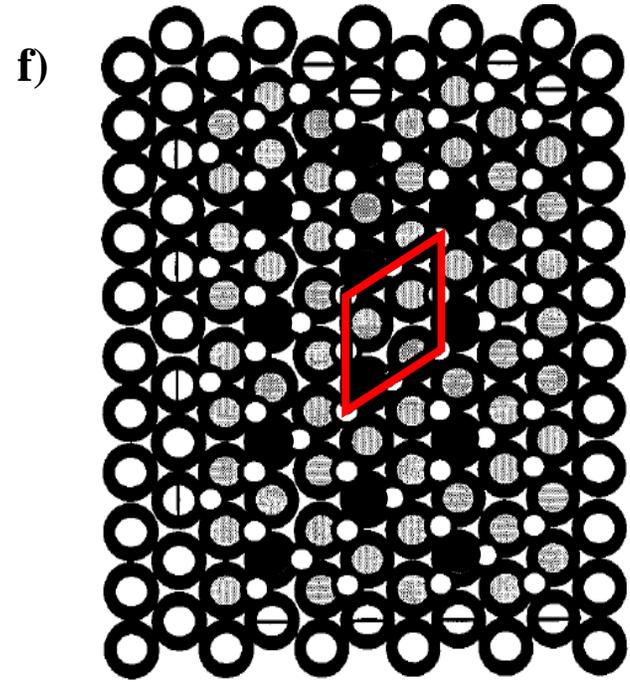
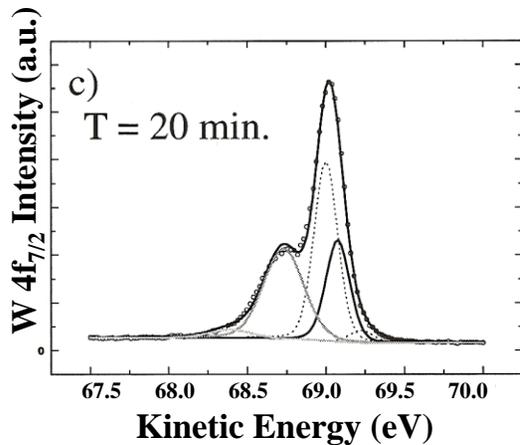
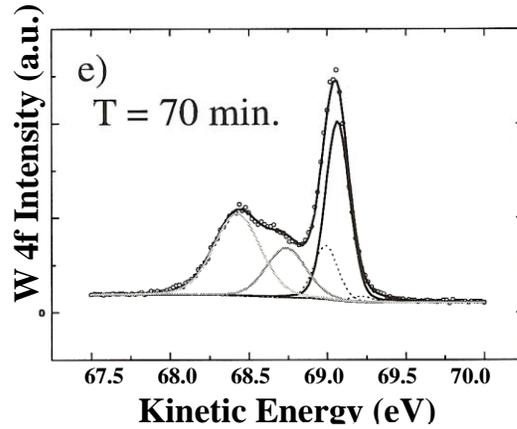
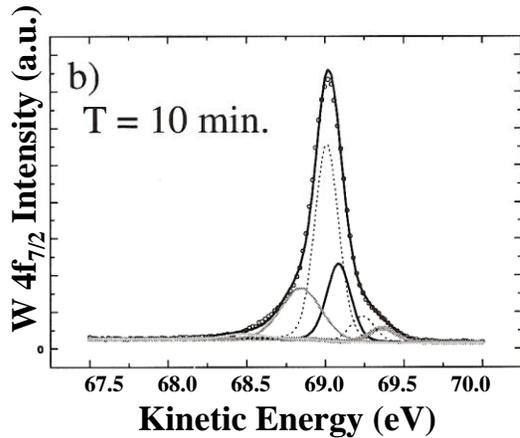
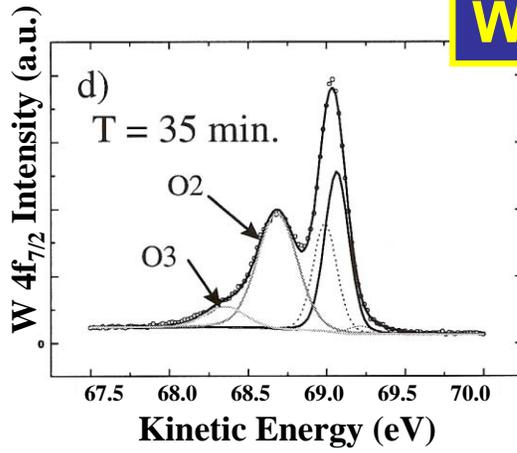
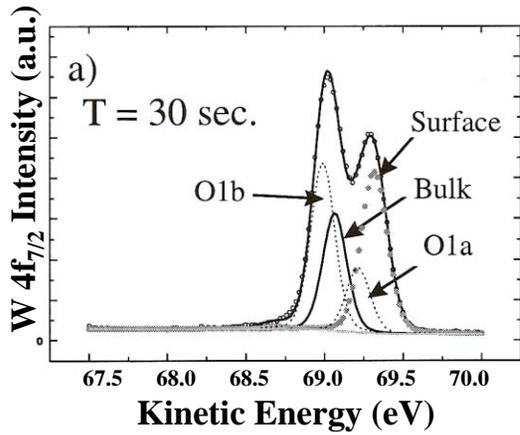
Charge transfer,  $e^- - e^-$  coulomb integral:

$$\text{Shift} \approx q_{\text{Si}} K_{\text{Si}2p, \text{Si}3p} = q_{\text{Si}} \int \psi_{2p}^*(\vec{r}_1) \psi_{3p}^*(\vec{r}_2) \frac{e^2}{r_{12}} \psi_{2p}(\vec{r}_1) \psi_{3p}(\vec{r}_2) dV_1 dV_2$$

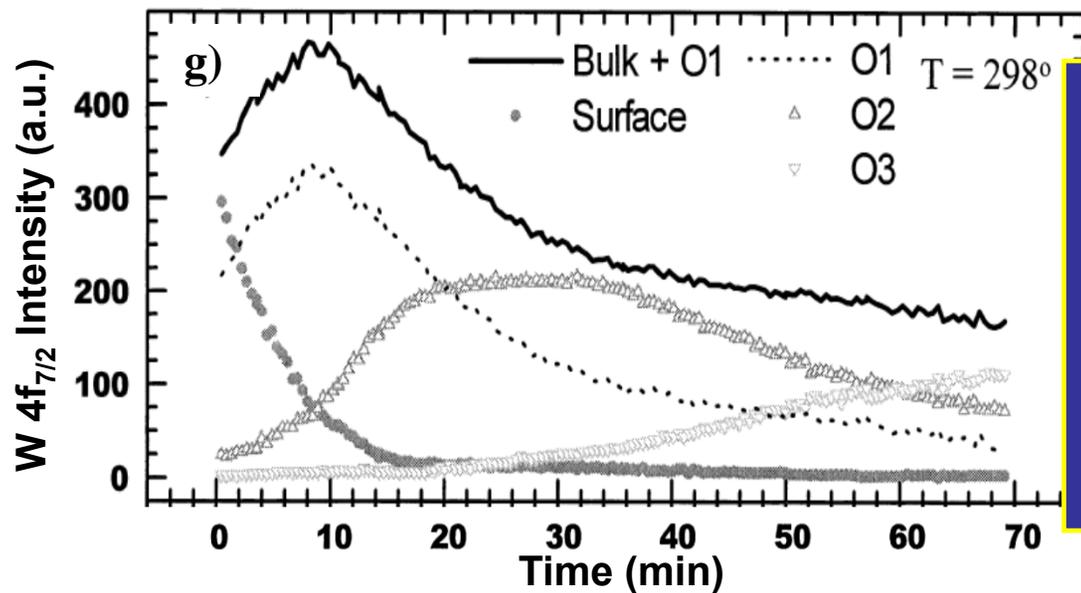
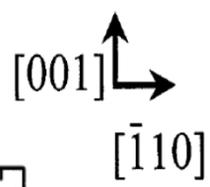
No. of photoelectrons from the silicon 2p



# W(110)/O—W 4f<sub>7/2</sub> Chemical Shifts



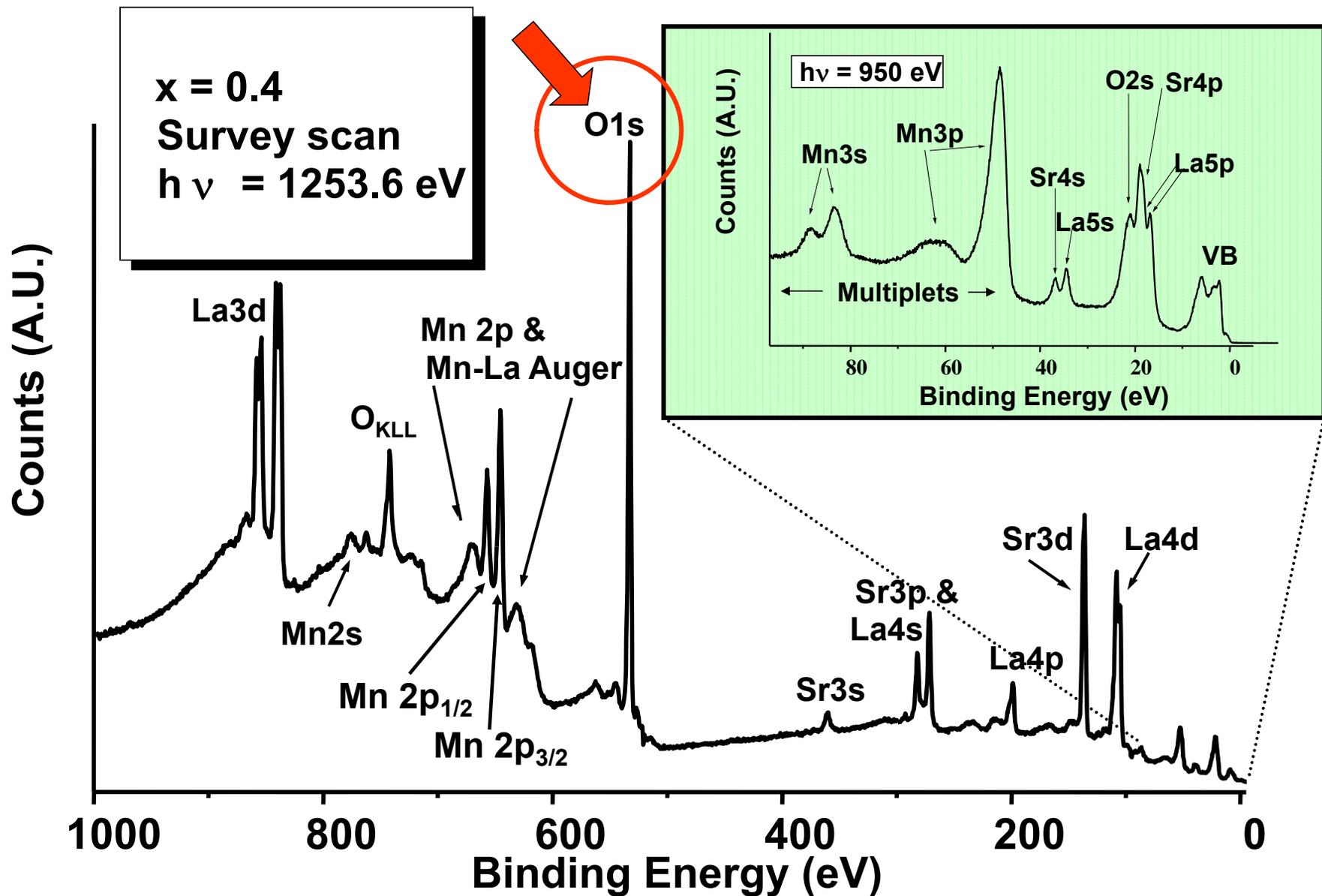
○ Oxygen  
 ○ O1a  
 ○ O2  
 ○ Surface  
 ○ O1b  
 ○ O3



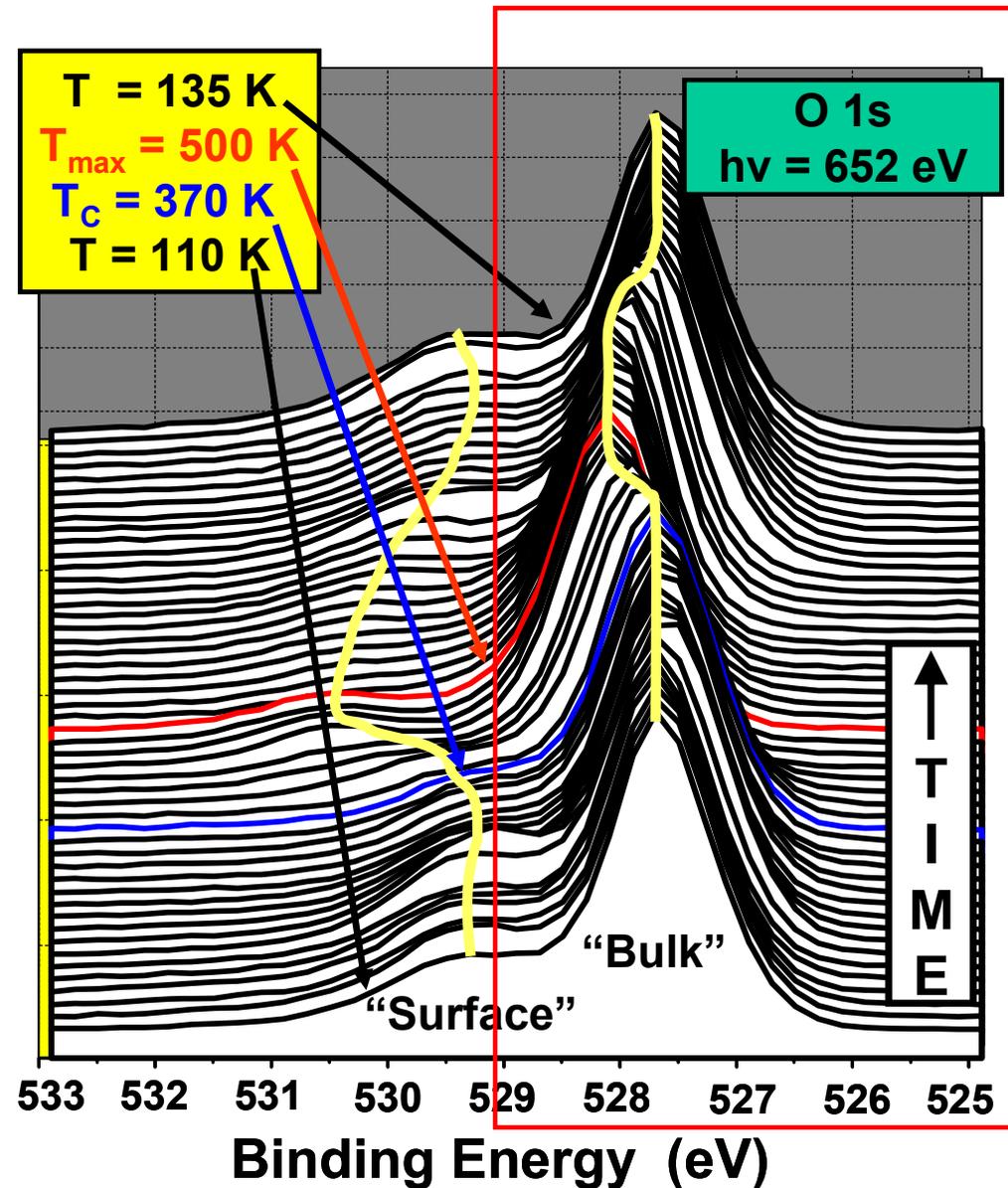
An early time-resolved reaction study (more later)

Ynzunza et al.,  
 Surf. Sci. 459 (2000) 69

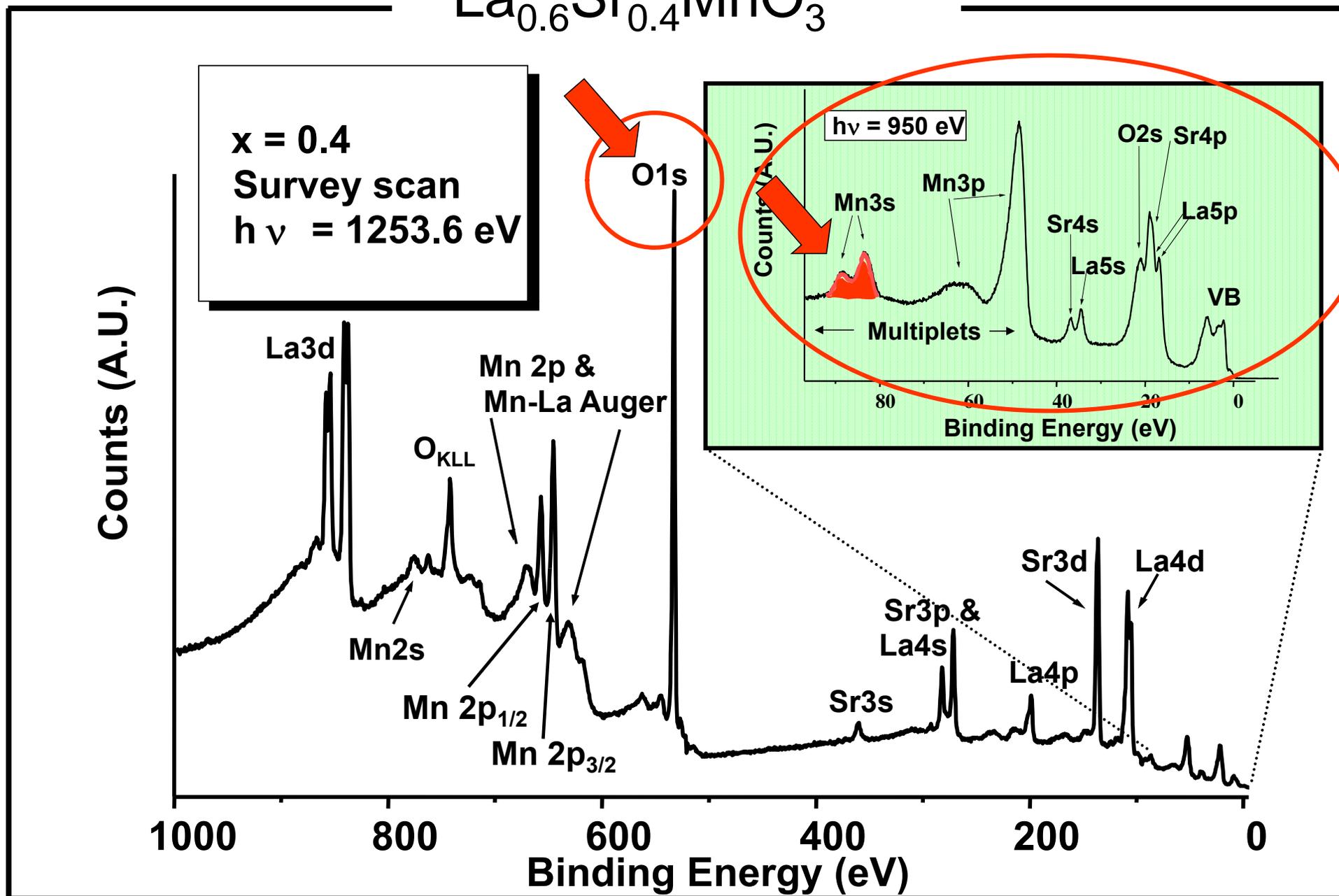
# Core and valence photoemission



# Temperature dependence of Mn3s and O1s spectra: $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$



# Core and valence photoemission



## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts



Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## **Valence-Level Photoemission**

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## **Some New Directions**

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

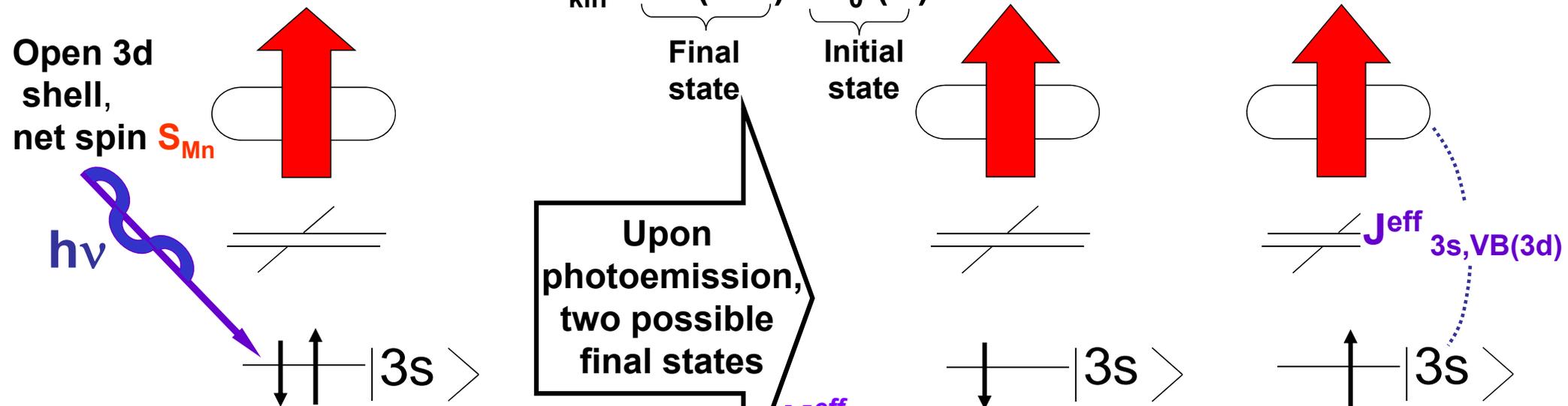
Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

# Multiplet splitting in core levels of transition metal oxides

$$BE = h\nu - E_{kin} = \underbrace{E^*(N-1)}_{\text{Final state}} - \underbrace{E_0(N)}_{\text{Initial state}}$$



The splitting between the two peaks is given by

$$\Delta E_{3s} \approx (2S_{Mn} + 1) K_{3s,VB(3d)}^{eff}$$

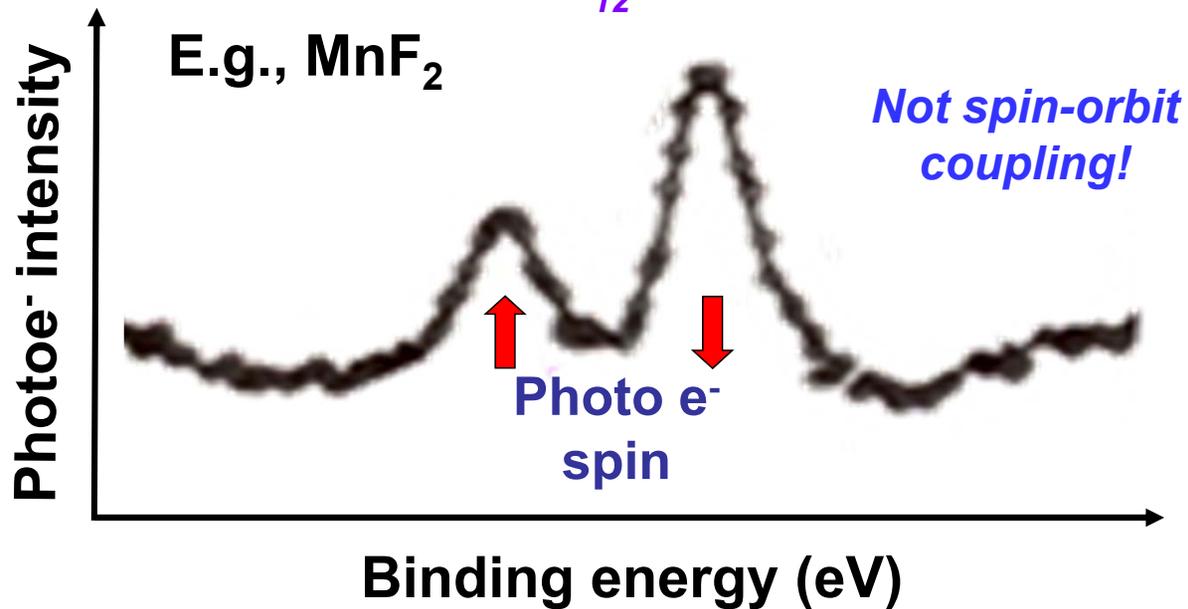
(Van Vleck Theorem)

For the cubic manganites in simplest doping model,

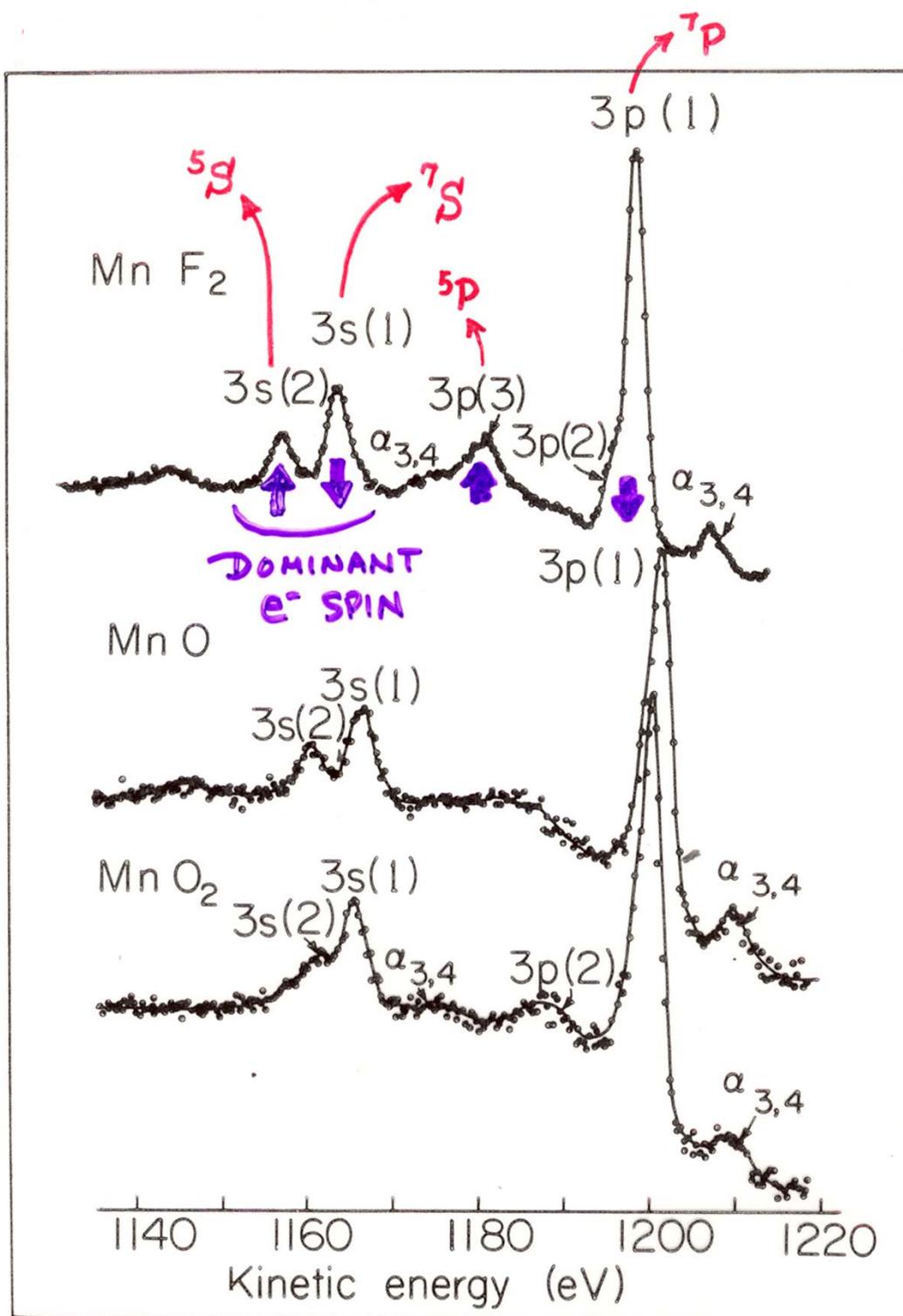
$$S_{Mn} = 1/2(4-x) \rightarrow$$

$$\Delta E_{3s} \approx [5-x] K_{3s,VB(3d)}^{eff}$$

with  $J_{3s,VB}^{eff} \approx 1.1 \text{ eV}$



# CORE-LEVEL MULTIPLET SPLITTINGS IN Mn COMPOUNDS



“Basic Concepts of XPS”  
Figure 31

# Intensities in photoelectron spectra in the sudden approximation

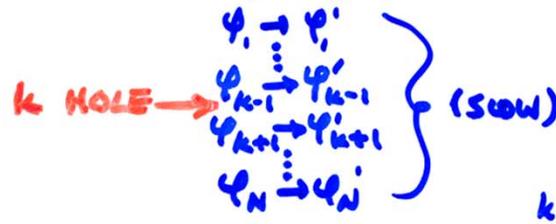
- GENERAL: FINAL STATE  $K$  ( $k$ -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPENHEIMER:  $e^-$ 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION:  $\Psi_K \rightarrow \Psi_F = \text{PHOTO}^-$  (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 |\langle \Psi_e^f(N-1, K) | \Psi_e^i(N-1, k) \rangle|^2$$

$$|\hat{e} \cdot \langle \psi_f | \vec{r} | \psi_k \rangle|^2$$

SAME SUBSHELL COUPLING + TOTAL L, S  $\rightarrow$  "MONOPOLE"

$$\rightarrow \text{NORMAL } \frac{d\sigma_K}{d\Omega}$$

- SLATER DETS. FOR  $\Psi_e^f = \det(\psi'_1, \psi'_2, \dots, \psi'_{k-1}, \psi'_{k+1}, \dots, \psi'_N)$

$$\Psi_e^i = \det(\psi_1, \psi_2, \dots, \psi_{k-1}, \psi_{k+1}, \dots, \psi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 |\langle \psi'_1 | \psi_1 \rangle|^2 |\langle \psi'_2 | \psi_2 \rangle|^2 \dots$$

$$|\langle \psi'_{k-1} | \psi_{k-1} \rangle|^2 |\langle \psi'_{k+1} | \psi_{k+1} \rangle|^2 \dots |\langle \psi'_N | \psi_N \rangle|^2$$

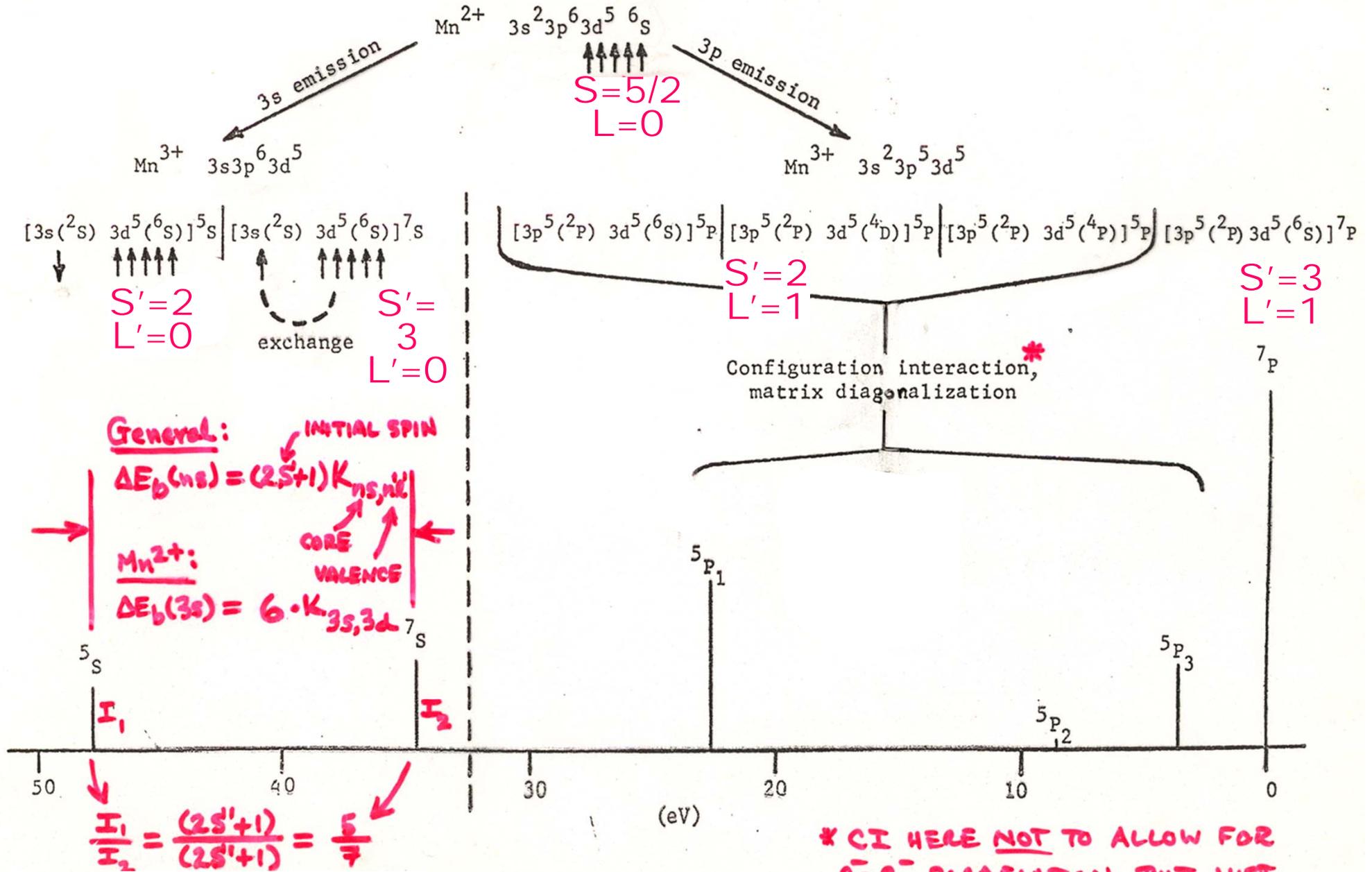
$$|\hat{e} \cdot \langle \psi_f | \vec{r} | \psi_k \rangle|^2$$

$1e^-$  DIPOLE  $\rightarrow d\sigma/d\Omega$

( $N-1$ ) $e^-$  SHAKE-UP/  
SHAKE-OFF  $\rightarrow$   
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN  $\Psi_f$  ESCAPE

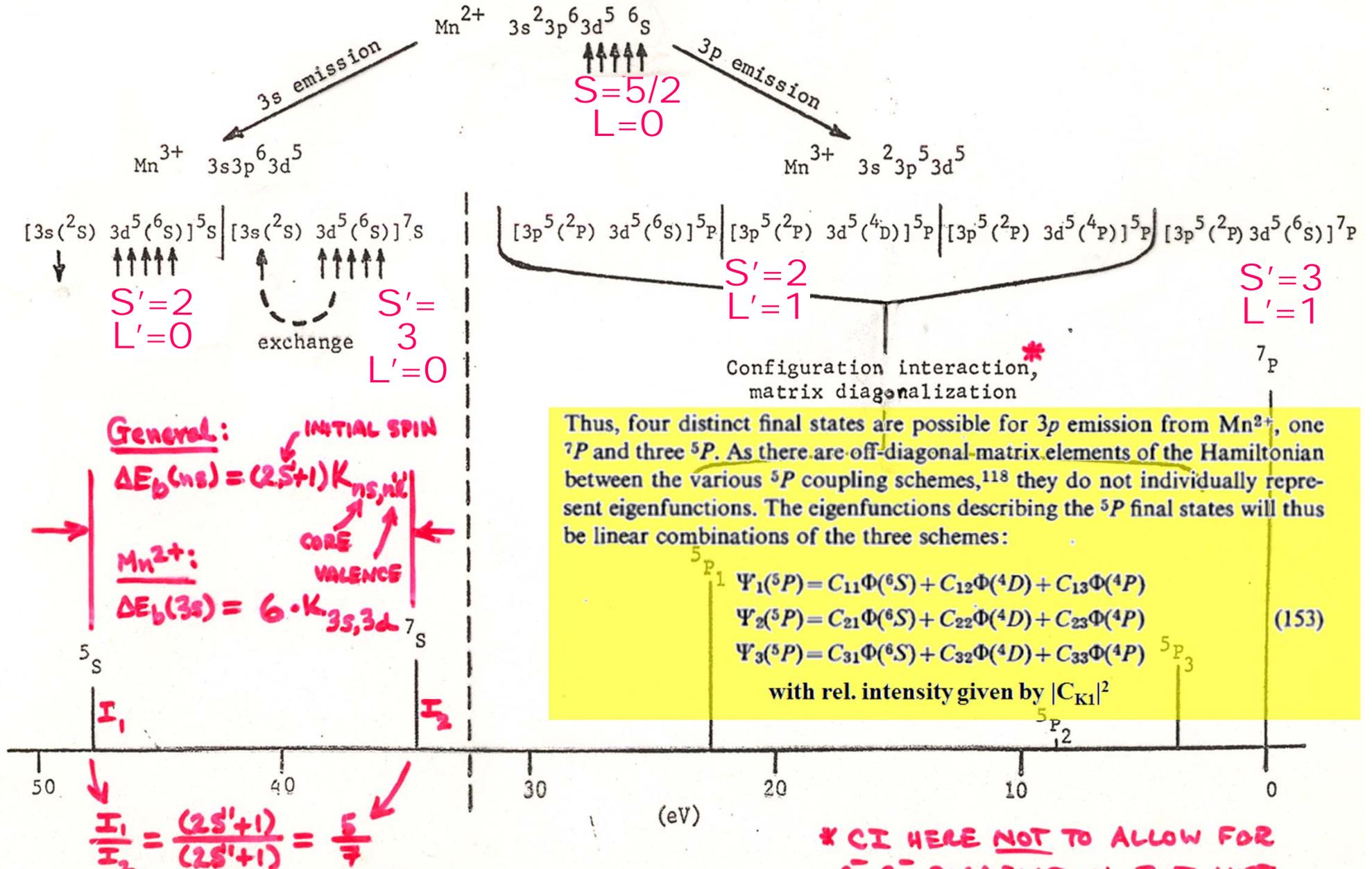
# ORIGIN OF MULTIPLY SPLITTINGS IN $Mn^{2+}$ : "ONE-ELECTRON" THEORY



"Basic Concepts of XPS"  
Figure 30

\* CI HERE NOT TO ALLOW FOR  $e^-e^-$  CORRELATION, BUT JUST DIFFERENT COUPLING IN  $3p^5 3d^5$

# ORIGIN OF MULTIPLY SPLITTINGS IN Mn<sup>2+</sup>: "ONE-ELECTRON" THEORY



"Basic Concepts of XPS"  
Figure 30

\* CI HERE NOT TO ALLOW FOR e<sup>-</sup>e<sup>-</sup> CORRELATION, BUT JUST DIFFERENT COUPLING IN 3p<sup>5</sup>3d<sup>5</sup>

in order for relaxation to occur in forming the lowest-binding-energy "primary" or "adiabatic" final state corresponding to the ionic ground state, excited ionic states corresponding to binding energies higher than  $-\epsilon_k$  must also arise. The peaks due to these states have been variously called "shake-up", "shake-off", "many-electron transitions", "configuration-interaction satellites", or "correlation peaks", and more specific illustrations are given in Section V.D. The high-intensity lowest-binding-energy peak has often been associated with a "one-electron transition", although this name is unduly restrictive in view of the inherently many-electron nature of the photoemission process. Thus, the intimate relationship between relaxation and correlation is demonstrated, although it still is possible to determine uniquely a relaxation energy with initial- and final-state Hartree-Fock wave functions that are often assumed to be uncorrelated in the sense that  $E_{\text{corr}}$  is measured relative to them. The second sudden-approximation sum rule deals with intensities, and it states that the sum of all intensities associated with the states  $\Psi^f(N-1, K)$  is given by

$$I_{\text{tot}} = \sum_K I_K = C \sum_K |\langle \phi^f(1) | \hat{i} | \phi_k(1) \rangle|^2 |\langle \Psi^f(N-1, K) | \Psi_{\text{R}}(N-1) \rangle|^2 = C |\langle \phi^f(1) | \hat{i} | \phi_k(1) \rangle|^2 \quad (78)$$

where  $C$  is a constant for a given photon energy. One experimental consequence of this sum rule is that matrix elements and cross-sections calculated with unrelaxed final-state orbitals and thus using Eq. (76) apply only to absolute intensities summed over all states  $\Psi^f(N-1, K)$ , as was first pointed out by Fadley.<sup>137</sup> Thus, absolute photoelectron intensities for the usually-dominant ionic-ground-state peaks may be below those predicted by unrelaxed or frozen-orbital cross-sections, as has been noted experimentally by Wuilleumier and Krause,<sup>139</sup> by contrast, x-ray absorption coefficients, which inherently sum over all final states for a given  $k \rightarrow f$  excitation, are well predicted by unrelaxed cross-sections.<sup>137</sup>

At a higher level of accuracy than any of the approximations discussed up to this point, configuration-interaction wave functions can also be used in the calculation of matrix elements and cross-sections.<sup>91, 127</sup> In particular, Manson<sup>91</sup> has discussed in a general way the effects that this can have, pointing out several mechanisms by which calculated intensities can be significantly modified by the inclusion of CI in the initial-state wave function and the final-state wave function. For computational convenience, it is customary (although not essential) to use the same set of orthonormal one-electron orbitals  $\phi_1, \phi_2, \dots, \phi_M$  ( $M > N$ ) in making up the configurations of both initial and final states. This apparent lack of allowance for relaxation in the final state can be more than compensated by using a large number of configurations with mixing coefficients  $C_j^i$  and  $C_j^f$  that are optimized for

both states:

$$\Psi^i(N) = \sum_j C_j^i \Phi_j^i(N) \quad (79)$$

$$\Psi^f(N) = \sum_m C_m^f \Phi_m^f(N) \quad (80)$$

The exact expressions for matrix elements determined with such wave functions are rather complex, particularly if more than one continuum orbital is included, corresponding to an allowance for continuum CI (also referred to as interchannel coupling or close coupling).<sup>91</sup> Although such continuum effects may be important in certain special cases (see Section V.D.5), several many-electron phenomena noted in XPS spectra can be well explained in terms of only initial-state CI and final-state-ion CI. In visualizing these effects, it is thus useful to take a sudden approximation point of view, in which a single primary  $k \rightarrow f$  transition is considered and the individual configurations  $\Phi_j^i(N)$  and  $\Phi_m^f(N)$  are thus written as antisymmetrized products with forms analogous to Eqs (66) and (67):

$$\Phi_j^i(N) = \hat{A}(\phi_k(1)\chi_k(1), \Phi_j^i(N-1)) \quad (81)$$

$$\Phi_m^f(N) = \hat{A}(\phi^f(1)\chi^f(1), \Phi_m^f(N-1)) \quad (82)$$

In these equations, the  $(N-1)$ -electron factors can if desired be indexed identically, so that, for the fixed one-electron basis set,  $\Phi_j^i(N-1) = \Phi_m^f(N-1)$  if  $j=m$  and thus also  $\langle \Phi_j^i(N-1) | \Phi_m^f(N-1) \rangle = \delta_{jm}$ . Matrix elements in this limit are then given by repeated application of Eq. (68) as

$$\langle \Psi(N) | \sum_{i=1}^N \hat{i}_i | \Psi^i(N) \rangle = \langle \phi^f(1) | \hat{i} | \phi_k(1) \rangle \left[ \sum_j (C_j^f)^* C_j^i \right] \quad (83)$$

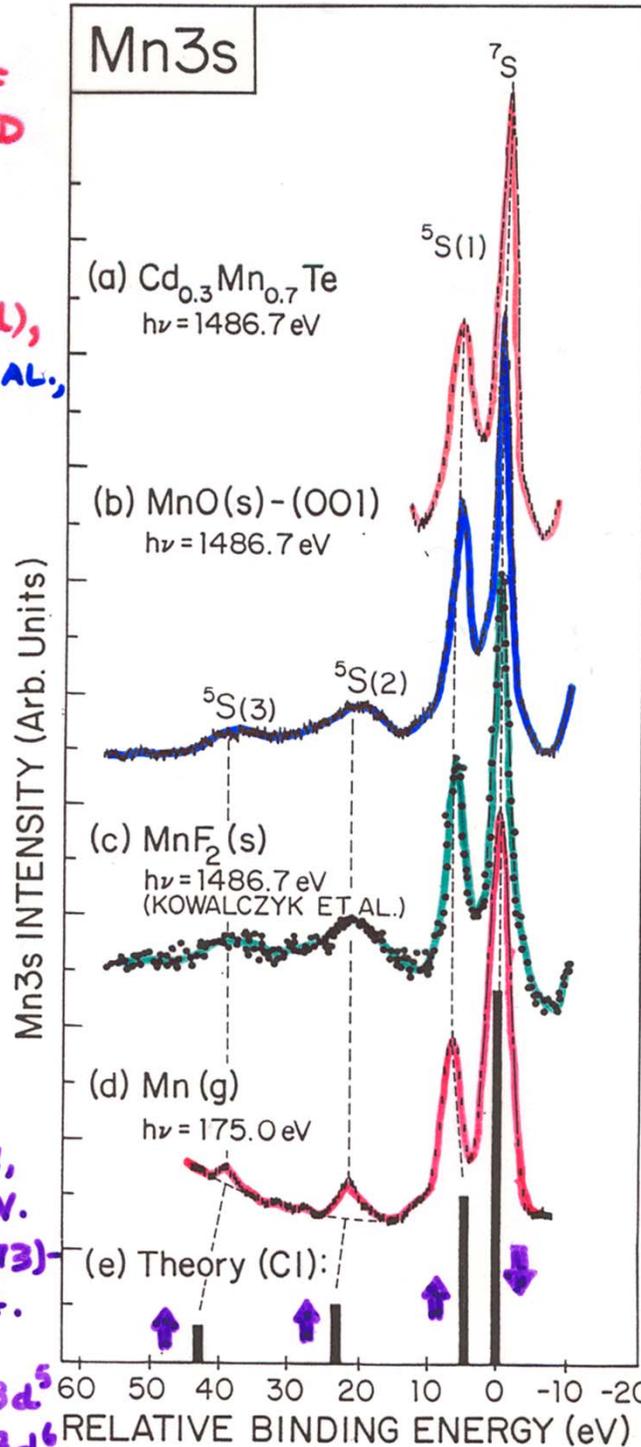
Thus, the mixing of various configurations into either the initial or final states can affect the observed intensity of a given final state appreciably, as it is only if a certain configuration has a non-zero coefficient in both states that it will contribute a non-zero  $(C_j^f)^* C_j^i$  product. For the useful limiting case in which a single configuration  $j=1$  dominates the initial state, then  $C_j^i \approx 1.0$ ,  $C_j^f \approx 0$  for  $j \neq 1$ , and the square of the matrix element (83) for transitions to a given final state is simply

$$\left| \langle \Psi^f(N) | \sum_{i=1}^N \hat{i}_i | \Psi^i(N) \rangle \right|^2 \propto |C_{1f}|^2 \quad (84)$$

(If relaxation is permitted in the final-state one-electron orbitals, then overlap integrals of the form  $\langle \Phi_m^f(N-1) | \Phi_j^i(N-1) \rangle \equiv S_{jm}$  must be computed,<sup>14</sup> and Eqs (83) and (84) become more complex. However, in general  $S_{jm} \approx \delta_{jm}$ .) Such CI effects are important in understanding the simplest forms of multiplet

COMPARISON OF  
GAS-PHASE AND  
SOLID-STATE  
SPECTRA

EXPT. : (a), (b), (d),  
HERMSMEIER ET AL.,  
PHYS. REV. LETT.  
61, 2592 (1988)  
(OUR GROUP)



Correlation  
effects through  
configuration  
interaction (CI):

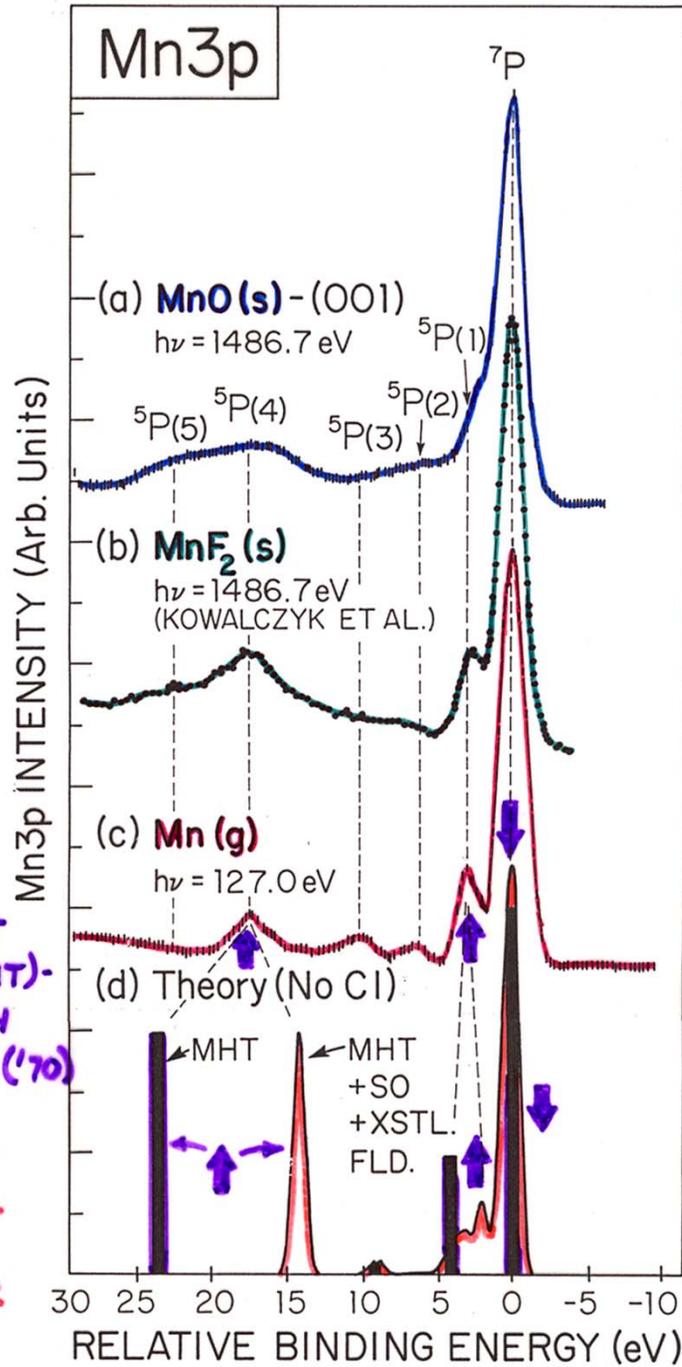
$$\Psi_{CI} = \sum_{\text{Config. } i} \Phi_i, \text{ better wave function}$$

$$= \Phi(\text{Mn}^{3+} \dots 3s^1 3p^6 3d^5) + \Phi(\text{Mn}^{3+} \dots 3s^2 3p^4 3d^6)$$

esp. anti-parallel  
electrons

THEORY:  
BAGUS, FREEMAN,  
SASAKI, PHYS. REV.  
LETT. 30, 850 (1973)  
ATOMIC CONFIG.  
INT. IN  
 $\text{Mn}^{3+} \dots 3s^1 \dots 3d^5$   
 $+ \text{Mn}^{3+} \dots 3s^2 3p^4 3d^6$

“Basic Concepts of XPS”  
Figure 33



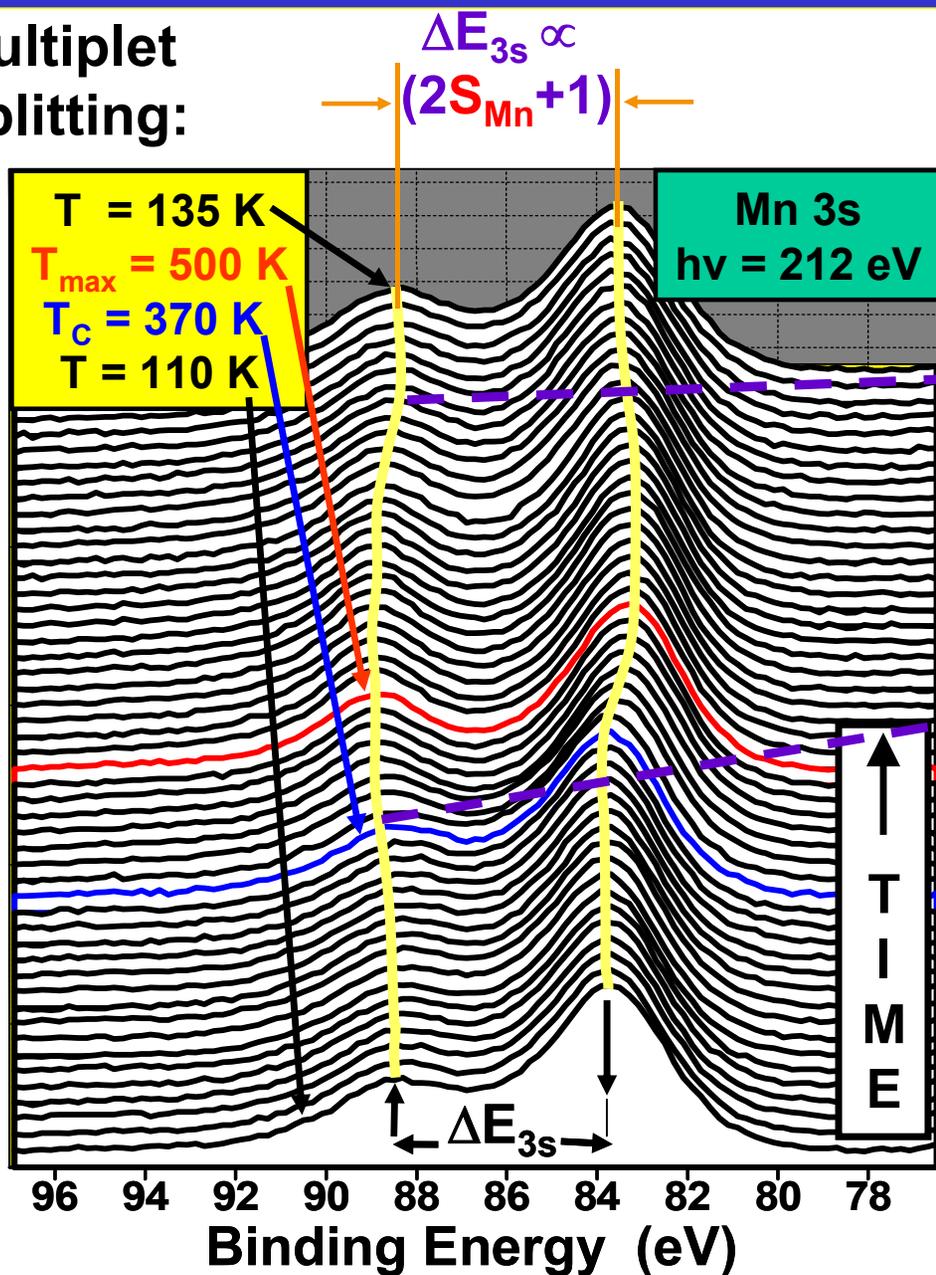
**THEORY: NO CI**  
**SIMPLE MULTIPLY  
 HOLE THEORY (MHT)-  
 FADLEY, SHIRLEY  
 PHYS. REV. A2, 1109 (70)**  
**EMPIRICAL  
 MHT WITH SPIN  
 ORBIT & CRYSTAL  
 FIELD - SUGANO  
 ET AL., J. PHYS. C  
 15, 2625 (1982)**

**HERMSMEIER  
 ET AL.,  
 P.R.L. 61, 2592 (88)**

# Case study: Temperature dependence of Mn3s and O1s spectra in a colossal magnetoresistive (CMR) oxide: $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$

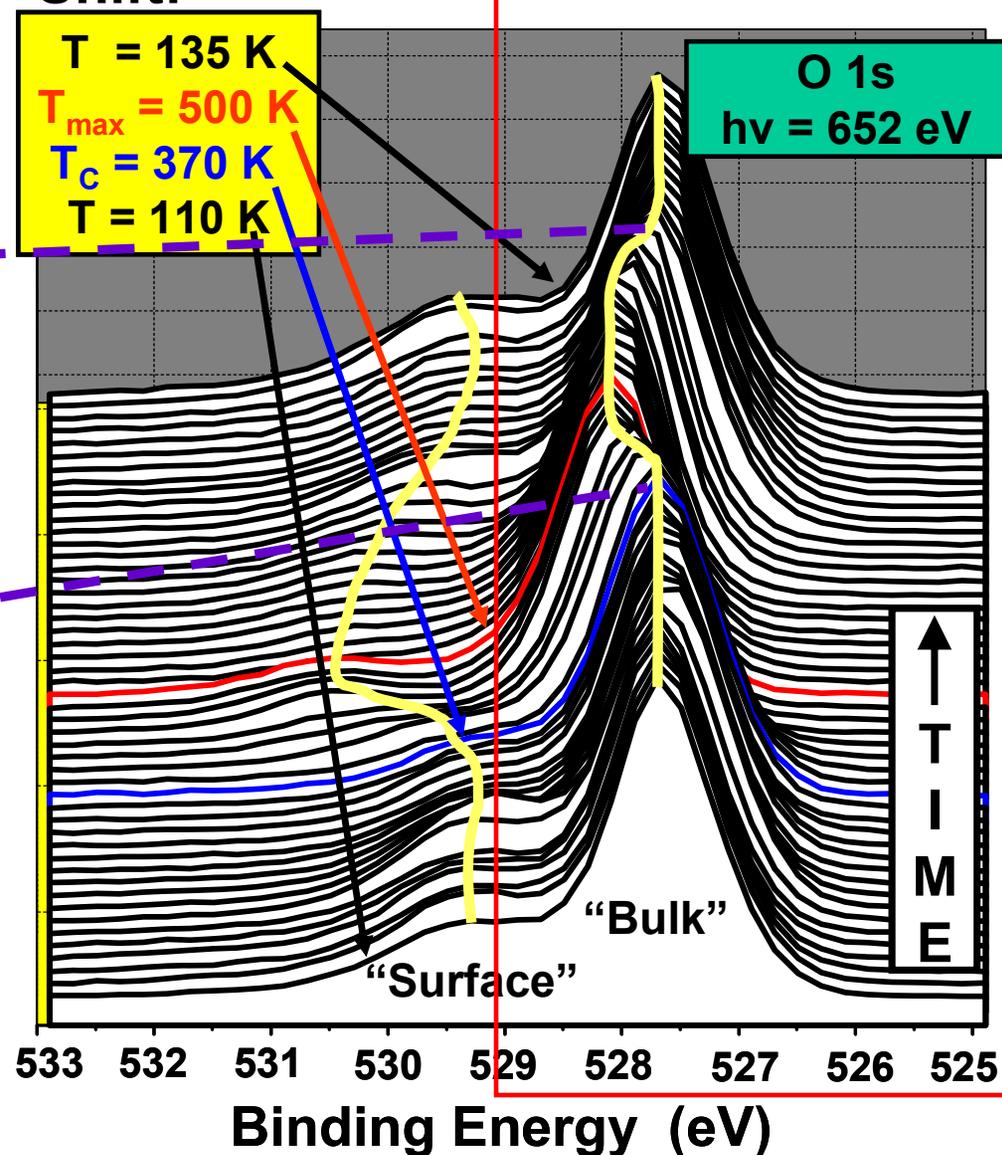
**Multiplet Splitting:**

Photoelectron Intensity (a.u.)



of the Mn3s splitting-reversible

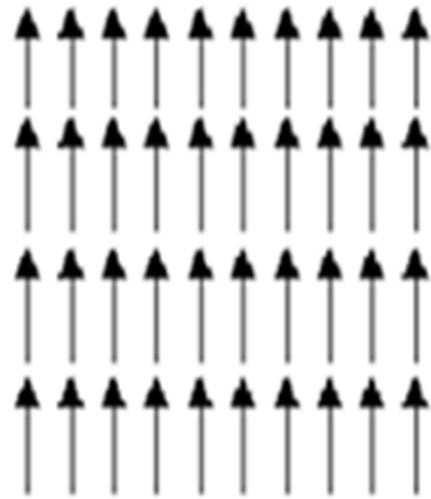
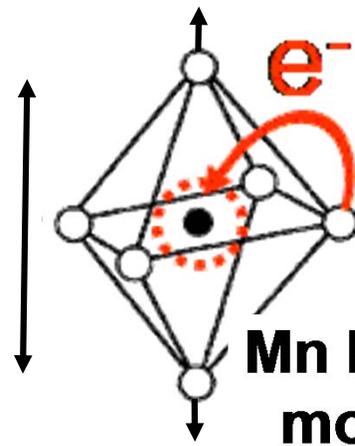
**Chemical Shift:**



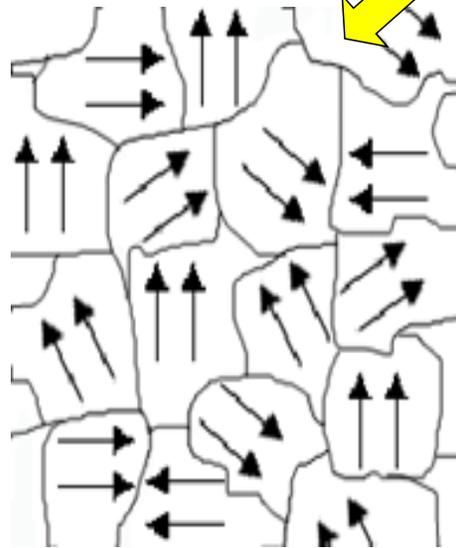
Increase of O1s BE-reversible

# Suggested scenario

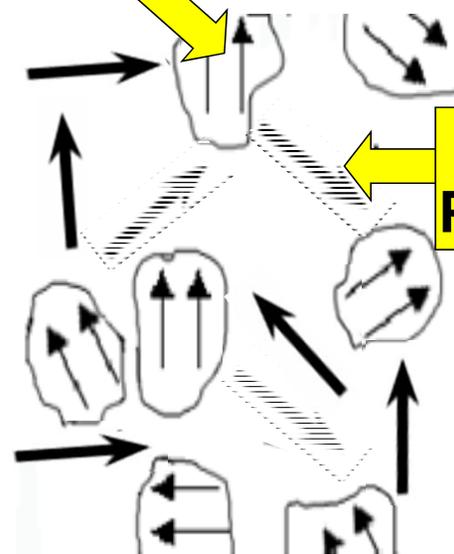
Jahn-Teller distortion



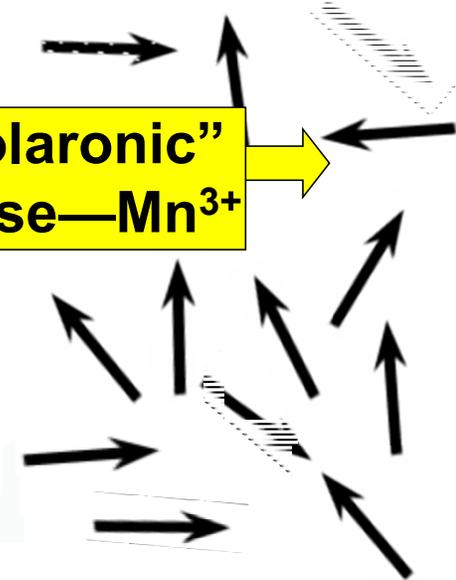
Long-range  
ferromagnetic  
order



Loss of long - range  
order at  $T_c$



Short - range order  
above  $T_c$  up to  $T_{sat}$   
Jahn-Teller distortion



Mixed  
 $Mn^{3+}$  -  $Mn^{4+}$

“Polaronic”  
Phase— $Mn^{3+}$

## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings



Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## **Valence-Level Photoemission**

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## **Some New Directions**

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

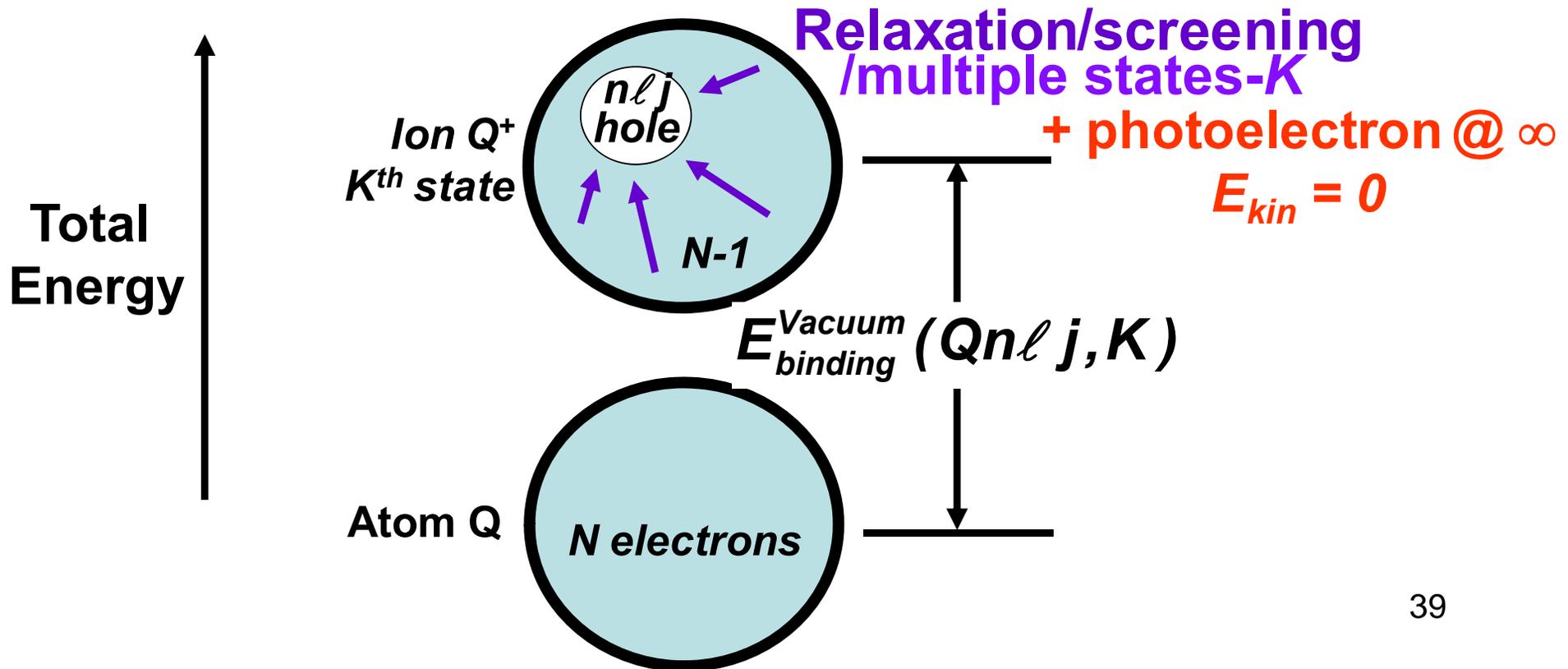
# Photoemission: The correct energy picture

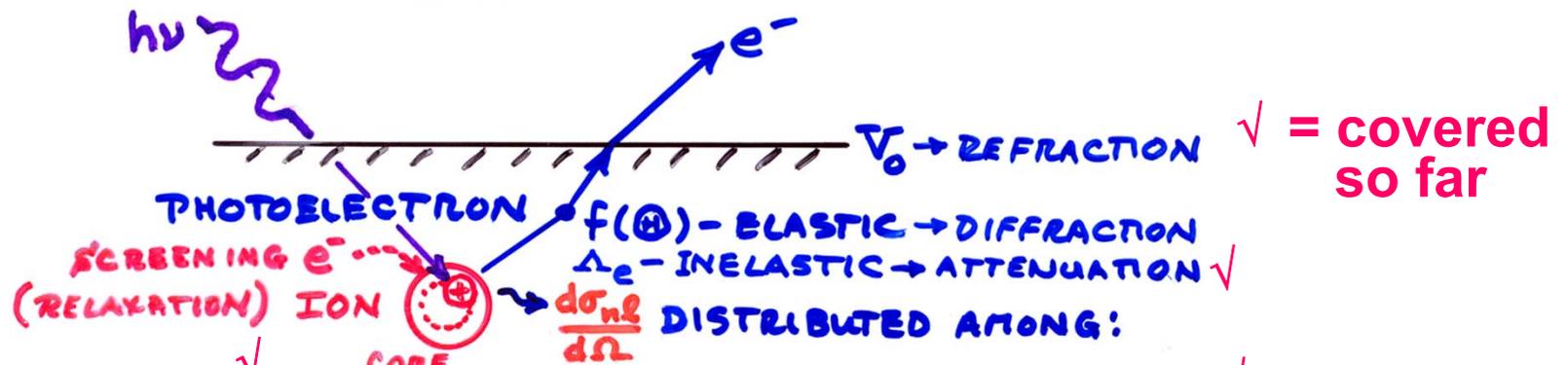
$$h\nu = E_{\text{binding}}^{\text{Vacuum}} + E_{\text{kinetic}} = E_{\text{binding}}^{\text{Fermi}} + \phi_{\text{spectrometer}} + E_{\text{kinetic}}$$

↓

$$E_{\text{binding}}^{\text{Vacuum}}(Qn\ell j, K) = E_{\text{final}}(N-1, Qn\ell j \text{ hole}, K) - E_{\text{initial}}(N)$$

= a difference of final and initial state energies

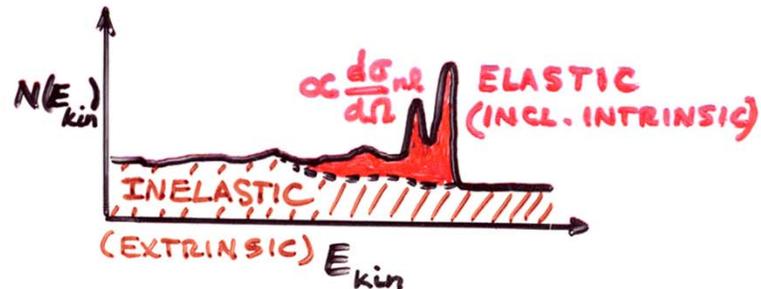




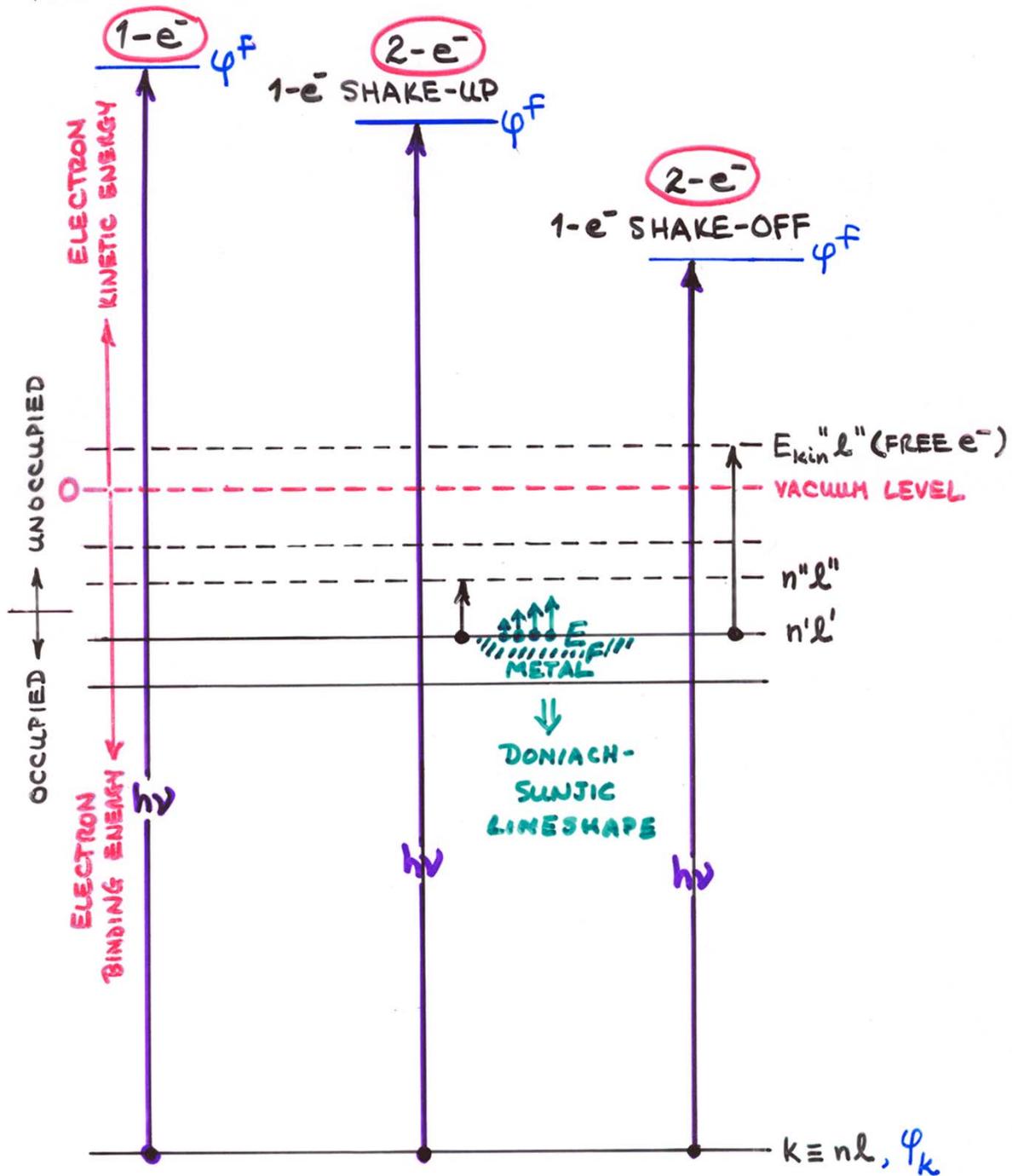
ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- ✓ CORE HOLE  $k = nl$
- ✓ SPIN-ORBIT SPLITTING (EASY) ✓
- ✓ + MULTIPLET SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD ✓
- ✓ + CORRELATION / CONFIGURATION INTERACTION ✓
- ✓ + SHAKE-UP / SHAKE-OFF /  $e^-$ -HOLE ←
- ✓ + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION
- ✓ + VIBRATIONAL EXCITATIONS
- ✓ + RESONANT PHOTOEMISSION ( $h\nu \approx E_{b, nl}$ ) ✓

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



TOTAL NO.  $e^-$ :



MULTIELECTRON EFFECTS IN CORE EMISSION

# Intensities in photoelectron spectra in the sudden approximation

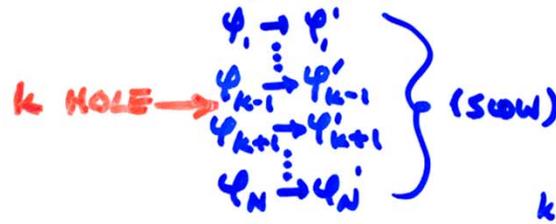
- GENERAL: FINAL STATE  $K$  ( $k$ -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_i^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPENHEIMER:  $e^-$ 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION:  $\Psi_K \rightarrow \Psi_F = \text{PHOTO}^-$  (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 |\langle \Psi_e^f(N-1, K) | \Psi_e^i(N-1, k) \rangle|^2$$

$$|\hat{e} \cdot \langle \psi_f | \vec{r} | \psi_k \rangle|^2$$

SAME SUBSHELL COUPLING + TOTAL L, S  $\rightarrow$  "MONOPOLE"

$$\rightarrow \text{NORMAL } \frac{d\sigma_K}{d\Omega}$$

- SLATER DETS. FOR  $\Psi_e^f = \det(\psi'_1, \psi'_2, \dots, \psi'_{k-1}, \psi'_{k+1}, \dots, \psi'_N)$

$$\Psi_e^i = \det(\psi_1, \psi_2, \dots, \psi_{k-1}, \psi_{k+1}, \dots, \psi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, v}^f | \Psi_{\text{vib}, v}^i \rangle|^2 |\langle \psi'_1 | \psi_1 \rangle|^2 |\langle \psi'_2 | \psi_2 \rangle|^2 \dots$$

$$|\langle \psi'_{k-1} | \psi_{k-1} \rangle|^2 |\langle \psi'_{k+1} | \psi_{k+1} \rangle|^2 \dots |\langle \psi'_N | \psi_N \rangle|^2$$

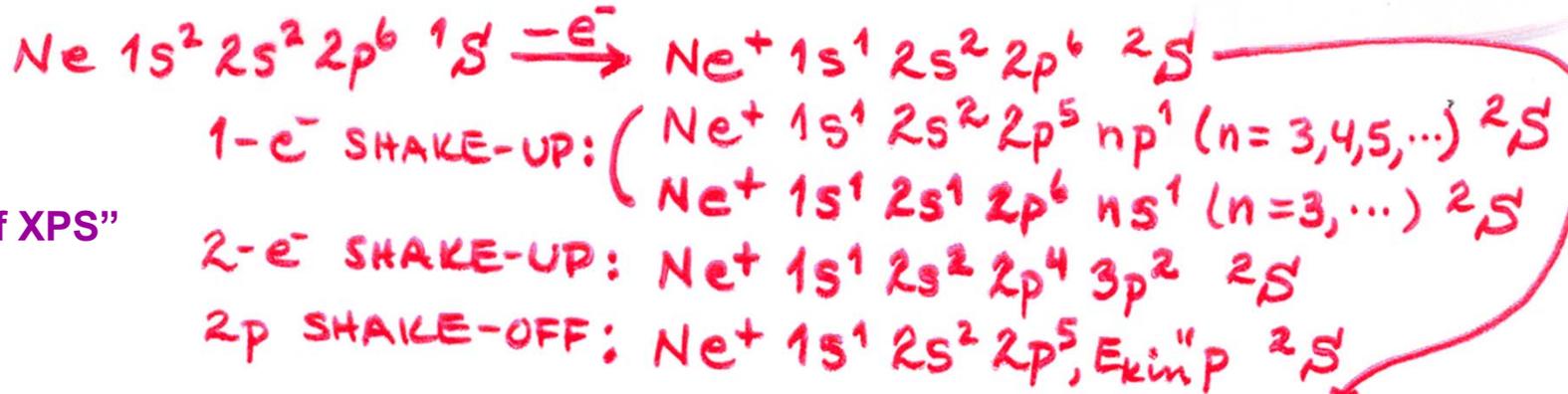
$$|\hat{e} \cdot \langle \psi_f | \vec{r} | \psi_k \rangle|^2$$

$1e^-$  DIPOLE  $\rightarrow d\sigma/d\Omega$

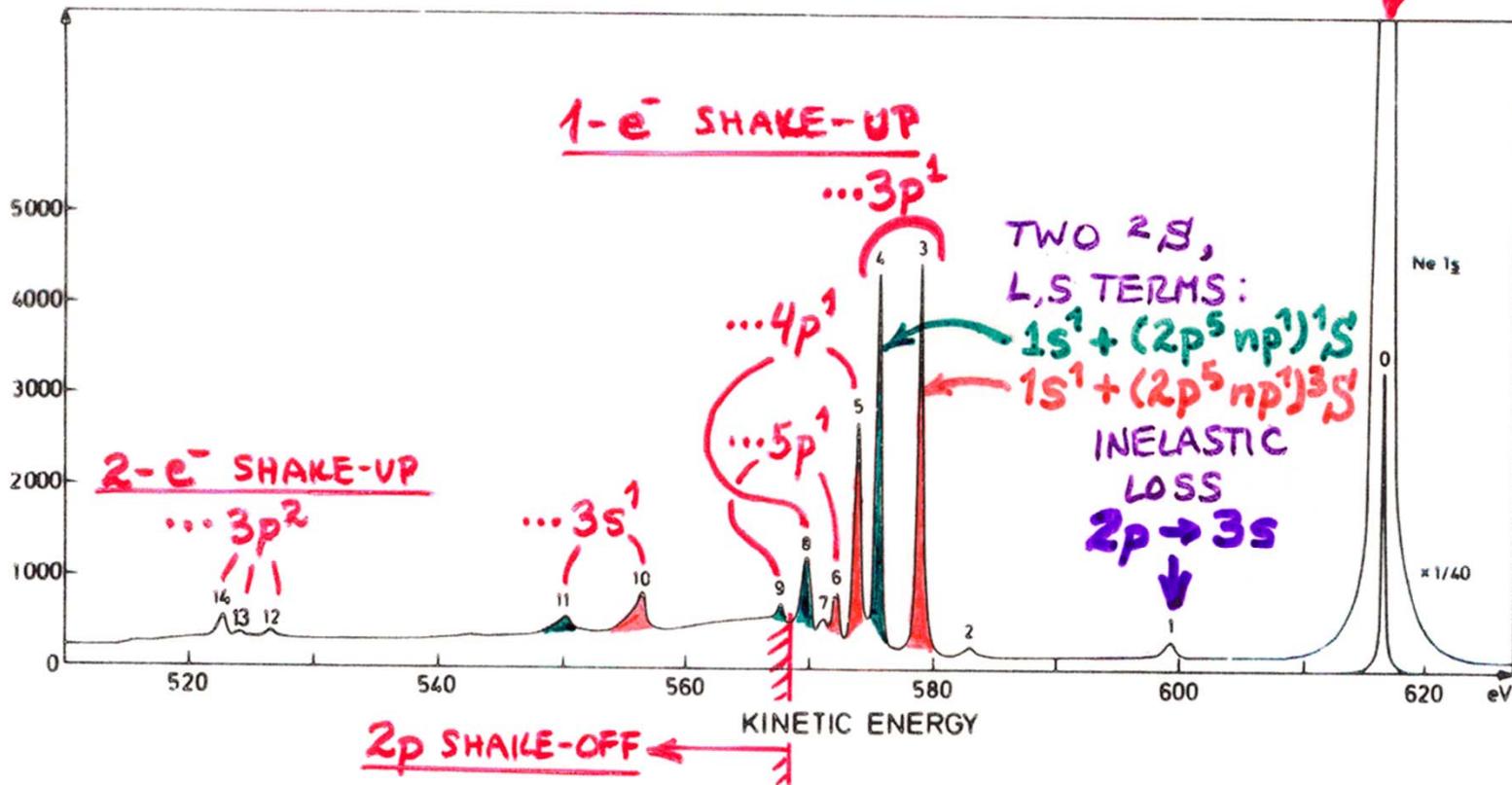
( $N-1$ ) $e^-$  SHAKE-UP/  
SHAKE-OFF  $\rightarrow$   
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN  $\Psi_f$  ESCAPE

# Neon 1s shake-up and shake-off

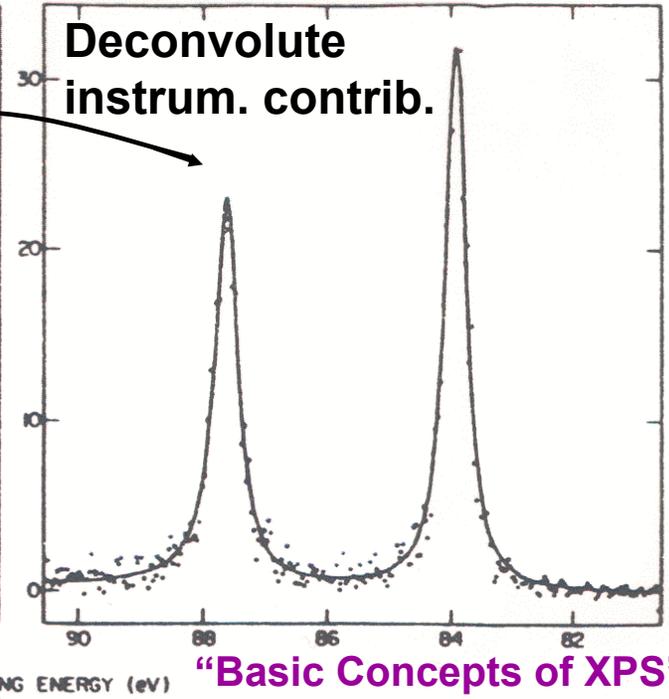
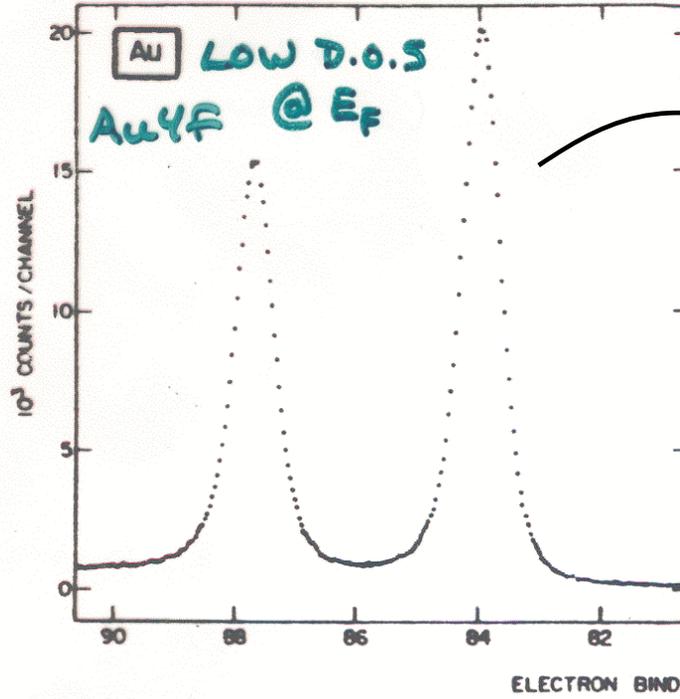
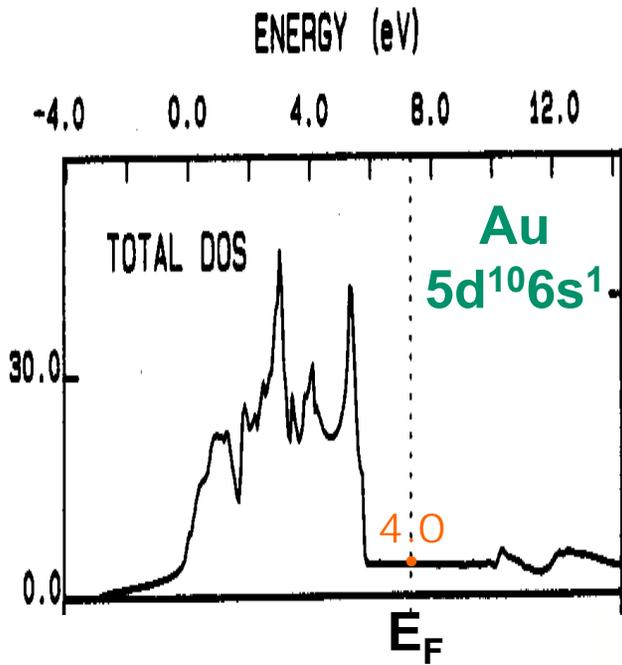


“Basic Concepts of XPS”  
Figure 36

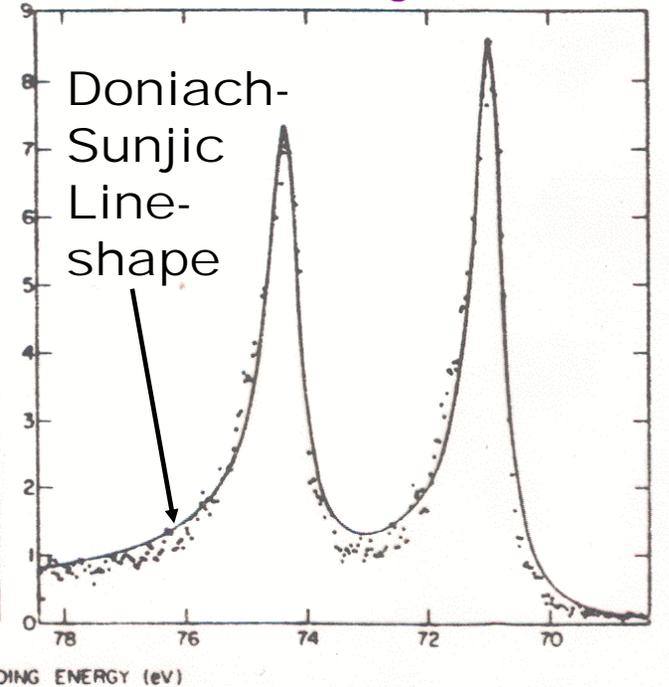
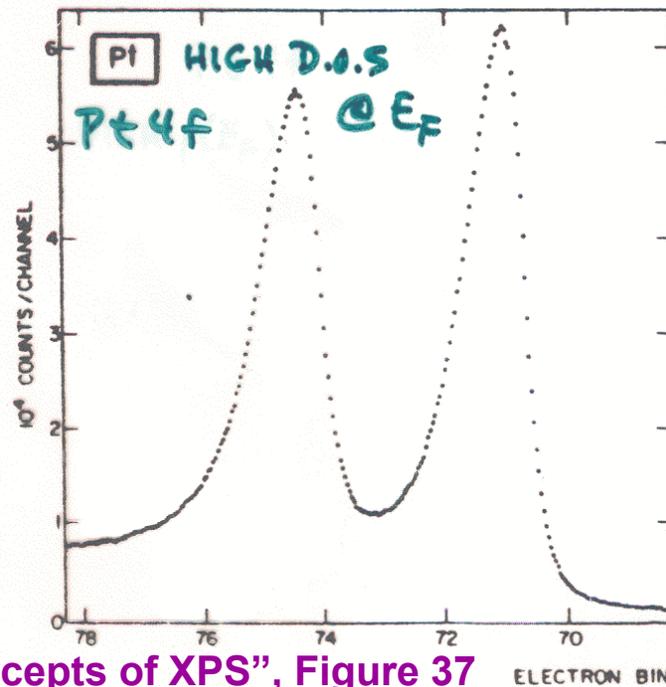
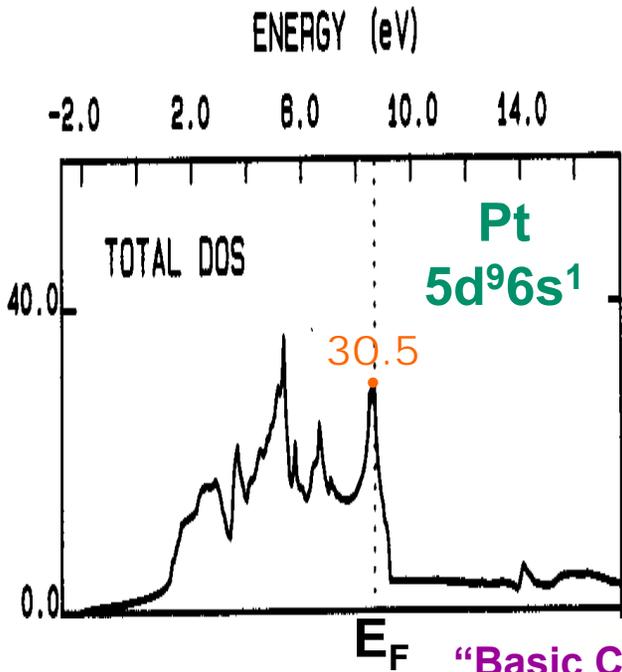


**OVERALL: ~12% SHAKE-UP + 16% SHAKE-OFF  $\approx$  28% OF EVENTS**

# Shake-up like excitations in metals



“Basic Concepts of XPS”  
Figure 10



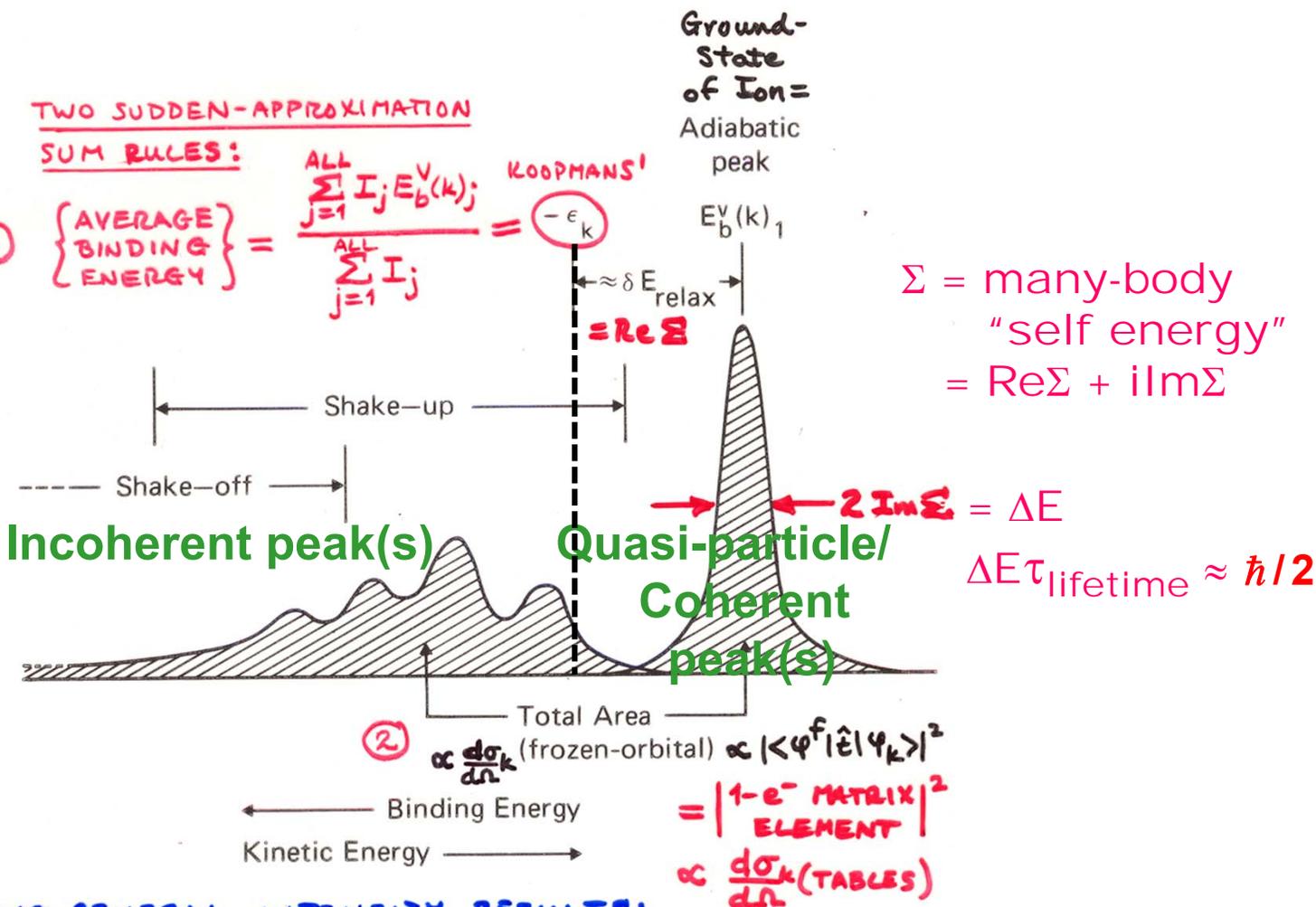
“Basic Concepts of XPS”, Figure 37

**Global sum rules and many-electron description of photoemission**

TWO SUDDEN-APPROXIMATION

SUM RULES:

①  $\left\{ \text{AVERAGE BINDING ENERGY} \right\} = \frac{\sum_{j=1}^{\text{ALL}} I_j E_b^V(k)_j}{\sum_{j=1}^{\text{ALL}} I_j} = \text{Koopmans' } -\epsilon_k$

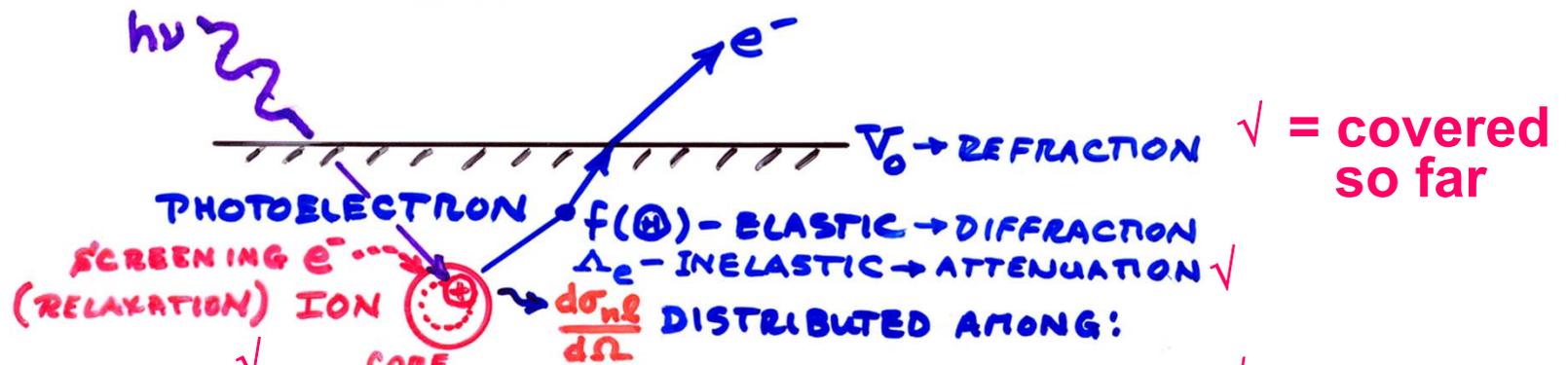


TWO GENERAL INTENSITY RESULTS:

①  $I_j \propto |\langle \psi^f_{(1)} | \hat{\epsilon} | \psi_k_{(1)} \rangle|^2 |\langle \Psi^F_{(N-1,j)} | \Psi^R_{(N-1)} \rangle|^2$   
k e<sup>-</sup> MISSING

Figure 8 -- Schematic illustration of a photoelectron spectrum involving shake-up and shake-off satellites. The weighted average of all binding energies yields the Koopmans' Theorem binding energy  $-\epsilon_k$  (sum rule (77)), and the sum of all intensities is proportional to a frozen-orbital cross section  $\sigma_k$  (sum rule (78)). The adiabatic peak corresponds to formation of the ground-state of the ion ( $E_b(k)_1 \equiv E_b(k=1)$ ).

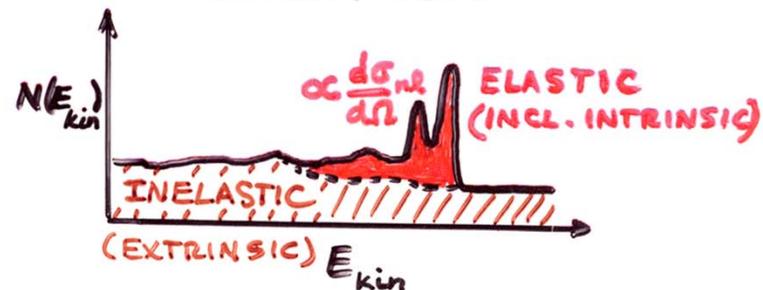
②  $\left( \text{TOTAL SHAKE-UP} + \text{SHAKE-OFF} \right) = 1 - |\langle \Psi^F_{(N-1,1)} | \Psi^R_{(N-1)} \rangle|^2 \approx 15 - 25 \% \text{ FOR ATOMS/MOLEC.}$



ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- ✓ CORE HOLE  $k = nl$
- ✓ SPIN-ORBIT SPLITTING (EASY) ✓
- ✓ + MULTIPLET SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD ✓
- ✓ + CORRELATION / CONFIGURATION INTERACTION ✓
- ✓ + SHAKE-UP / SHAKE-OFF /  $e^-$ -HOLE ✓
- ✓ + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION ←
- ✓ + VIBRATIONAL EXCITATIONS
- ✓ + RESONANT PHOTOEMISSION ( $h\nu \approx E_{b, nl}$ ) ✓

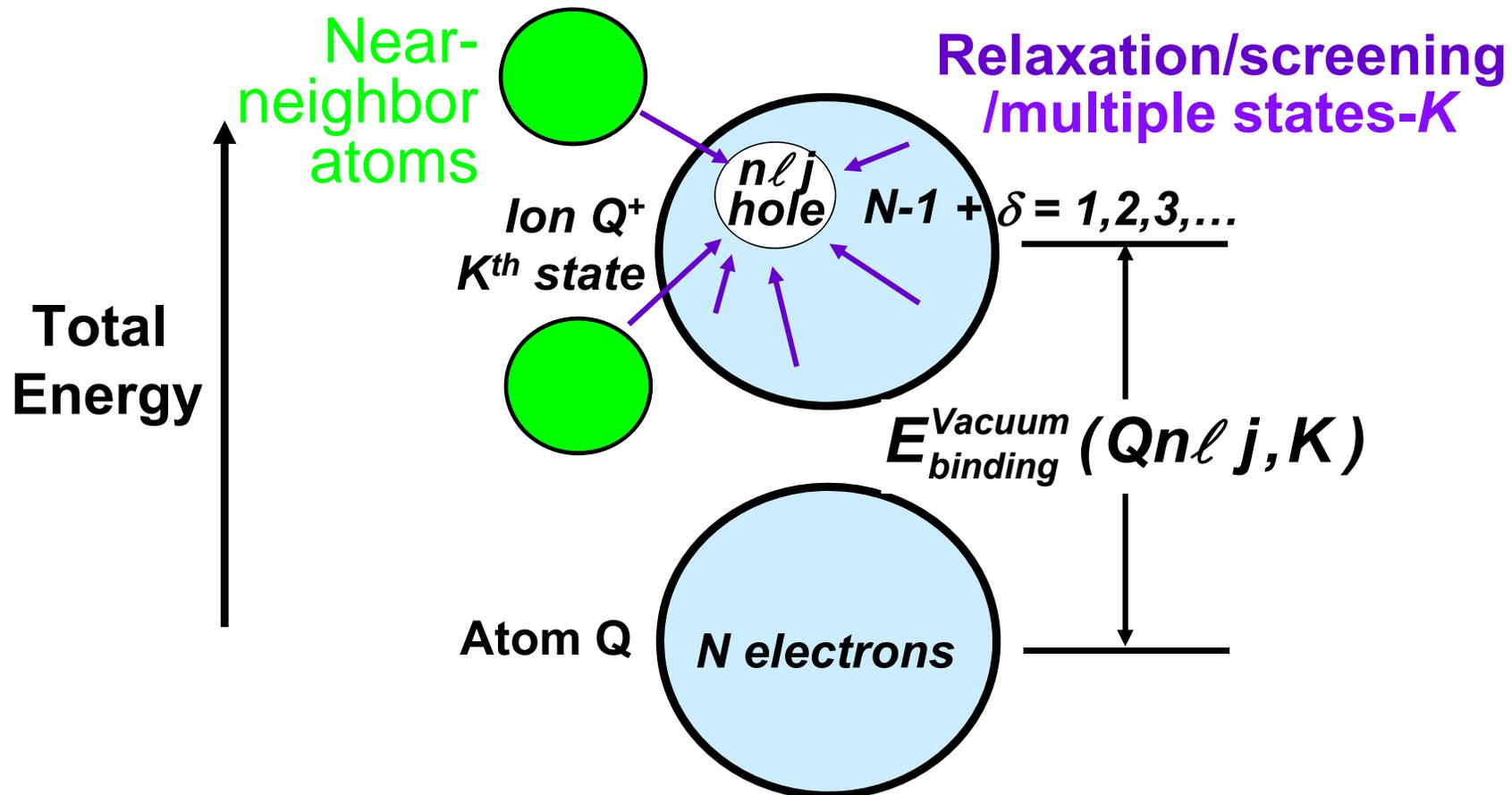
REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



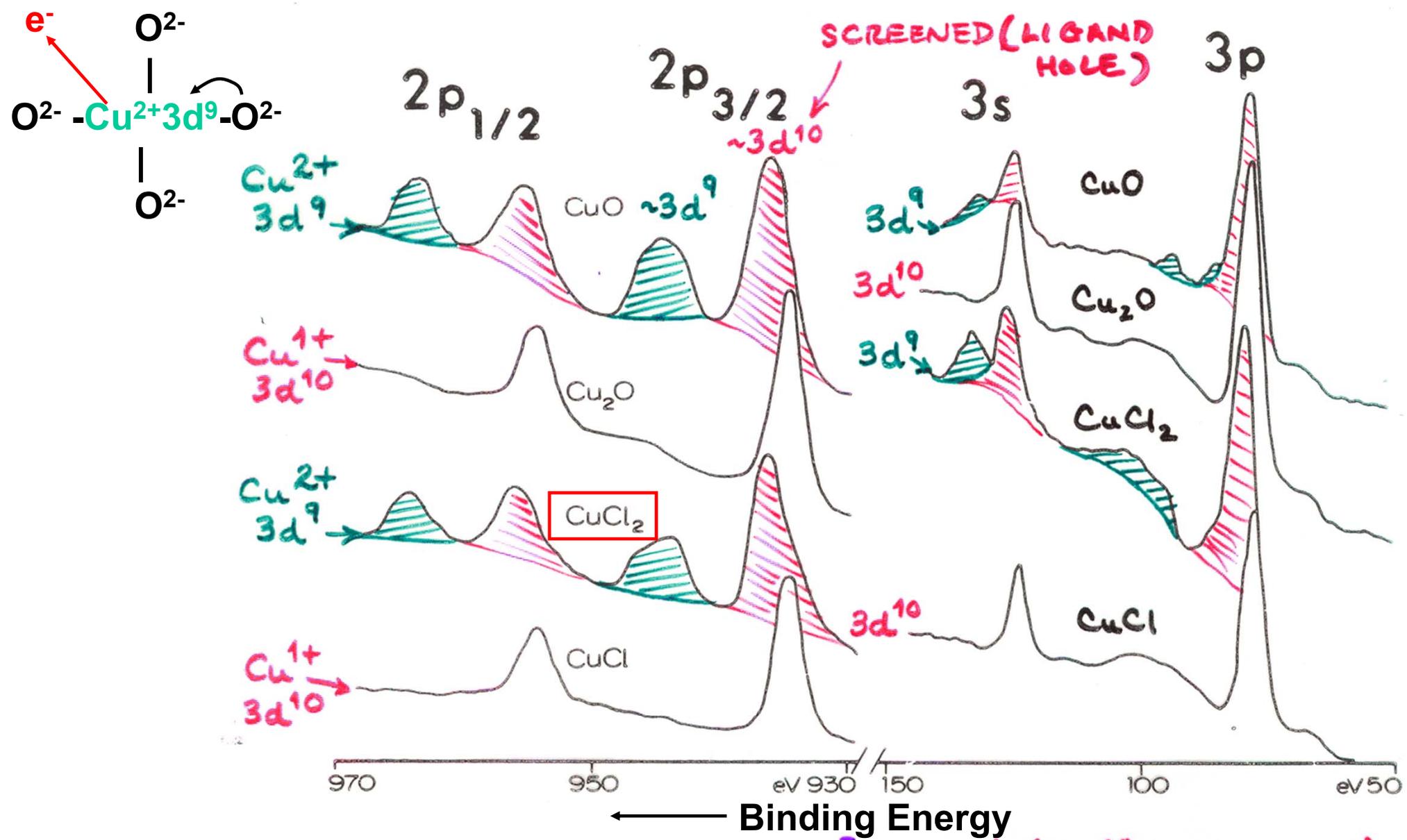
# Basic energetics—Many e<sup>-</sup> & many atom picture

$$h\nu = E_{\text{binding}}^{\text{Vacuum}} + E_{\text{kinetic}} = E_{\text{binding}}^{\text{Fermi}} + \phi_{\text{spectrometer}} + E_{\text{kinetic}}$$

$$E_{\text{binding}}^{\text{Vacuum}}(Qn\ell j, K) = E_{\text{final}}(N-1, Qn\ell j \text{ hole}, K) - E_{\text{initial}}(N)$$

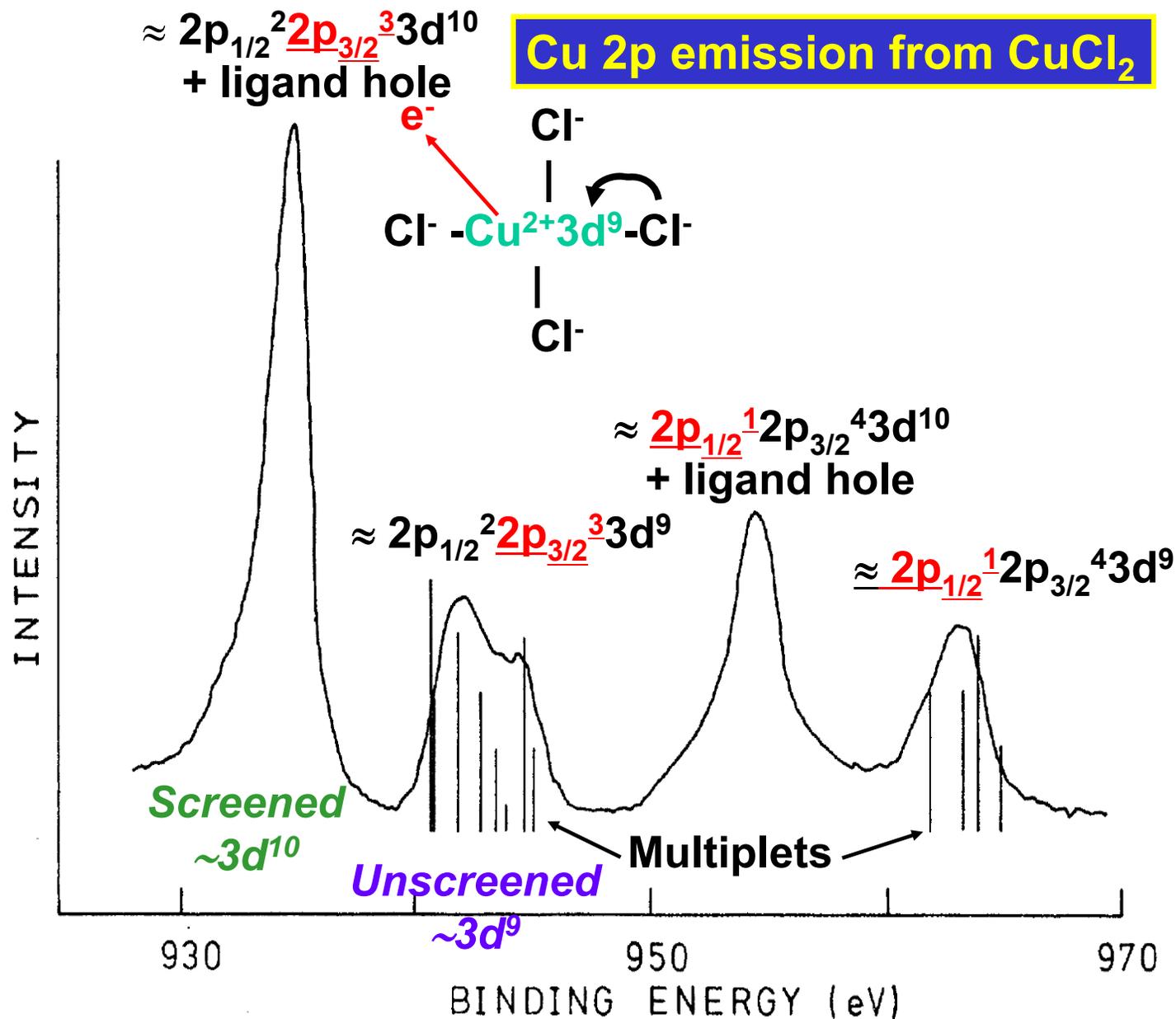


# Satellites & charge-transfer screening



“Basic Concepts of XPS” **ACTUAL FINAL STATE  $\Psi \approx C_1 \phi_1 (3d^{10} - \text{SCREENED}) + C_2 \phi_2 (3d^9 - \text{UNSCREENED})$**

Figure 38



$$\Psi_{final,K}(N-1) = C_{1,K}(2p_{1/2}^2 2p_{3/2}^3 3d^{10} + Cl \text{ hole}) + C_{2,K}(2p_{1/2}^2 2p_{3/2}^3 3d^9)$$

$$I_{final,K}(N-1) \propto |C_{2,K}(2p_{1/2}^2 2p_{3/2}^3 3d^9)|^2$$

Screening depends on ionicity/covalency → satellite intensities can be used to measure interaction parameters

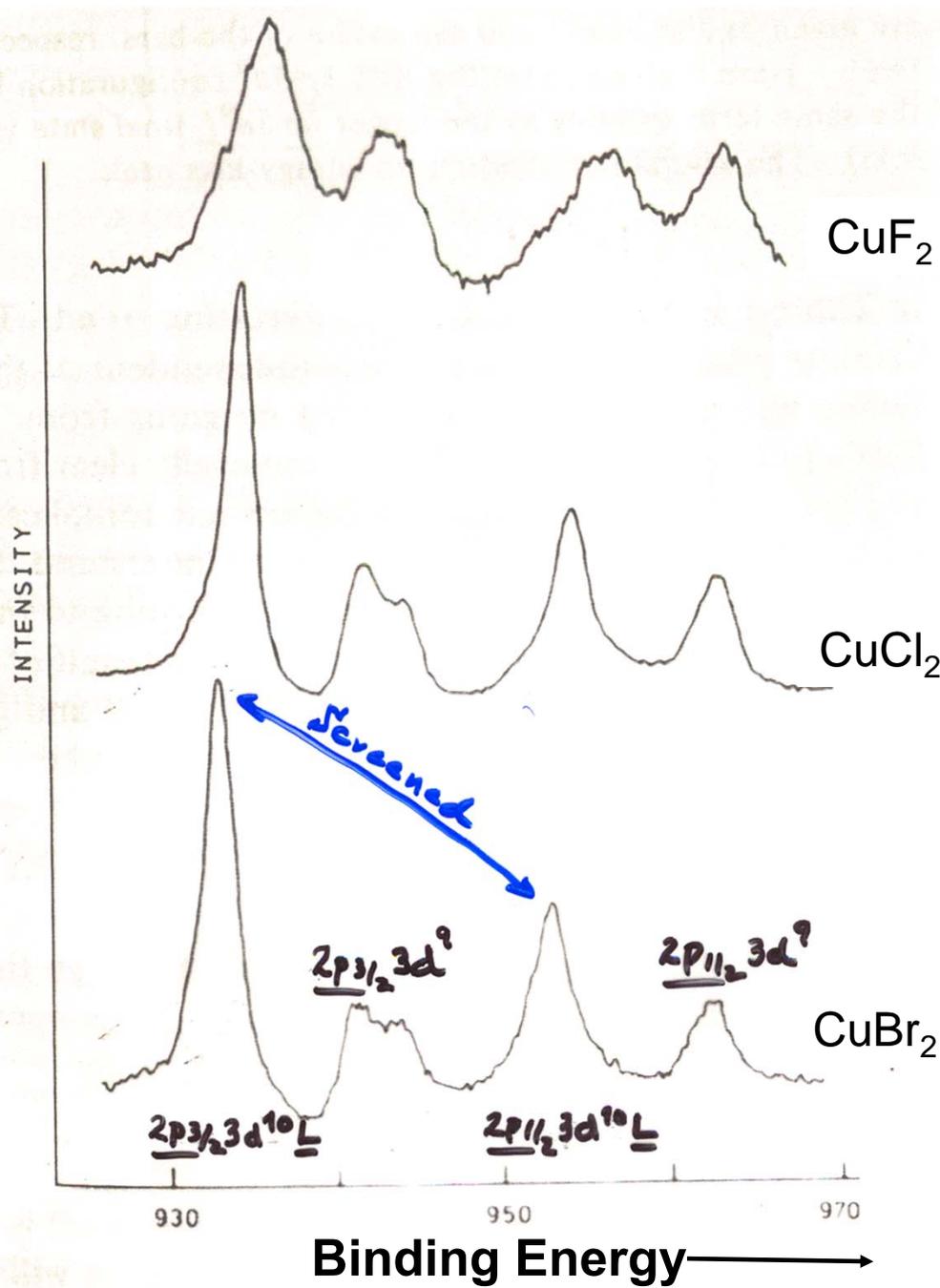
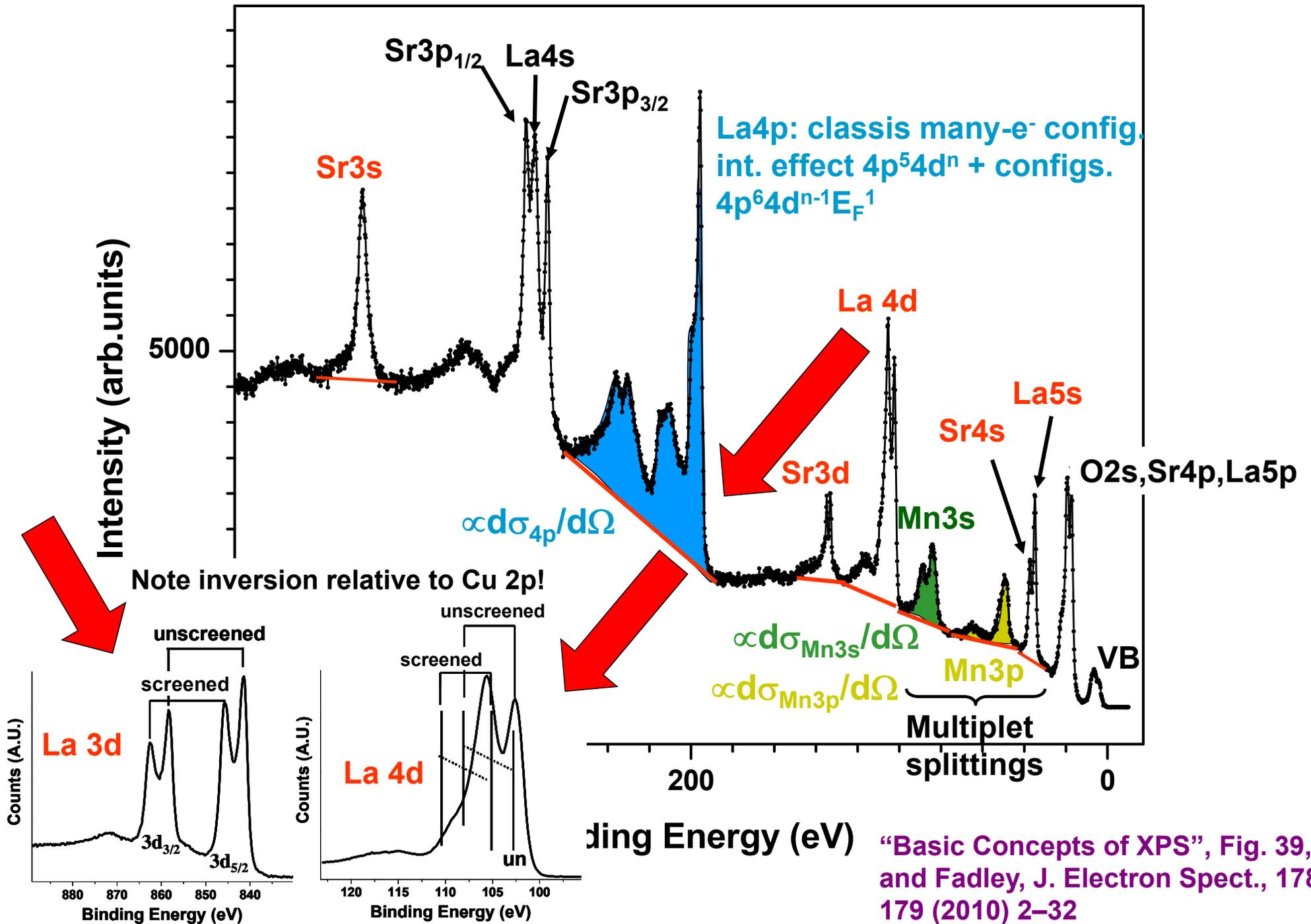
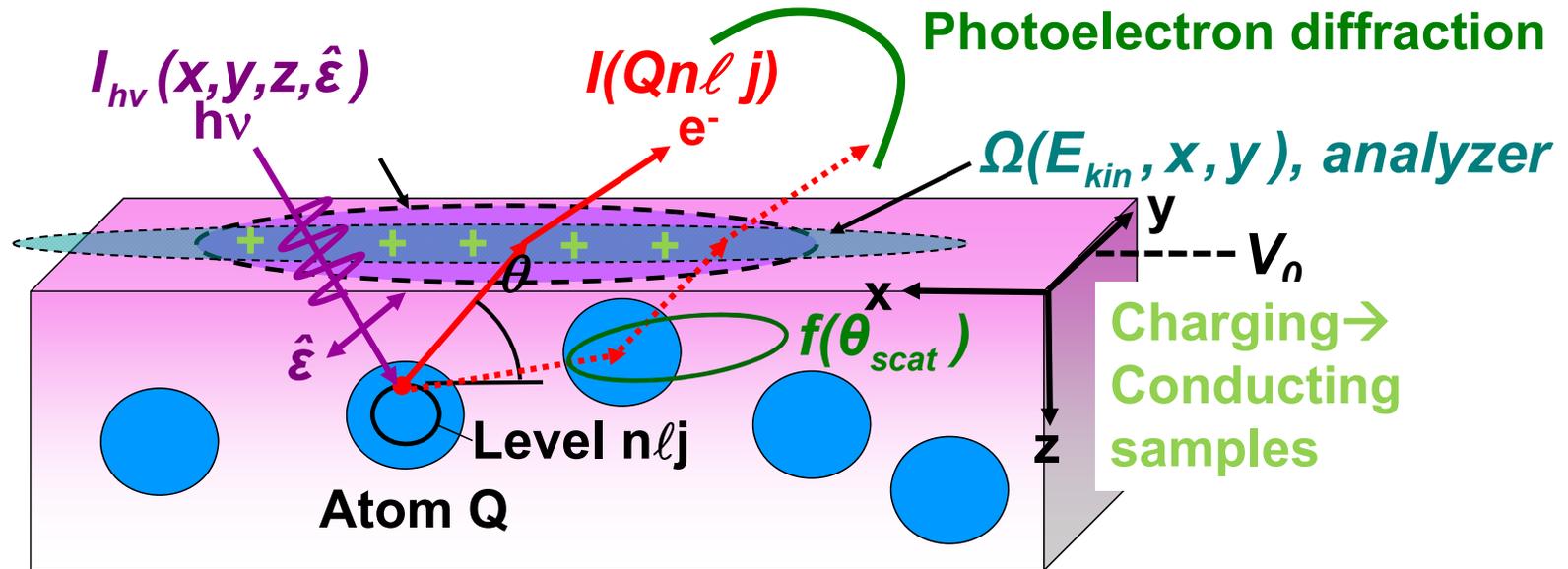


FIG. 1. Cu 2p photoelectron spectra of Cu dihalides. The lines leading to a final state with a ligand hole ( $\underline{L}$ ) show a chemical shift.

Many-electron and screening effects:  $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ ,  $h\nu = 7700 \text{ eV}$



# ATOMIC (CORE) PHOTOELECTRON INTENSITIES: THE "FOUR-STEP" MODEL



$I(Qn\ell j) =$  Non-dipole effects\* and resonant interchannel#

$$C \int_0^{\infty} I_{h\nu}(x, y, z, \hat{\epsilon}) \rho_Q(x, y, z) \frac{d\sigma_{Qn\ell j}(h\nu, \hat{\epsilon})}{d\Omega} \exp\left[-\frac{z}{\Lambda_e(E_{kin}) \sin\theta}\right] \Omega(E_{kin}, x, y) dx dy dz$$

$I_{h\nu}(x, y, z, \hat{\epsilon}) =$  x-ray flux,  $\hat{\epsilon}$  = polarization

$\rho_Q(x, y, z) =$  density of atoms Q  $\rightarrow$  quantitative analysis

Energy dependent factors needing calibration at usual XPS energies  $\sim 1$  keV

$\frac{d\sigma_{Qn\ell j}(h\nu, \hat{\epsilon})}{d\Omega} =$  energy-dependent differential photoelectric cross section for subshell  $Qn\ell j$

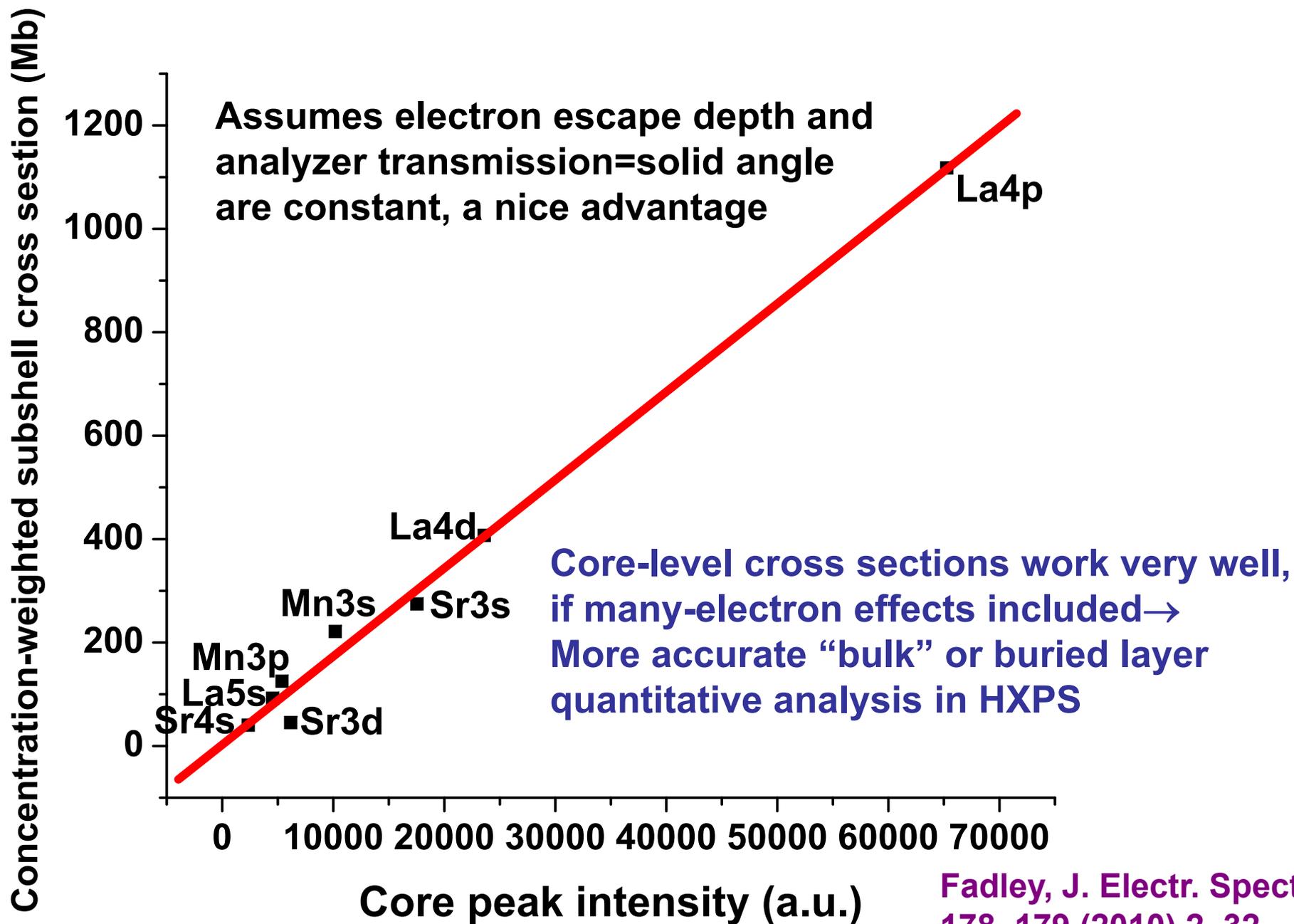
$\Lambda_e(E_{kin}) =$  energy-dependent inelastic attenuation length + elastic scattering:  $f(\theta_{scatt})$   
 $\rightarrow$  Effective Attenuation Length (EAD)  $\rightarrow$  Mean Emission Depth (MED)

$\Omega(E_{kin}, x, y) =$  energy-dependent analyzer acceptance solid angle = transmission function

$V_0 =$  inner potential

#Guilleumin et al., Radiation Physics and Chemistry 75, 2258 (2006)  
 #Drube et al., J. Phys. B: At. Mol. Opt. Phys. 46, 245006 (2013)

**Quantitative analysis of peak intensities using theoretical cross sections (Scofield) and hard x-ray excitation:  $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ ,  $h\nu = 7700$  eV**



Screening depends on ionicity/covalency → satellite intensities can be used to measure interaction parameters

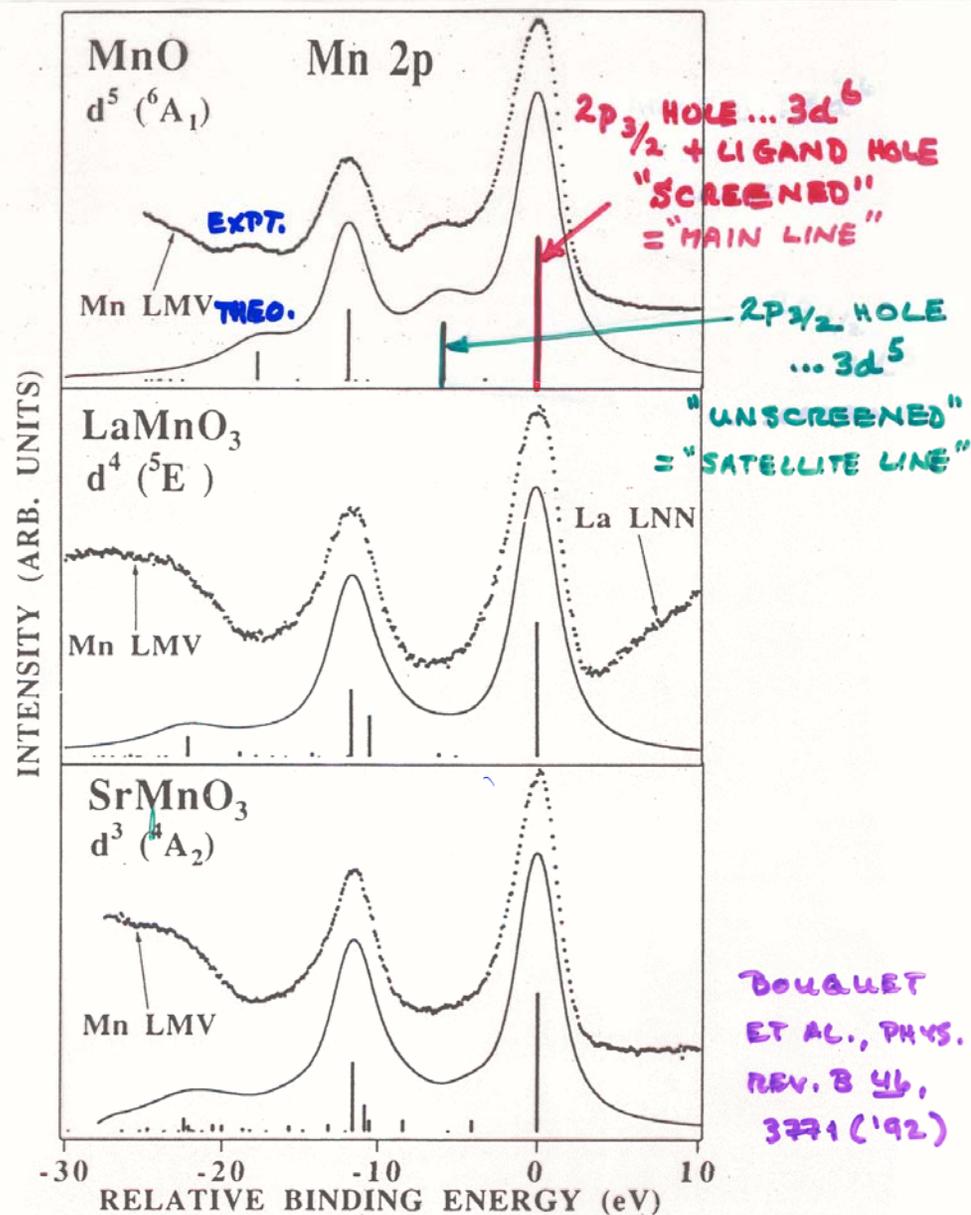
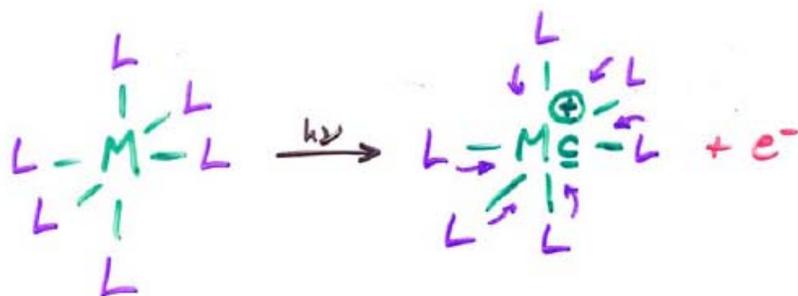


FIG. 1. Theoretical 2p core-level XPS spectra (solid line) compared with experimental data (dots) after background subtraction for Mn cations with varying valence. Emission due to the Mn LMV Auger peak is observed on the high-binding-energy side of the 2p<sub>1/2</sub> spin-orbit peak, partially obscuring the 2p<sub>1/2</sub> satellite structure.

# Localized configuration interaction approach to spectrum simulation: Hubbard Model → Anderson impurity model for PS, XAS, XES

(SUGANO, LARSSON → SAWATSKY, VANDER LAAN, FUJIMORI, OH, ET AL.)



$\underline{c}$  = CORE HOLE ON METAL  
 $\underline{l}$  = VALENCE (?) HOLE ON LIGAND

$$\psi_i = a_0 |d^n\rangle + \sum_m a_m |d^{(n+m)} \underline{l}^m\rangle$$

$$\psi_f = b_0 |\underline{c} d^n\rangle + \sum_m b_m |\underline{c} d^{(n+m)} \underline{l}^m\rangle$$

WITH INTERACTIONS OF:

$\Delta_{0d}$  = CRYSTAL FIELD (OFTEN NEGLECTED)

$\Delta$  = LIGAND-TO-METAL CHARGE TRANSF. ENERGY  
=  $E(d^{n+1} \underline{l}) - E(d^n)$

$U_{dd} = U$  = d-d COULOMB REPULSION ENERGY  
=  $E(d^{n-1}) + E(d^{n+1}) - 2E(d^n) \approx J_{dd}$

$T$  = LIGAND p-TO-METAL d HYBRIDIZATION  
=  $\langle d_\alpha | \hat{H} | p_\alpha \rangle$  ( $\alpha$  = SAME SYMMETRY)

$U_{cd} = Q$  = CORE-HOLE-TO-d INTERACTION:  $\langle \underline{c} | \hat{H} | d \rangle \approx J_{cd}$  = coulomb integral

Good discussion of model:  
Bocquet & Fujimori, J. Elect.  
Spect. & Rel. Phen. 82, 87  
(1996)-at course website

$$\rho(e_k) = \sum_f |\langle \psi_f | c | \psi_g \rangle|^2 \delta(h\nu - e_k - E_f)$$

By now:  
CTM4XAS program  
for calculating this  
for some cases:

<http://www.anorg.chem.uu.nl/CTM4XAS/Updates>

WITH INTENSITIES FROM SUDDEN APPROX.

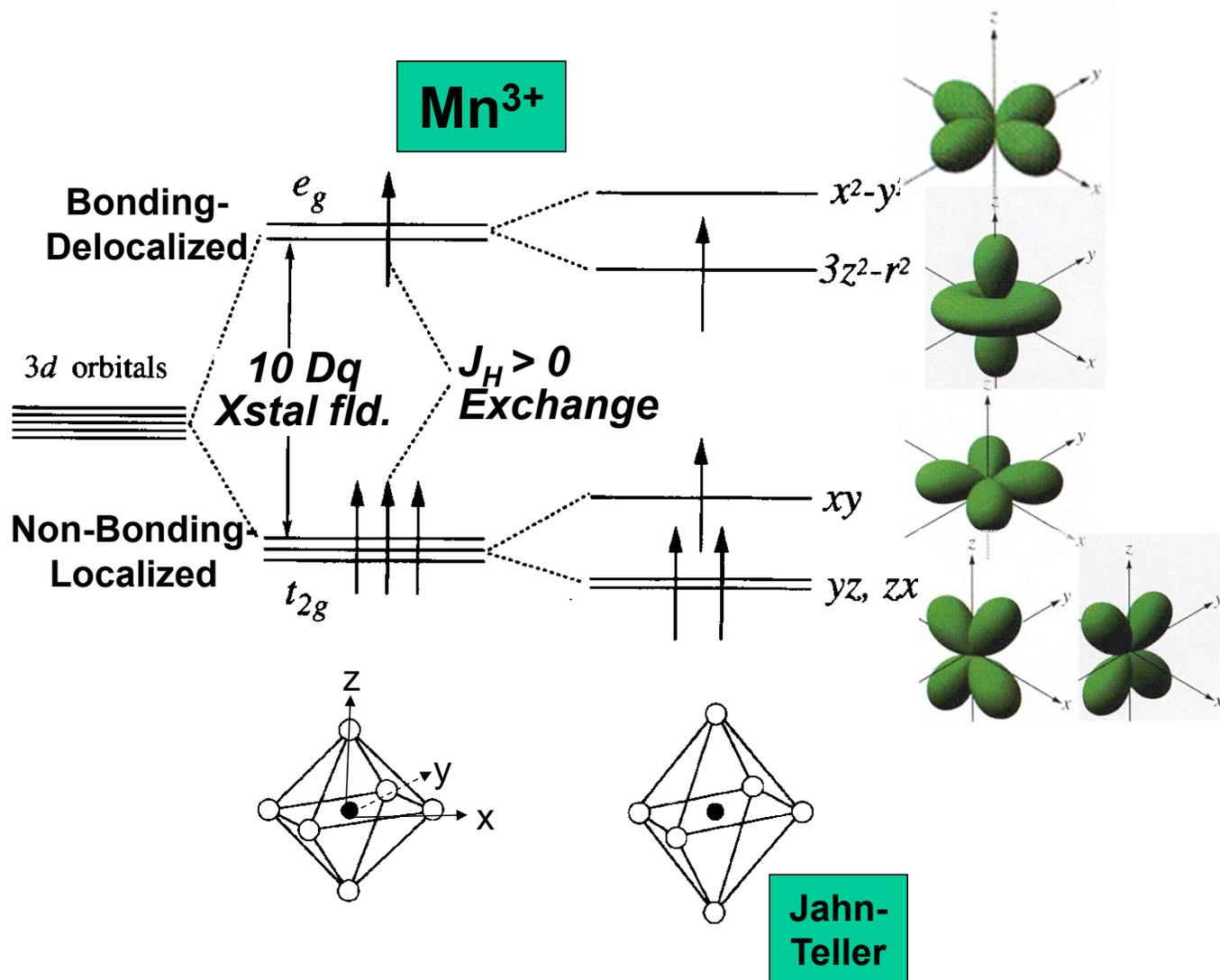
AS:

$$I(E_{kin}) \propto \sum_{f,k} |\langle \psi_f(N-1,k) | \psi_i(N-1,k) \rangle|^2 \delta(h\nu - E_f - E_{kin})$$

$\underline{c} = \underline{c}$  = CORE HOLE

WHERE:  $\psi_i(N-1,k) = \psi_i(N \text{ WITH } k \text{ HOLE} = \underline{c})$

# E.g.—Crystal field in $Mn^{3+}$ with negative octahedral ligands



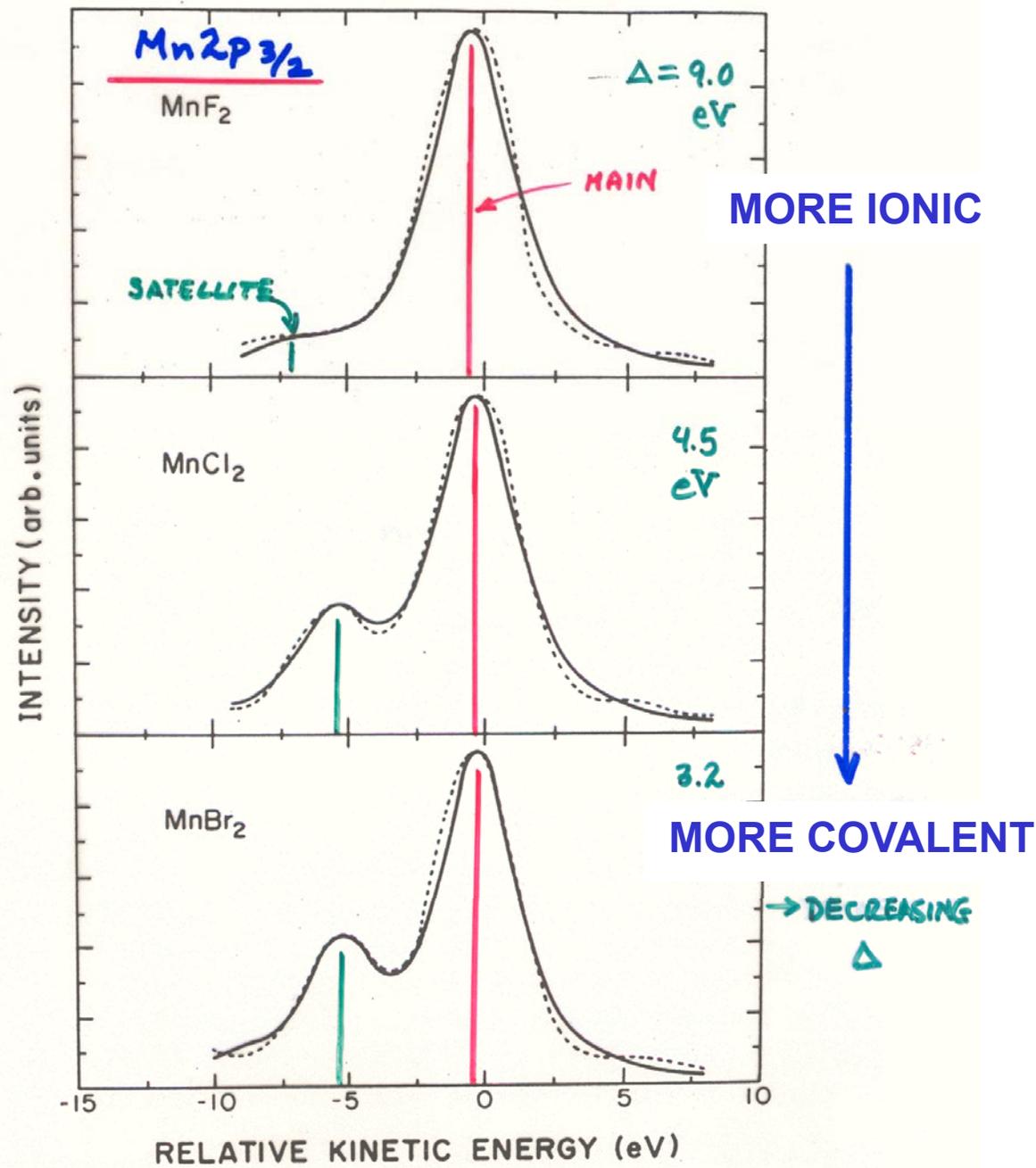
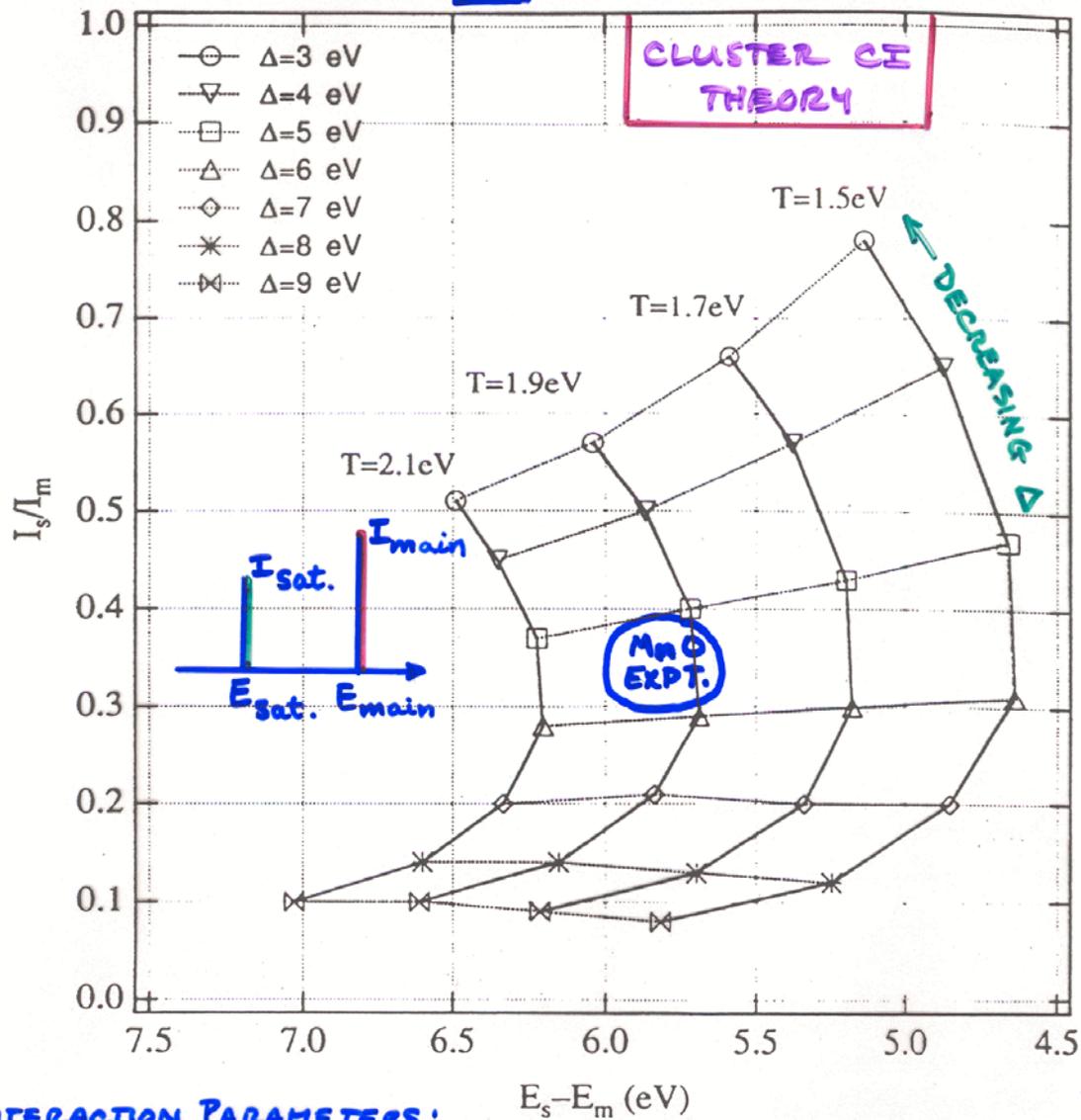


FIG. 6. Fits of the cluster model results with the experimental  $2p_{3/2}$  spectra of the manganese dihalides. The parameters used are listed in Table II. A Lorentzian broadening is 2.6–3.0 eV, and a Gaussian broadening of 1.2 eV (FWHM) was used.

# ANALYSIS VIA ANDERSON IMPURITY MODEL

$\text{Mn}^{2+}(\text{HS})$   $U=6.0$  eV



INTERACTION PARAMETERS:

$U$  = 3d-3d COULOMB REPULSION ENERGY

$\Delta$  = LIGAND-TO-METAL CHARGE TRANSFER ENERGY

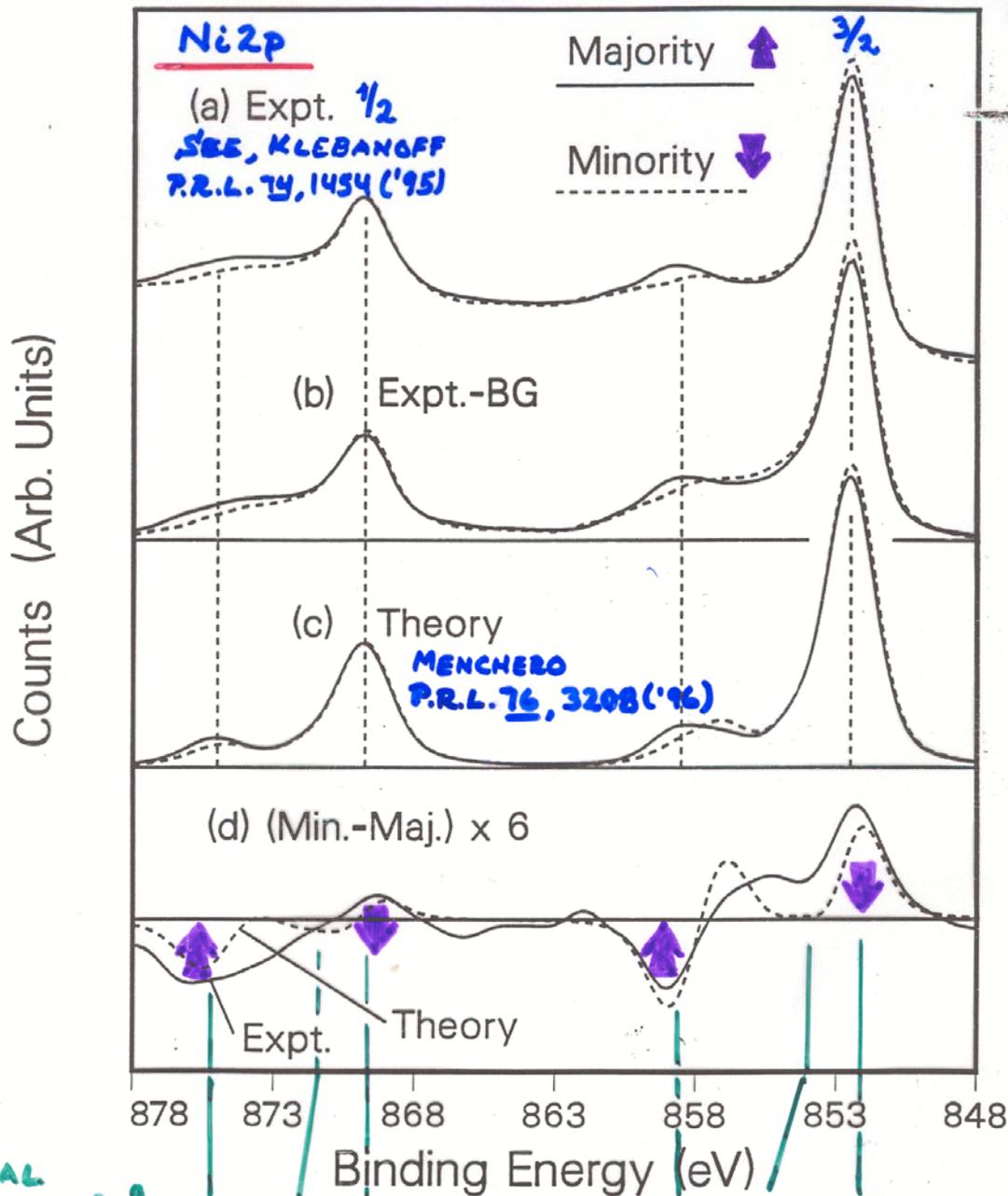
$T$  = LIGAND p - METAL 3d HYBRIDIZATION ENERGY

$Q$  = CORE HOLE-3d COULOMB

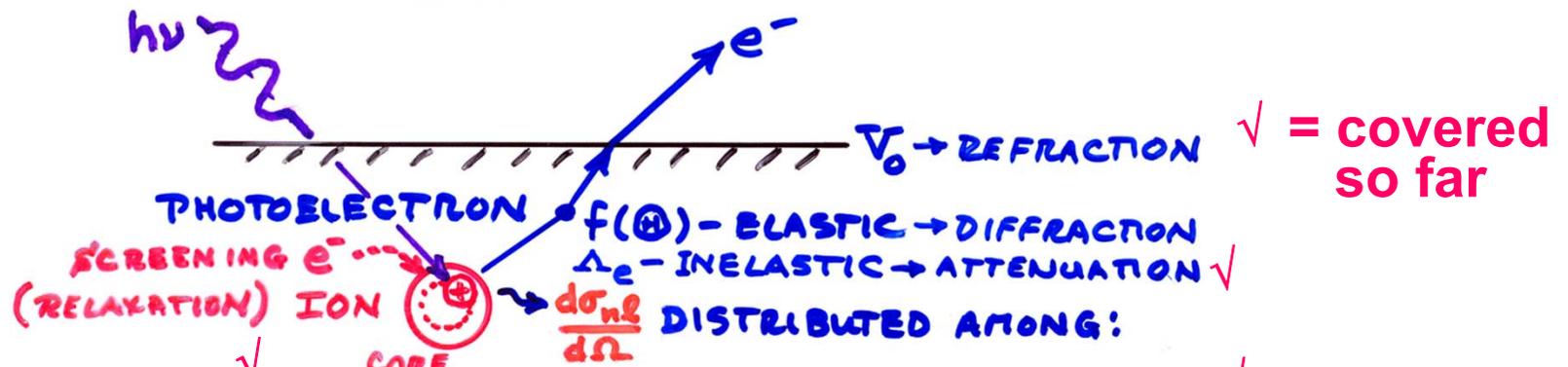
BOUQUET ET AL.,  
J. EL. SP. 82, 87 (196)

SPIN-ORBIT SPLITTING + MULTIPLETS +  
SCREENING IN A METAL: Ni - INITIAL CONFIG.:  $3d^9$

$\sim 15\% 3d^8$   
 $42\% 3d^{10}$



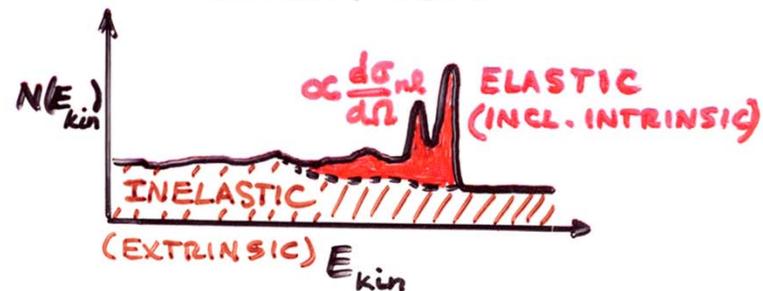
FINAL CONFIG.:  $3d^9$  65% 15% 10% "UNSCREENED" { 65% 15% 10% } "SCREENED"  
 $3d^{10}$  35% 85% 90% { 35% 85% 90% }



ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- ✓ CORE HOLE  $k = nl$
- ✓ SPIN-ORBIT SPLITTING (EASY) ✓
- ✓ + MULTIPLET SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD ✓
- ✓ + CORRELATION / CONFIGURATION INTERACTION ✓
- ✓ + SHAKE-UP / SHAKE-OFF /  $e^-$ -HOLE ✓
- ✓ + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION ✓
- ✓ + VIBRATIONAL EXCITATIONS ←
- ✓ + RESONANT PHOTOEMISSION ( $h\nu \approx E_{b, nl}$ ) ✓

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



# Intensities in photoelectron spectra in the sudden approximation

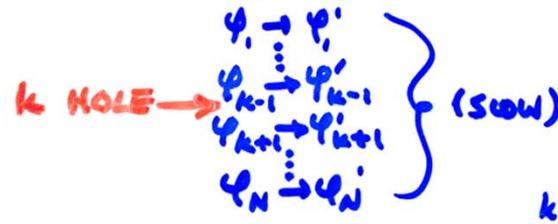
- GENERAL: FINAL STATE  $K$  ( $k$ -SUBSHELL + ALL OTHER DESIG.)

$$\text{INT.}_K \propto |\hat{e} \cdot \langle \Psi_{\text{tot}}^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_i^i(N) \rangle|^2 \quad (\text{DIPOLE APPROX.})$$

- BORN-OPPENHEIMER:  $e^-$ 's FAST, VIBRATIONS SLOW

$$\text{INT.}_K \propto \underbrace{|\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2}_{\text{FRANCK-CONDON FACTOR}} |\hat{e} \cdot \langle \Psi_e^f(N, K) | \sum_{i=1}^N \vec{r}_i | \Psi_e^i(N) \rangle|^2$$

- SUDDEN APPROXIMATION:  $\Psi_k \rightarrow \Psi_f = \text{PHOTO}^-$  (FAST)



$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 |\langle \Psi_e^f(N-1, K) | \Psi_e^i(N-1, K) \rangle|^2$$

$$|\hat{e} \cdot \langle \psi_f | \vec{r} | \psi_k \rangle|^2$$

SAME SUBSHELL COUPLING + TOTAL L, S  $\rightarrow$  "MONOPOLE"

$$\rightarrow \text{NORMAL } \frac{d\sigma_K}{d\Omega}$$

- SLATER DETS. FOR  $\Psi_e^f = \det(\psi_1', \psi_2', \dots, \psi_{k-1}', \psi_{k+1}', \dots, \psi_N')$

$$\Psi_e^i = \det(\psi_1, \psi_2, \dots, \psi_{k-1}, \psi_{k+1}, \dots, \psi_N)$$

$$\text{INT.}_K \propto |\langle \Psi_{\text{vib}, \nu}^f | \Psi_{\text{vib}, \nu}^i \rangle|^2 |\langle \psi_1' | \psi_1 \rangle|^2 |\langle \psi_2' | \psi_2 \rangle|^2 \dots$$

$$|\langle \psi_{k-1}' | \psi_{k-1} \rangle|^2 |\langle \psi_{k+1}' | \psi_{k+1} \rangle|^2 \dots |\langle \psi_N' | \psi_N \rangle|^2$$

$$|\hat{e} \cdot \langle \psi_f | \vec{r} | \psi_k \rangle|^2$$

$1e^-$  DIPOLE  $\rightarrow d\sigma/d\Omega$

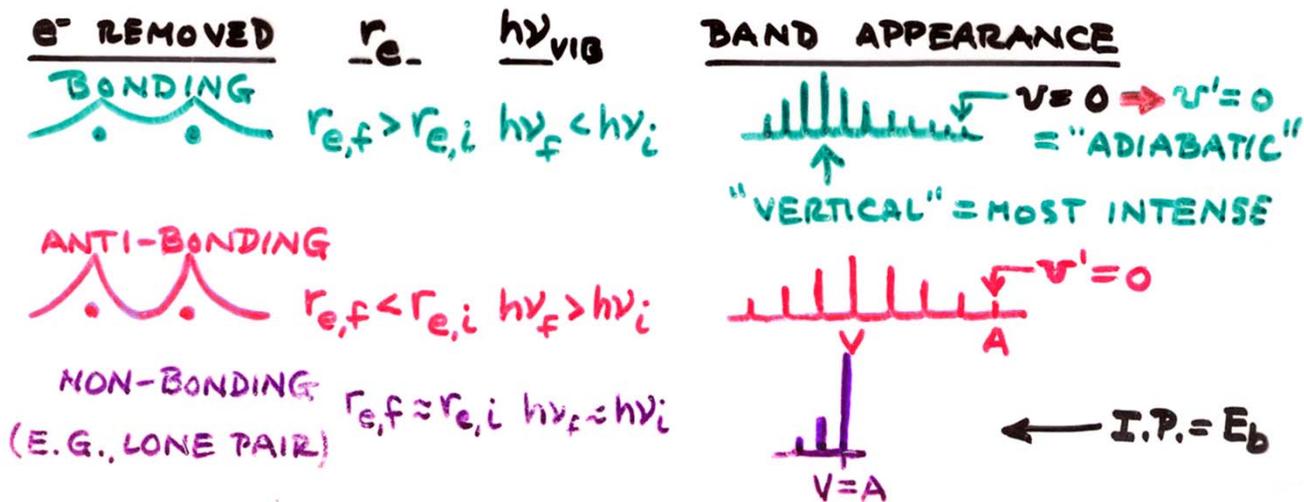
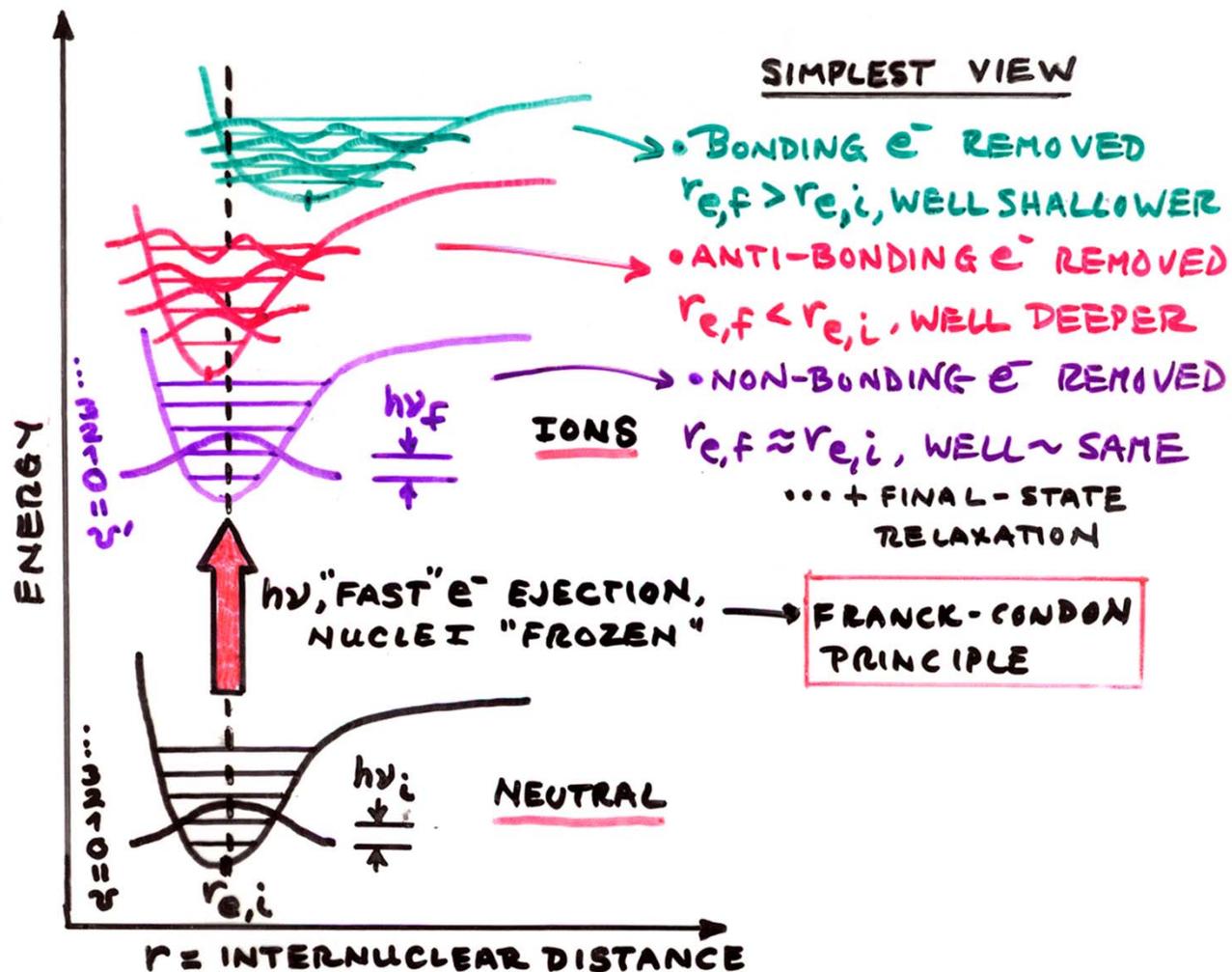
( $N-1$ ) $e^-$  SHAKE-UP/  
SHAKE-OFF  $\rightarrow$   
"MONOPOLE"

- PLUS DIFFRACTION EFFECTS IN  $\Psi_f$  ESCAPE

# VIBRATIONAL STRUCTURE IN VALENCE-LEVEL (MO) SPECTRA

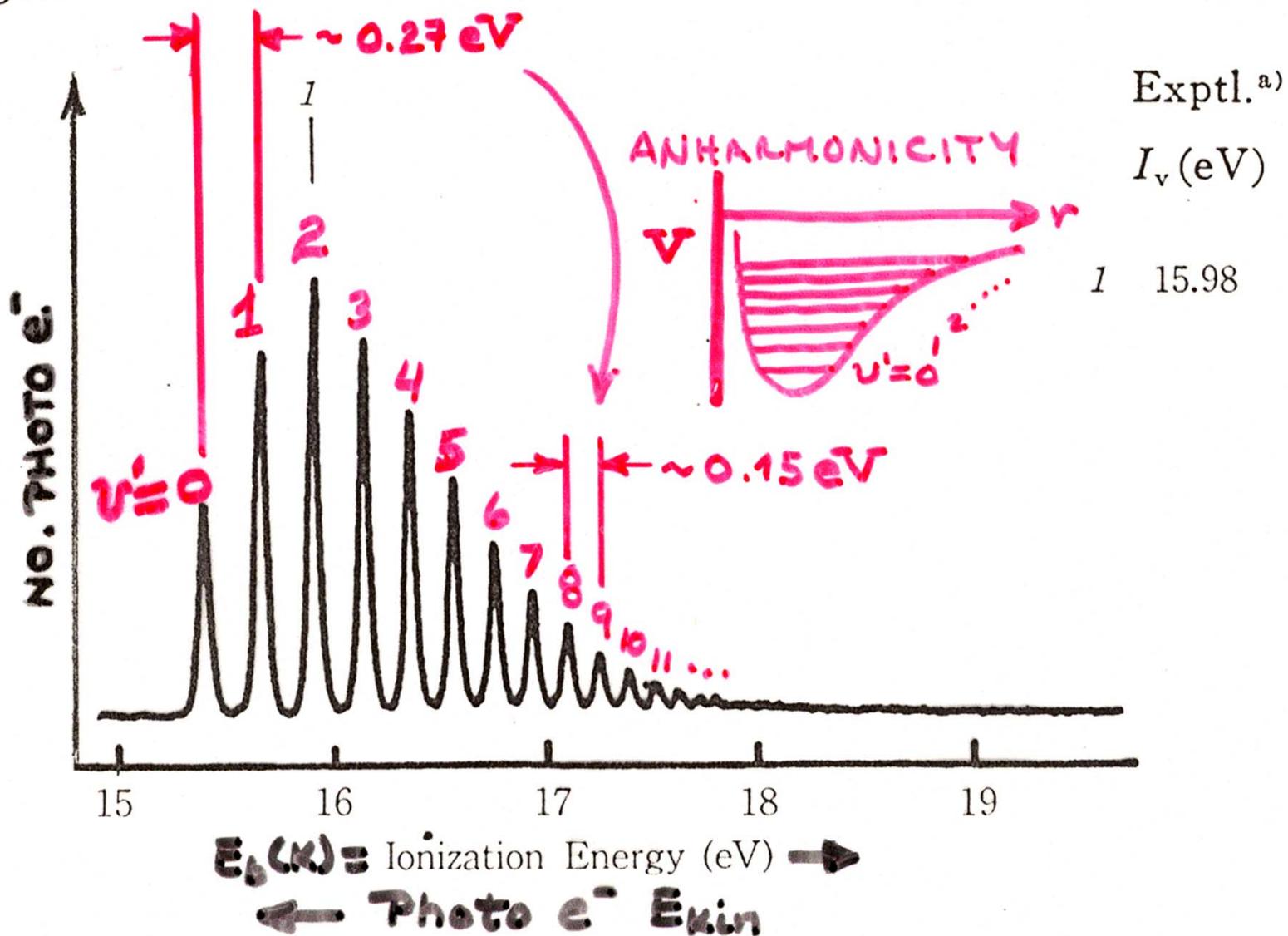
Diatomic A-B example

(Also applies to core-level emission if equilibrium distance changes on forming core hole)



# VIBRATIONAL STRUCTURE IN VALENCE-LEVEL (MO) SPECTRA

**H<sub>2</sub>** Hydrogen



## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission



Photoelectron Diffraction and Holography

## **Valence-Level Photoemission**

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## **Some New Directions**

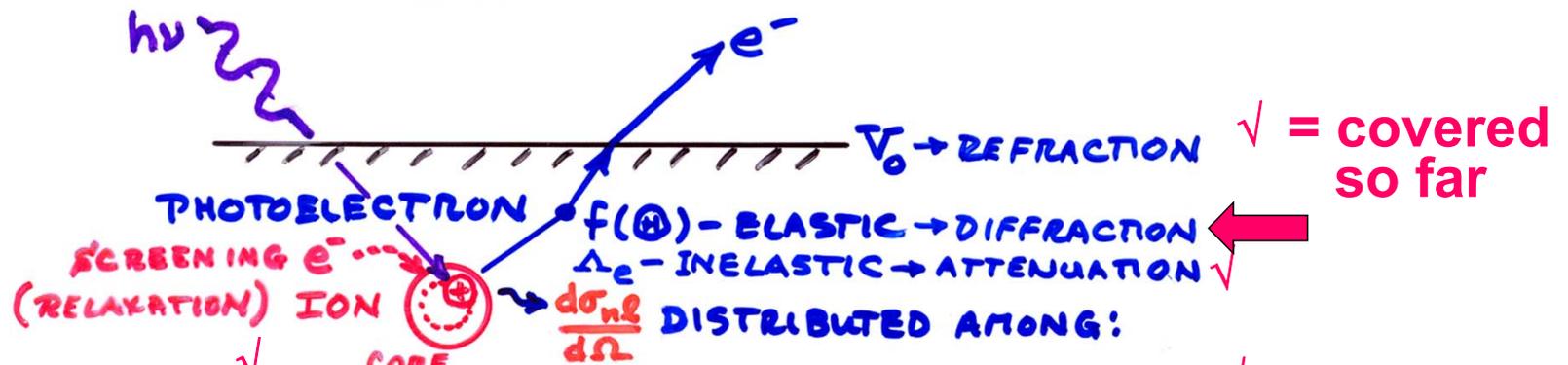
Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

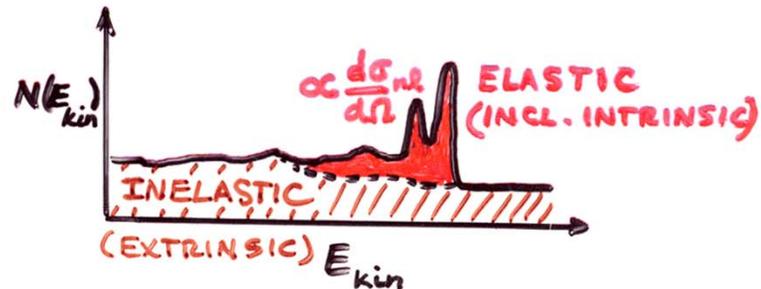
Temporal Resolution



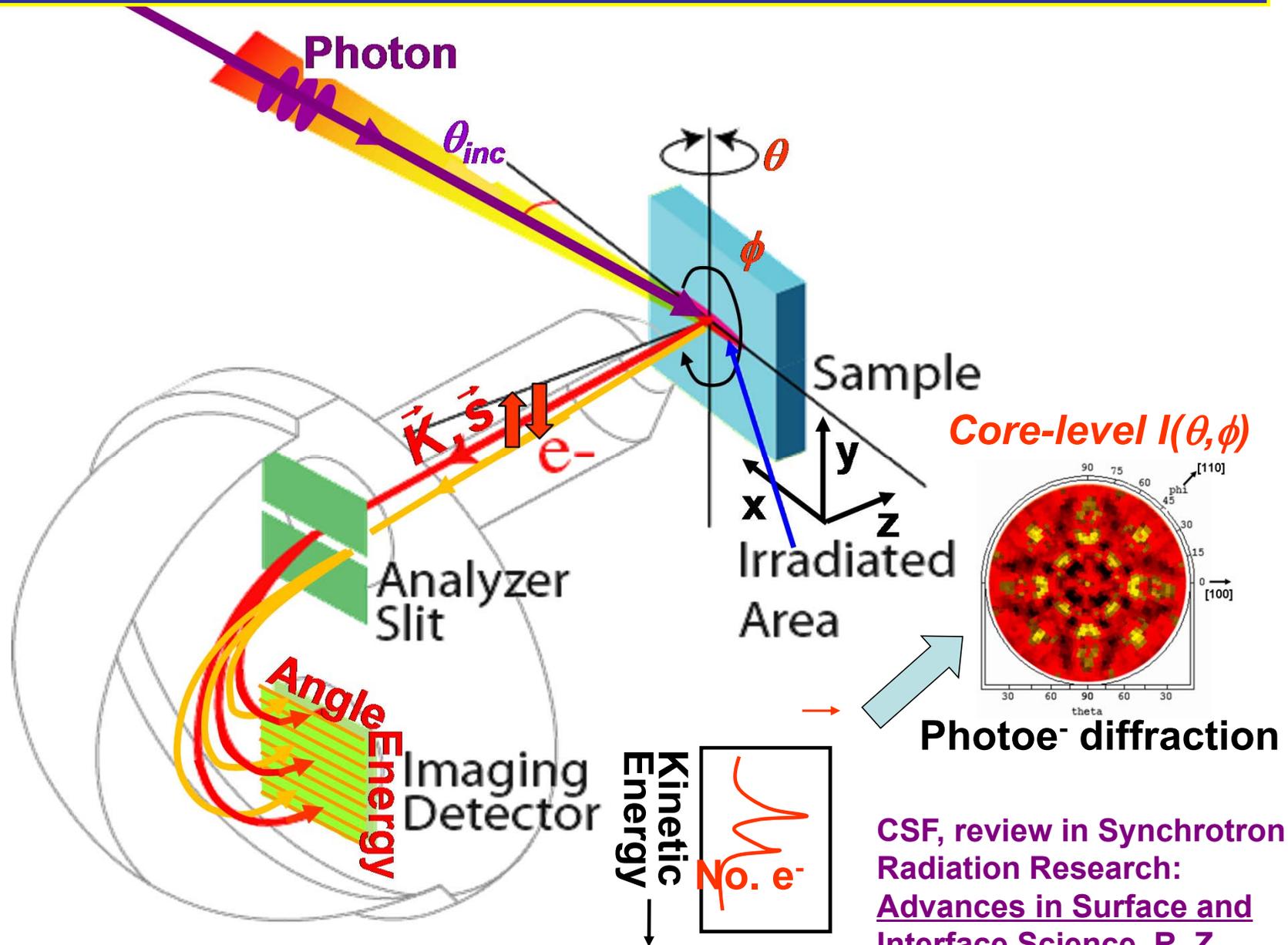
ADDITIONAL SOURCES OF STRUCTURE (AND INFORMATION!) IN SPECTRA BEYOND CHEMICAL SHIFTS

- + SPIN-ORBIT SPLITTING (EASY) ✓
- + MULTIPLY SPLITTING (OPEN-SHELL SYSTEMS), XSTAL FIELD ✓
- + CORRELATION / CONFIGURATION INTERACTION ✓
- + SHAKE-UP / SHAKE-OFF /  $e^-$ -HOLE ✓
- + SCREENING / NON-SCREENING: CONFIGURATION INTERACTION ✓
- + VIBRATIONAL EXCITATIONS ✓
- + RESONANT PHOTOEMISSION ( $h\nu \approx E_{b, nl}$ ) ✓

REALLY ALL AT ONCE, BUT SUM RULES + THEORY HELP



# Typical experimental geometry for energy- and angle-resolved photoemission measurements

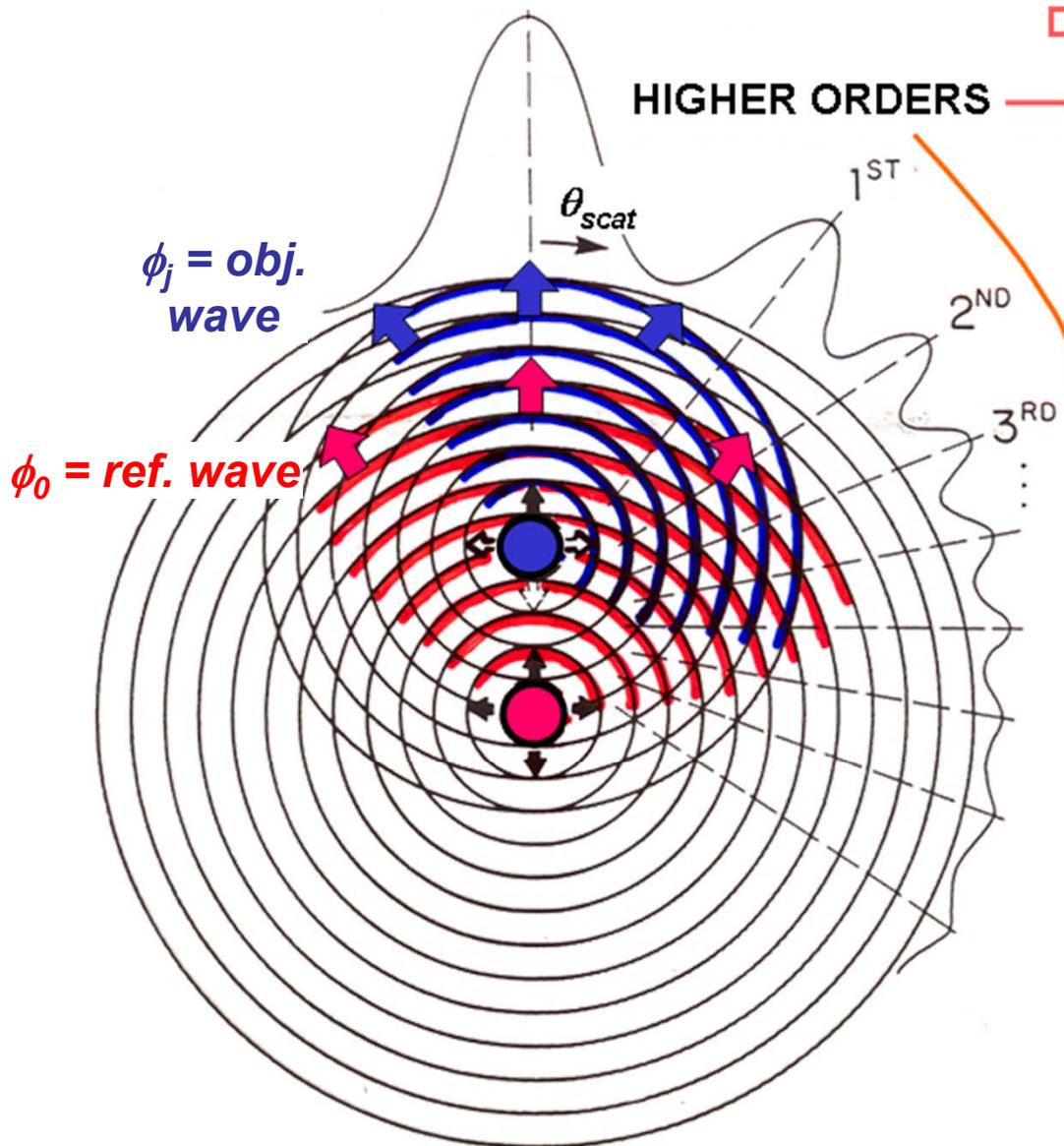


CSF, review in Synchrotron Radiation Research: Advances in Surface and Interface Science, R. Z. Bachrach, Ed. (Plenum Press, New York, 1992).

FORWARD SCATT. = "0<sup>TH</sup> ORDER" → Bond & Low-Index Directions

HIGHER ORDERS → Bond Lengths & Atomic Positions

→ Holographic fringes



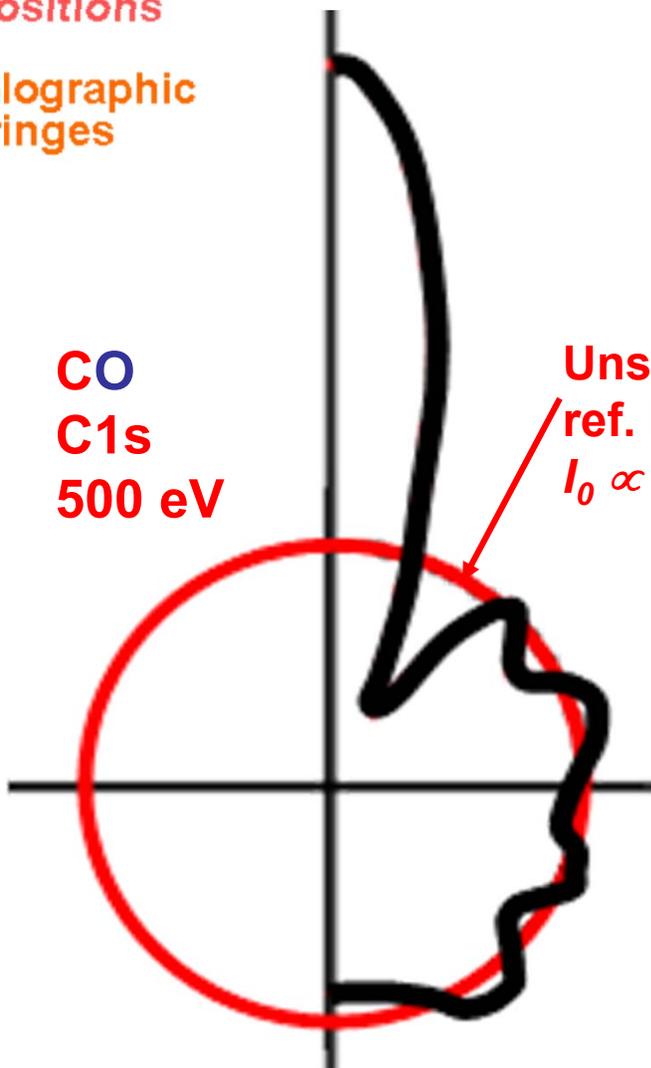
$\phi_j = obj.$   
wave

$\phi_0 = ref.$  wave

1<sup>ST</sup>  
2<sup>ND</sup>  
3<sup>RD</sup>  
...

CO  
C1s  
500 eV

Unscattered  
ref. intens.  
 $I_0 \propto |\phi_0|^2$

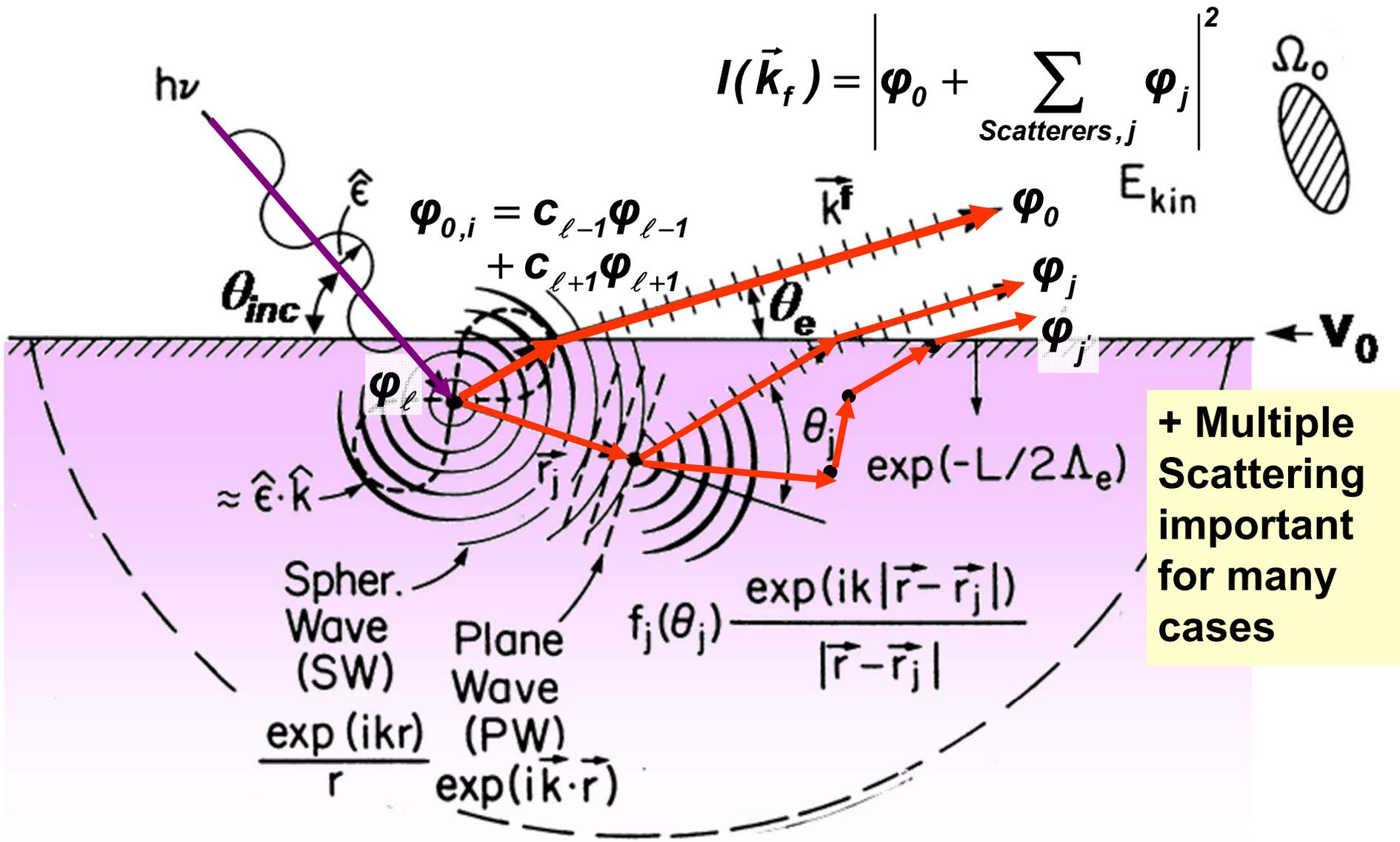


# Photoelectron Diffraction

EDAC photoelectron diffraction program: Javier Garcia de Abajo:

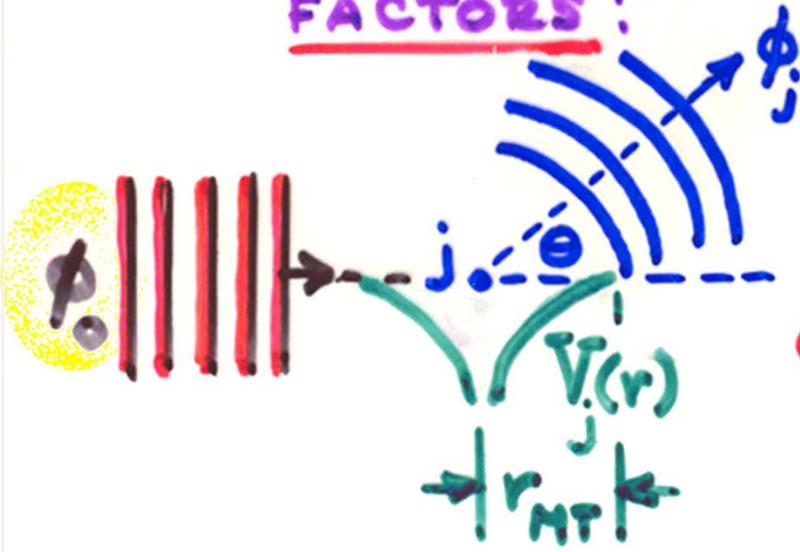
<http://garciadeabajos-group.icfo.es/widgets/edac/index.html>

# Photoelectron Diffraction: Single Scattering Theory



# CALCULATION OF e<sup>-</sup>-ATOM SCATTERING

## FACTORS:



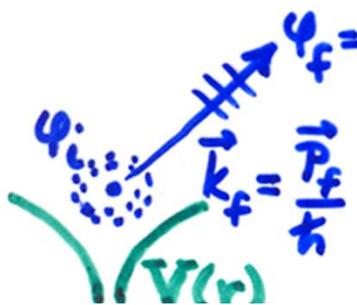
## PLANE-WAVE SCATTERING: PARTIAL-WAVE METHOD†

● PW  $f_j(\theta) = \frac{1}{k} \sum_{l=0}^{l_{max}} (2l+1) e^{i\delta_l} \sin \delta_l P_l(\cos \theta)$  PHASE SHIFT

$$l_{max} \approx kr_{MT}$$

† ANY TEXTBOOK ON SCATTERING

## COMPARE THE OUTGOING PHOTOELECTRON WAVE



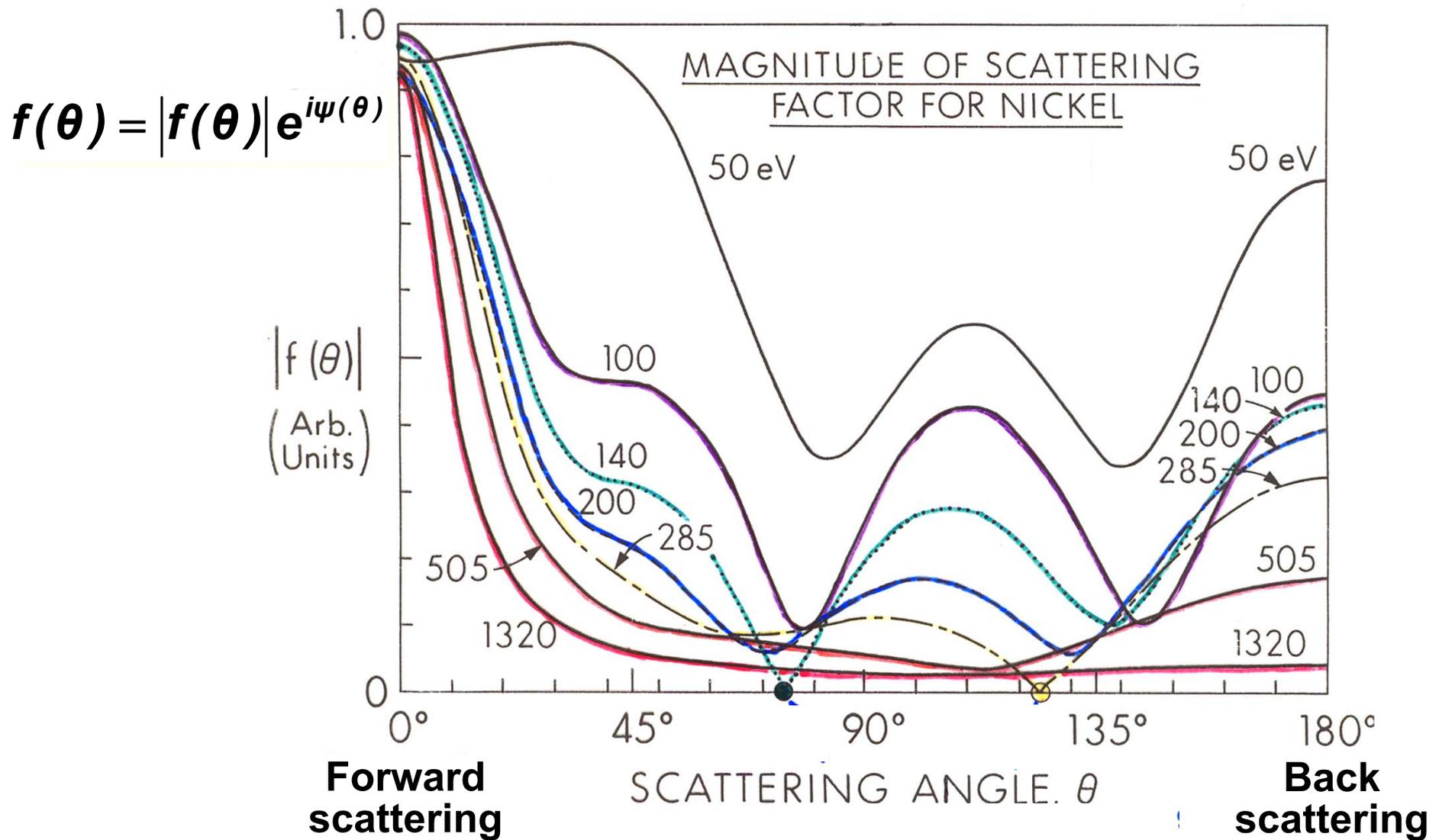
$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f m_f}^*(\theta, \phi) Y_{l_f m_f}(\theta, \phi) R_{E_f, l_f}(r) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

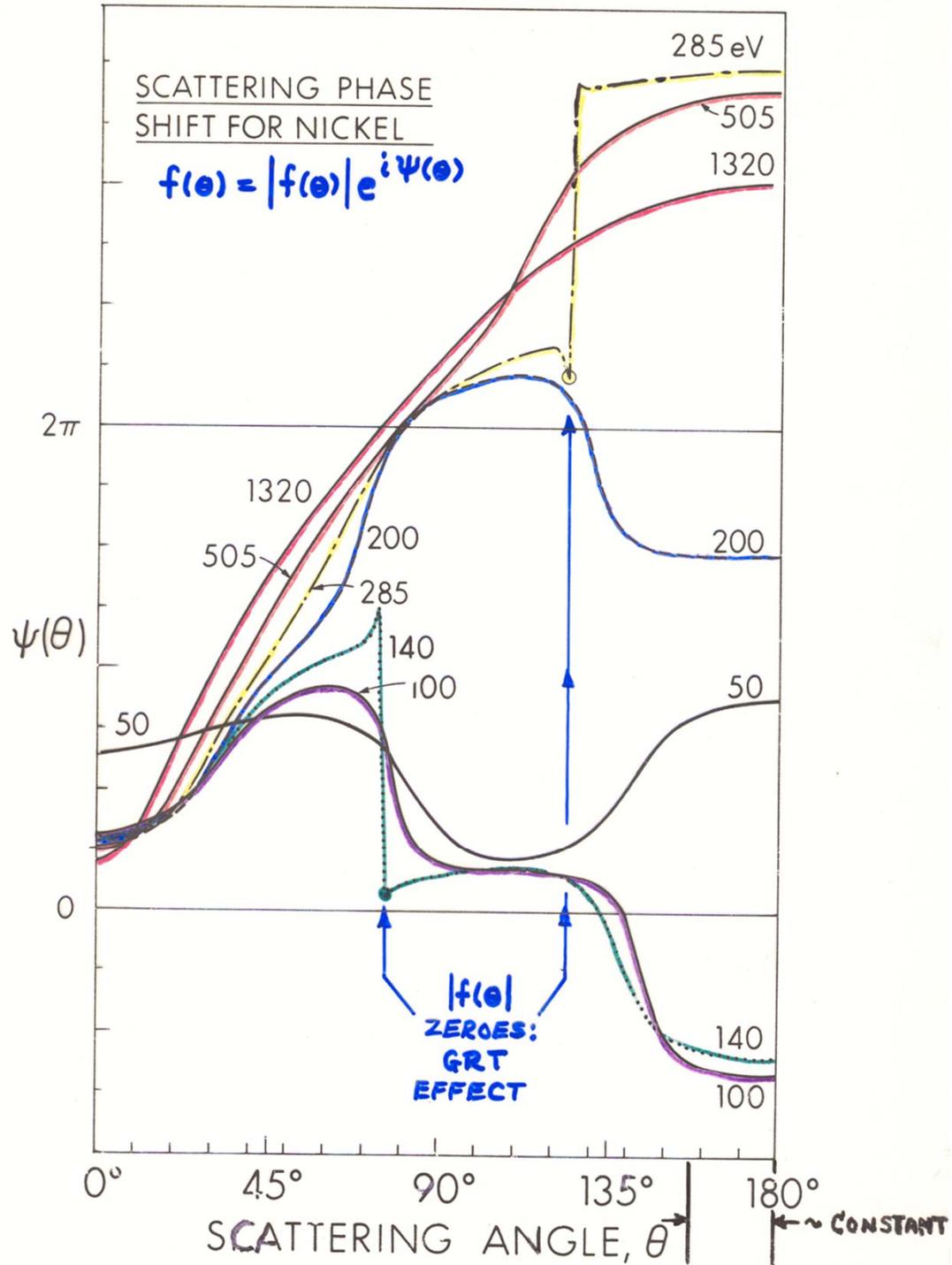
PHASE SHIFT OF  $l_f$  WAVE IN  $V(r)$

Same phase shifts involved

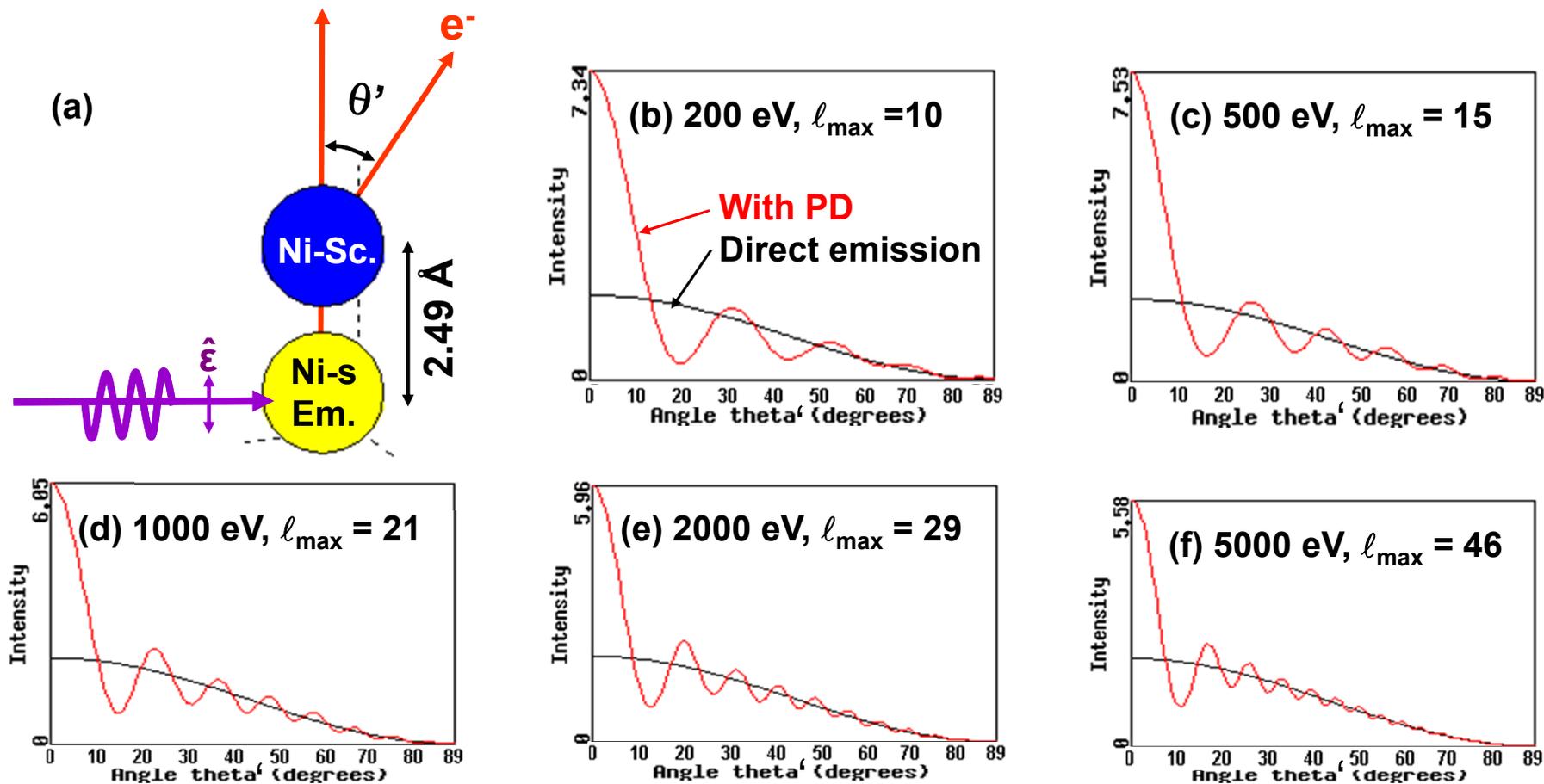
# ENERGY DEPENDENCE OF ELECTRON ELASTIC SCATTERING



# ENERGY DEPENDENCE OF ELECTRON ELASTIC SCATTERING



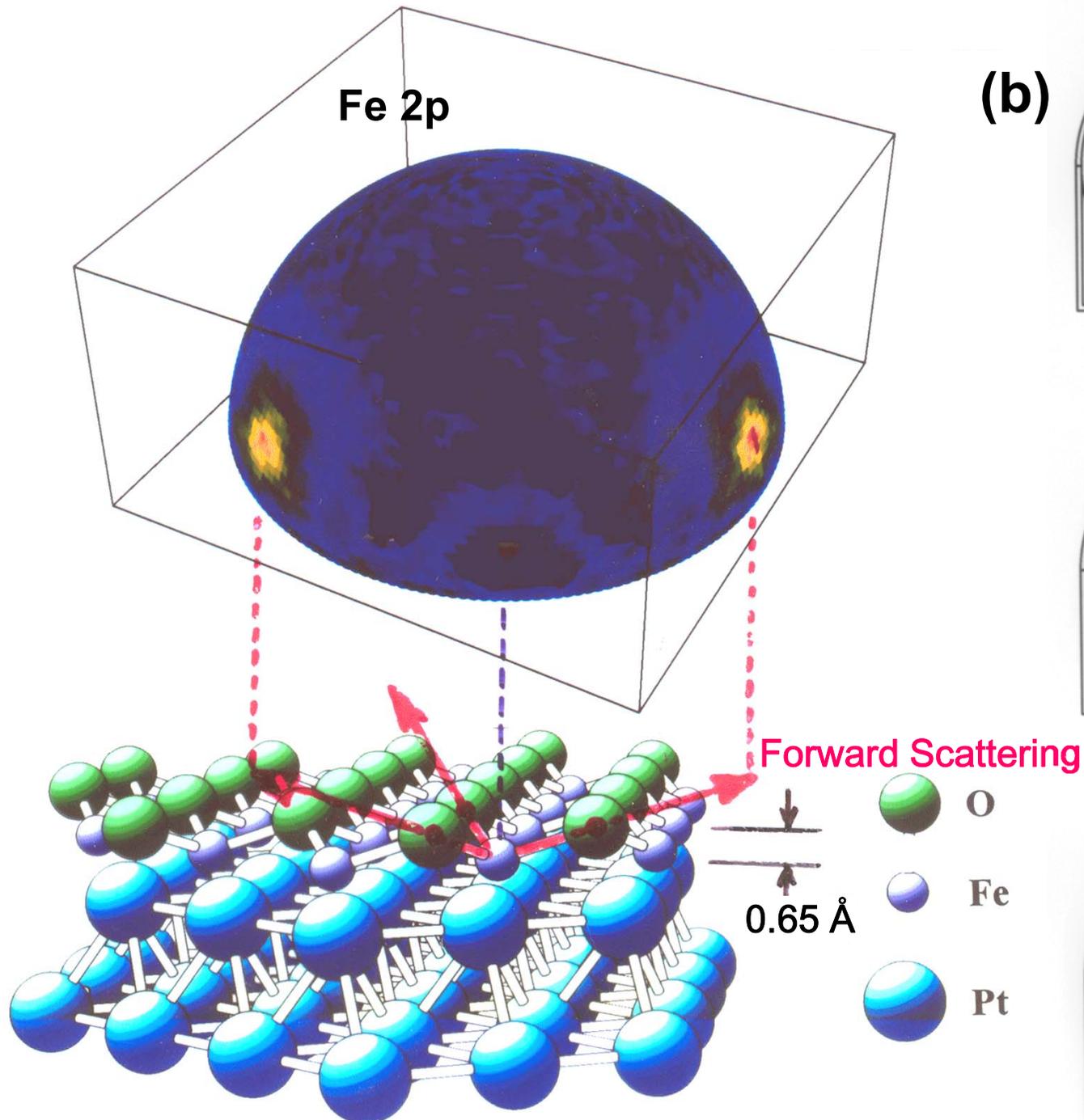
# Energy dependence of photoelectron diffraction: Theory



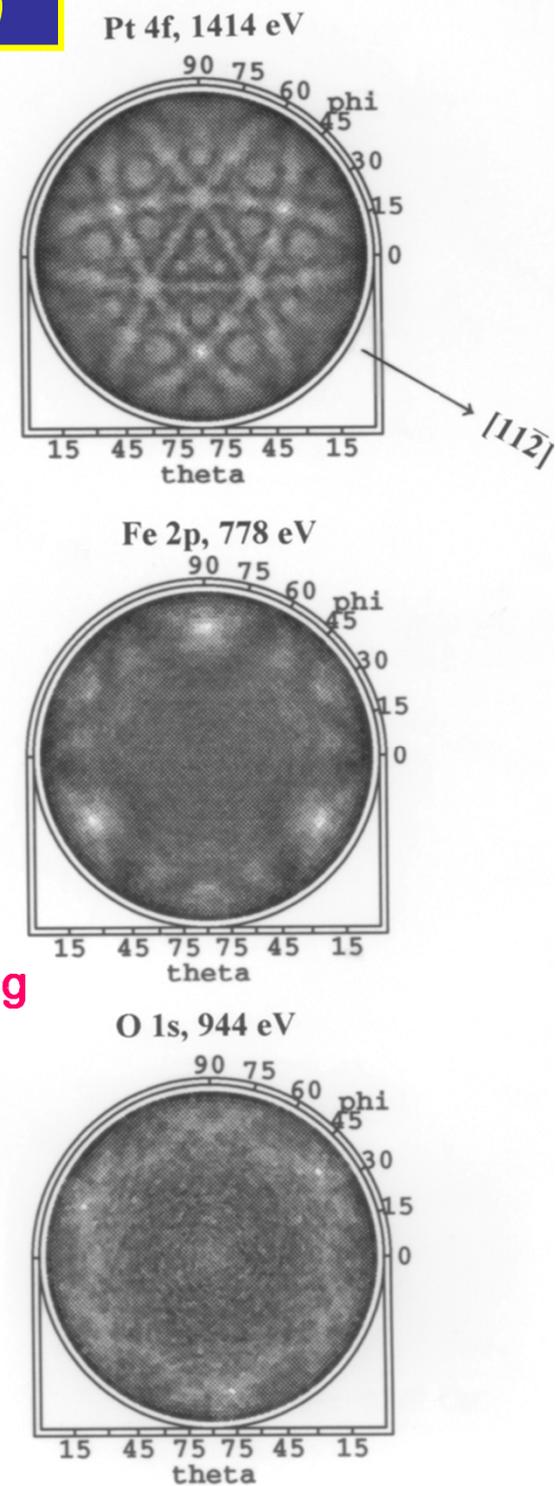
Much more forward peaked at higher energy, weaker in directions away from forward

# X-ray Photoelectron Diffraction: 1ML FeO on Pt(111)

(a)

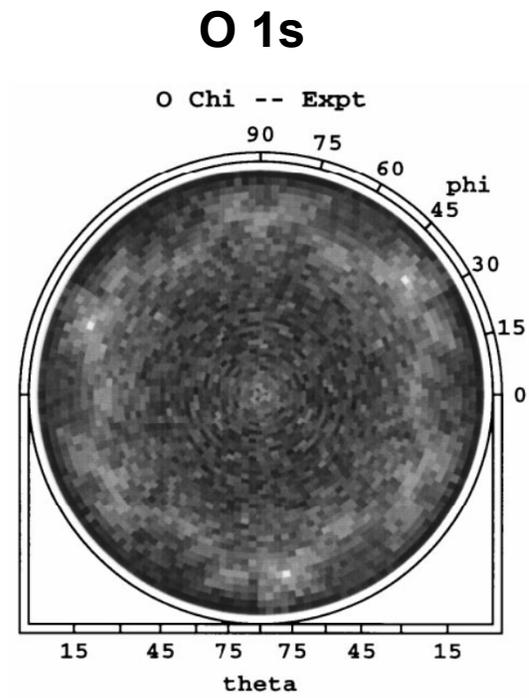
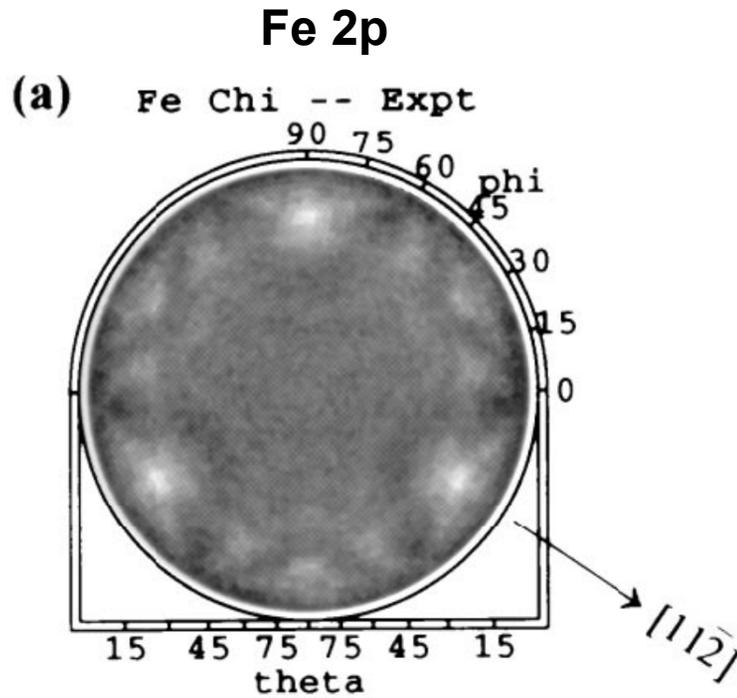


(b)

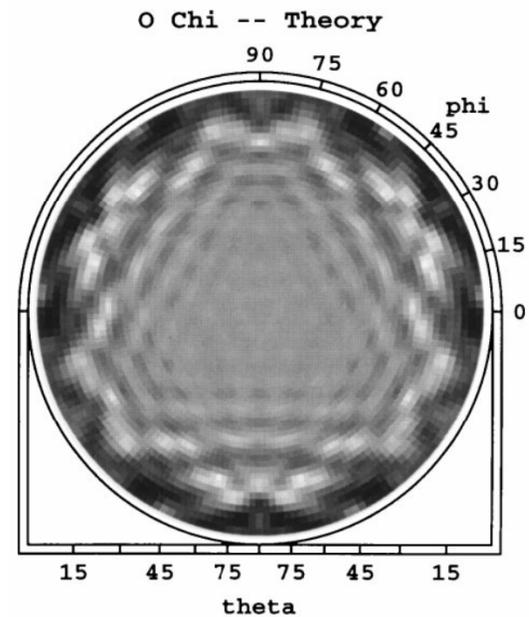
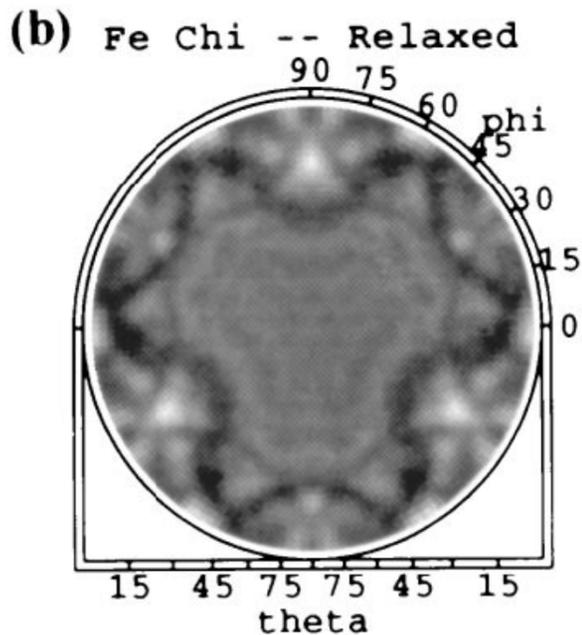


# X-ray Photoelectron Diffraction: 1ML FeO on Pt(111)

Experiment:  
In stereographic  
projection

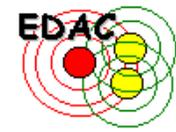


Theory:  
Single-  
scattering  
cluster model



Online calculation of photoelectron diffraction patterns:

# EDAC output for CO/Fe(001)

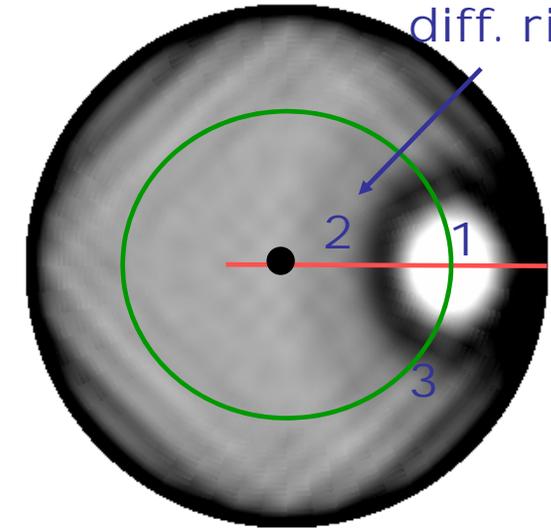
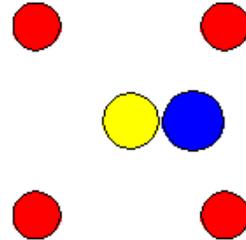
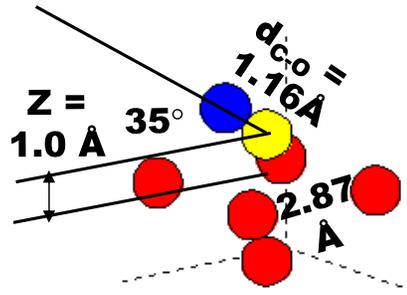


Click on the figure to download data.

<http://garciadeabajos-group.icfo.es/widgets/edac/index.html>

Oxygen  
1<sup>st</sup> order  
diff. ring

7 atoms:



**Left:** representation of the cluster rocking around a line parallel to the  $z$  direction and passing by the emitter (yellow atom). The dashed lines stand for the  $xyz$  axes. **Right:** top view of the cluster, where the  $x/y$  direction (not plotted) runs along the horizontal/vertical screen direction. Different atomic species have been assigned the colors O, Fe.

**Polar scan of photoemission intensity** (logarithmic scale). White/black regions correspond to high/low intensity. The orientation is the same as in the top-view of the cluster. The distance to the center of the figure is proportional to the polar angle  $\theta$ . The polar angle range is (0.0, 89.0) (in degrees).

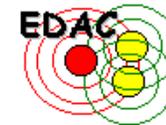
## Parameters used in the calculation:

$N=7$  atoms  
Iteration order=4  
 $l_{\max}=25$   
 $V_0=10.5$  eV  
Photoelectron energy=1202 eV  
p-polarized light  
 $z_0=1.435$  Å  
Recursion iteration method

X 4 domains  
rotated by 90°

*User friendly web-based program for PD calculations by Javier Garcia de Abajo, DIPC, Donostia-San Sebastian, Spain*

# Electron Diffraction in Atomic Clusters



## for Core Level Photoelectron Diffraction Simulations

<http://nanophotonics.csic.es/widgets/edac/index.html>

Created by [F. Javier García de Abajo](#) (CSIC and DIPC, San Sebastian, Spain)

in collaboration with [M. A. Van Hove](#) and [C. S. Fadley](#) (LBNL, Berkeley, and UCD, Davis, California)

This site allows performing on-line photoelectron diffraction calculations. Multiple scattering (MS) of the photoelectron is carried out for a cluster representing a solid or molecule. Select the corresponding parameters and click on the "Calculate" button below to perform the actual calculation and to produce a plot of the calculated data (a separate window pops out to display it). A numerical data table can be downloaded by clicking on the resulting plot. Click on the different parameter names in blue to see fuller explanations. Click on the "Preview Cluster" button to display the currently selected atomic cluster (but without performing a MS calculation) or the button "Download Cluster" to download the currently selected cluster. Notice that the [scattering phase shifts](#) and [excitation radial matrix elements](#) are calculated internally for each cluster configuration, so that the user does not have to provide them. Please, read the [terms of use](#) and the [restrictions on input parameters](#) before using this site for the first time.

### Terms and conditions of use

[Terms of use](#)

[Restrictions on input parameters](#)

Password:

**jarabe12**

A password is only necessary for large computation times (click [here](#) for more details). Leave it blank otherwise.

Title (optional):

### Cluster definition

The cluster and the list of emitters are defined by a list of commands with the following format (click [here](#) or on the items of this list for further details):

atom symbol  $x y z$       layer symbol  $x y z a b \alpha_1 \alpha_2$

surface symbol  $x y z a$  type      emitter  $x y z$

Fill in the text box with these commands according to the cluster specifications that you need. [Some examples are provided by clicking here](#) (you may cut and paste them to this page and modify them further).

```

atom O 0.95 0 1.66
atom C 0 0 1.0
surface Fe 1.435 1.435 0 2.87 bcc100
emitter 0 0 1.0
end

```

The cluster consists of a maximum of  atoms. (Warning: a finite number of atoms generally introduces symmetry breaking.)

The size of the cluster is determined by the distance  $d_{\max} = \text{ \text{\AA}}$  and the reference point  $x_0 = \text{ \text{\AA}}$ ,  $y_0 = \text{ \text{\AA}}$ ,  $z_0 = \text{ \text{\AA}}$ .

See [cluster shape](#) for more details.

Plot cluster on output?  Yes  
 No

Cluster shape:  Parabolic  
 Spherical

Preview Cluster\*

Download Cluster\*

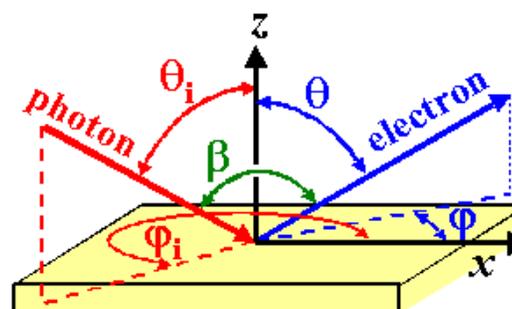
## Geometry of beam and analyzer

**Incoming beam parameters** (see figure)

Polar angle  $\theta_i = \text{ degrees}$

Azimuthal angle  $\varphi_i = \text{ degrees}$

**Polarization:**  p-polarization  
 s-polarization  
 RCP  
 LCP



**Schematic representation of the geometry**

**Mobility of cluster beam, and sample**  Only the sample moves with constant  $\beta = \text{ degrees}$   
 Only the analyzer moves  
 Both the sample and the analyzer move  
[\(click here for details\):](#)

## Energy and angle scanning parameters (see figure above)

The following entries will select the range of photoelectron energies and angles of emission.

Energy scans for a given emission angle can be chosen by selecting more than one energy of emission and only one polar angle and one azimuthal angle (the value of each angle is then taken as the lower limit of the selected angular range, and the value of the upper limits are disregarded). In this case, the output is a 1D plot with the photoelectron intensity as a function of photoelectron energy.

Electron energy range:  equally-spaced value(s) of the electron energy from  eV to  eV  
Polar angle:  equally-spaced value(s) of the polar angle  $\theta$  from  degrees to  degrees  
Azimuthal angle:  equally-spaced value(s) of the azimuthal angle  $\phi$  from  degrees to  degrees  
Type of 2D angular representation:  Linear scale  Logarithmic scale  
Type of azimuthal of polar angular representation:  Cartesian  Polar

Photoelectron detector half-width acceptance angle =  degrees. The photoelectron intensities are angle-averaged over a cone with half aperture given by this parameter.

## Multiple scattering parameters

**Internal code parameters**  
Maximum orbital quantum number  $l_{\max} =$    
Scattering order =   
Iteration method:  Jacobi (regular MS)  Recursion

### Additional solid parameters

Inner potential  $V_0 =$   eV

Electronic edge  $z_0 =$   Å

8.1 eV from band struct.  
+ work function = 4.3 eV  
= 12.4 eV

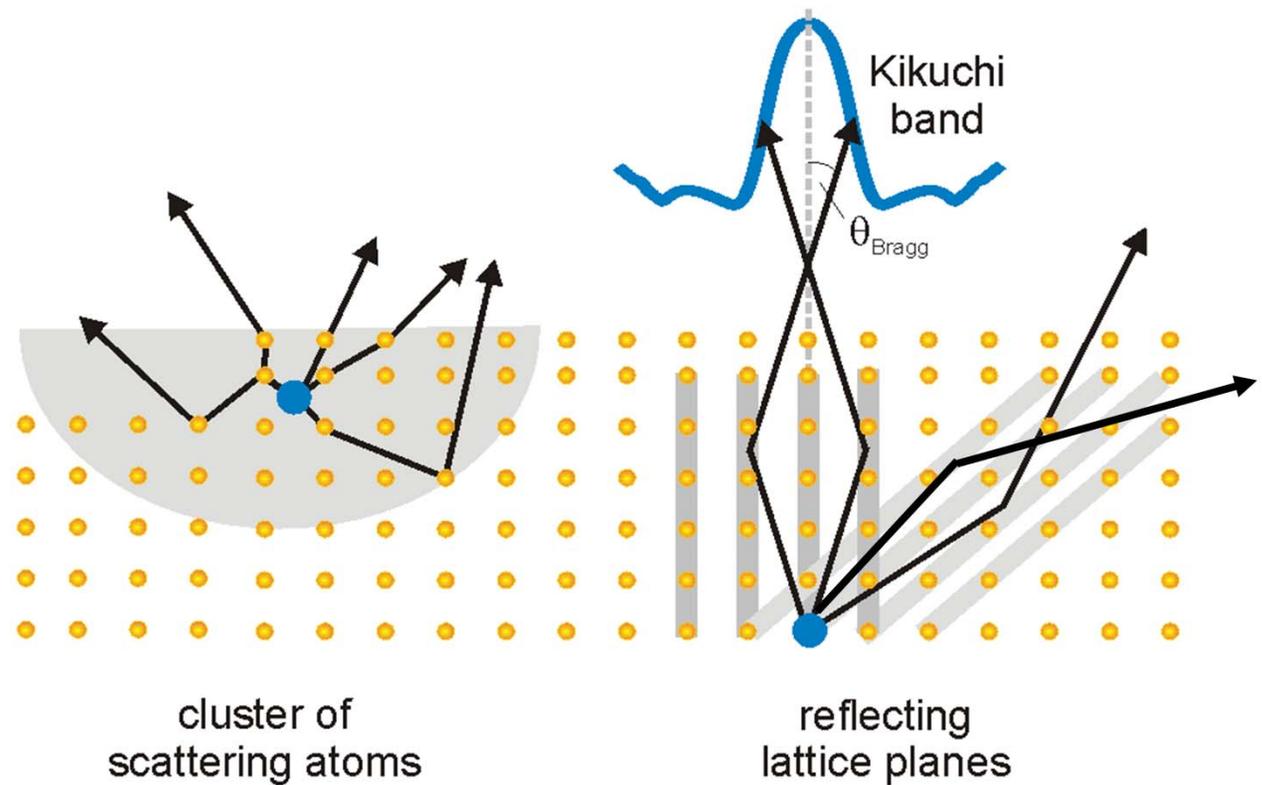
Inelastic mean free path: either choose a fixed value =  Å

or (if that last entry is <0) use the TPP-2M formula  
with parameters  $\rho =$   g/cm<sup>3</sup>,  $N_v =$  ,  $E_p =$   eV, and  $E_g =$   eV

Temperature (K) =  and Debye temperature (K) =

# Photoelectron Diffraction with soft and hard x-ray excitation: two viewpoints

The scattering of photoelectrons from localized sources can be described in real space (multiple scattering cluster) and reciprocal space (dynamical theory of electron diffraction)

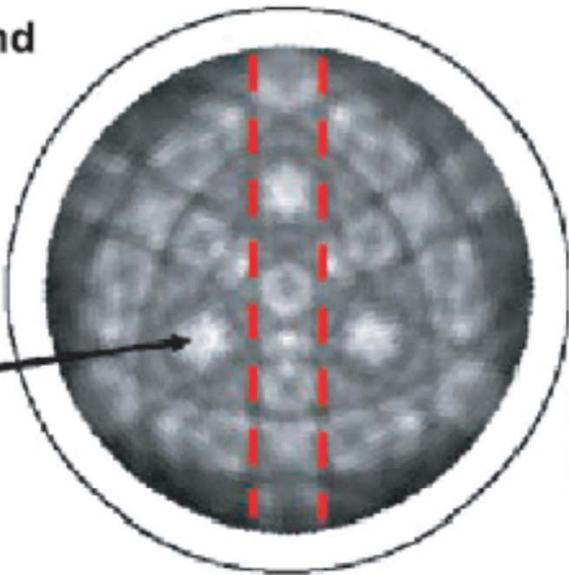


Soft x-ray excitation  $\longrightarrow$  Hard x-ray excitation

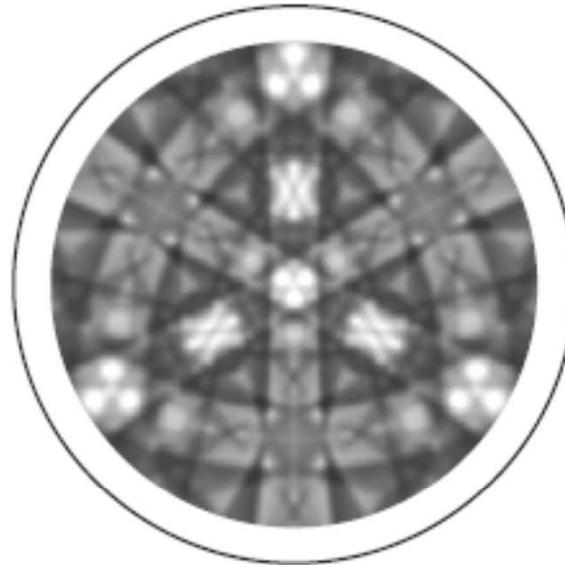
# Photoelectron Diffraction with soft and hard x-ray excitation: two viewpoints, expt. vs. theory

Diamond  
C(111)  
964eV

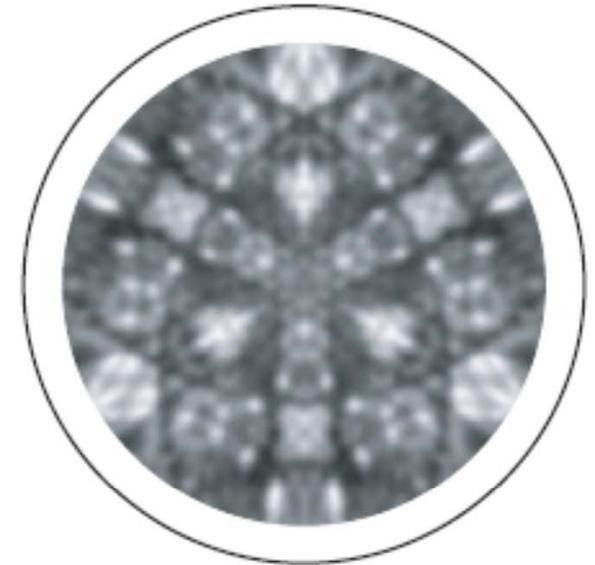
Fwd.  
scatt.



(a) experiment  
Osterwalder et al.



(b) dynamical  
simulation



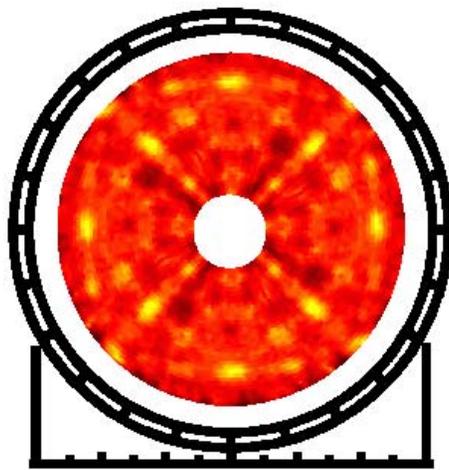
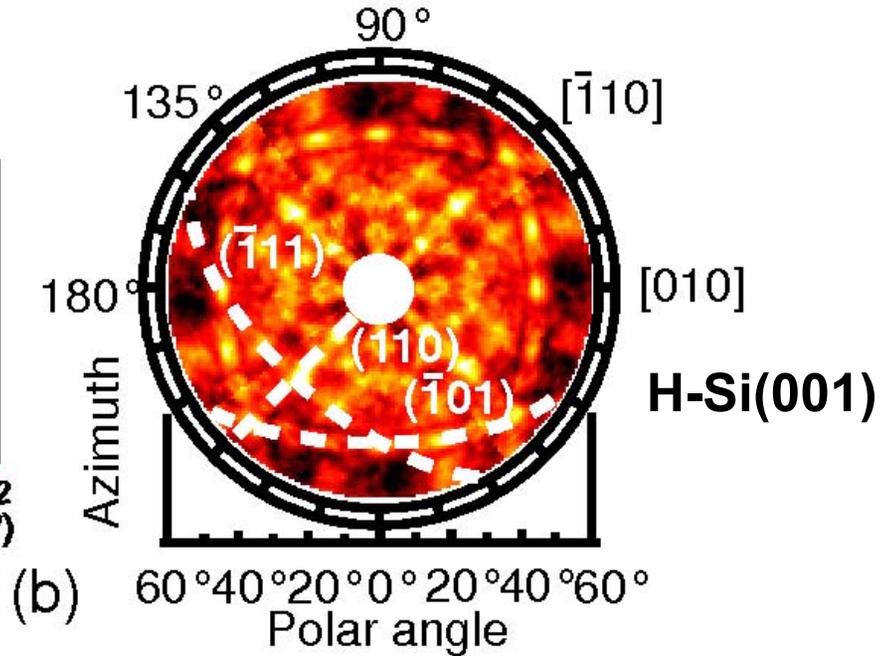
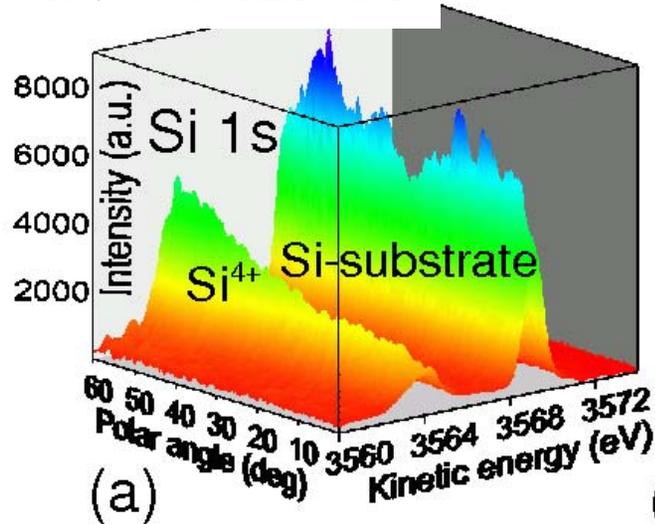
(c) multiple scattering  
simulation (EDAC)

*Easier to use for higher  
energies, “bulk” or long-  
range order emission*

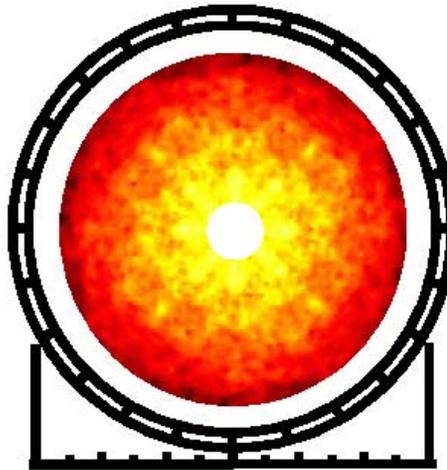
# Bulk sensitive HXPD of Si 1s

$h\nu = 5417 \text{ eV}$

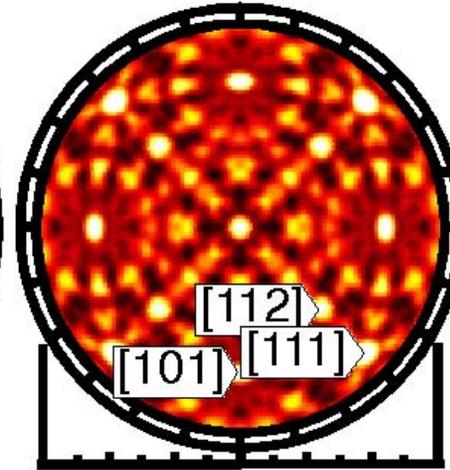
Native  $\text{SiO}_2$   
/Si(001)



(c) 4.1 nm  $\text{SiO}_2$ /Si(001)



(d) 7.0 nm  $\text{SiO}_2$ /Si(001)



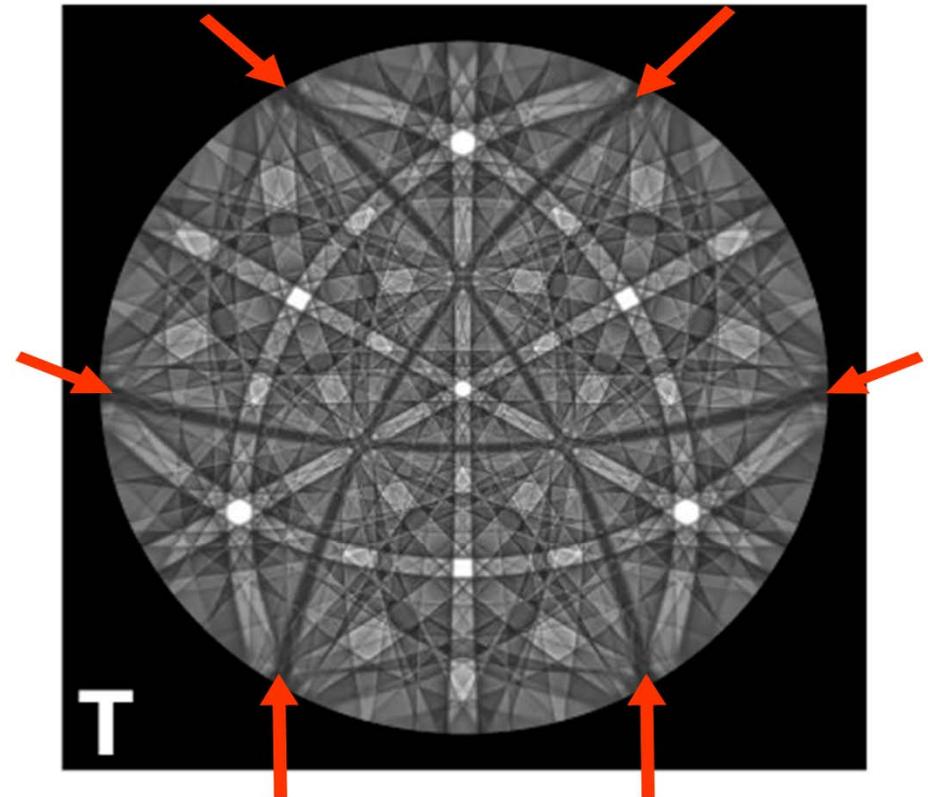
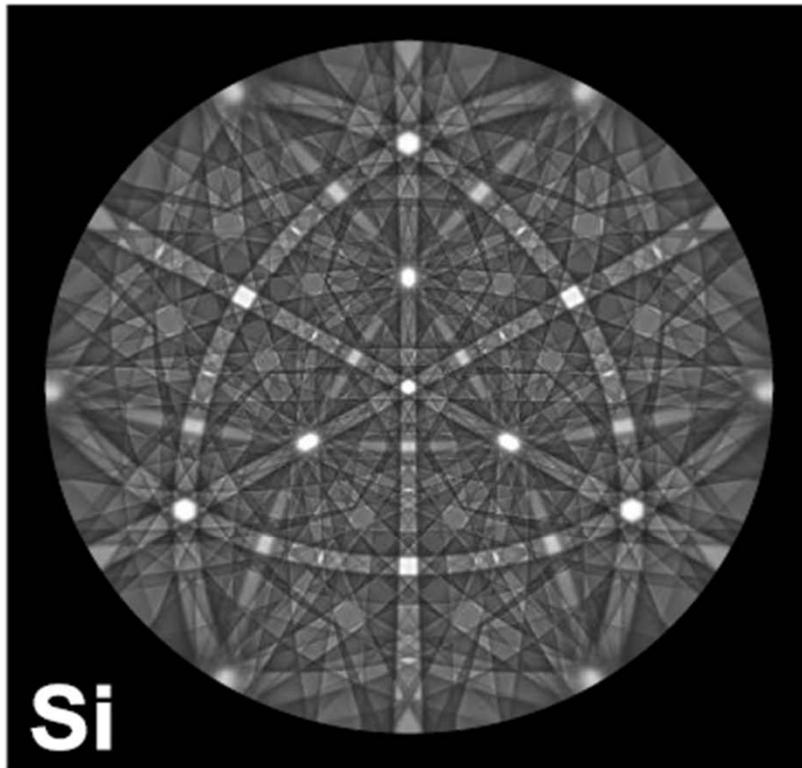
(e) Multiple scattering cluster simulation

Pis et al., Applied Physics Express 3 (2010) 056701;

Kobata et al., SPring8: Surf. Interf. Anal., <http://onlinelibrary.wiley.com/doi/10.1002/sia.3760/pdf>

# Hard x-ray photoelectron diffraction--Theory: Sensitivity to lattice distortions and atomic site type?

Si(111)-6 keV: Impurity atom on lattice site (Si) vs. tetrahedral interstitial (T)



A. Winkelman, J. Garcia de Abajo,  
MPI Halle, CF, New Journal of  
Physics 10 (2008) 113002

Missing Kikuchi bands-->"forbidden reflections"

## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

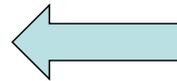
Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography



## **Valence-Level Photoemission**

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## **Some New Directions**

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

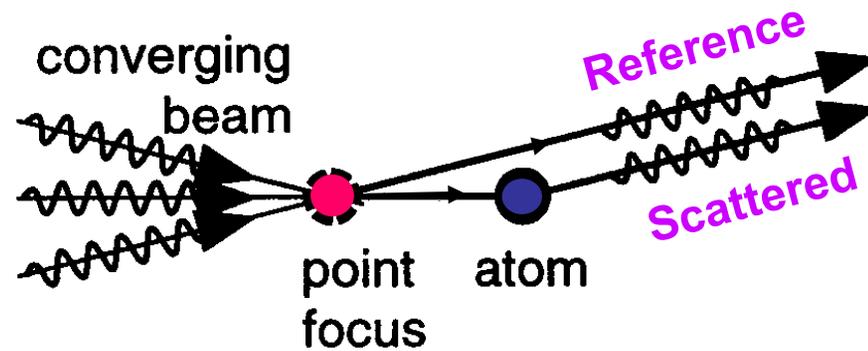
Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

# Diffraction and Holography: What's the Difference?

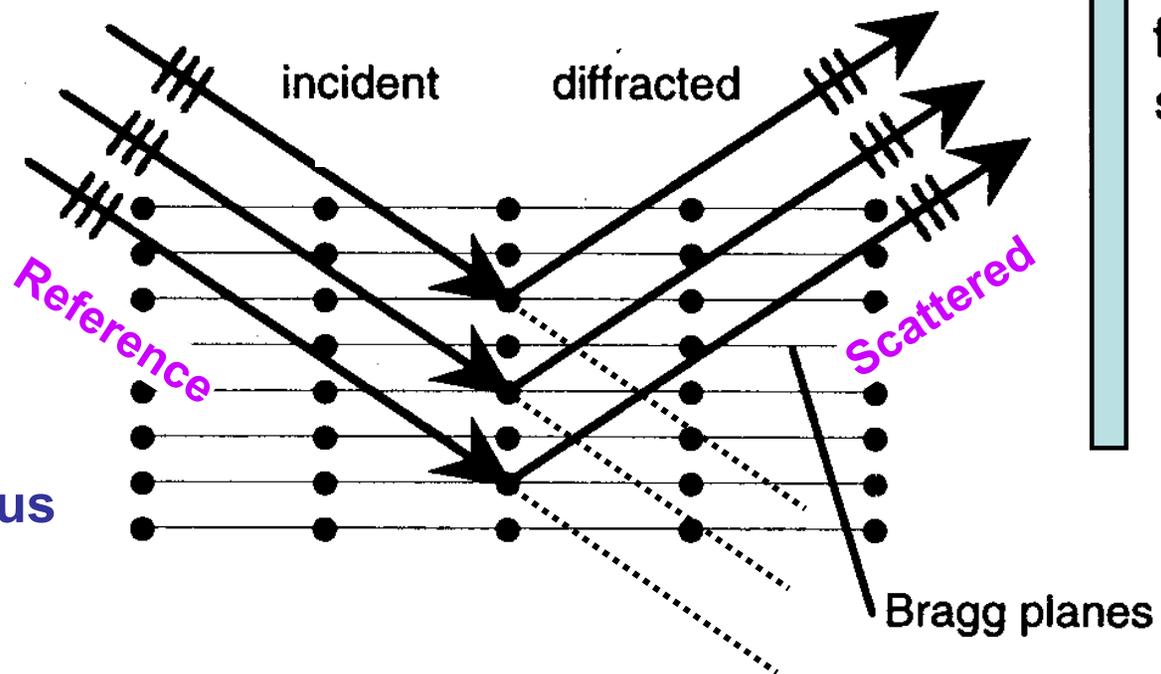
## Holography:

Reference and scattered interfere → phase relation preserved



## Diffraction:

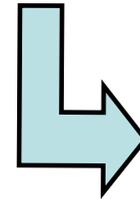
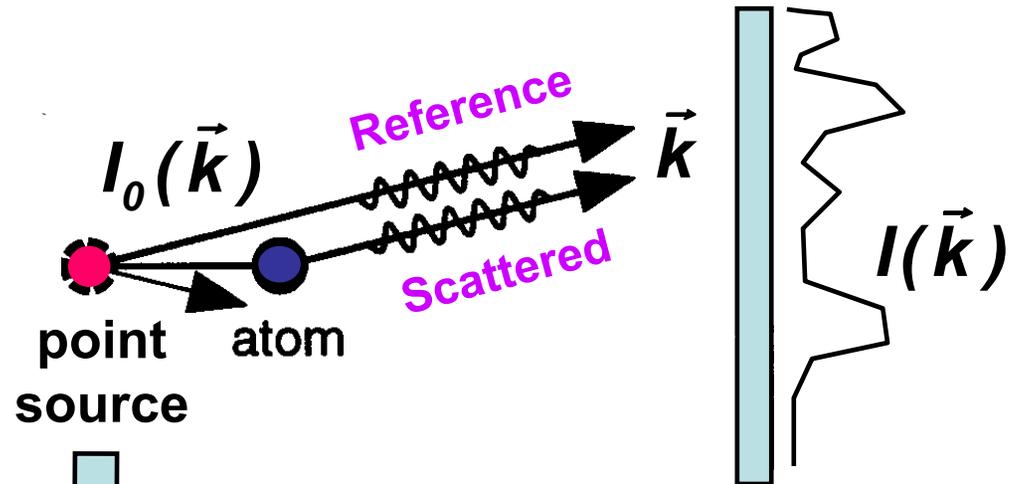
Reference lost → “The phase problem”: solved for x-rays via “direct methods”, multiple anomalous dispersion, isomorphous replacement



# Photoelectron Holography: An Additional Trick

## Holography:

Reference and scattered interfere → phase relation preserved



Use an “inside-source”: atomic or nuclear emitter (Szöke, in “Short Wavelength Radiation: Generation and Applications”, D. Attwood and J. Bokor, Eds., AIP Conference Proceedings No. 147 (1986))

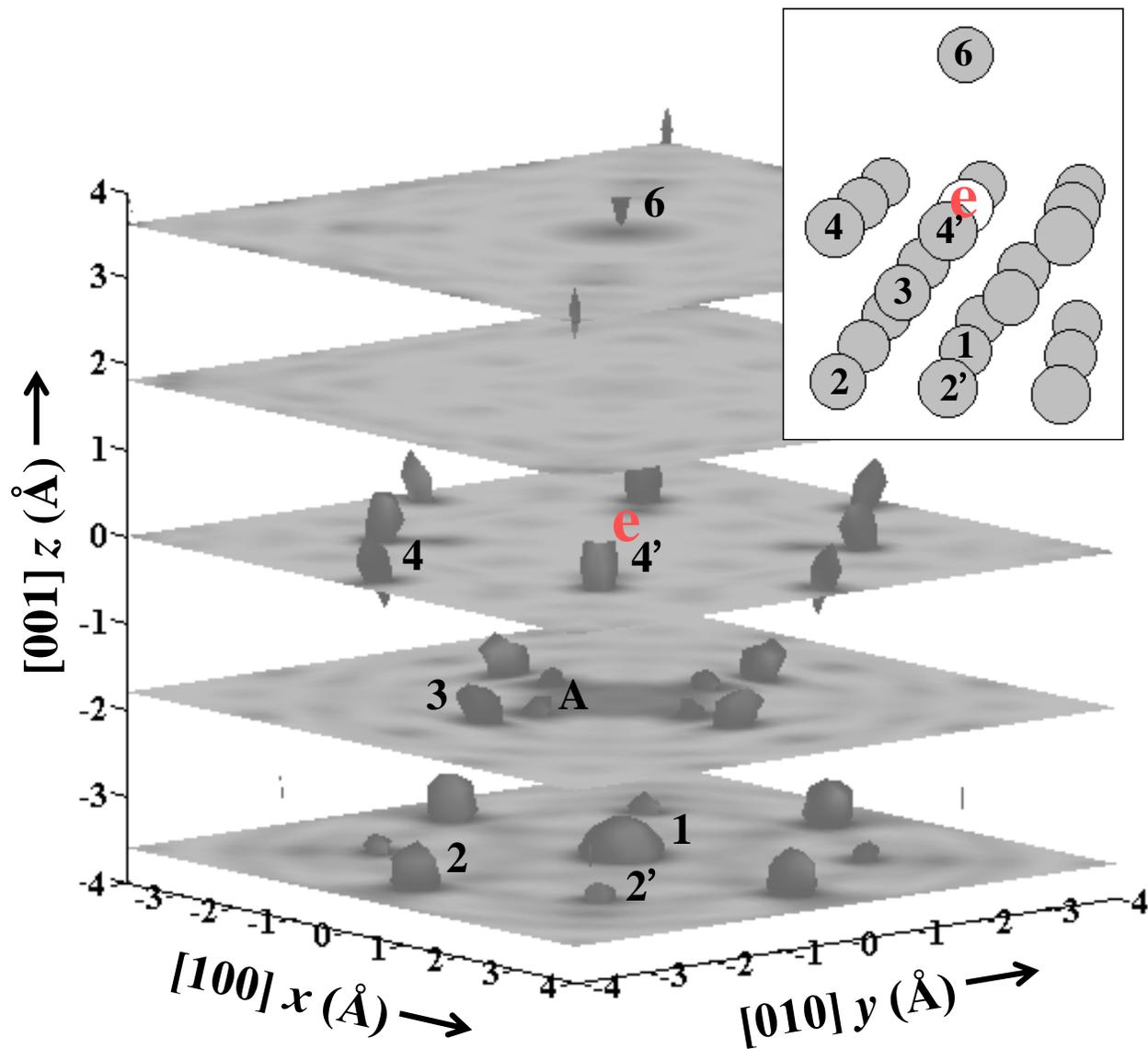
$$\chi(\vec{k}) = [I(\vec{k}) - I_0(\vec{k})] / I_0(\vec{k})$$

*Holographic image of scatterers =*

$$U(\vec{r}) = \left| \iiint \chi(\vec{k}) \exp[i\vec{k} \cdot \vec{r} - ikr] d^3 k \right|$$

Review in: C.S. Fadley, M.A. Van Hove, A. Kaduwela, S. Omori, L. Zhao, and S. Marchesini, J. Phys. Cond. Mat. 13, 10517 (2001)

# Differential photoelectron holography in Cu(001) —Cu 3p emission



# Derivative photoelectron holography: As and Si emission from As/Si(111):

$$U(\vec{r}) = \left| \iiint \chi(\vec{k}) \exp[i\vec{k}\vec{r} - ikr] d^3k \right|$$

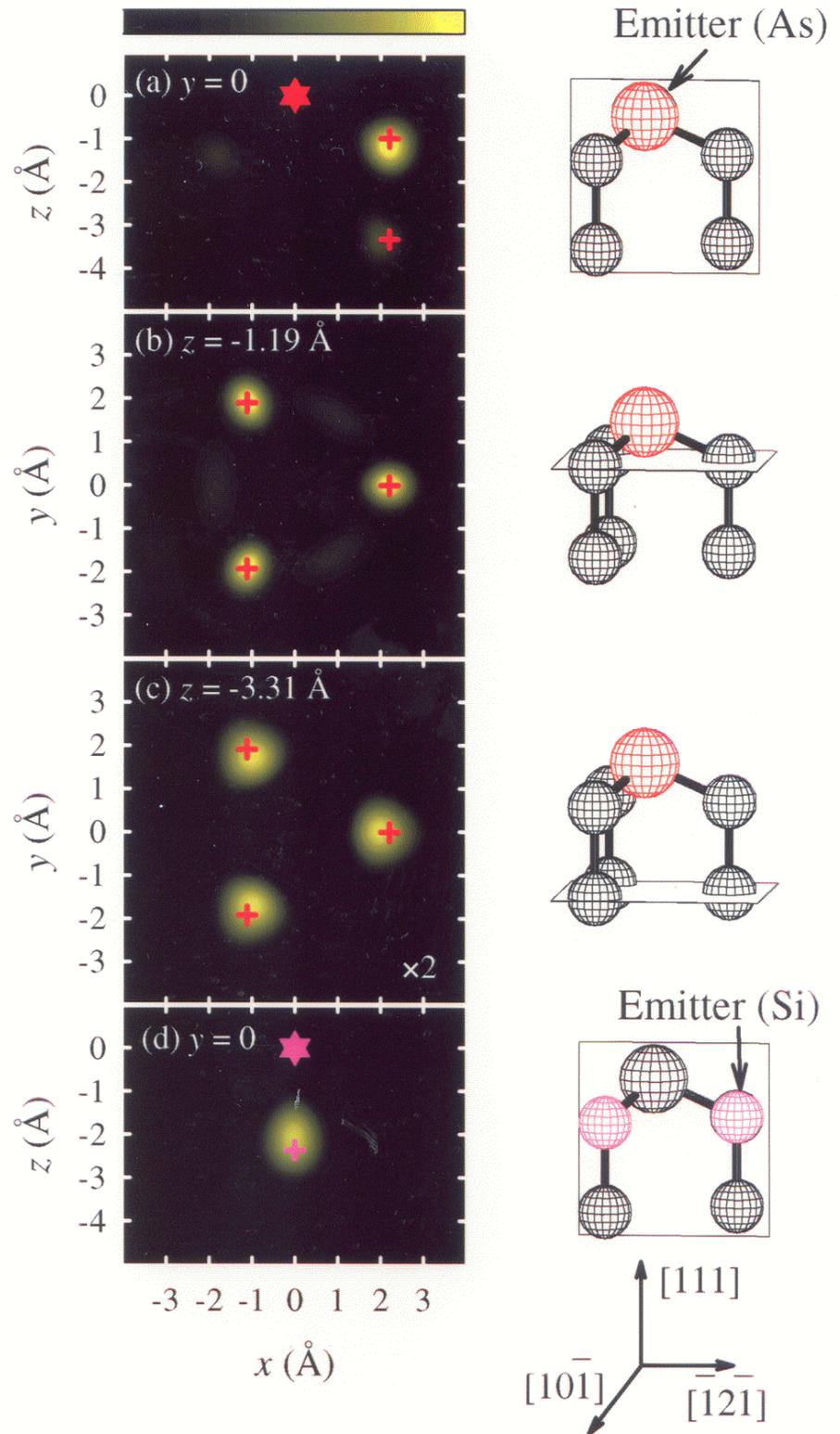
$$\text{with } \chi = \frac{I(\vec{k}) - I_0}{I_0}$$

and  $I(\vec{k})$  from integration of log arithmetic derivative

$$L(h\nu, \hat{k}) = \frac{I(h\nu + \delta, \hat{k}) - I(h\nu - \delta, \hat{k})}{[I(h\nu + \delta, \hat{k}) + I(h\nu - \delta, \hat{k})] \delta}$$

$$I(\vec{k}) \equiv I(k, \hat{k}) = A \int L(h\nu, \hat{k}) d^3k$$

Luh et al. Phys. Rev. Lett.,  
81, 4160 (1998)



## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission



Photoelectron Diffraction and Holography Model-**With Spin**

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

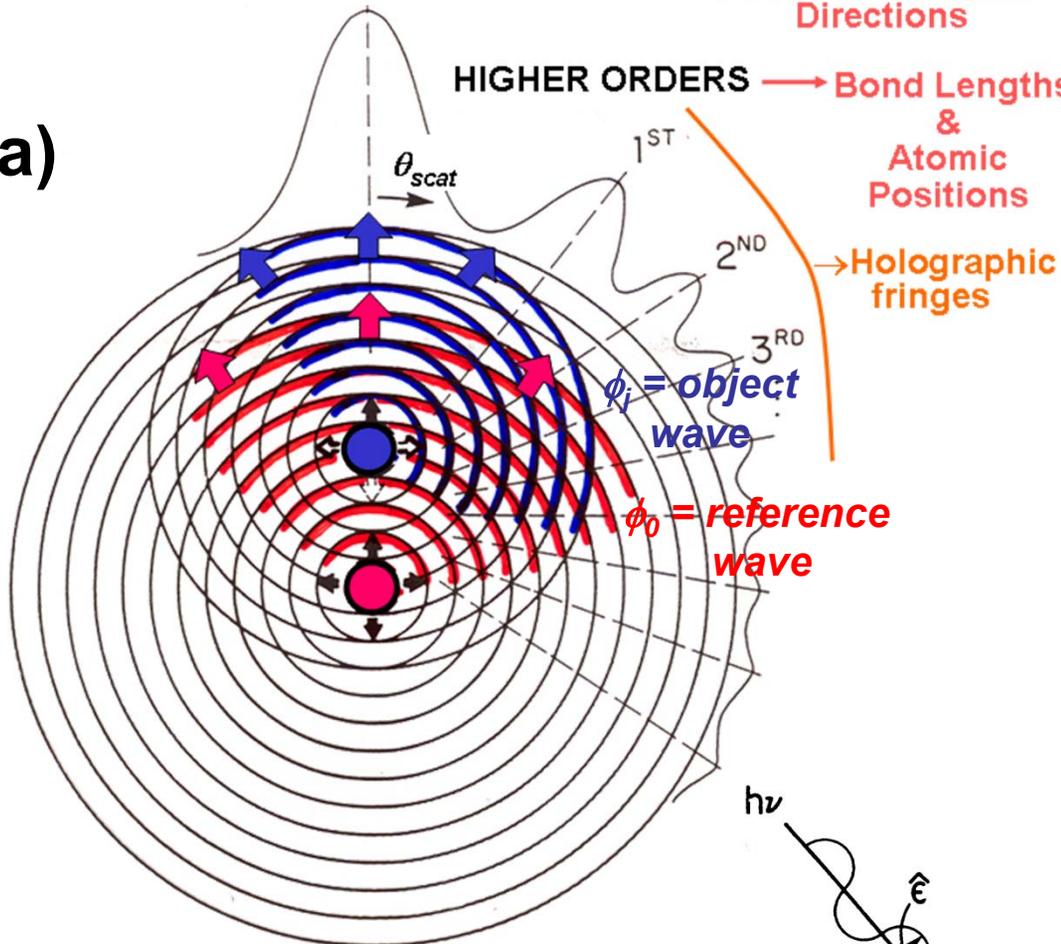
Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

FORWARD SCATT. = "0<sup>TH</sup> ORDER" → Bond & Low-Index Directions

HIGHER ORDERS → Bond Lengths & Atomic Positions

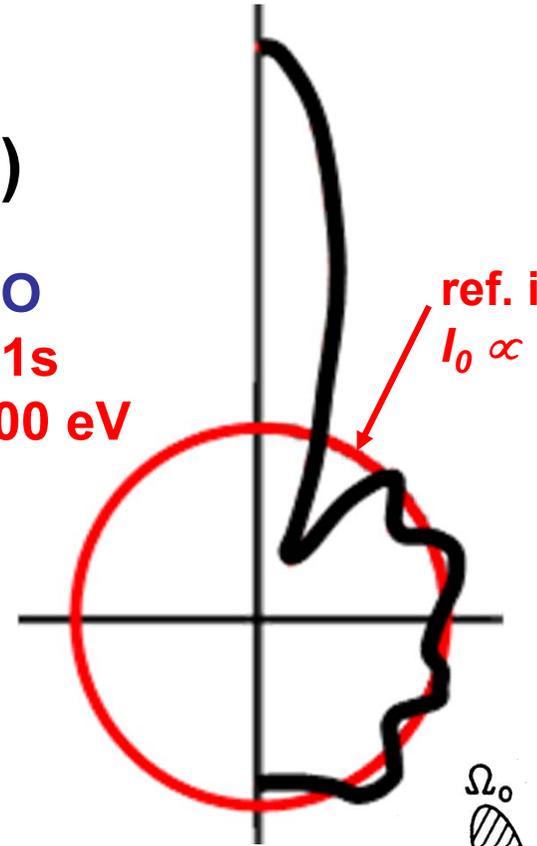
(a)



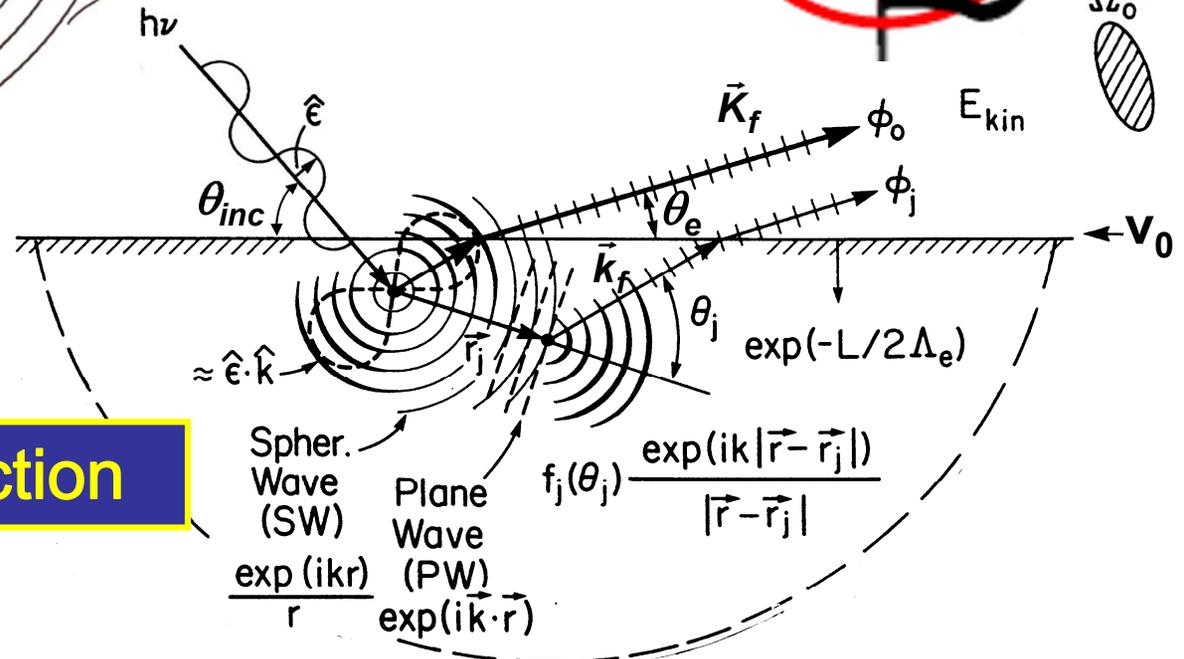
(b)

CO  
C1s  
500 eV

ref. intens.  
 $I_0 \propto |\phi_0|^2$

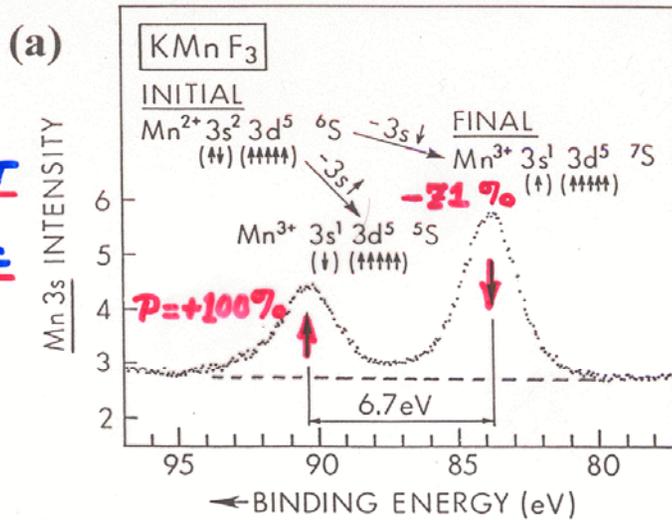


(c)



# Photoelectron Diffraction

①  
MULTIPL  
ET  
IN A  
MAGNETIC  
ATOM



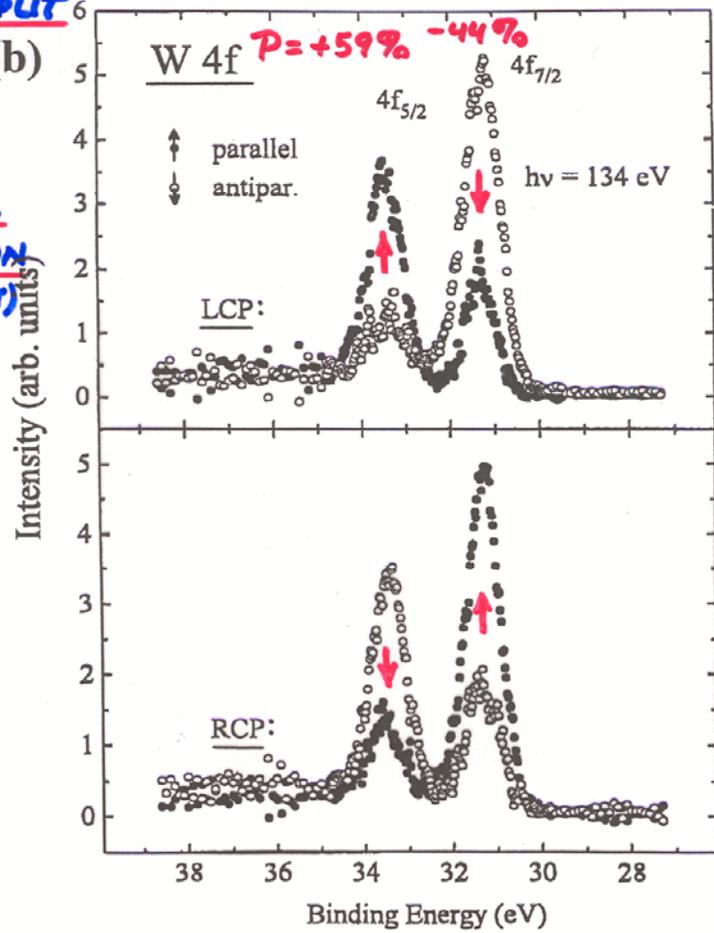
**SPIN POLARIZATION  
 IN CORE SPECTRA**

$$P = \frac{I_{\uparrow} - I_{\downarrow}}{I_{\uparrow} + I_{\downarrow}}$$

EXPT. - ZINKOVIC  
 ET AL.  
 P.R.L. 55,  
 1227 (1985)

Spin  
internally  
referenced  
to spin of  
each ion

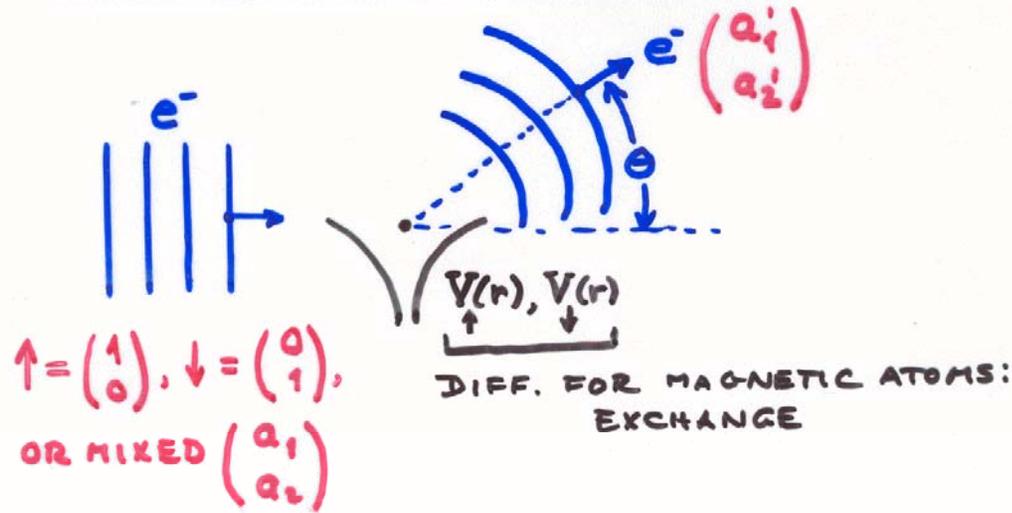
②  
SPIN-ORBIT SPLIT  
LEVEL  
EXCITED  
WITH  
CIRCULAR  
POLARIZATION  
(FANO EFFECT)



EXPT. - STARKE ET  
 AL.  
 PRB 53, R10544  
 (1996)

Spin  
externally  
referenced  
to  $\vec{k}_{hv}$  and  $\vec{M}$   
of sample

# SPIN-DEPENDENT SCATTERING:



IN GENERAL:

$$\begin{pmatrix} a_1' \\ a_2' \end{pmatrix} = \begin{pmatrix} f_{\uparrow}(\theta) & -g(\theta)e^{-i\Phi(\theta)} \\ g(\theta)e^{i\Phi(\theta)} & f_{\downarrow}(\theta) \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \end{pmatrix}$$

WITH:  $f_{\uparrow\downarrow}(\theta)$  = USUAL COULOMB + EXCHANGE SCATTERING FACTOR (PERHAPS SPIN-DEP.)

$g(\theta), \Phi(\theta)$  = SPIN-ORBIT SCATTERING EFFECTS

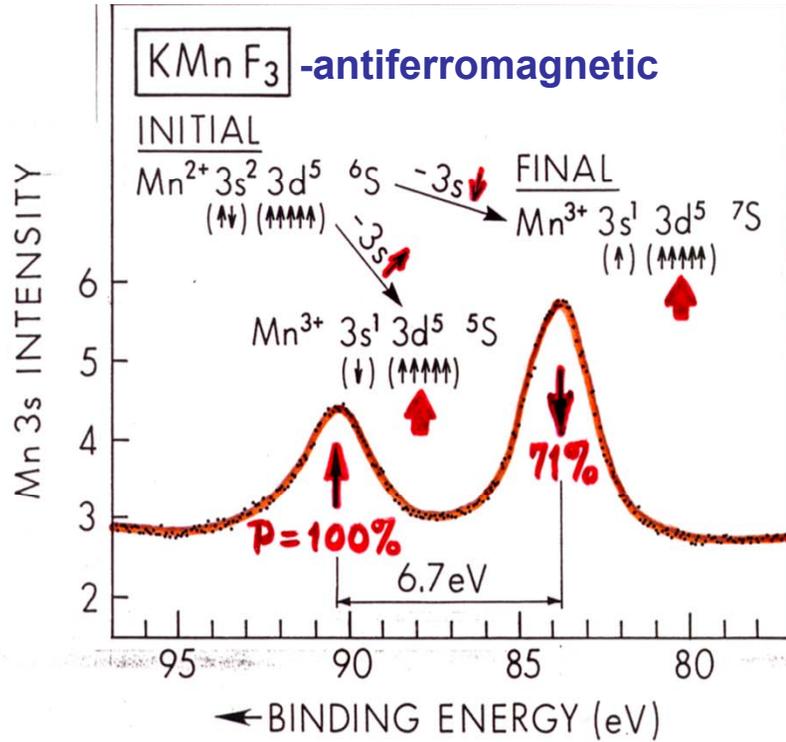
Compare:  
Mott spin detector  
at 10-100 keV

TYPICAL NOS. FOR Co @ 100 eV:

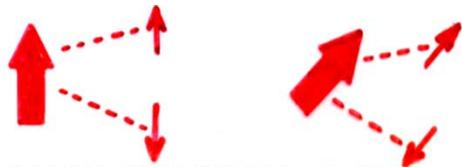
$$|f(\theta)| \approx 100 |g(\theta)|$$

(FINK + INGRAM, AT. DATA 5, 129 ('72))

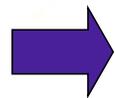
# CORE MULTIPLETS AS INTERNAL SPIN-POLARIZED e<sup>-</sup> SOURCES



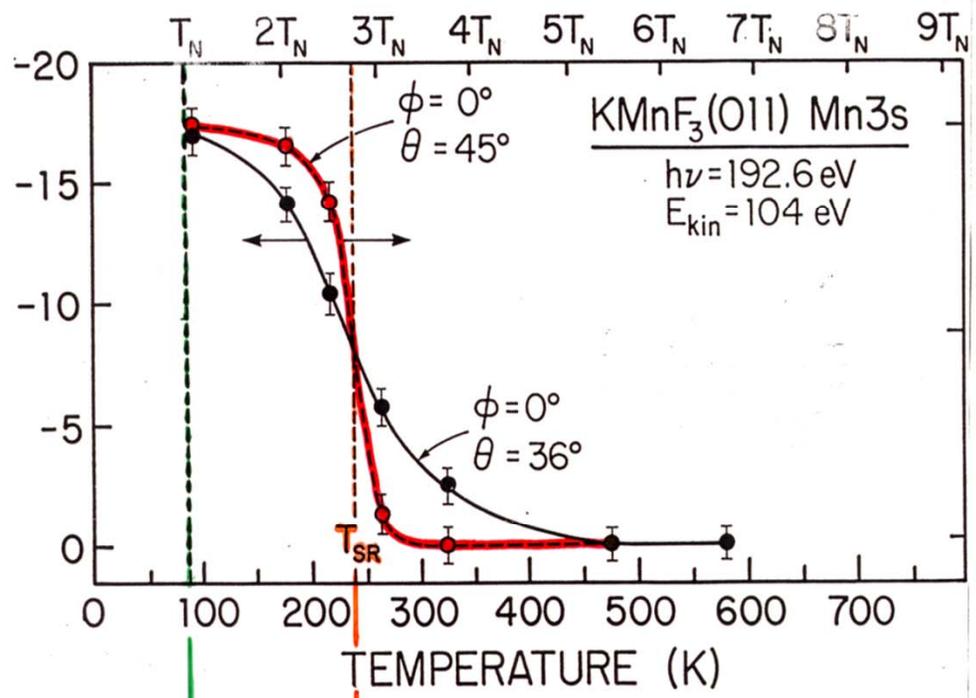
- Peak separation ∝ spin moment
- Peak separation affected by spin-dependent final-state/screening effects
- Peak intensities affected by spin-dependent scattering/diffraction
- No external spin detector required
- Photoe<sup>-</sup> spin referred to moment of emitting atom:



# SPIN-POLARIZED PHOTOELECTRON DIFFRACTION



Normalized spin-up/spin down intensity ratio (%)



Loss of long-range AF order

Loss or change of short-range AF order (near surface)

## Simulation: MnO-AF cluster

*Future experiment:  
Spin-polarized  
photoelectron holography:  
direct imaging of magnetic  
moments in 3D?:*

**Normal image-**

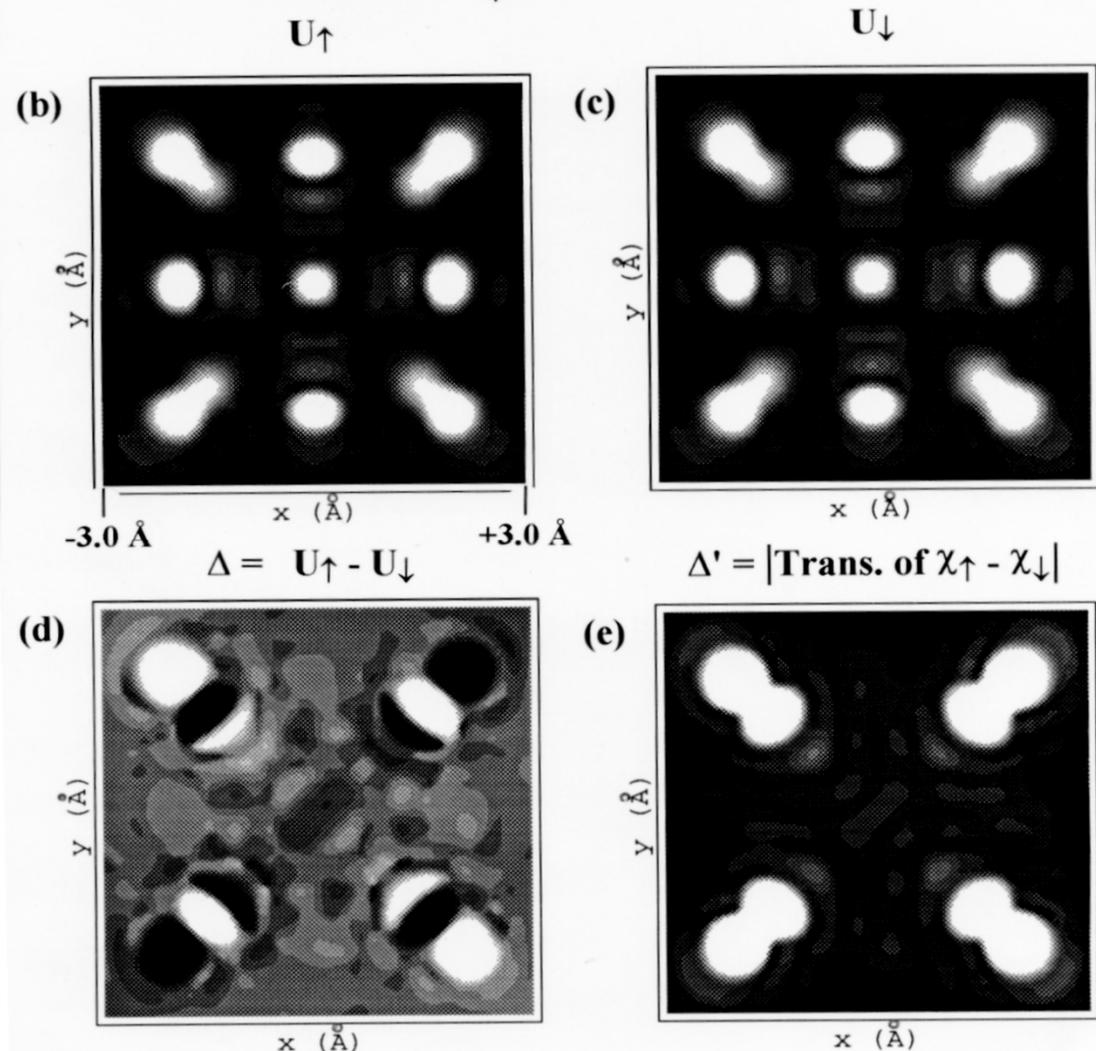
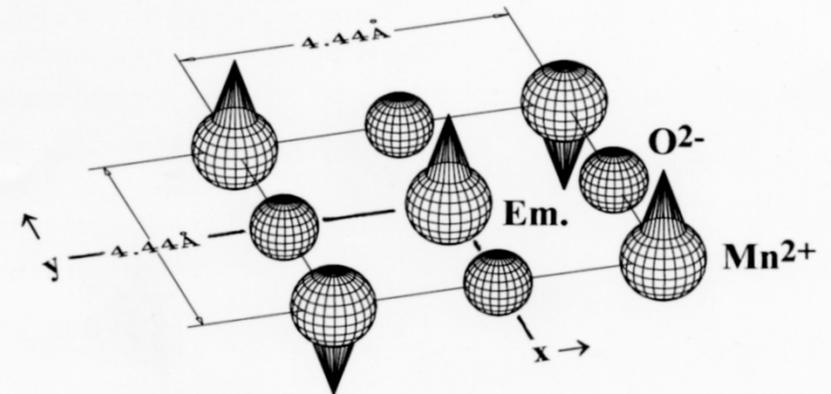
$$U(\vec{r}) = \left| \int \chi(\vec{k}) \exp[-ikr + i\vec{k} \cdot \vec{r}] d^3k \right|^2$$

**Spin-selective images-**

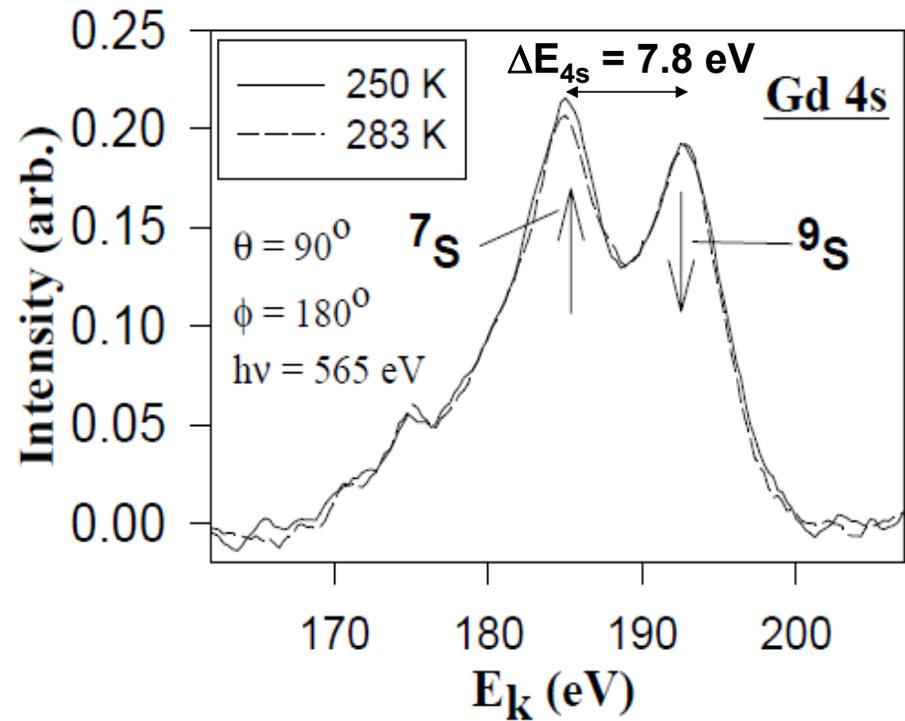
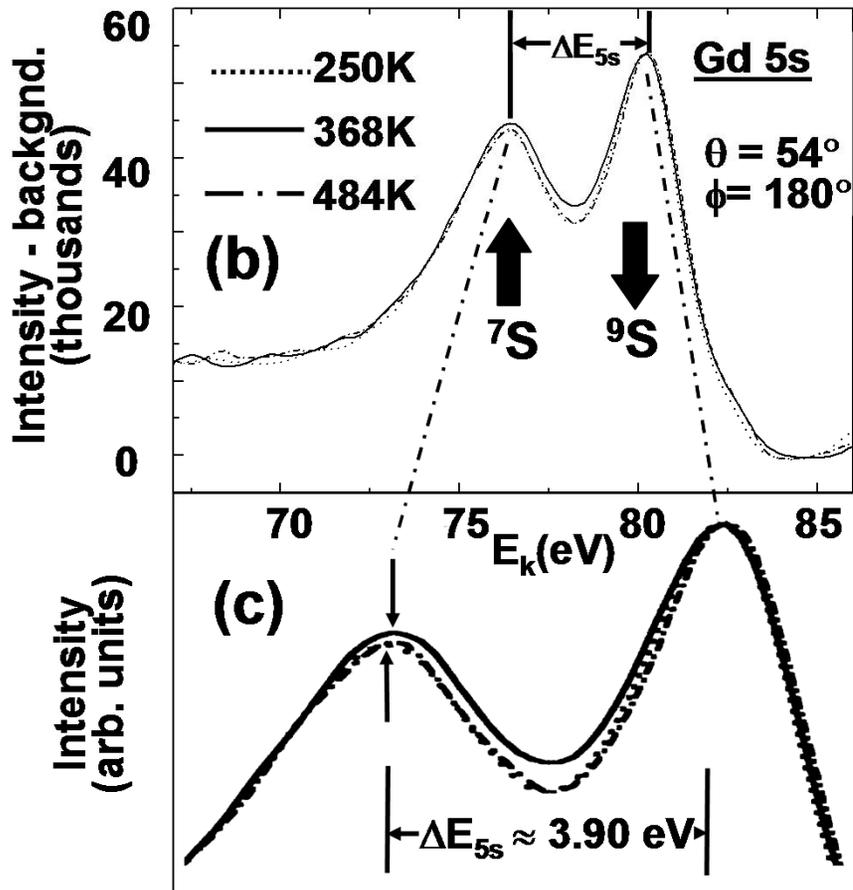
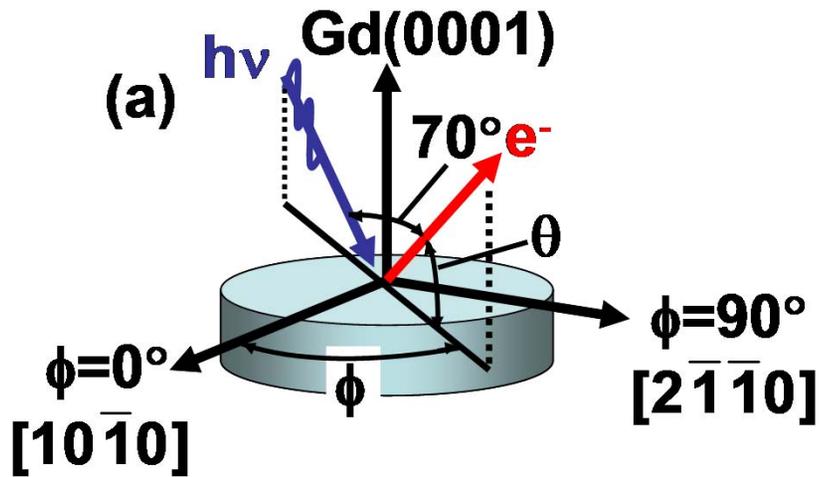
$$\Delta(r) = U_{\uparrow}(r) - U_{\downarrow}(r)$$

$$\Delta'(r) = \left| \int_k \exp(-ikr) \times \iint_k \exp(i\vec{k} \cdot \vec{r}) [\chi_{\uparrow}(\vec{k}) - \chi_{\downarrow}(\vec{k})] d^3k \right|$$

Kaduwela et al., Phys. Rev. B 50, 9656 (1994); Fadley et al., J. Phys. B Cond. Matt. 13, 10517 (2001)

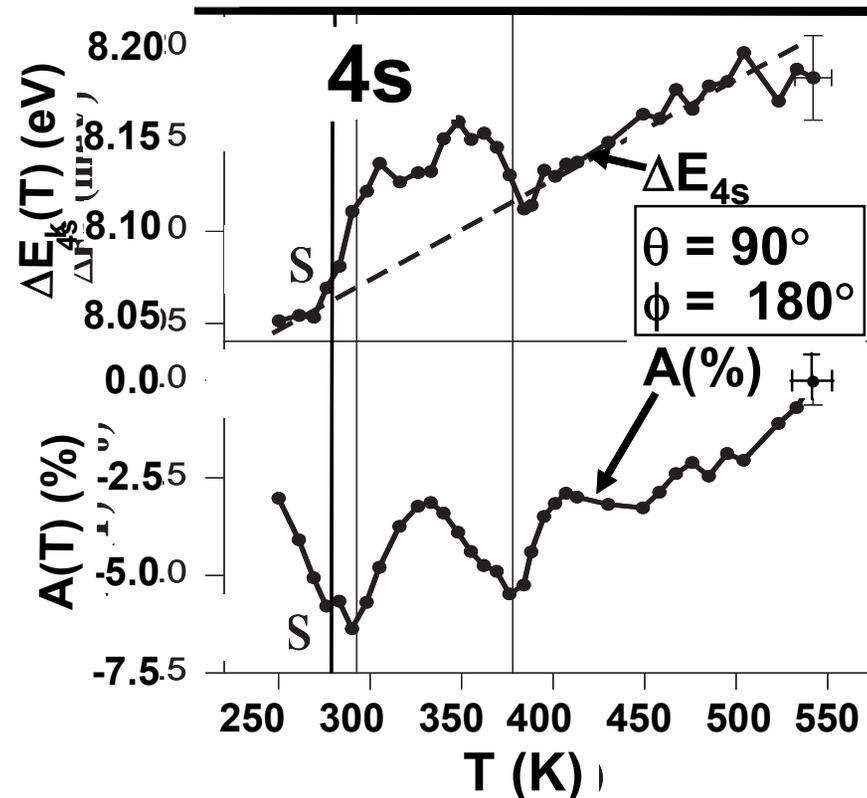
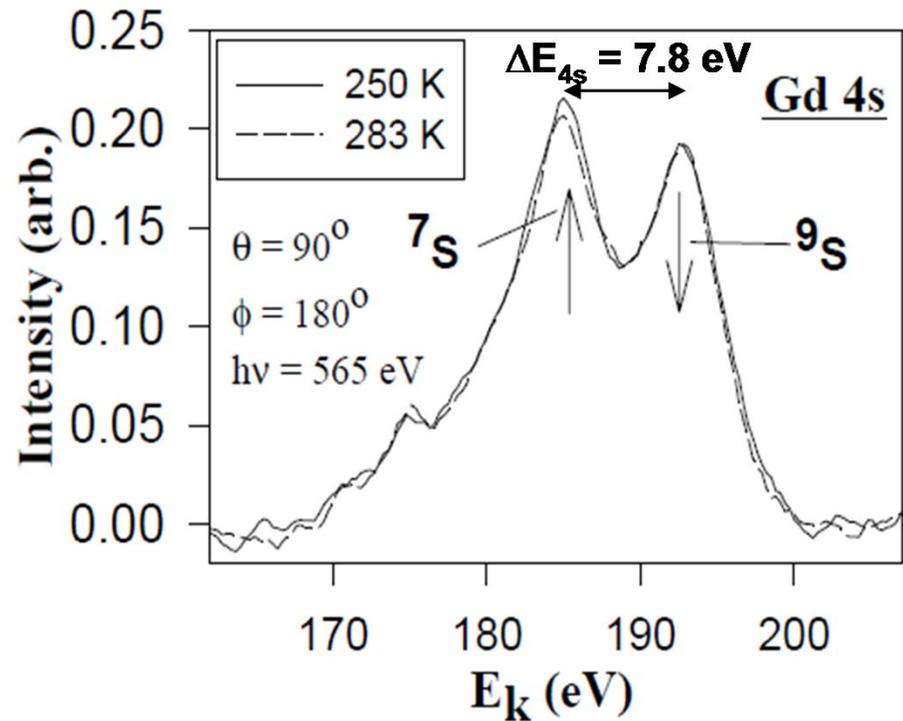


**Spin-dependent diffraction and screening during a magnetic transition at the Gd(0001) surface**

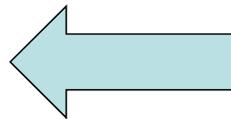


Tober et al., PRL 81, 2360 (1998)  
and J. Electron Spectrosc. 189,  
152– 156 (2013)

# Spin-dependent diffraction and screening during a magnetic transition at the Gd(0001) surface



LDA+U calculations for binding energy diff. between FM and PM states: changes too small. Suggests spin-dependent final-state screening. Future: Higher resolution, spin and time-resolved measurements



$$\text{Spin-up/spin-down asymmetry} = A(T) = \frac{[I(^7S)/I(^9S)]_T}{[I(^7S)/I(^9S)]_{HT=PM}}$$

Tober et al., PRL 81, 2360 (1998) J. Electron Spectrosc. 189, 152–156 (2013)

## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

 **Magnetic** and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

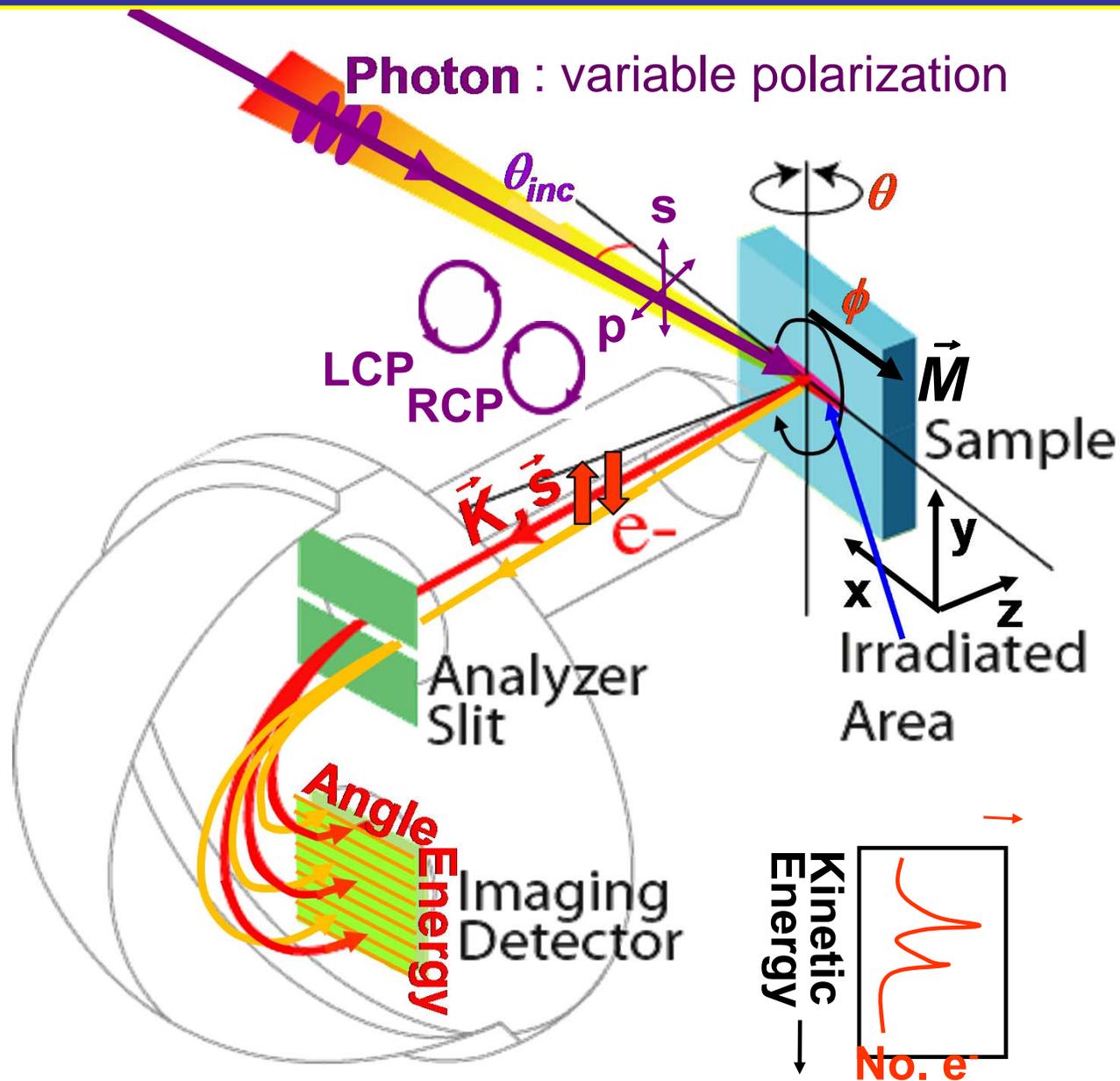
Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

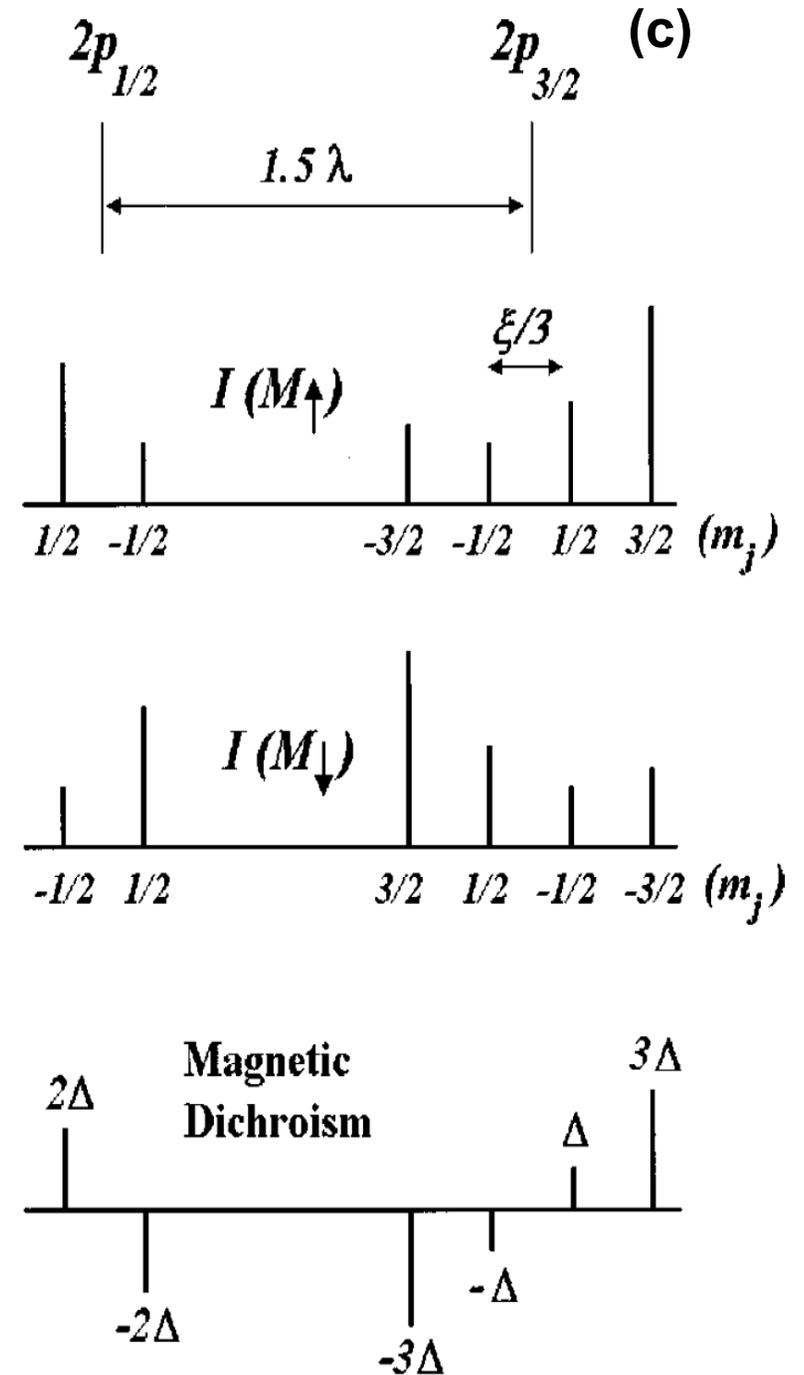
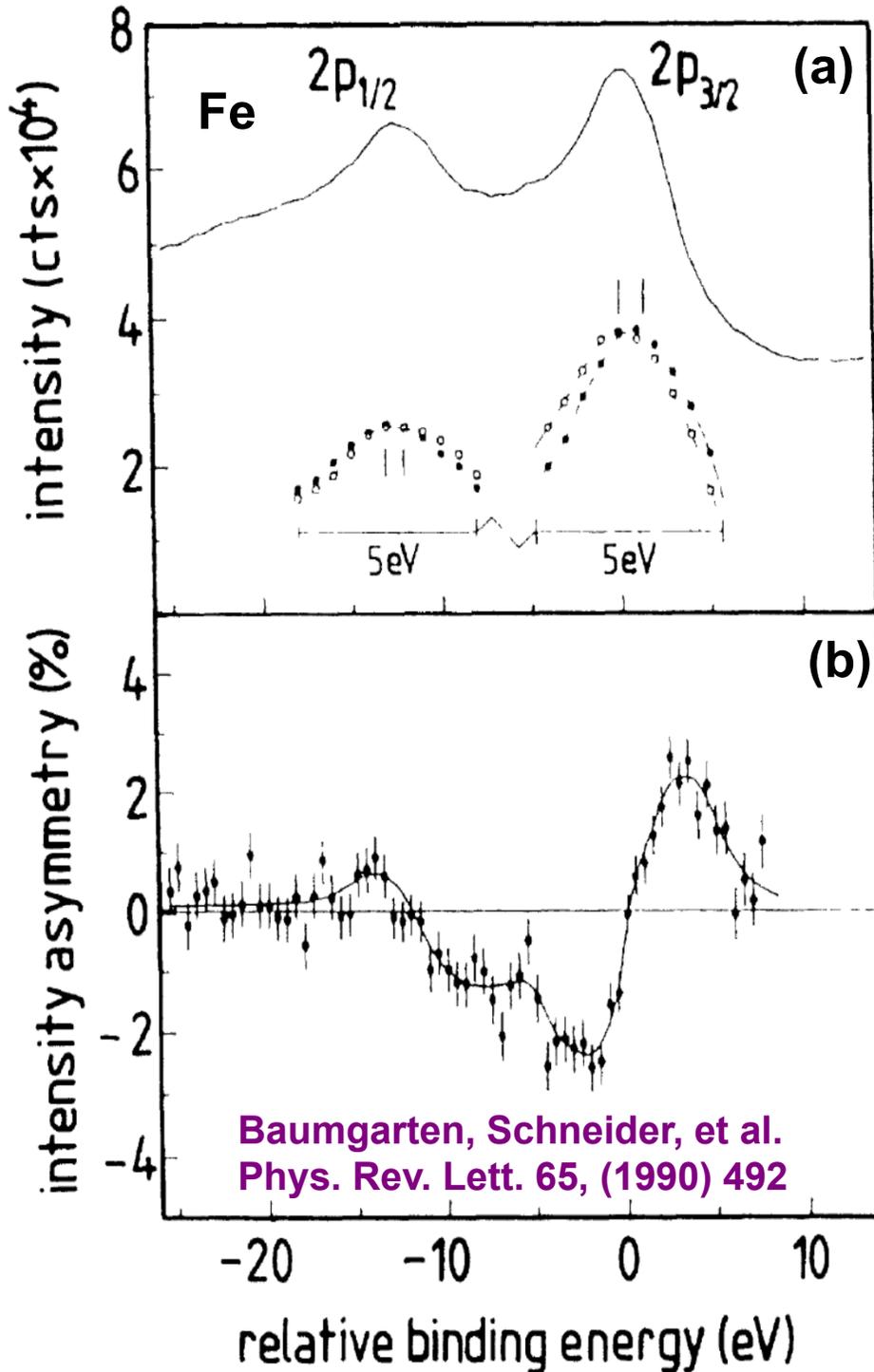
Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

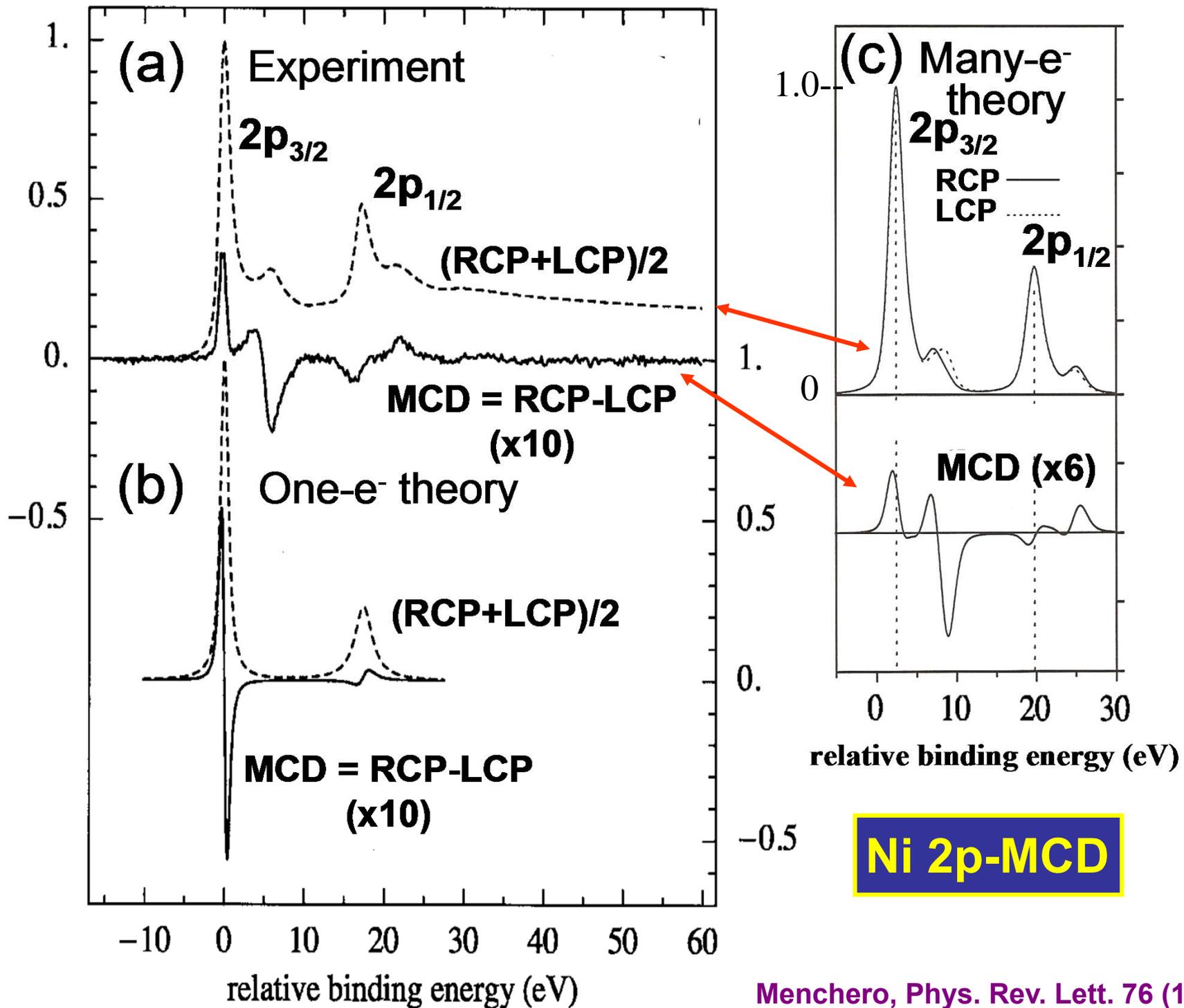
# Typical experimental geometry for energy- and angle-resolved photoemission measurements



# 1<sup>st</sup> Expt. Magnetic Circular Dichroism 1-e<sup>-</sup> Theo.



Menchero, Phys. Rev. B 57 (1998) 993

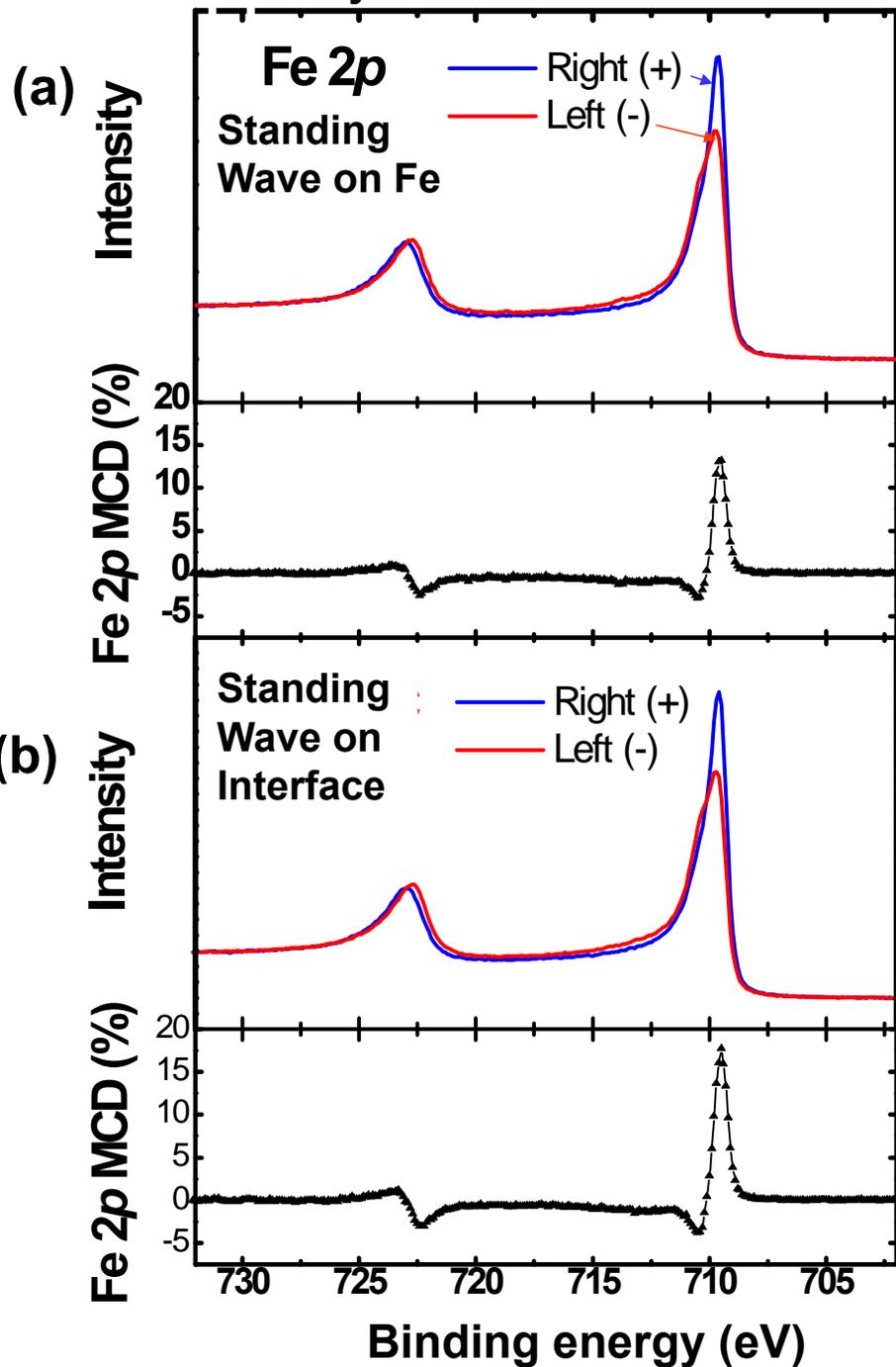


Menchero, Phys. Rev. Lett. 76 (1996) 3208

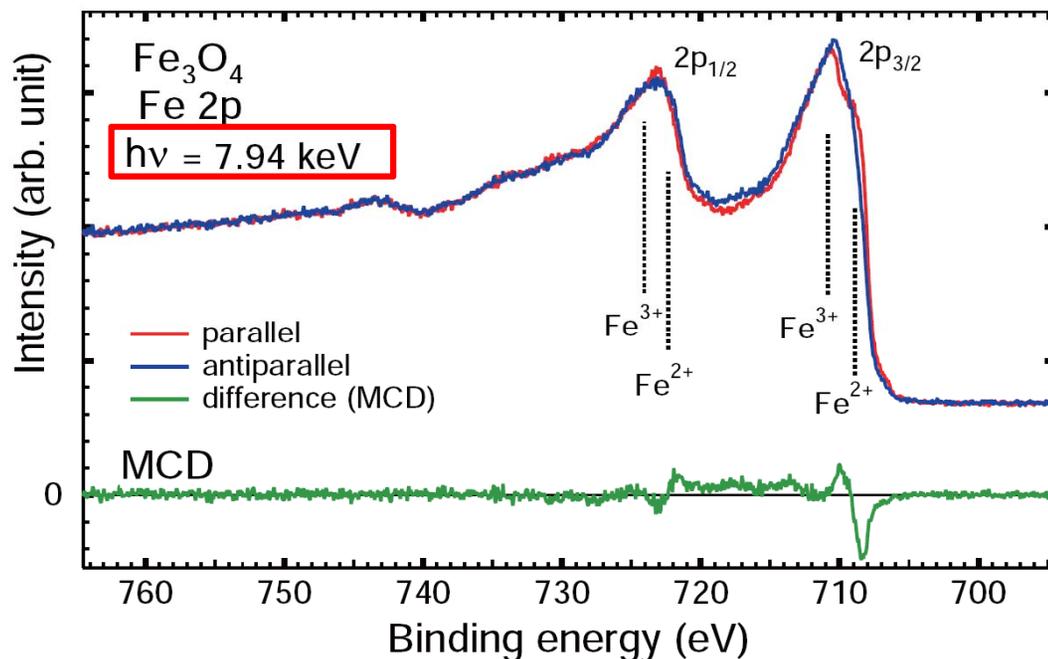
Van der Laan et al., J. Phys. Condens. Matter 12 (2000) L275

# Fe 2p Magnetic Circular Dichroism

Soft x-ray:  $h\nu = 825$  eV



(c) Hard x-ray:  $h\nu = 7.94$  keV



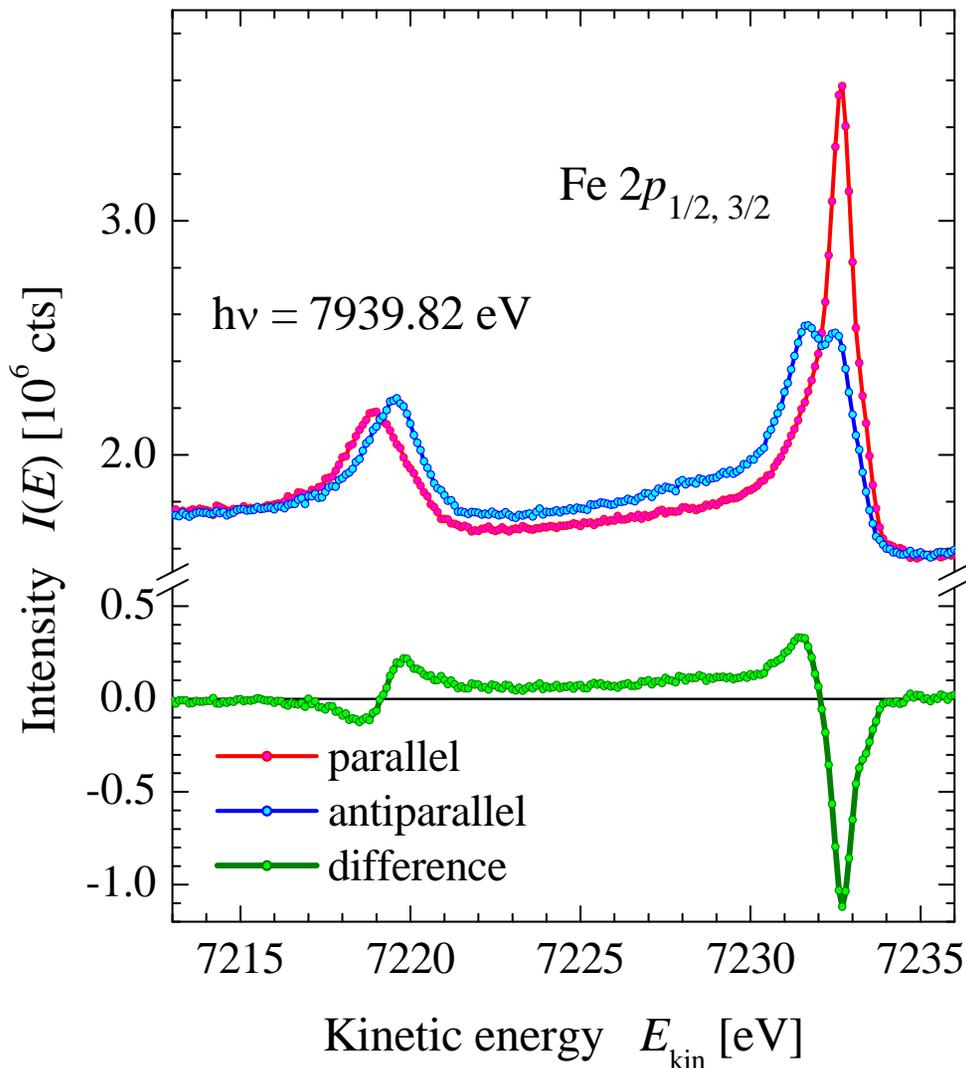
S. Ueda et al., *Appl. Phys. Express* 1 (2008) 077003

S.-H. Yang, B.S. Mun et al., *Condens. Matter* 14 (2002) L406.

# Magnetic circular dichroism in core-level HXPS

Magnetic circular dichroism from the Heusler compound  $\text{Co}_2\text{FeAl}$  in a deeply buried layer underneath a 10 nm thick MnIr exchange bias layer:

➤ multilayer [ $\text{MgO}(001)$  /  $\text{Co}_2\text{FeAl}$  (30 nm) / MnIr (10nm) /  $\text{AlO}_x$ -cap (1 nm)]



- Huge dichroism in Fe 2p core level emission is still detected in the deeply buried layer, even at relaxed energy resolution—Asymmetry max.: - 40%
- Element-specific magnetism in buried layers and interfaces

G. Fecher et al., Mainz  
Measured at SPring8

## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and **Non-Magnetic** Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

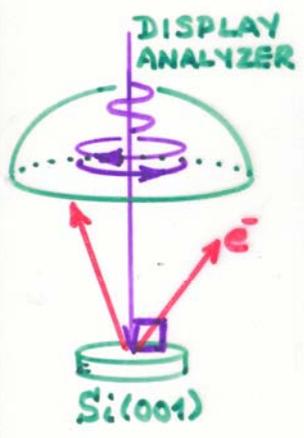
Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

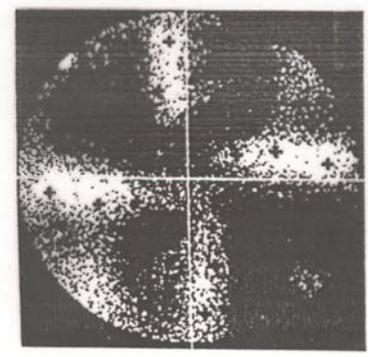
Temporal Resolution

# XPD and circular dichroism in non-magnetic systems

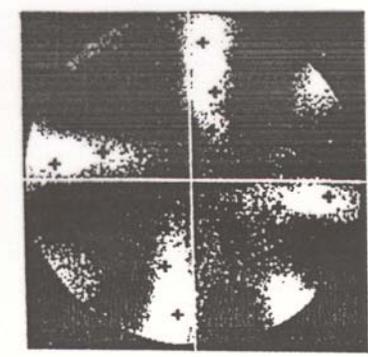
Si2p -- 250eV =  $E_{kin}$   
EXPERIMENT



(a) LCP



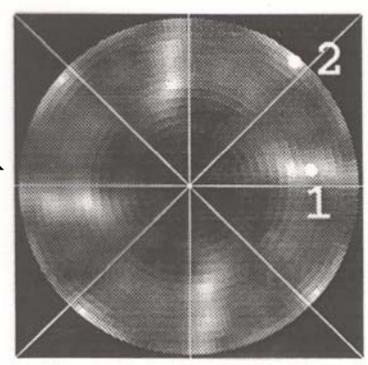
(b) RCP



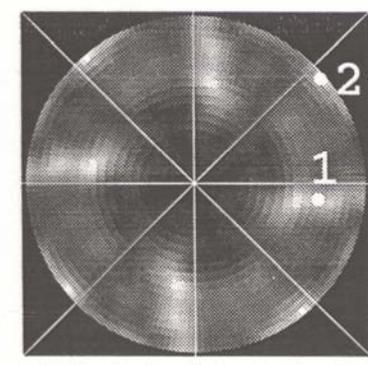
DAIMON ET AL.  
JPN. J. APPL. PHYS.  
32, L1480 ('93)

THEORY

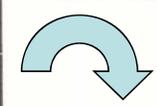
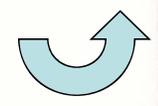
(c) LCP



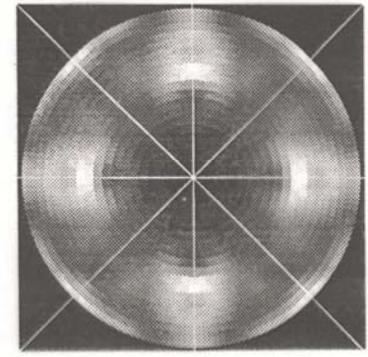
(d) RCP



IKADUWELA ET AL.  
P. R. B 50, 6203 ('94)

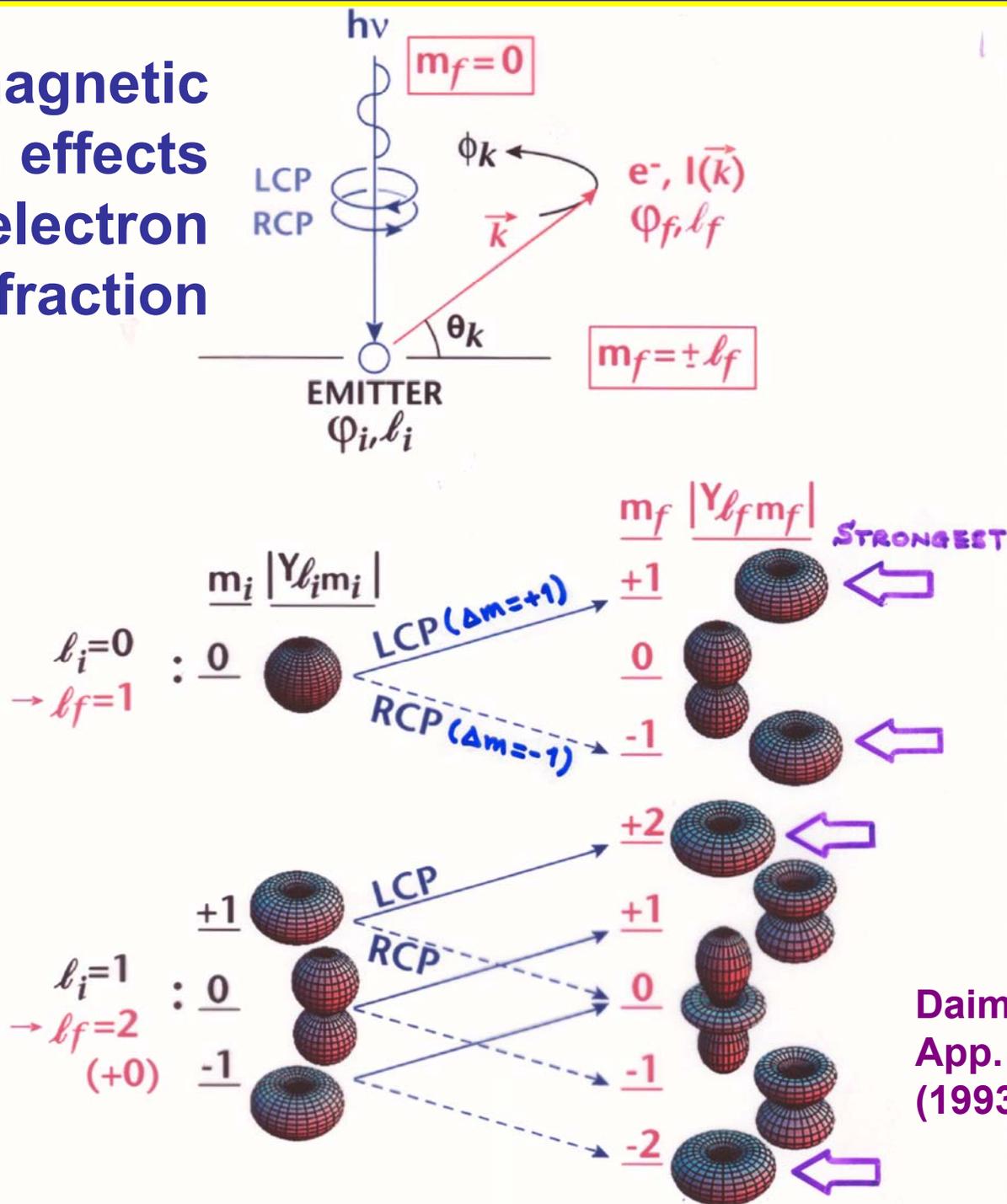


(e) UNPOLARIZED



# Circular dichroism in photoelectron angular distributions (CDAD)

→ Non-magnetic dichroism effects due to photoelectron diffraction

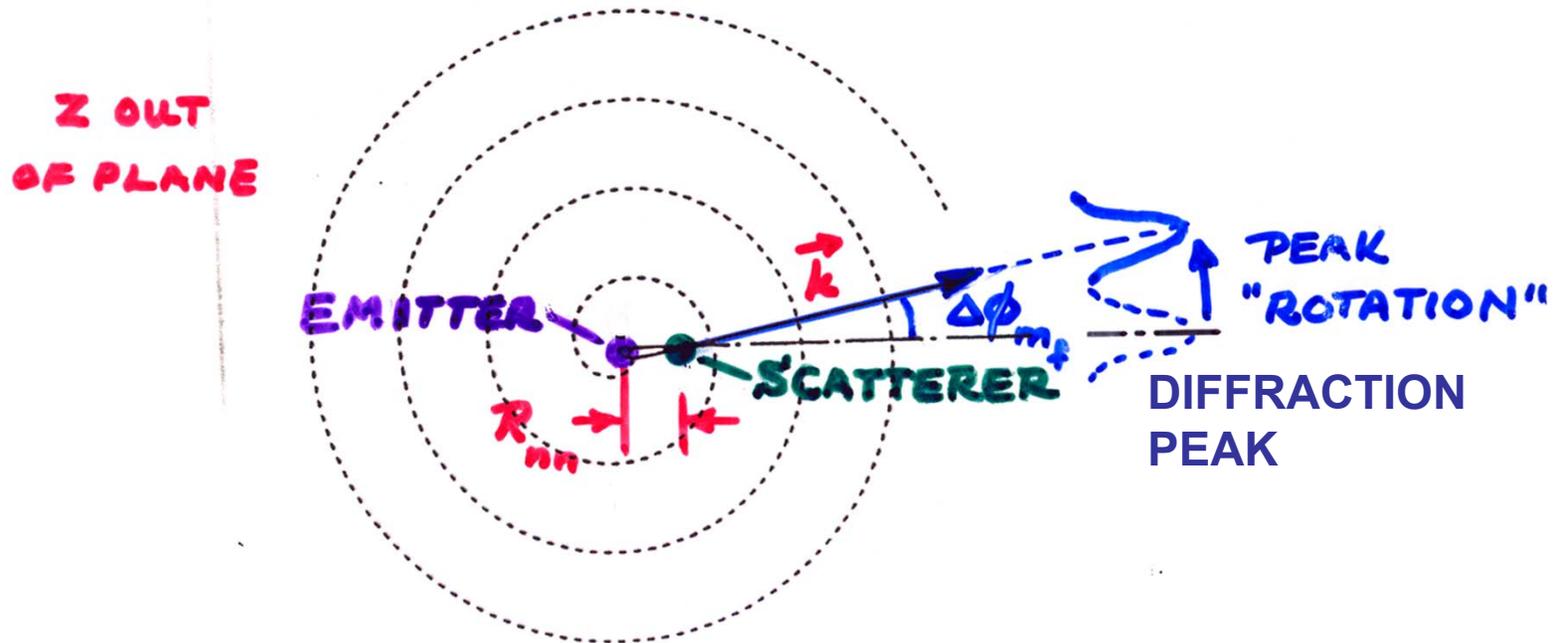


Daimon et al., Jpn. J. of App. Phys. 32, L1480 (1993)

# Circular dichroism in photoelectron angular distributions (CDAD)

CONSTANT-PHASE SURFACE OF:

$$\psi_{\text{PHOTOE}}(r, \theta, \phi) \propto \frac{e^{ikr}}{r} \textcircled{H}_{lm} e^{im_f \phi}$$



$$\Delta\phi_{m_f} = \frac{m_f}{R_{nn, ||k||}}$$

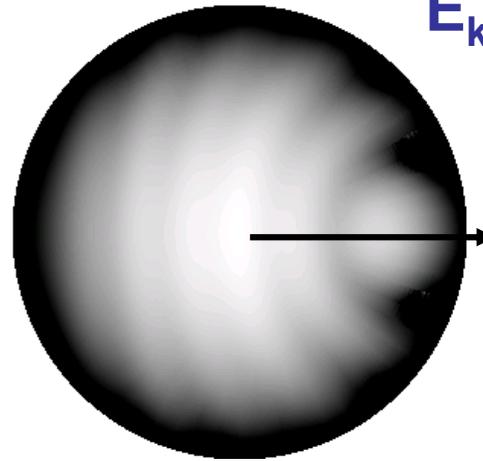
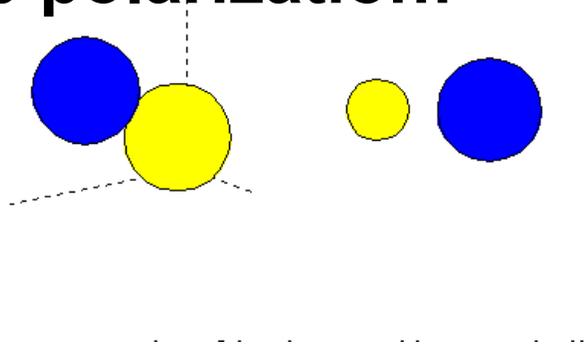
$$\overline{m_f} \approx m_{f, \max}$$

DAIMON ET AL.  
JPN. J. APPL. PHYS.  
32, L1480 ('93)

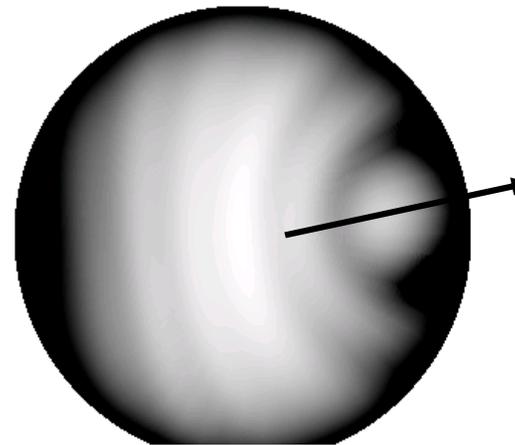
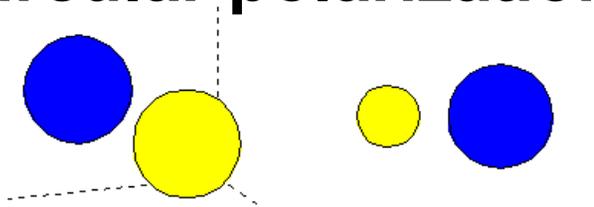
# Theory: Effect of varying the polarization?: C 1s emission from CO

$E_{\text{kin}} = 200 \text{ eV}$

**Linear p polarization:**

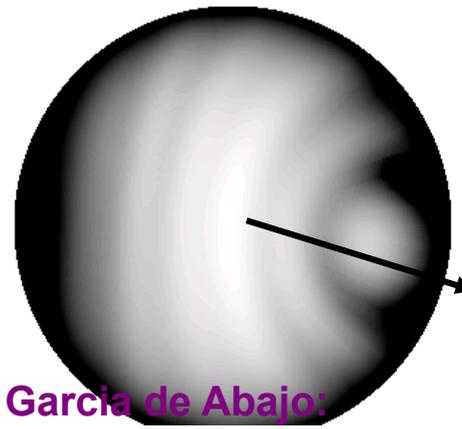
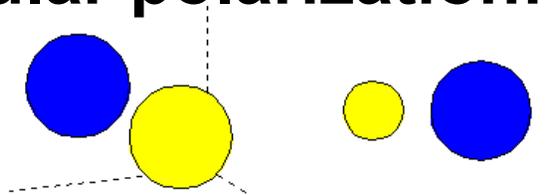


**Right circular polarization:**



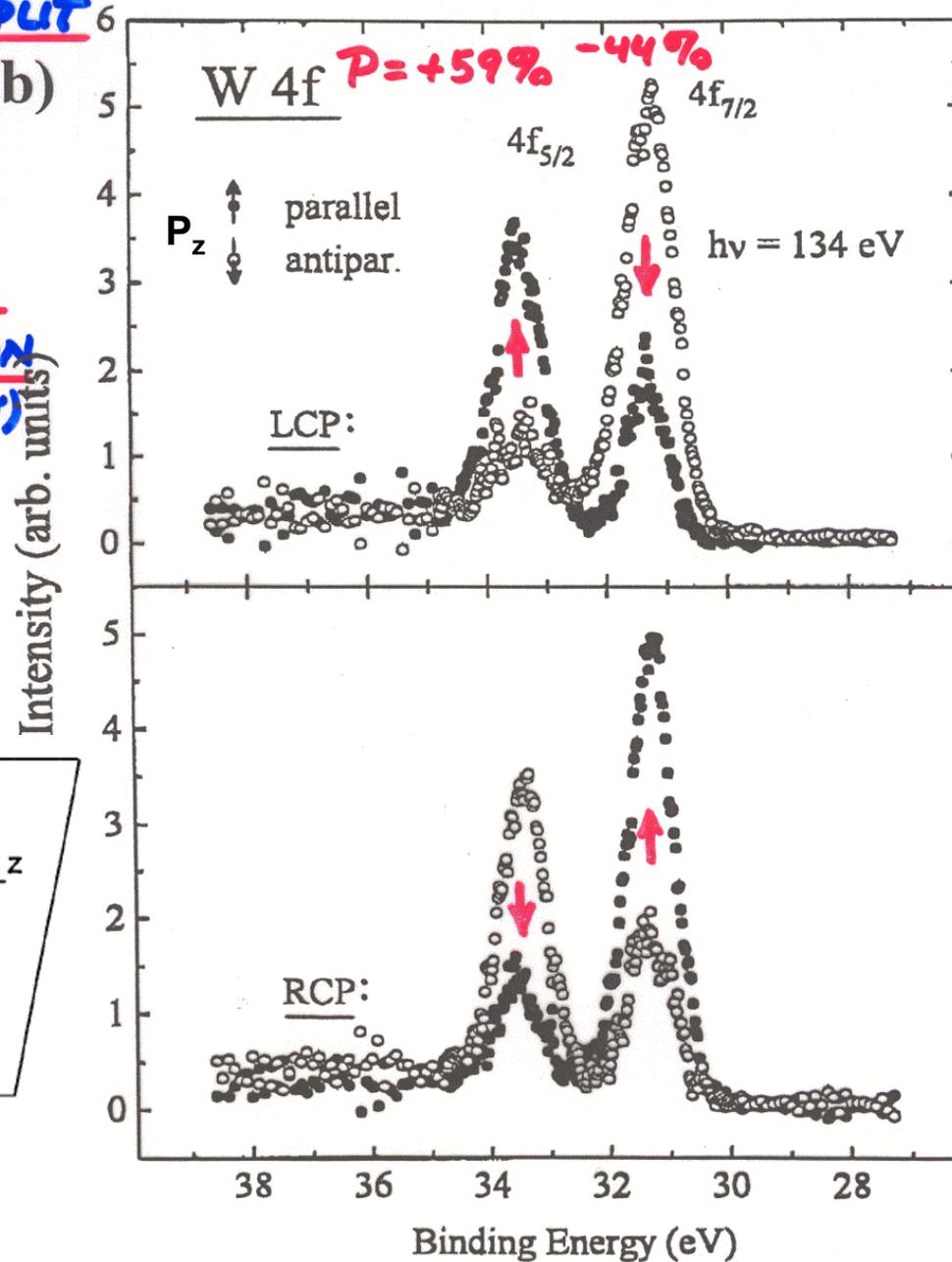
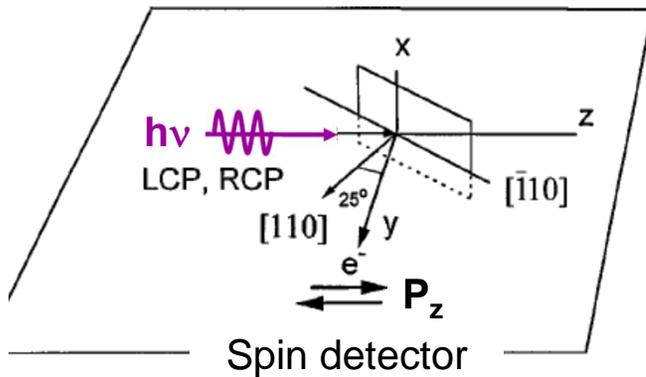
**Circular dichroism in angular distributions (CDAD)**

**Left circular polarization:**



# Fano effect and spin polarization (SP) in core photoelectron spectra—expt.

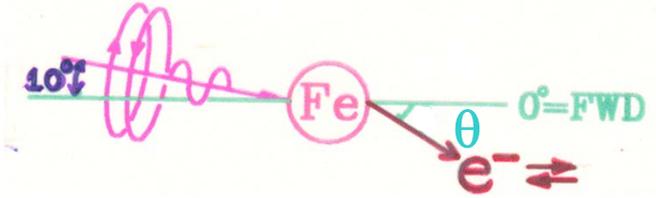
**SPIN-ORBIT SPLIT**  
**LEVEL (b)**  
**EXCITED**  
**WITH**  
**CIRCULAR**  
**POLARIZATION**  
**(FANO EFFECT)**



EXPT. - STARKE ET AL.  
 PRB 53, 210544  
 (1996)

Putting non-magnetic CD (CDAD) together with spin polarization: Theory with proper final-state channel interference: Single Atom

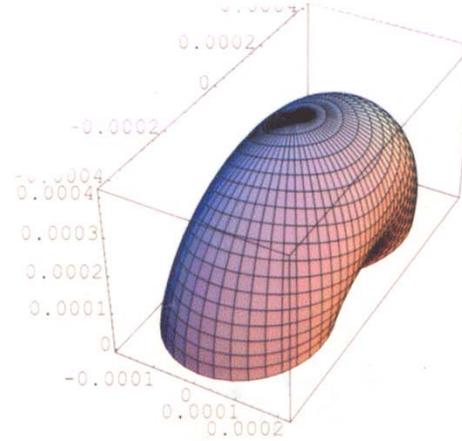
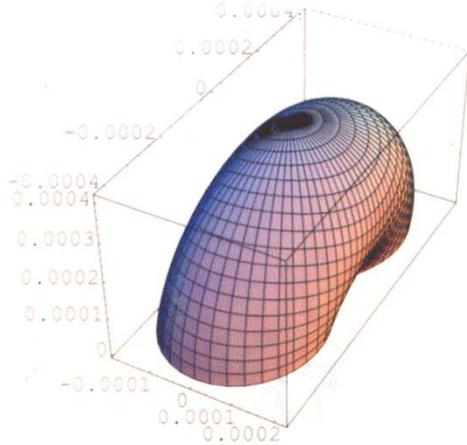
Free Fe  $2p_{1/2}$   
 THEORY (s+d)



$E_{kin} = 145 \text{ eV}$

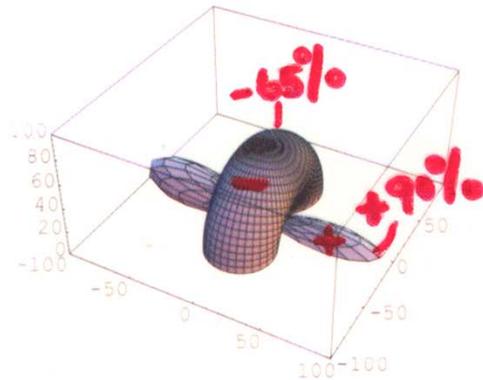
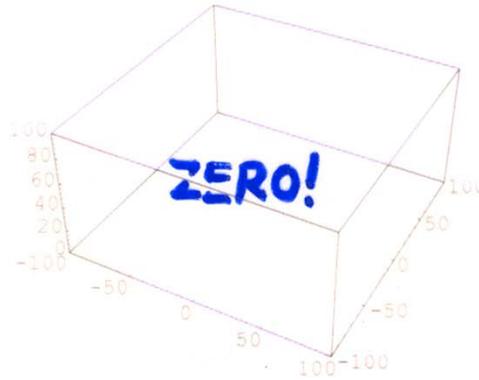
LCP

RCP



%CDAD

Spin Pol. (LCP)



$$\%CDAD = \frac{RCP - LCP}{RCP + LCP} \times 100$$

$$\%P = \frac{LCP(\uparrow) - LCP(\downarrow)}{LCP(\uparrow) + LCP(\downarrow)} \times 100$$

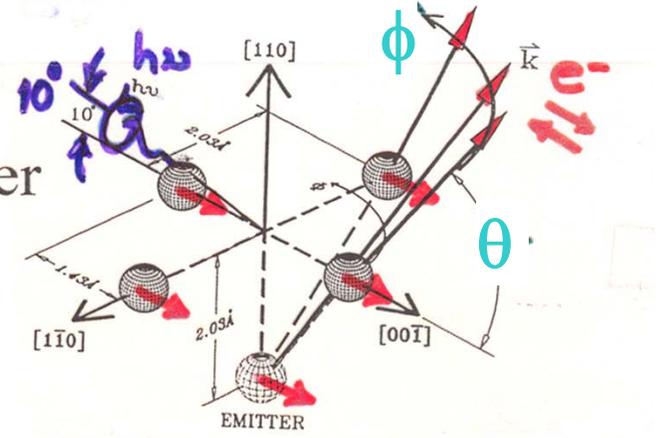
= CIRCULAR DICHOISM IN ANGULAR DISTRIBUTION

A. Kaduwela, C.F., unpublished

Putting non-magnetic CD (CDAD) together with spin polarization: Theory with proper final-state channel interference: Single Atom

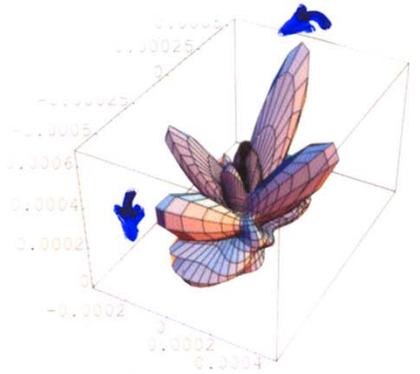
Fe 2p<sub>1/2</sub>  
Ferromagnetic Cluster

**THEORY (s+d)**  
**- ADDS PHOTOELECTRON DIFFRACTION**

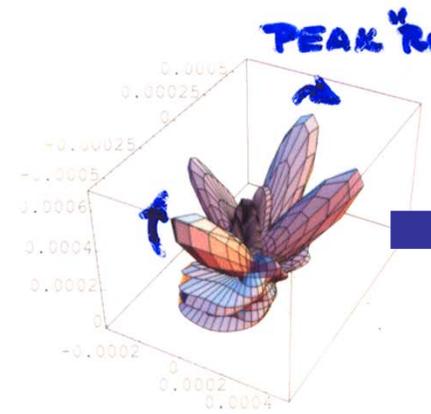


LCP

RCP



%CDAD

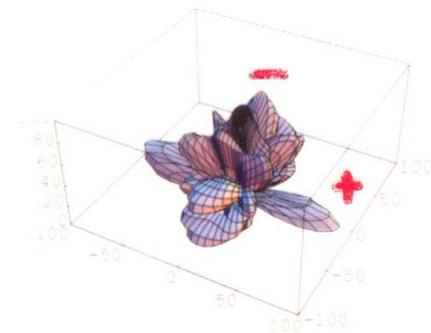
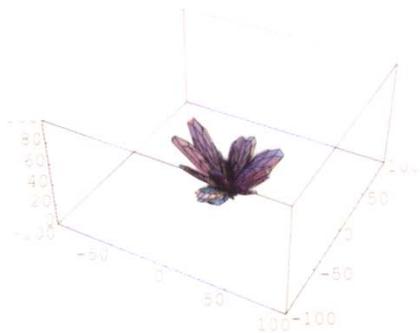


Spin Pol. (LCP)

**PEAK ROTATIONS<sup>II</sup>**  
**(ALA DAIMON ET AL.)**



“Circular Dichroism In Angular Distributions” (CDAD)



$$\%CDAD = \frac{RCP - LCP}{RCP + LCP} \times 100$$

$$\%P = \frac{LCP(\uparrow) - LCP(\downarrow)}{LCP(\uparrow) + LCP(\downarrow)} \times 100$$

A. Kaduwela, C.F., unpublished

## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

 Resonant Photoemission-**covered already**

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

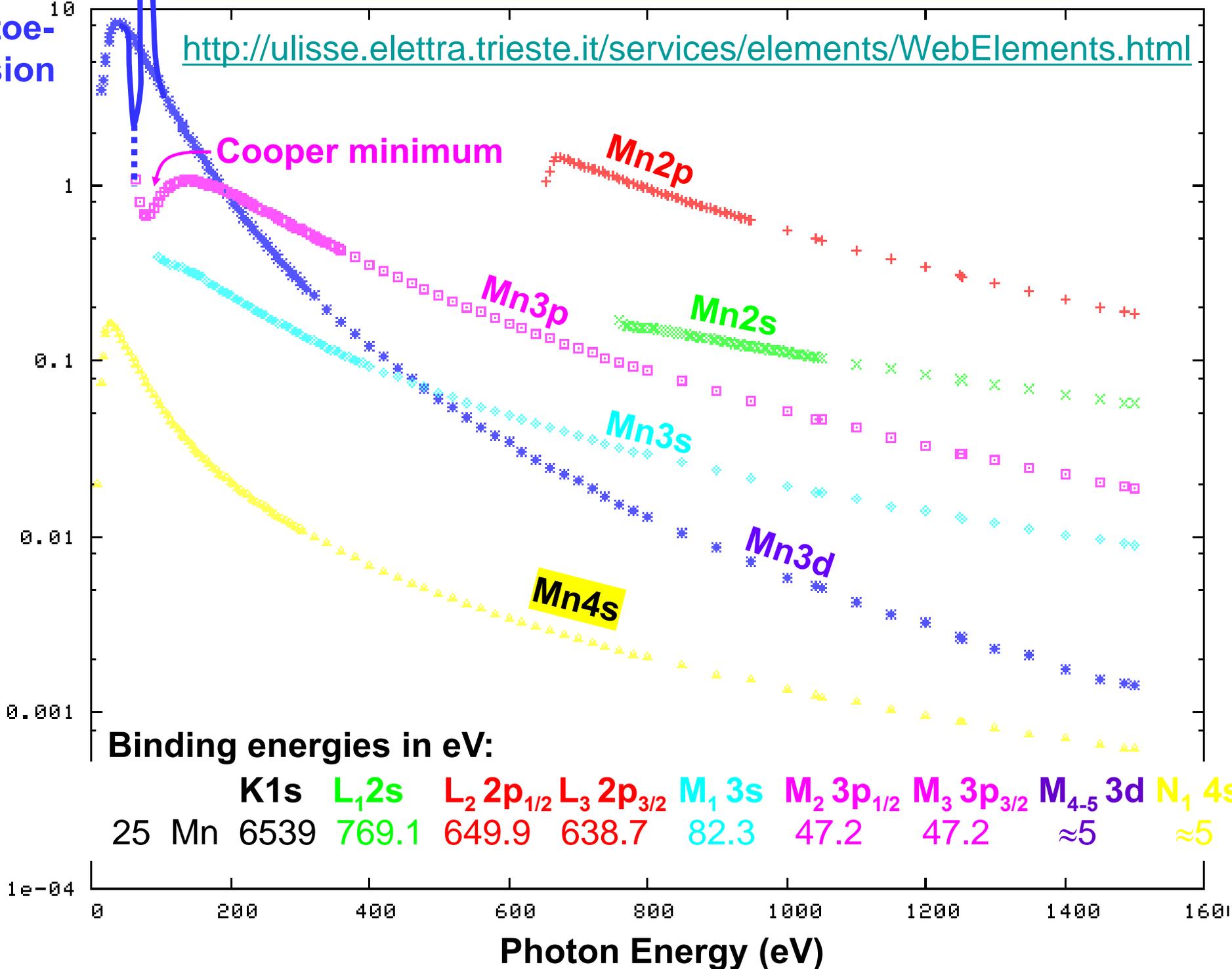
Temporal Resolution

# PHOTOELECTRIC CROSS SECTIONS FOR Mn

<http://ulisse.elettra.trieste.it/services/elements/WebElements.html>

Resonant  
Photoe-  
mission

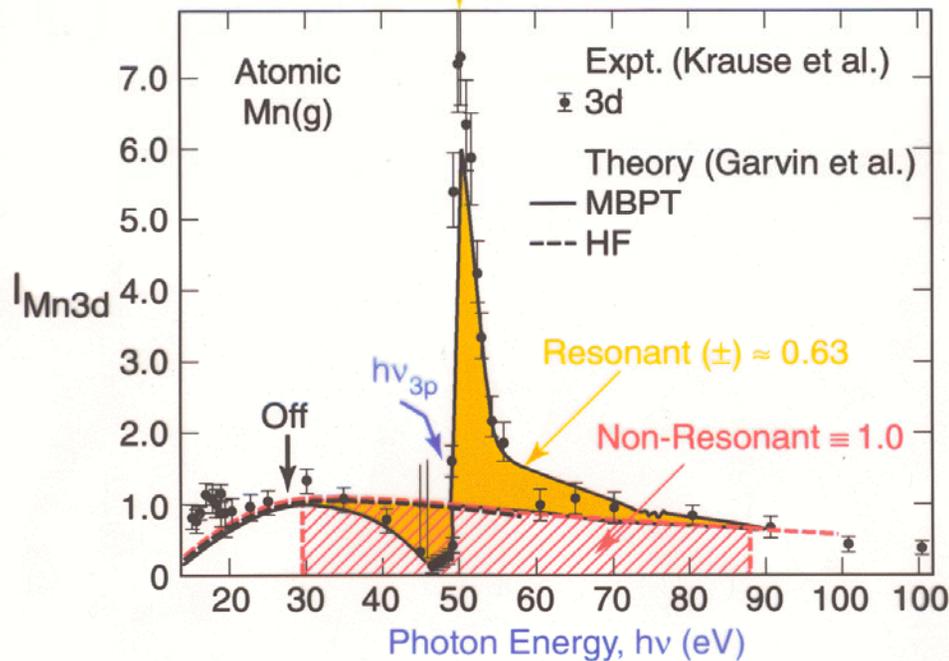
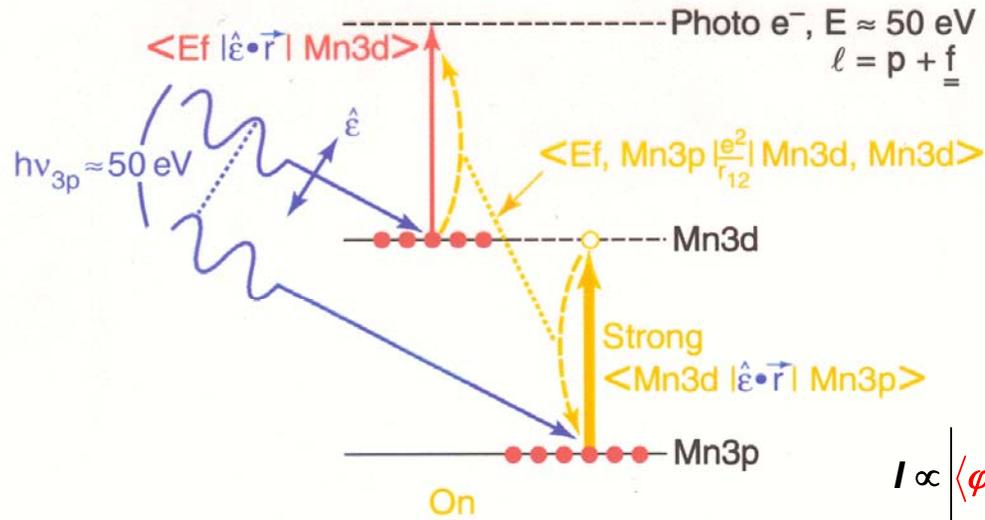
Cross section (Mbarns)



# Resonant Photoemission—Atomic Mn, Mn 3d with Mn 3p

## Single-atom resonant photoemission:

Ex. – Mn atom: Mn3d emission, resonance with Mn3p

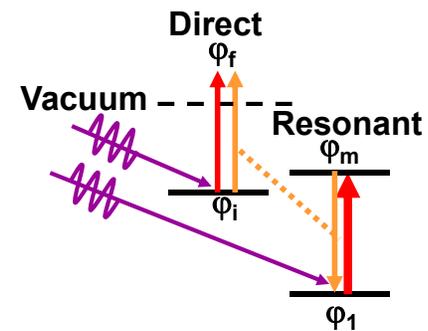


## Normal photoemission:

$$I \propto \left| \langle \varphi_f(\mathbf{1}) | \hat{e} \cdot \vec{r} | \varphi_i(\mathbf{1}) \rangle \right|^2$$

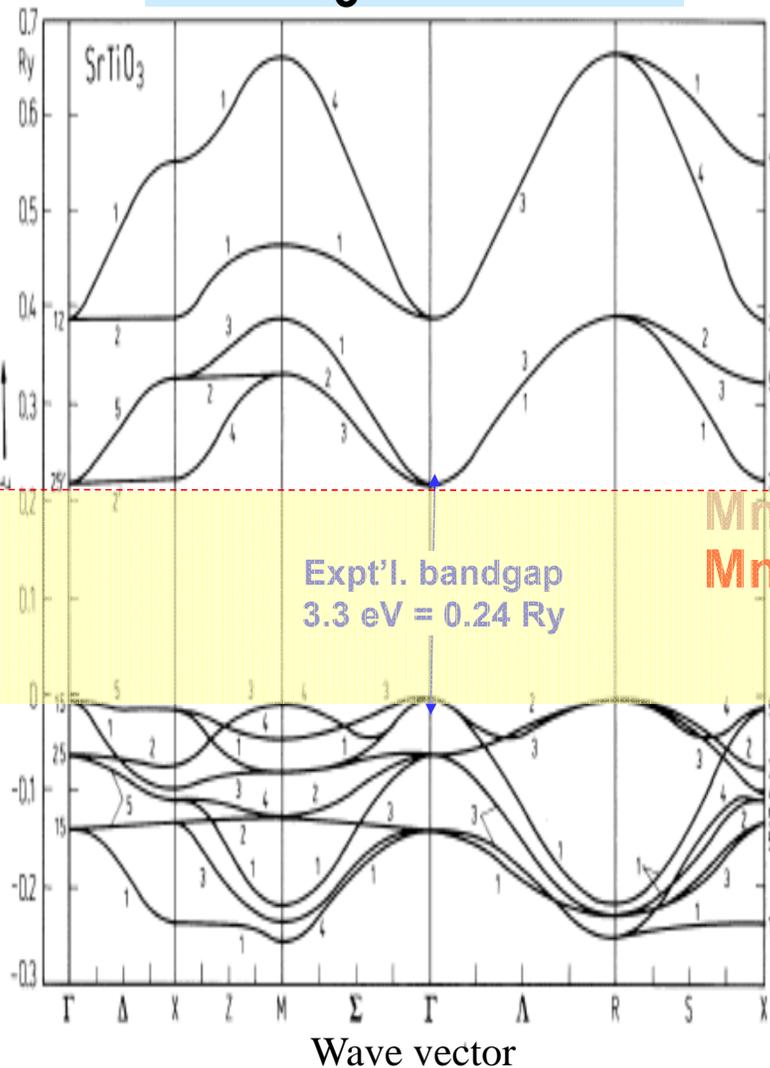
## Resonant photoemission:

$$I \propto \left| \langle \varphi_f(\mathbf{1}) | \hat{e} \cdot \vec{r} | \varphi_i(\mathbf{1}) \rangle + \sum_m \langle \varphi_f(\mathbf{1}) \varphi_1(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_i(\mathbf{1}) \varphi_m(\mathbf{2}) \rangle \langle \varphi_m(\mathbf{1}) | \hat{e} \cdot \vec{r} | \varphi_1(\mathbf{1}) \rangle \right|^2 \times \delta(h\nu - (E_m - E_1))$$



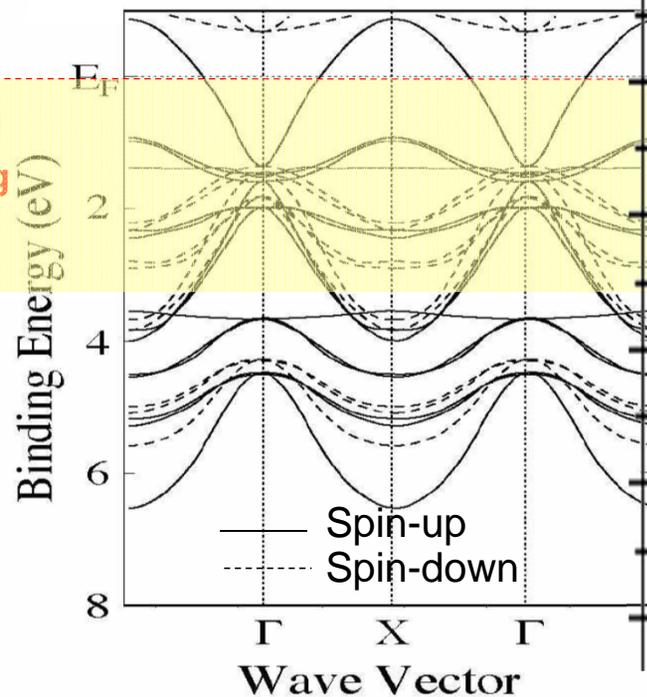
# SrTiO<sub>3</sub> and La<sub>0.67</sub>Sr<sub>0.33</sub>MnO<sub>3</sub> band structures and DOS

## SrTiO<sub>3</sub>-insulator



Mattheiss, PRB 6, 4718 (1972)

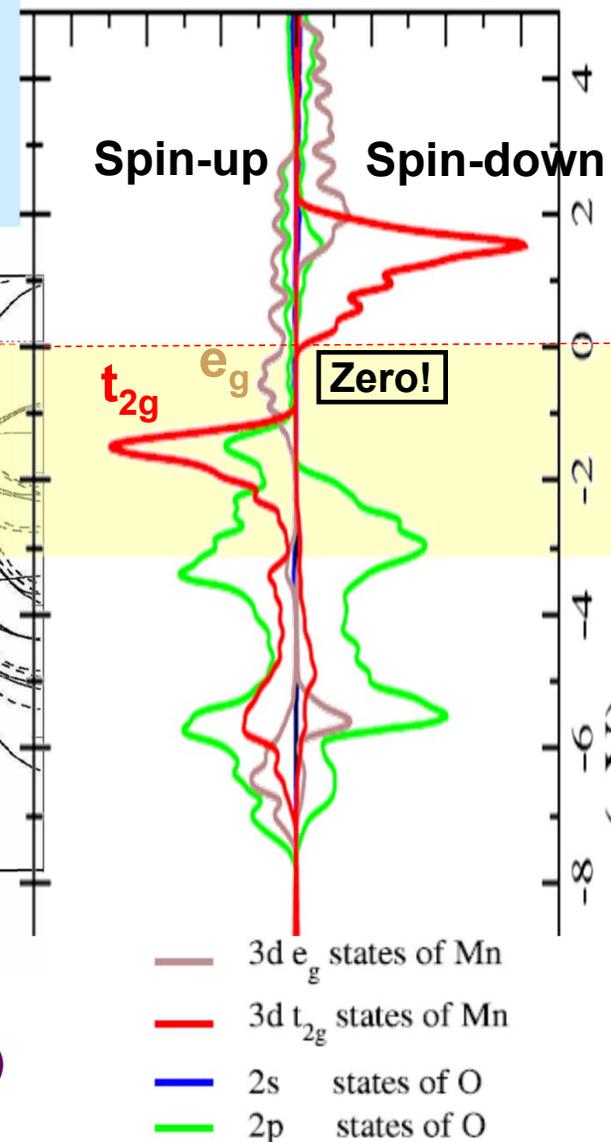
## La<sub>0.67</sub>Sr<sub>0.33</sub>MnO<sub>3</sub>- Half-Metallic Ferromagnetic metal



Chikamatsu et al.,  
PRB 73, 195105 (2006)

Zheng, Binggeli, J. Phys.  
Cond. Matt. 21, 115602 (2009)

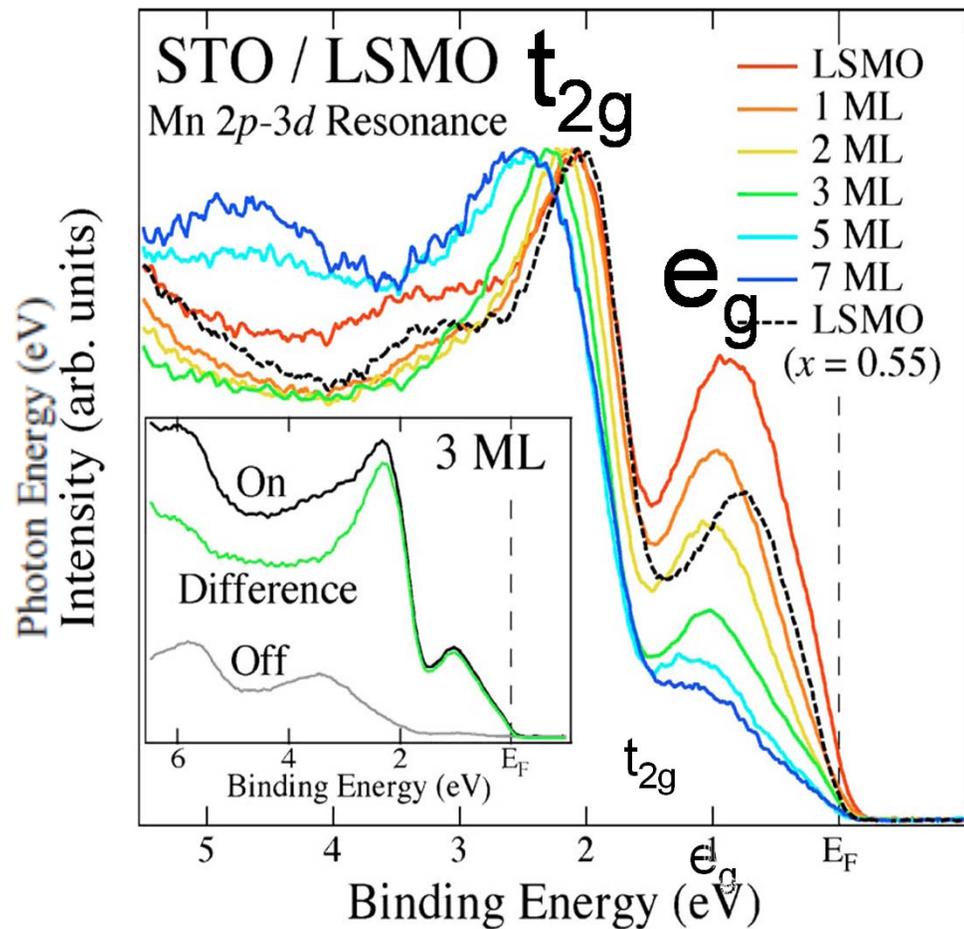
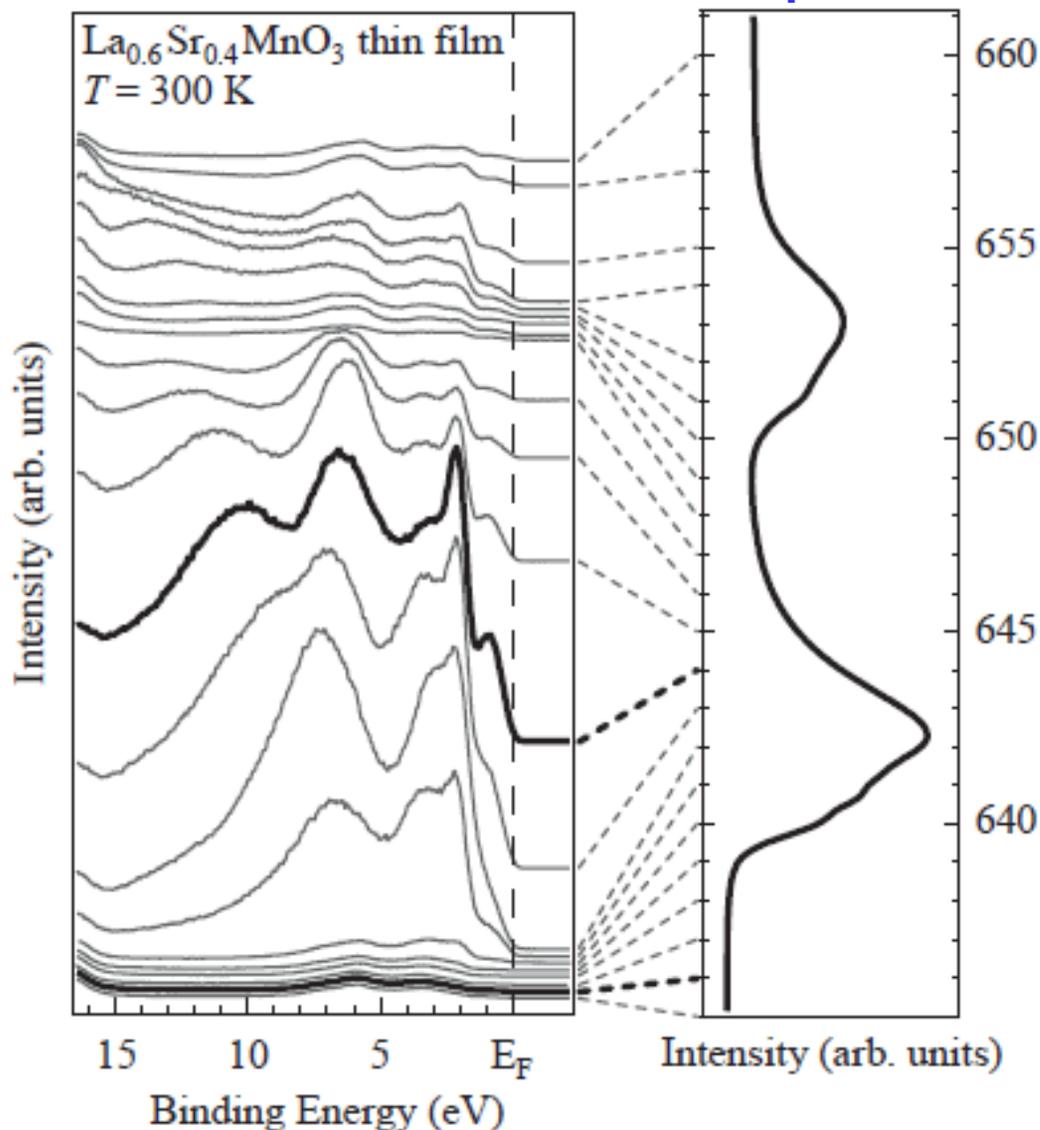
## Projected DOSs



# Resonant Photoemission— $\text{La}_{0.6}\text{Sr}_{0.4}\text{MnO}_3$ , Mn 3d with Mn 2p

Valence spectrum

Mn 2p absorption spectrum



Prior resonant PS: Fujimori et al., J.A.P 99, 08S903 (2006)

## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## **Valence-Level Photoemission**



Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit - Covered already

## **Some New Directions**

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

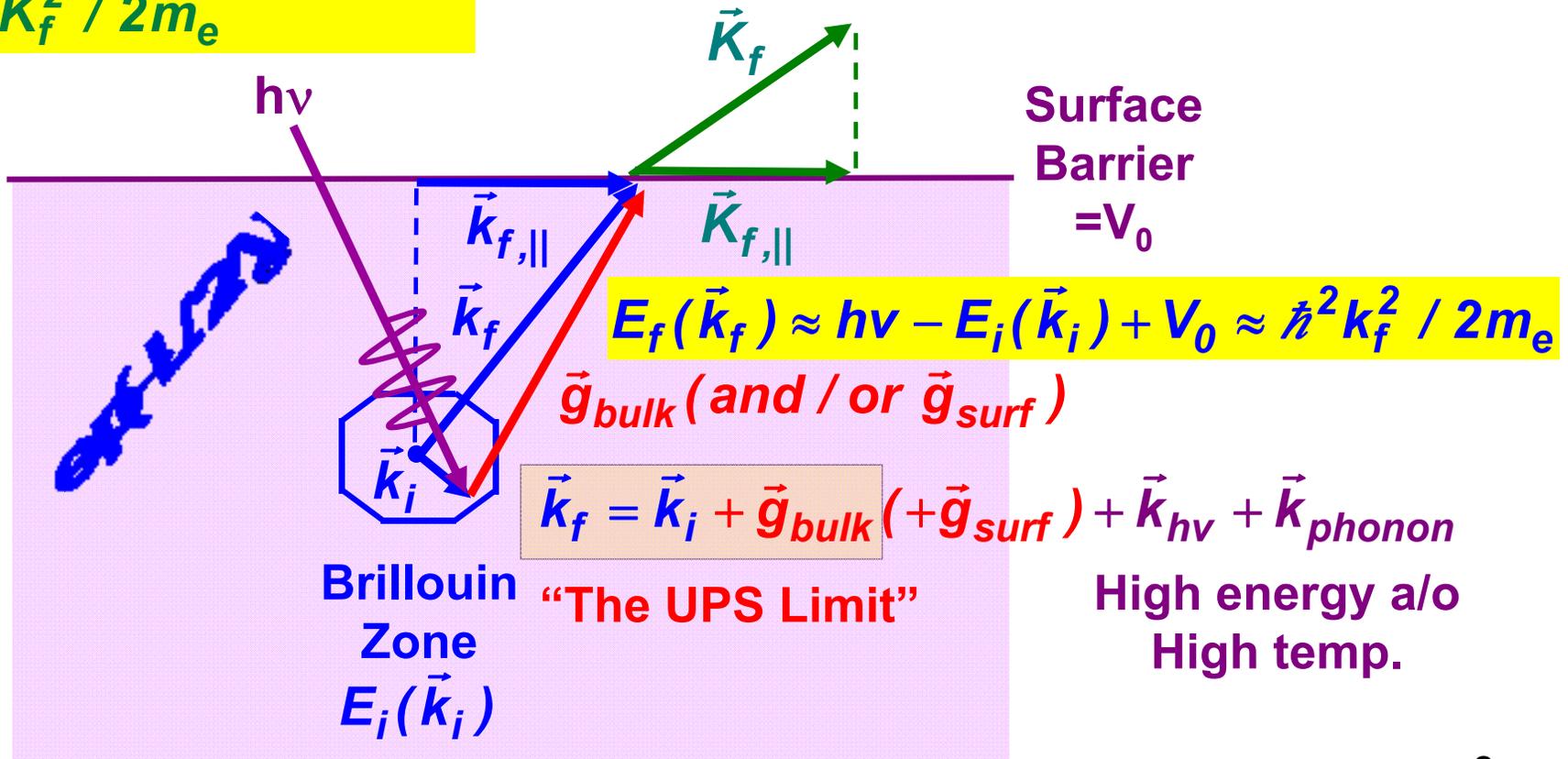
# Valence-band photoemission: Angle-Resolved Photoemission (ARPES)

$$E_f(\vec{K}_f) =$$

$$E_f(\vec{k}_f) - V_0 = h\nu - E_i(\vec{k}_i)$$

$$\approx \hbar^2 K_f^2 / 2m_e$$

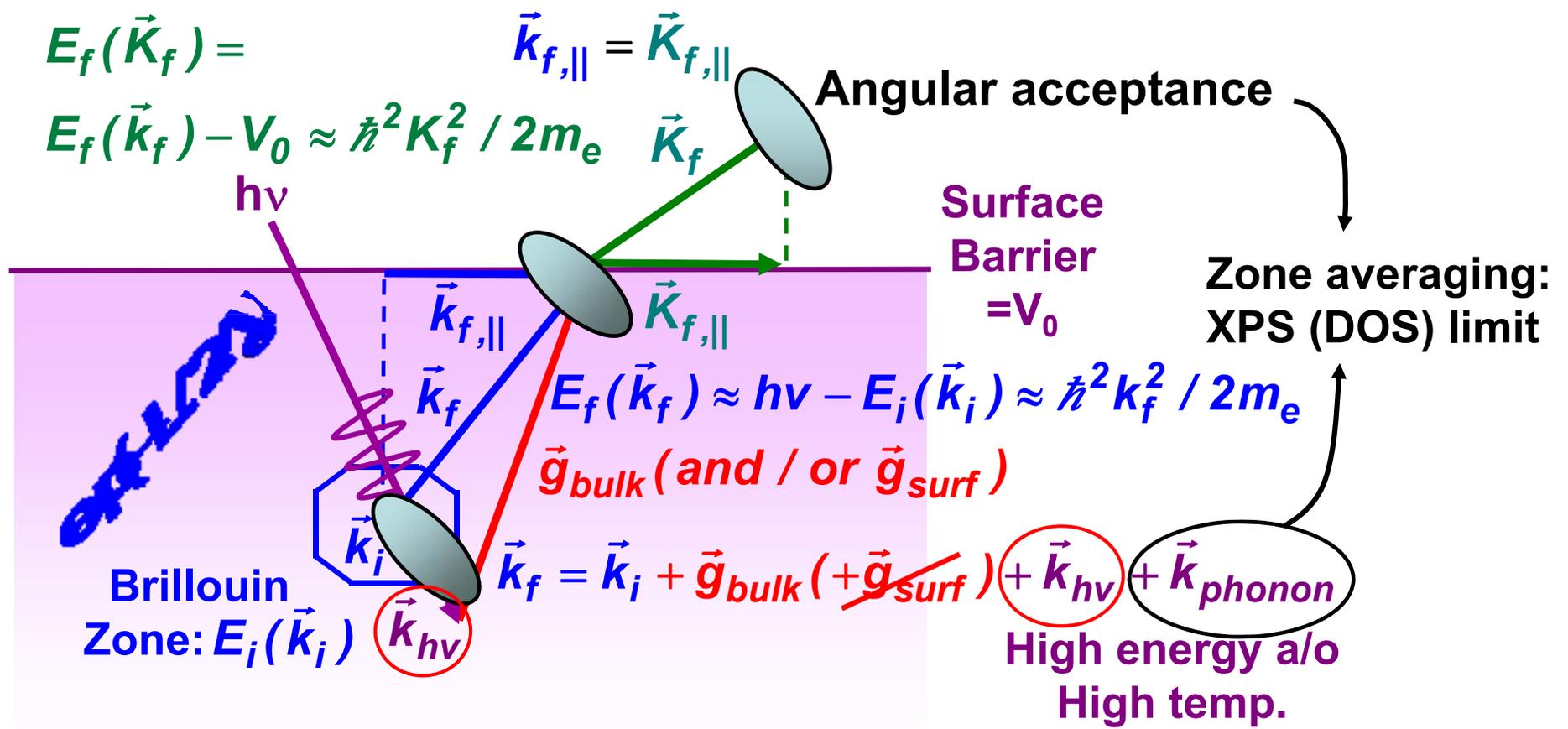
$$\vec{k}_{f,\parallel} = \vec{K}_{f,\parallel}$$



$$I(E_f, \vec{k}_f) \propto \left| \hat{\epsilon} \cdot \left\langle \varphi_{photoe}(E_f = h\nu + E_i, \vec{k}_f = \vec{k}_i + \vec{g}) \middle| \vec{r} \middle| \varphi(E_i, \vec{k}_i) \right\rangle \right|^2$$

"Direct" or k-conserving transitions

# ARPES—How high can we go in energy and temperature?



Fraction DTs  $\approx$  Debye-Waller factor =  $W(T) \approx \exp[-(k^f)^2 \langle u^2(T) \rangle]$   
 $\approx \exp[-C_1 (k^f)^2 T / (m \Theta_D^2)] \approx \exp(-C_2 E_{kin} T)$

$W \approx 1$

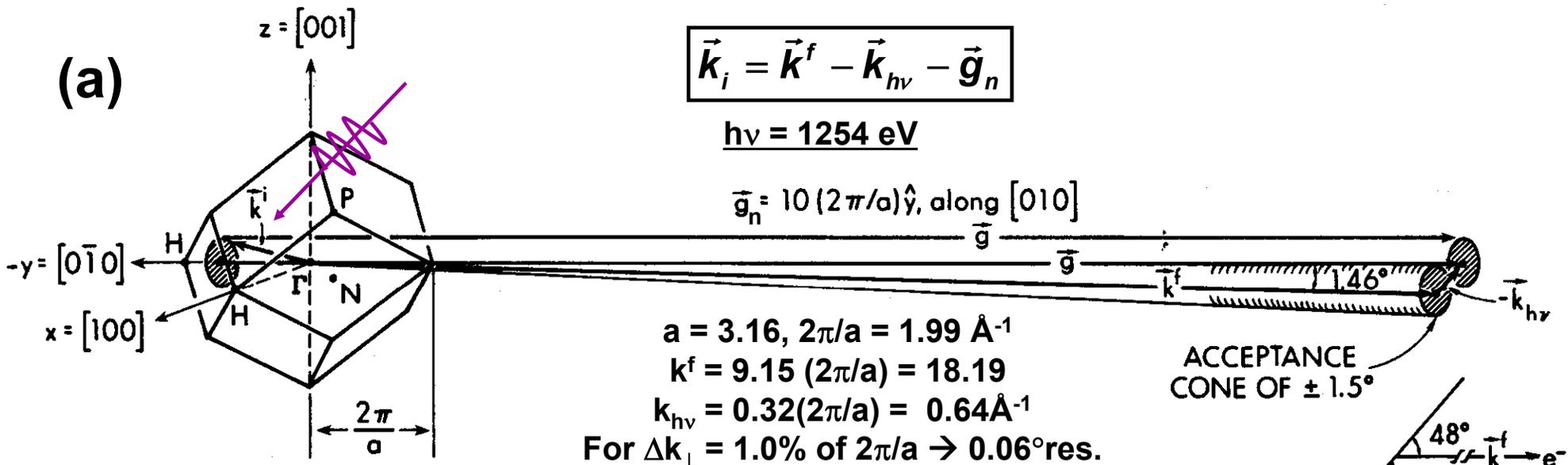
$W \approx 0$

**ARPES  $\rightarrow$  bands, quasiparticles**  
 (Low  $h\nu$ , Low  $T$ , High angul. Res.)

**XPS  $\rightarrow$  DOS+XPD**  
 (High  $h\nu$ , High  $T$ , Low angul. Res.)

Shevchik, Phys. Rev. B 16, 3428 (1977)  
 Hussain....CF, Phys. Rev. B 34 (1986) 5226

# Angle-Resolved Photoemission at High Energy--



Hussain et al....CF,  
 Phys. Rev. B 22 3750  
 (1980) Phys. Rev. B 34,  
 5226 (1986)

Shevchik, Phys. Rev.  
 B 16, 3428 (1977)

Alvarez et al., PRB 54,  
 14703 (1996)

Takata et al.,  
 Phys. Rev. B 75,  
 233404 (2007)

Additional effects at higher energies:

- Non-dipole--the photon momentum  $k_{h\nu} \rightarrow$  easy to allow for
- Angular acceptance  $\rightarrow$  B.Z. averaging  $\rightarrow$  need better angular res.
- Lattice recoil  $\rightarrow$  phonon creation  $\rightarrow$  more B.Z. averaging,

Fraction DTs  $\approx$  Debye-Waller factor =  $W(T) \approx \exp[-(k^f)^2 \langle u^2(T) \rangle]$

$\approx \exp[-C_1 (k^f)^2 T / (m\Theta_D^2)] \approx \exp(-C_2 E_{kin} T) \rightarrow$  need cryocooling

$\rightarrow$  the "XPS limit" of full B.Z. averaging and D.O.S. sensitivity

$\rightarrow$  core-like photoelectron diffraction

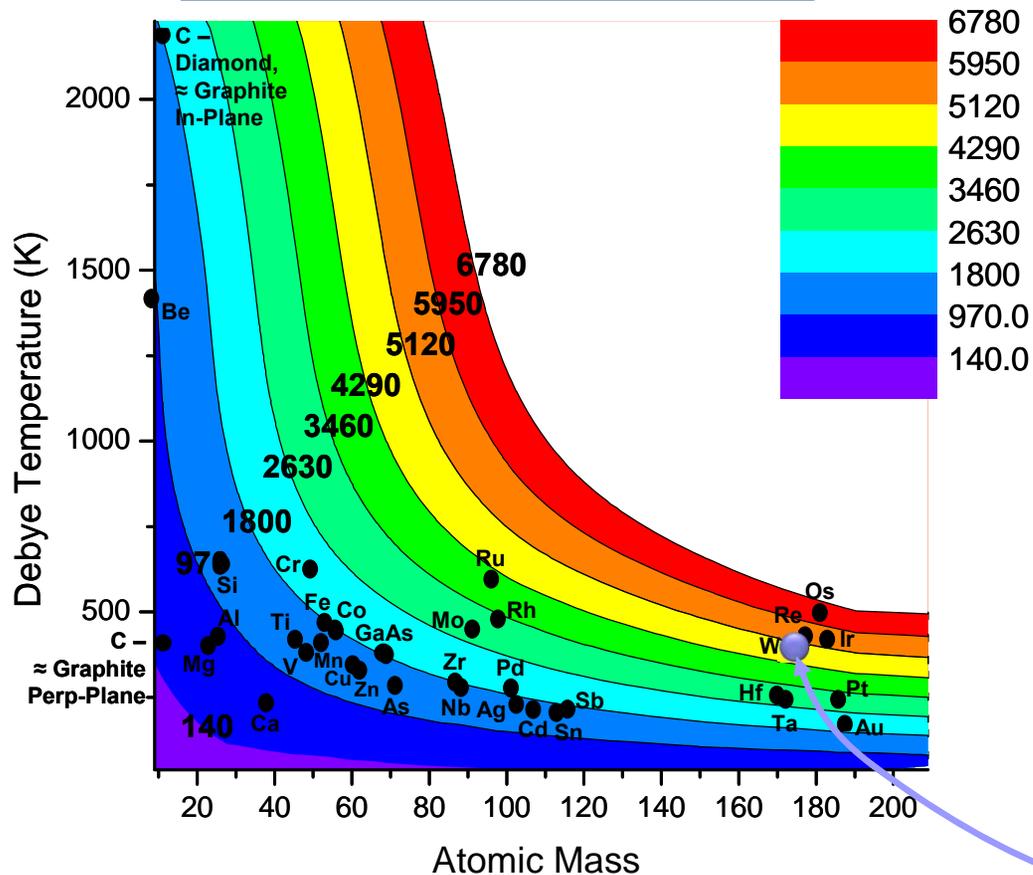
- Recoil  $\rightarrow$  peak shifts and broadening:

$$E_{recoil} (\text{eV}) \approx \left[ \frac{m_e}{M} \right] E_{kin} \approx 5.5 \times 10^{-4} \left[ \frac{E_{kin} (\text{eV})}{M(\text{amu})} \right]$$

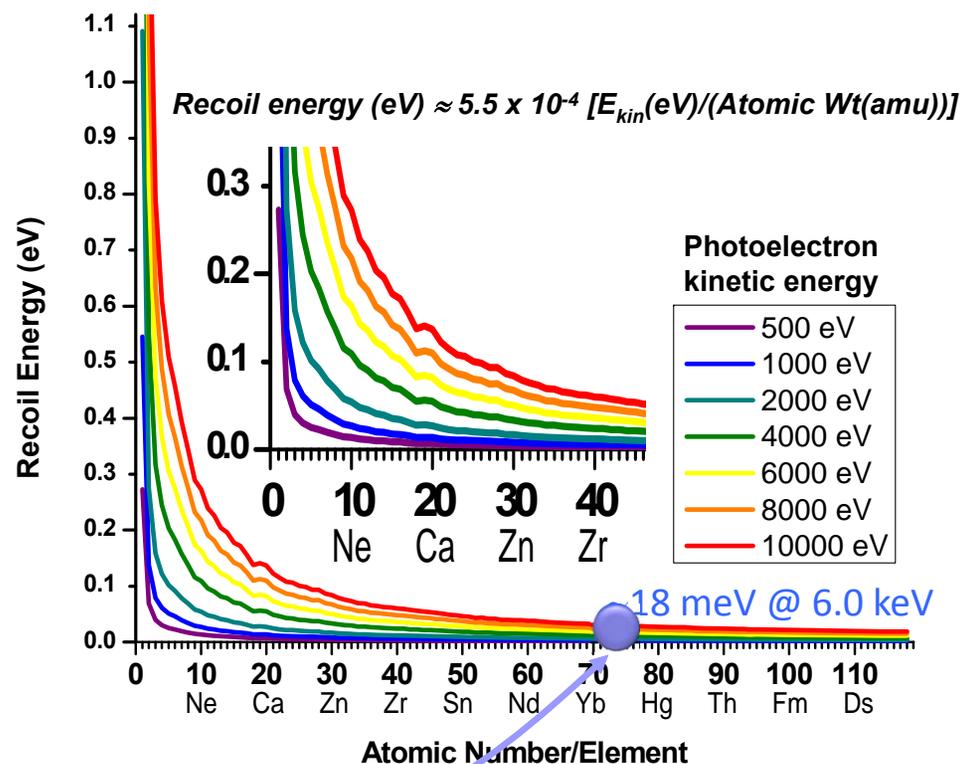
# ARPES → HARPES - How high can we go?

## Photoemission Debye-Waller Factors and Recoil Energies

Photon energy for ~50% DTs  
= 0.5 D-W @ 20K

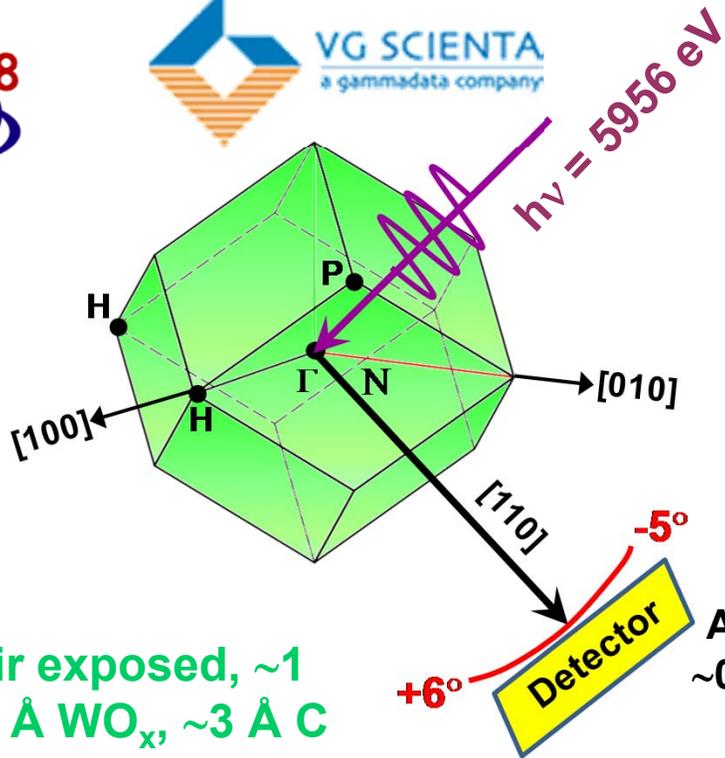


Recoil energy for all atoms and different photon energies



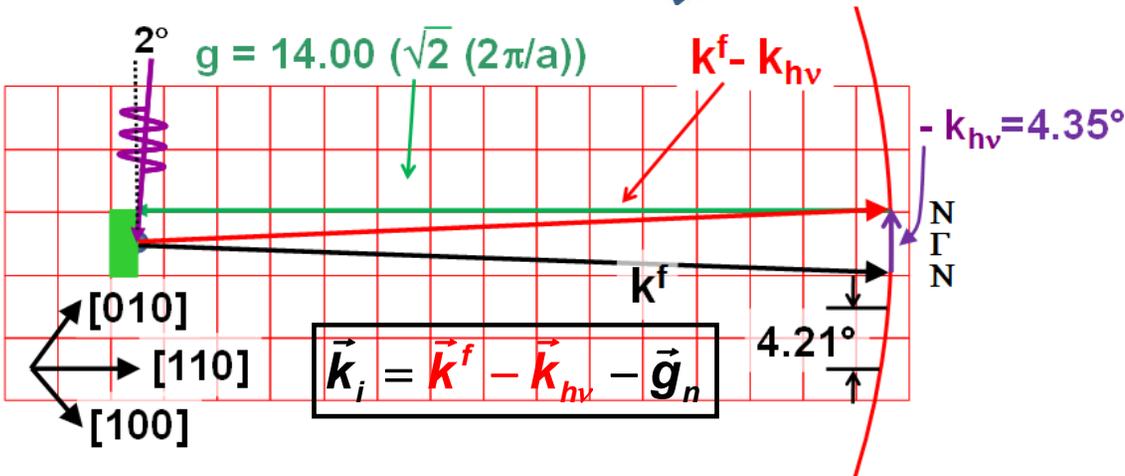
C. Papp, L. Plucinski, et al.,  
Phys. Rev. B 84, 045433 (2011)

# Hard x-ray ARPES for W(110): 6.0 keV

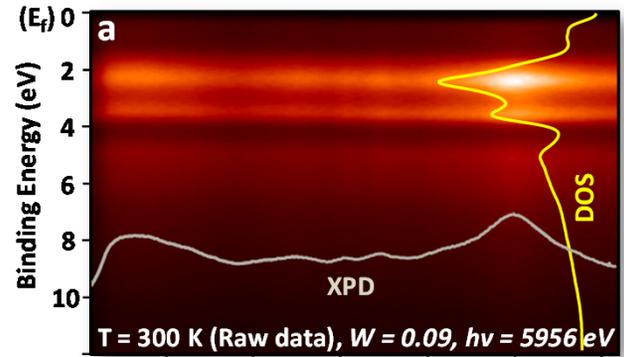


W(110)-air exposed, ~1 year, ~12 Å WO<sub>x</sub>, ~3 Å C

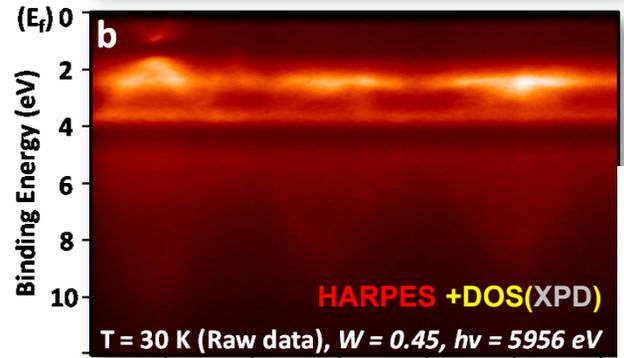
Ang. Res.:  
~0.2° → 0.02°  
in future



Gray, Minar et al., Nature Mat. 10, 759 (2011);  
Plus News and Views, Feng, Nature Mat. 10, 729-730 (2011)

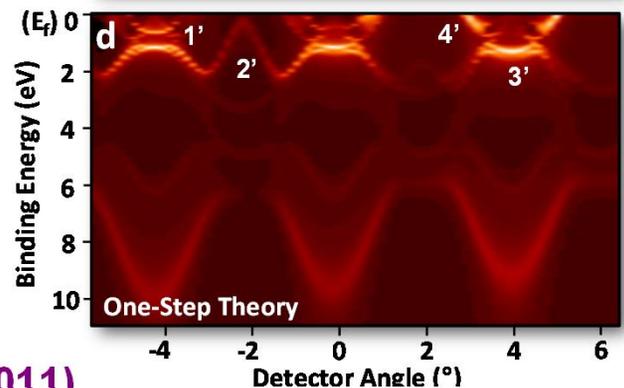
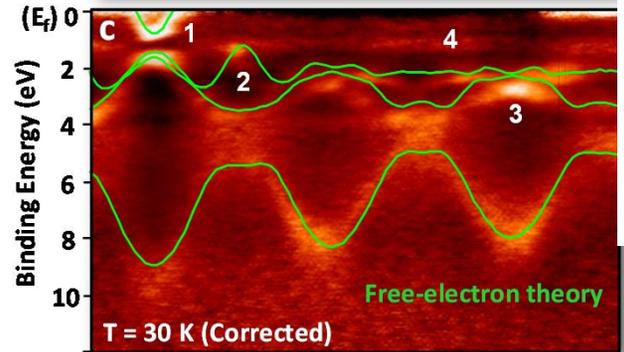


Room temp.



30 K

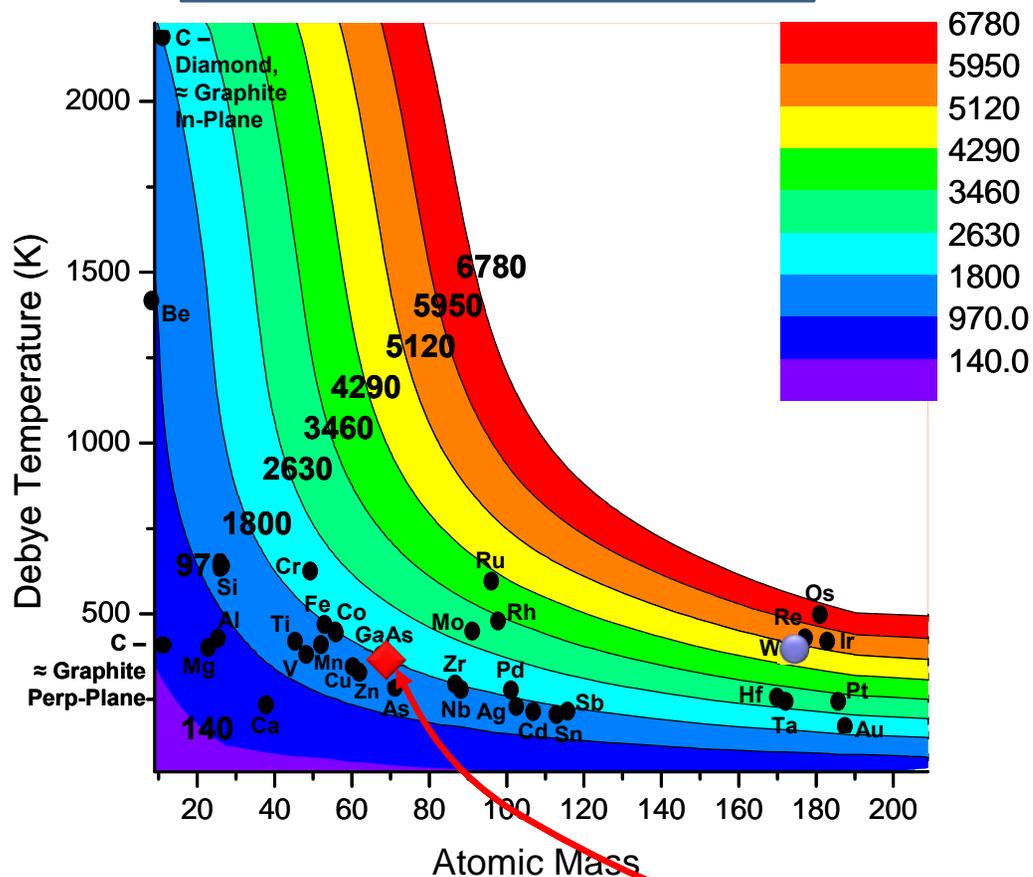
Bostwick-Rotenberg Correction:  
Divide by average over angle (~DOS) and energy (~XPD+Det. Signature)



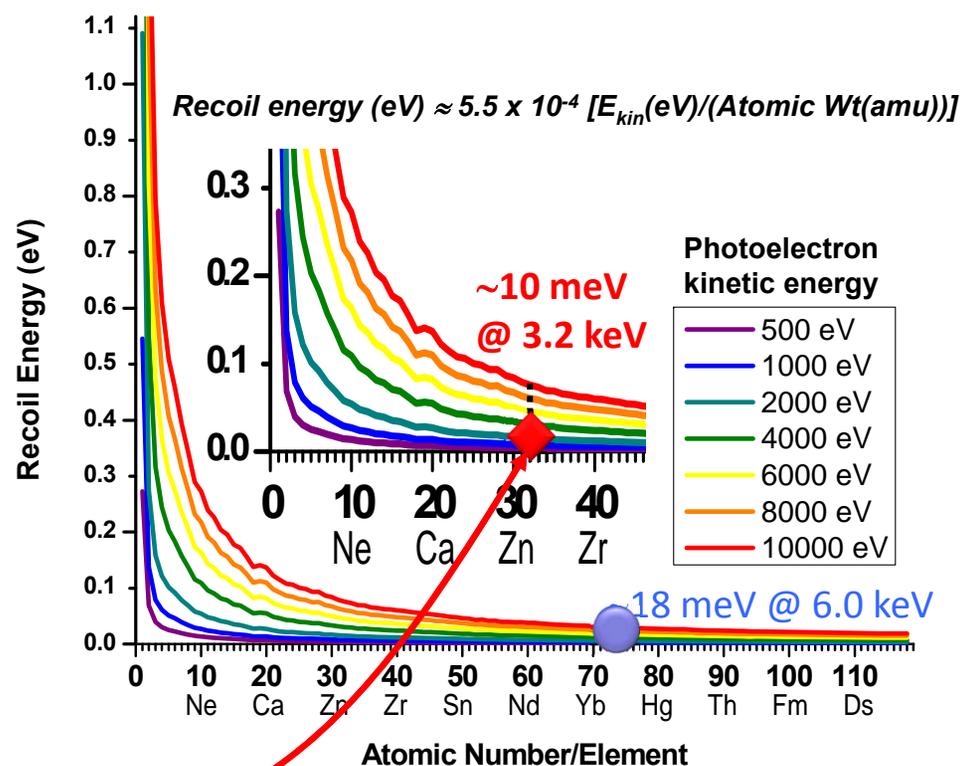
# ARPES → HARPES - How high can we go?

## Photoemission Debye-Waller Factors and Recoil Energies

Photon energy for ~50% DTs  
= 0.5 D-W @ 20K

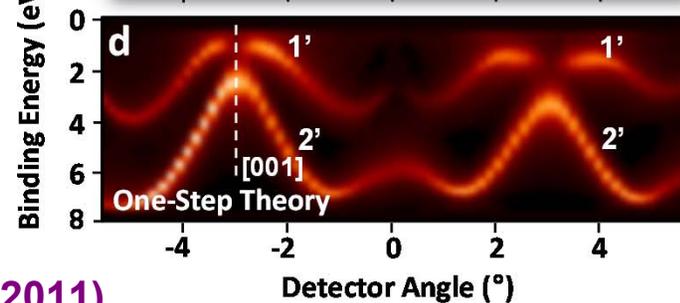
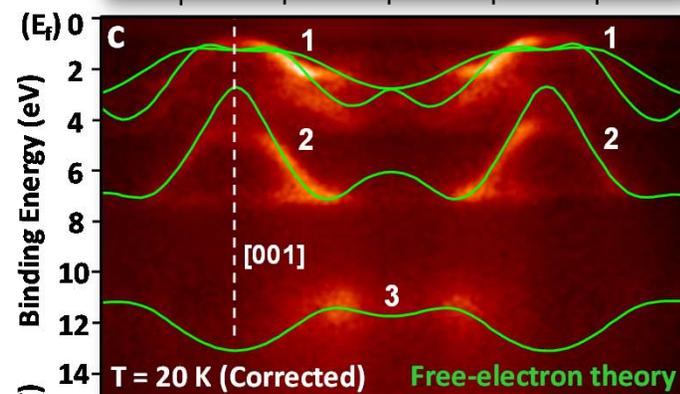
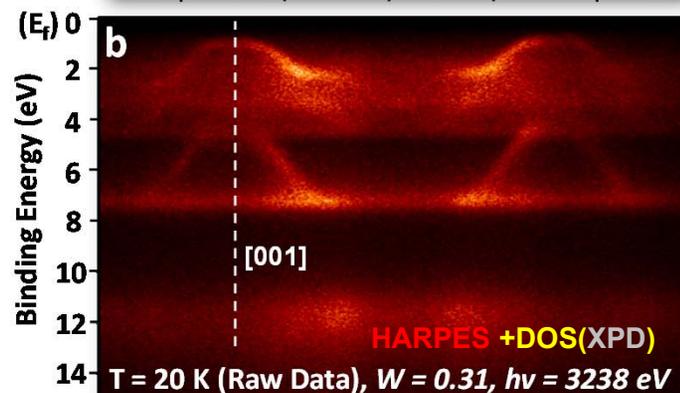
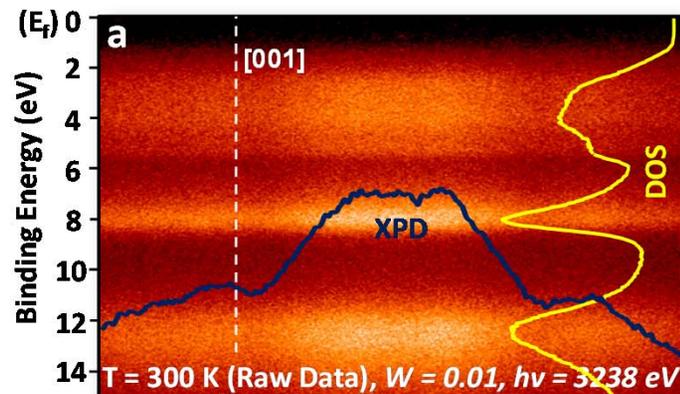
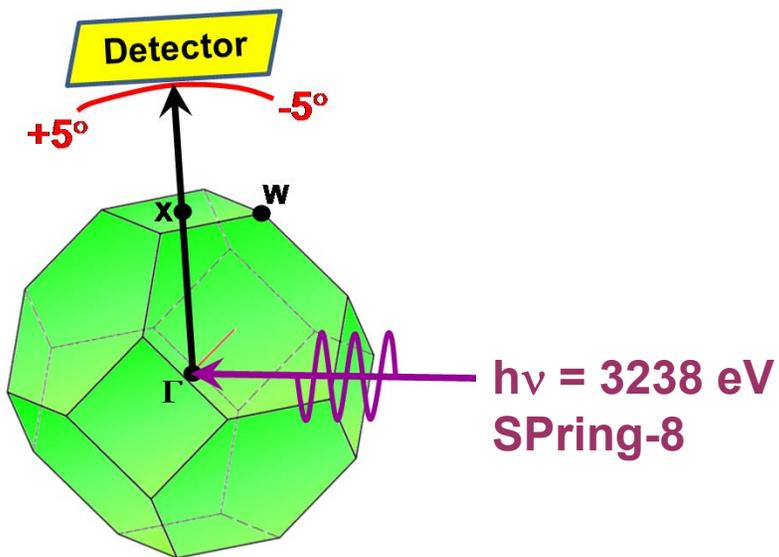


Recoil energy for all atoms and different photon energies

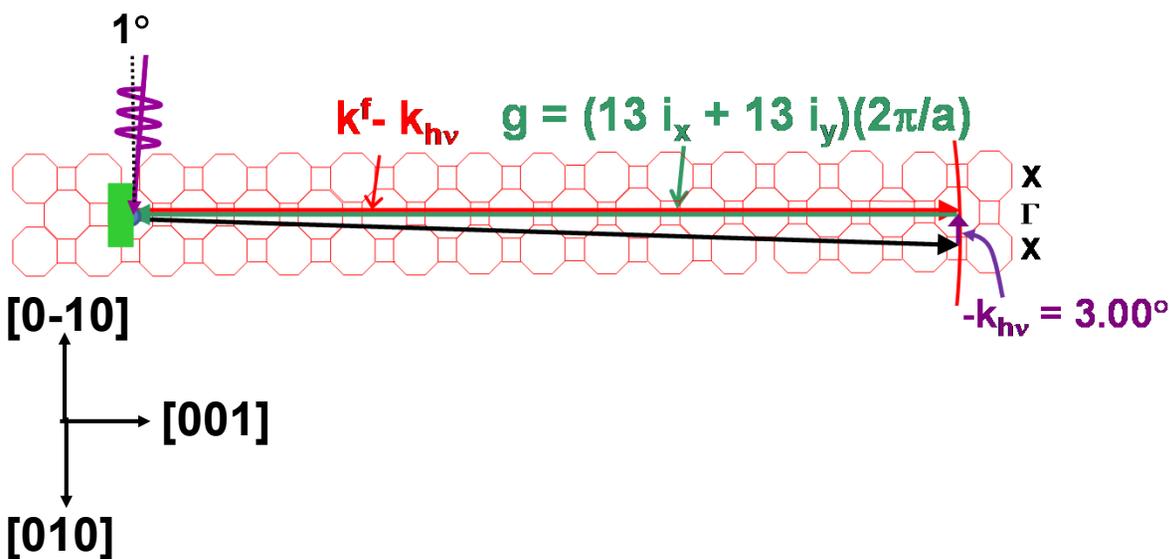


C. Papp, L. Plucinski, et al.,  
Phys. Rev. B 84, 045433 (2011)

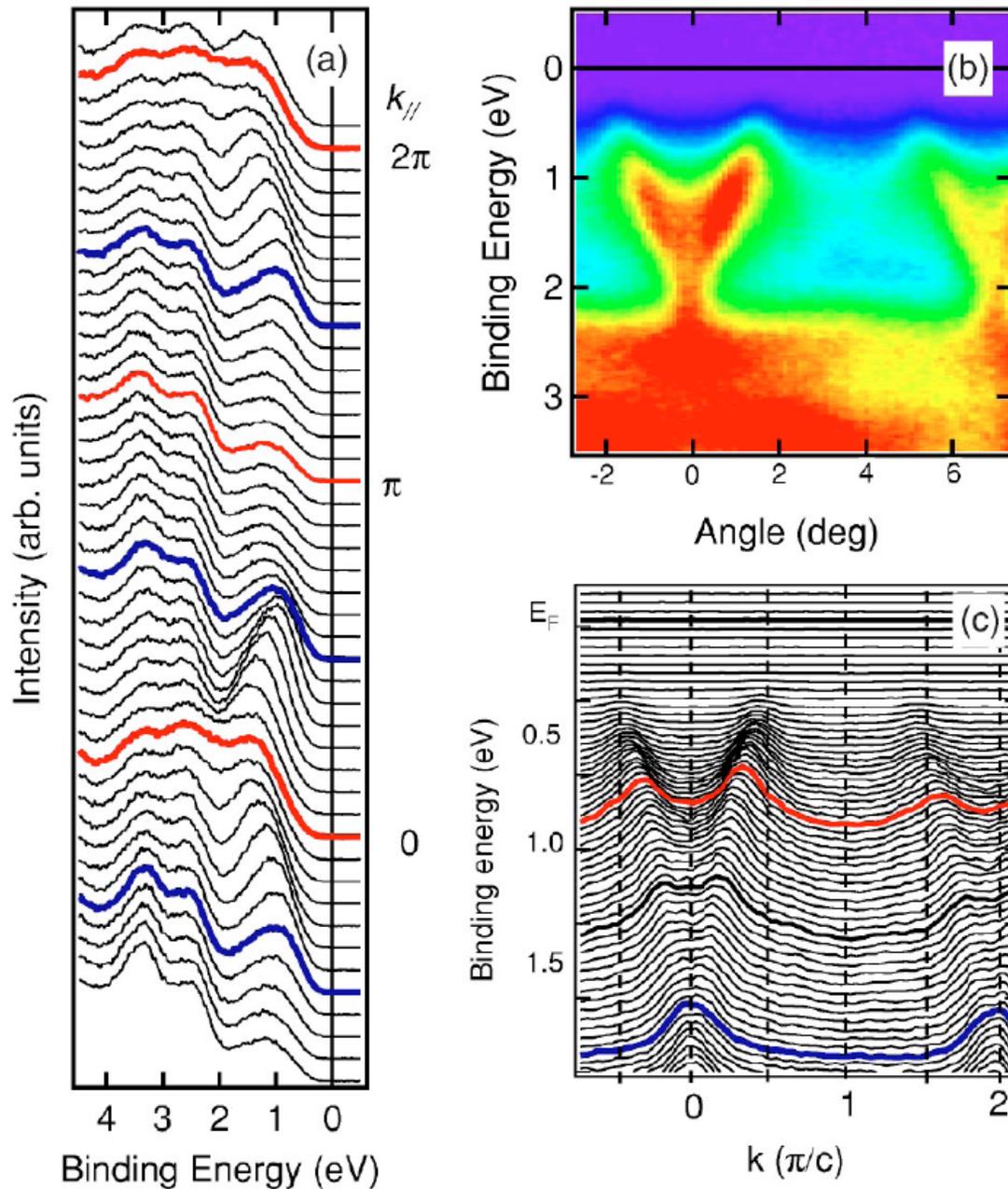
# Hard x-ray ARPES for GaAs(001): 3.2 keV



Bostwick-Rotenberg Correction:  
Divide by average over angle ( $\sim$ DOS) and energy ( $\sim$ XPD)

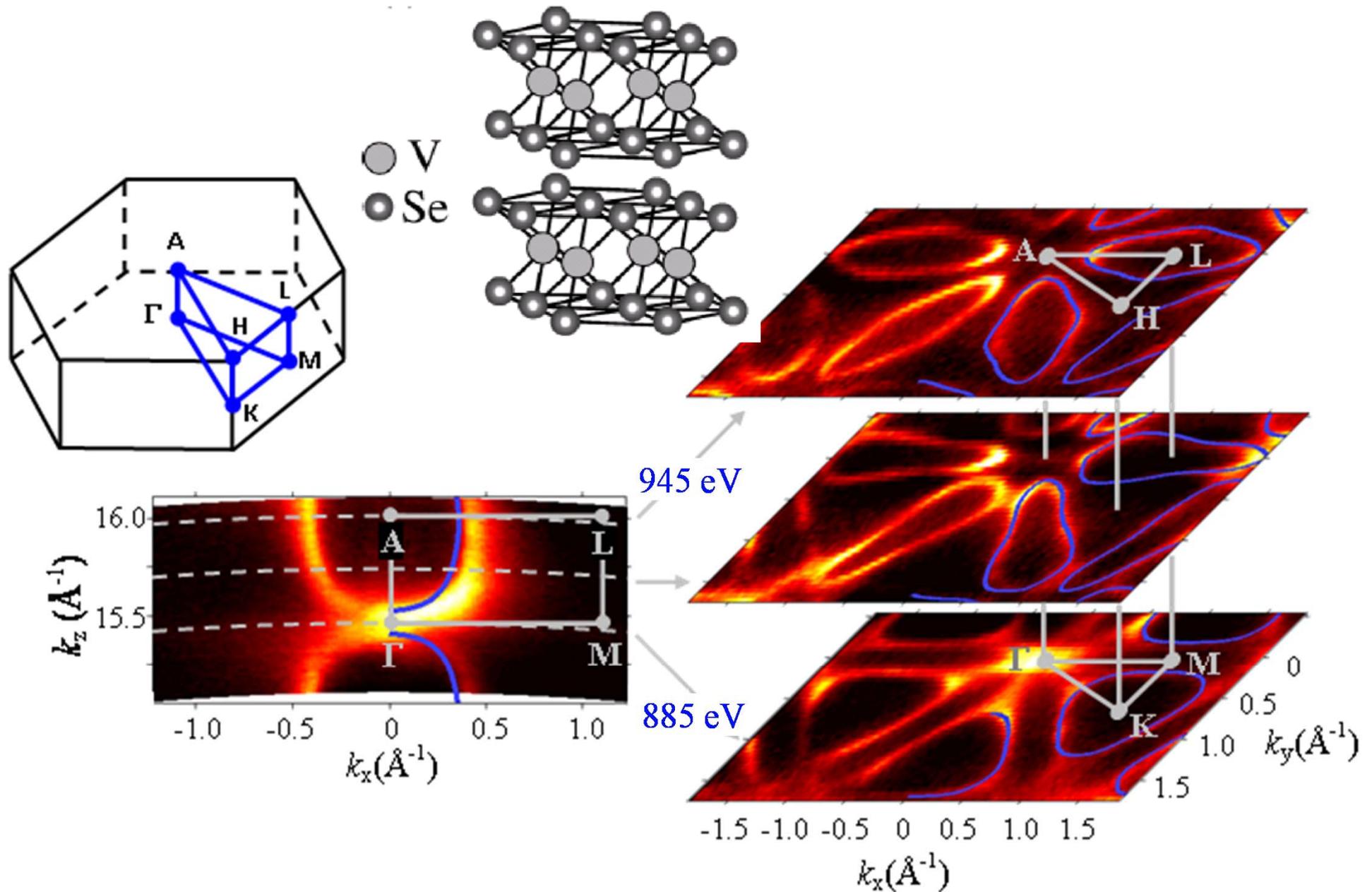


**A first real application of soft x-ray ARPES: Soft x-ray ARPES from SrCuO<sub>2</sub> at  $h\nu = 700$  eV and 300K, photoemission Debye-Waller factor of **only 0.03-0.04****



Photoemission DW factors can be too conservative for some systems (lack of correlated vibrations?)  
→ suggests a wider application of SARPES/HARPES

# 3D band mapping of a "2D" material $VSe_2$



Strocov et al., PRL 109, 086401 (2012)

$$\vec{k}_i = \vec{k}_f - \vec{k}_{hv} - \vec{g}_n$$

## Soft→Hard Angle-Resolved Photoemission: Basic Considerations

- + Deeper probing: “bulk” electronic structure, buried layers and interfaces, less surface sensitive
- + Free-electron final state: good approximation
- + Less  $k_{\perp}$  broadening:  $\Delta k_{\perp} \approx 1/\Lambda_e$  (inelastic)
- + 3D band mapping: possible with photon energy variation
- + Resonant excitation: enhance a given atom’s contribution, move standing wave in sample
- + Standing-wave excitation: possible, multilayers, epi-, single crystal- systems
- + Core-level spectra: provide complementary information on charge states, structure via XPD
- - Phonon smearing: need cryocooling, DW factor as criterion
- - Angular resolution: need higher for  $\Delta k_{\parallel}$  resolution
- - Non-dipole effects: allowance for photon momentum, but easy
- - Recoil effects: shift and smear energies

$$DW(T) \approx \exp[-g_n^2 \langle u^2(T) \rangle]$$

$$\vec{k}_i = \vec{k}_f - \vec{k}_{hv} - \vec{g}_n$$

$$E_{recoil} \approx \frac{\hbar^2 k_f^2}{2M} \approx 5.5 \times 10^{-4} \left[ \frac{E_{kin} \text{ (eV)}}{M \text{ (amu)}} \right]$$

CSF, Synch.Rad. News. 25, 26 (2012); V. Strocov et al., Appl. Phys. Lett. 101, 242103 (2012)

## Four levels of interpreting ARPES spectra

[1] Simply looking at the final state as a free electron in an extended-zone scheme, translating it into the first  $\text{BZ}$  via  $\vec{k}_{hv} - \vec{g}_n$ , and asking qualitatively where it cuts the ground-state band structure

[2] More rigorously requiring energy and  $k$ -conservation and computing the locus of points in energy and  $k$  that satisfy it, again ground-state band structure (e.g. Plucinski, et al., Phys. Rev. B 84, 045433 (2011))

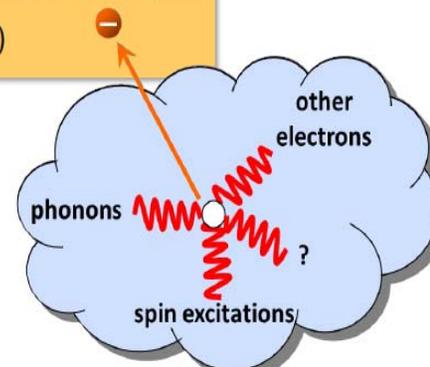
[3] Calculating the spectral function to allow for many-body excitations in the sudden approximation, but with no matrix elements:

$$I(\vec{k}, \varepsilon) \propto \sum_s |\langle N-1, \mathbf{k} | c_{\vec{k}} | N, 0 \rangle|^2 \delta(E_{N-1,s} + \varepsilon - E_{N,0} - \hbar\omega)$$

$$= A(\vec{k}, \varepsilon - \hbar\omega) \cdot f(\varepsilon - \hbar\omega)$$

  
spectral function

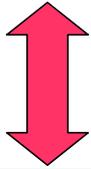
The ARPES signal  $I(\vec{k}, \varepsilon)$  directly proportional to the removal part of the spectral function  $A(\vec{k}, \omega) = -\frac{1}{\pi} \text{Im} G(\vec{k}, \omega)$



[4] Carrying out full one-step photoemission calculations that include the surface and all matrix elements, so as to be able to accurately represent intensities. For SARPES and HARPES (Minar, Braun, Ebert, J. Elect. Spect. 184, 91 (2011))

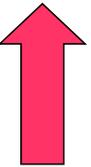


Angle resolved UV and X-ray photoemission for arbitrary **ordered** and **disordered correlated systems**



One-step model of photoemission

Standing-wave  $|E^2(\text{depth})|$



LSDA

Relativistic Dirac formalism

Full potential 2D Semi-infinite

DMFT

CPA-Alloys, dopants, **phonons** (Debye model)

Model Surface barrier

Reviews:

KKR: Ebert, Ködderitzsch, Minar, Rep. Prog. Phys. 74, 096501 (2011)

KKR+DMFT: Minar, JPCM Topical Review 23, 253201 (2011)

KKR+One step model: Minar, Braun, Ebert et al., JESRP 184, 91(2011)

Jan Minar  
Juergen Braun  
Hubert Ebert

# Phonon effects in photoemission



- Phonon excitations define fundamental limit to band mapping as energy or temperature is raised because of full BZ averaging Shevchik (1977)

- Photo current can be roughly divided into two contributions:

$$\langle I^{Tot}(E_F, k, T) \rangle \approx W(T) I^{DT}(E_F, k, T) + [1 - W(T)] I^{NDT}(E_F, k, T)$$

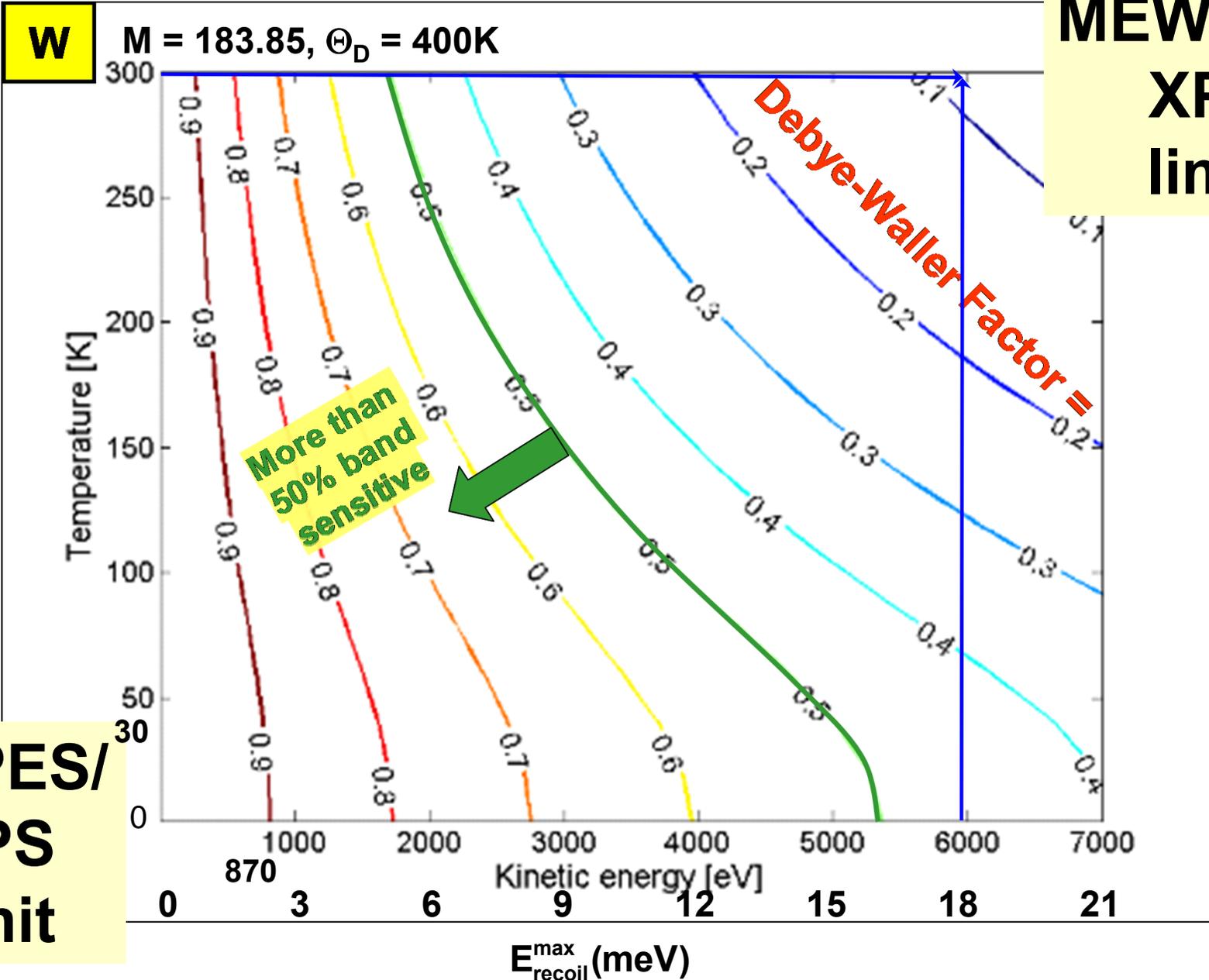
- Photoemission Debye-Waller Factor  $W(T) = \exp(-\Delta k^2 \langle u^2 \rangle) = \exp(-g_{hk\ell}^2 \langle u^2 \rangle)$

- Actual situation:  $\langle I^{Tot}(E_F, k, T) \rangle \approx \underbrace{W(T) \langle I^{Multiple\ scatt}(E_F, k, T) \rangle}_{\text{ARPES}} + \underbrace{\langle I^{Atomic}(E_F, k, T) \rangle + \langle I^{Incoherent}(E_F, k, T) \rangle}_{\text{MEWDOS, XPD}}$

via  $t(T)$  (Larson and Pendry, Feder)

- Improved treatment of phonon effects on LEED state – cluster implementation: Zampieri *et al.* (1996)
- Proper formulation for solids within multiple scattering formalism for high energy regime: Fujikawa and Arai (2009)

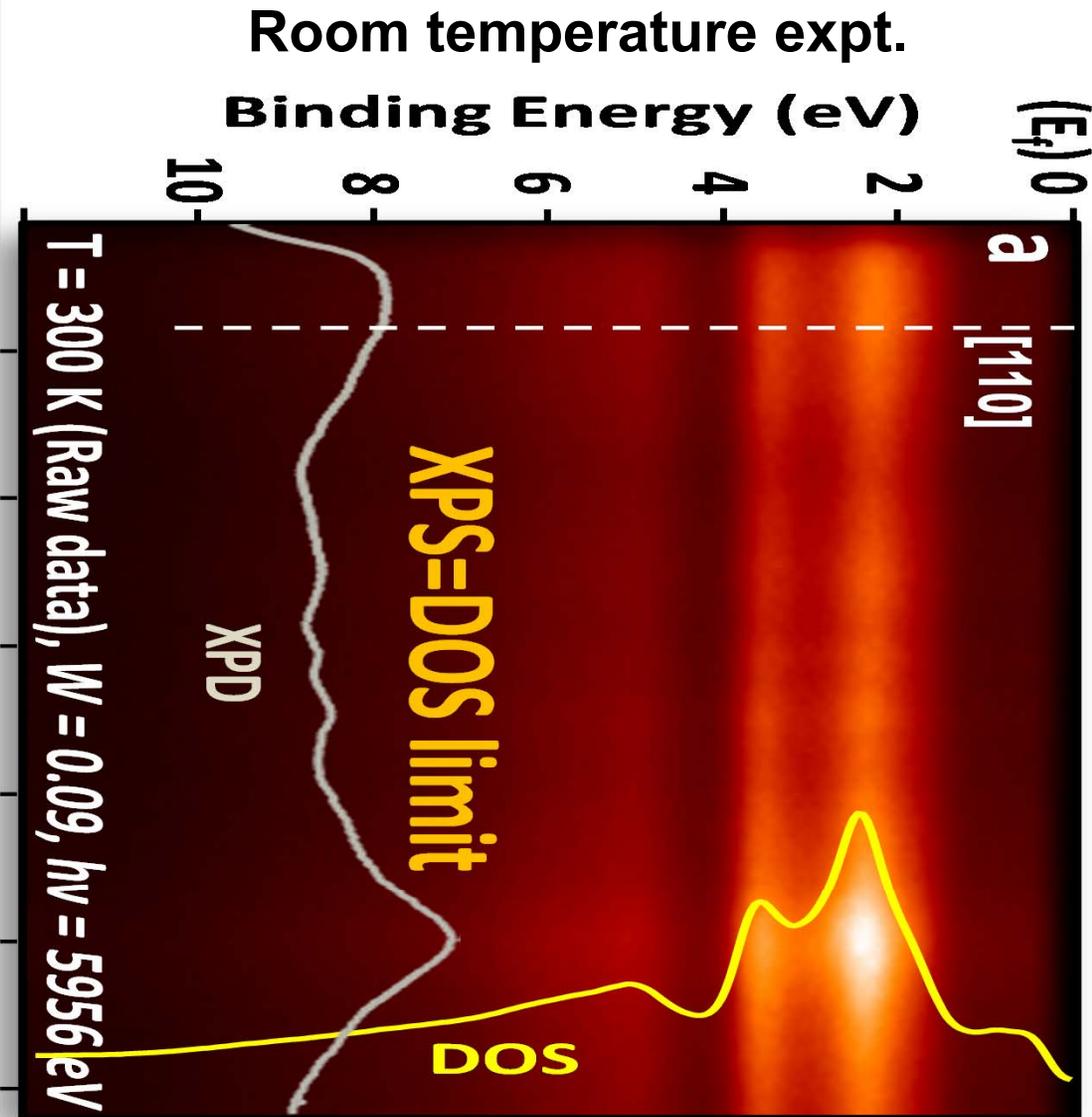
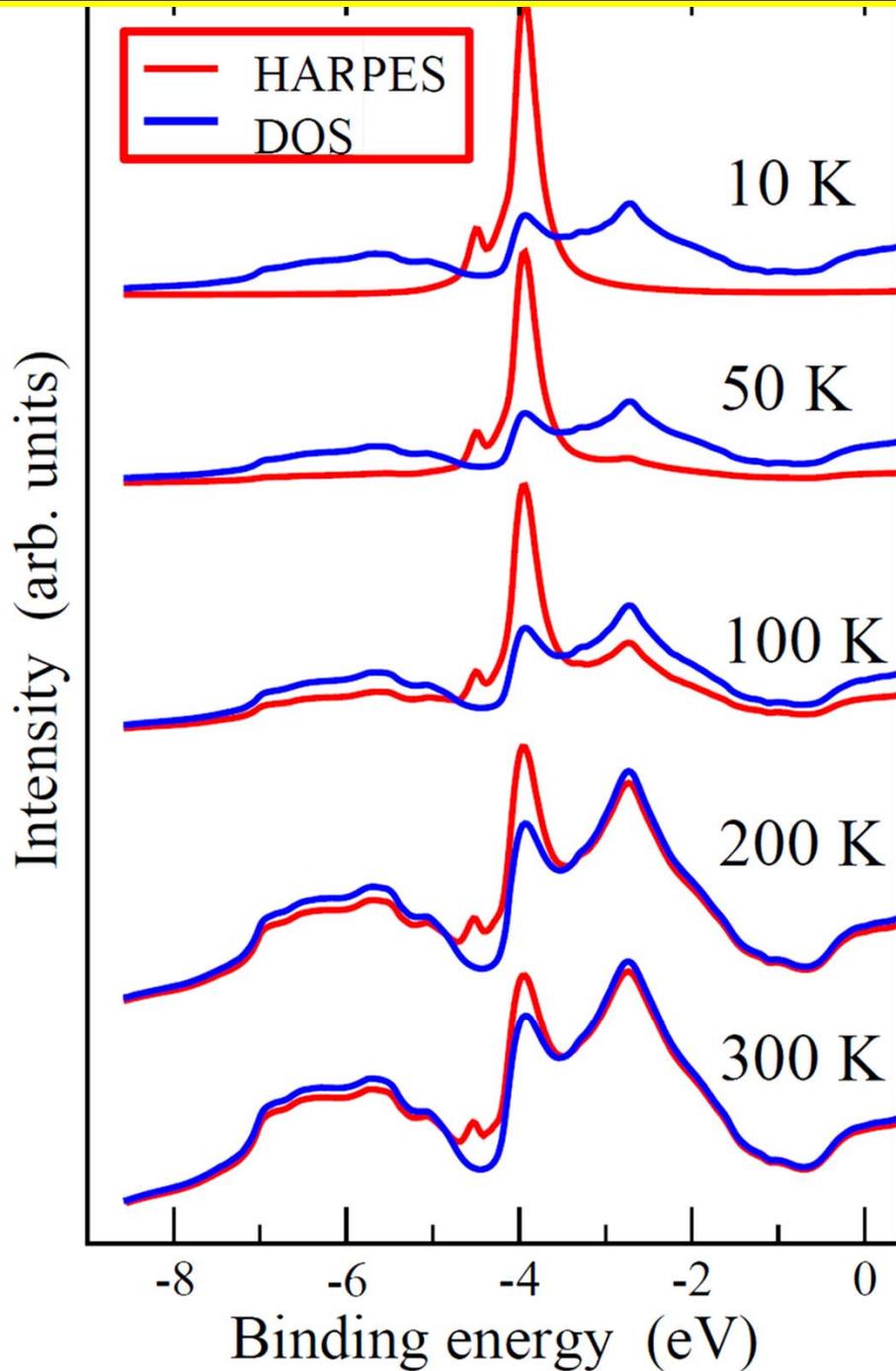
# Tungsten--Debye-Waller Factors and Recoil Energies



**MEWDOS/  
XPS  
limit**

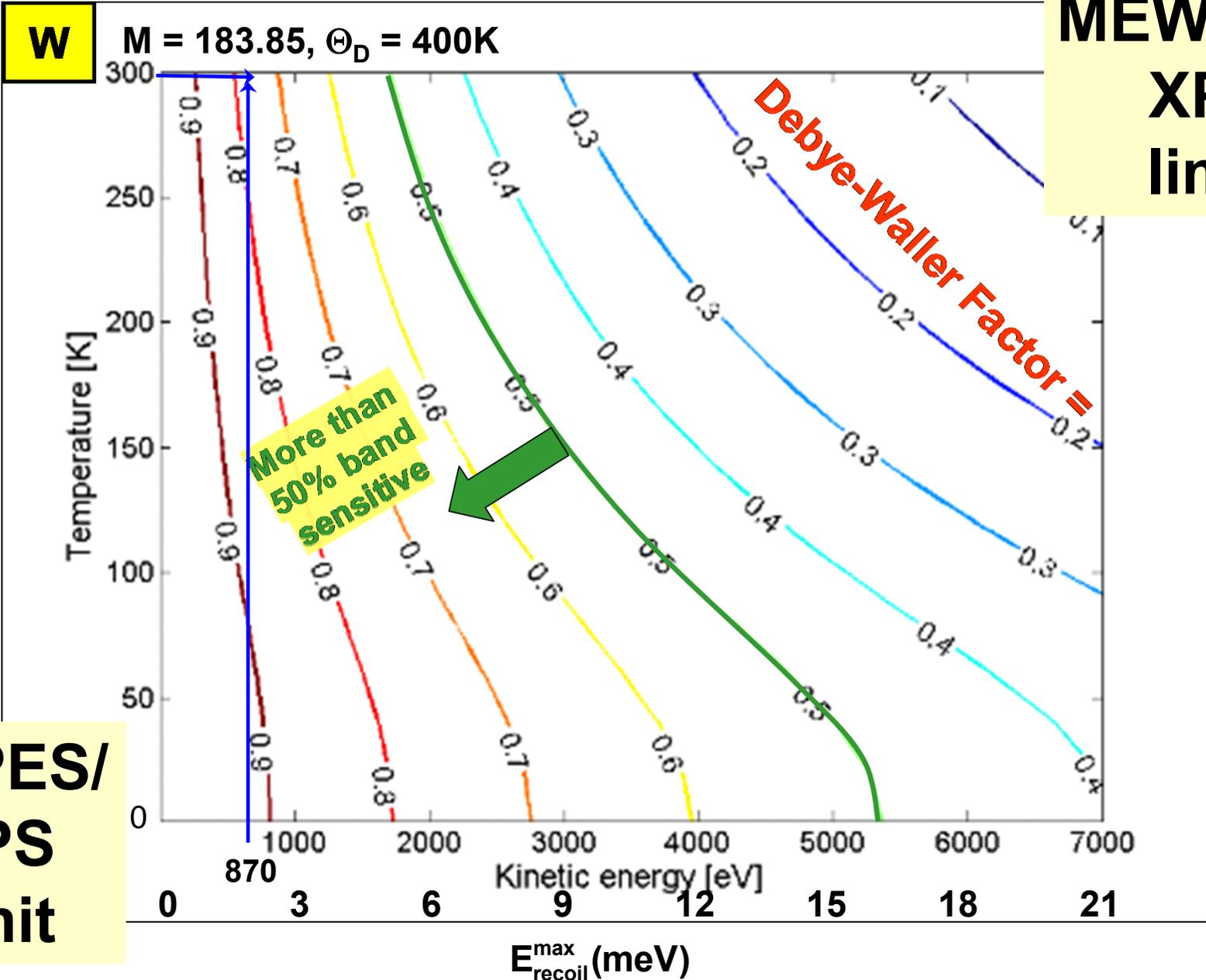
**ARPES/  
UPS  
limit**

Hard x-ray ARPES for W(110), 6 keV:  
One-step theory with phonons (Braun, Minar, Ebert) vs expt. (Gray et al.)



Braun et al., Phys. Rev. B 88, 205409 (2013)

# Tungsten--Debye-Waller Factors and Recoil Energies



**MEWDOS/  
XPS  
limit**

**ARPES/  
UPS  
limit**

# Phonon effects: Improved theoretical modeling

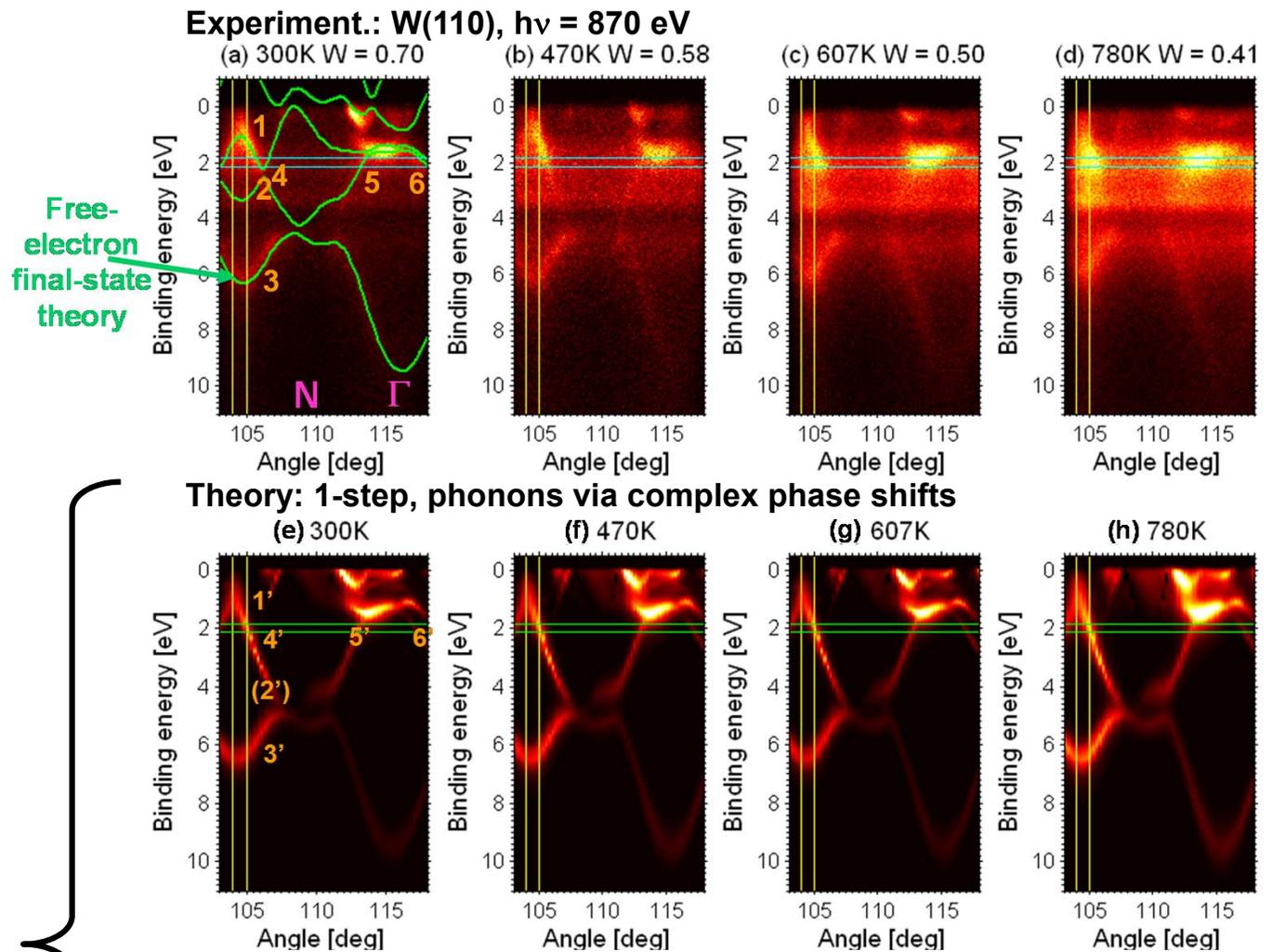
L. Plucinski, J. Minar, ...  
PRB 78, 035108 (2008)

One-step, t-reversed  
LEED, spin-polarized  
relativistic KKR:

- Phonons via complex phase shifts

- Phonons via the coherent potential model

J. Braun, J. Minar, S. Mankovsky, L. Plucinski, Phys. Rev. B 88, 205409 (2013).



# Phonon effects: Improved theoretical modeling

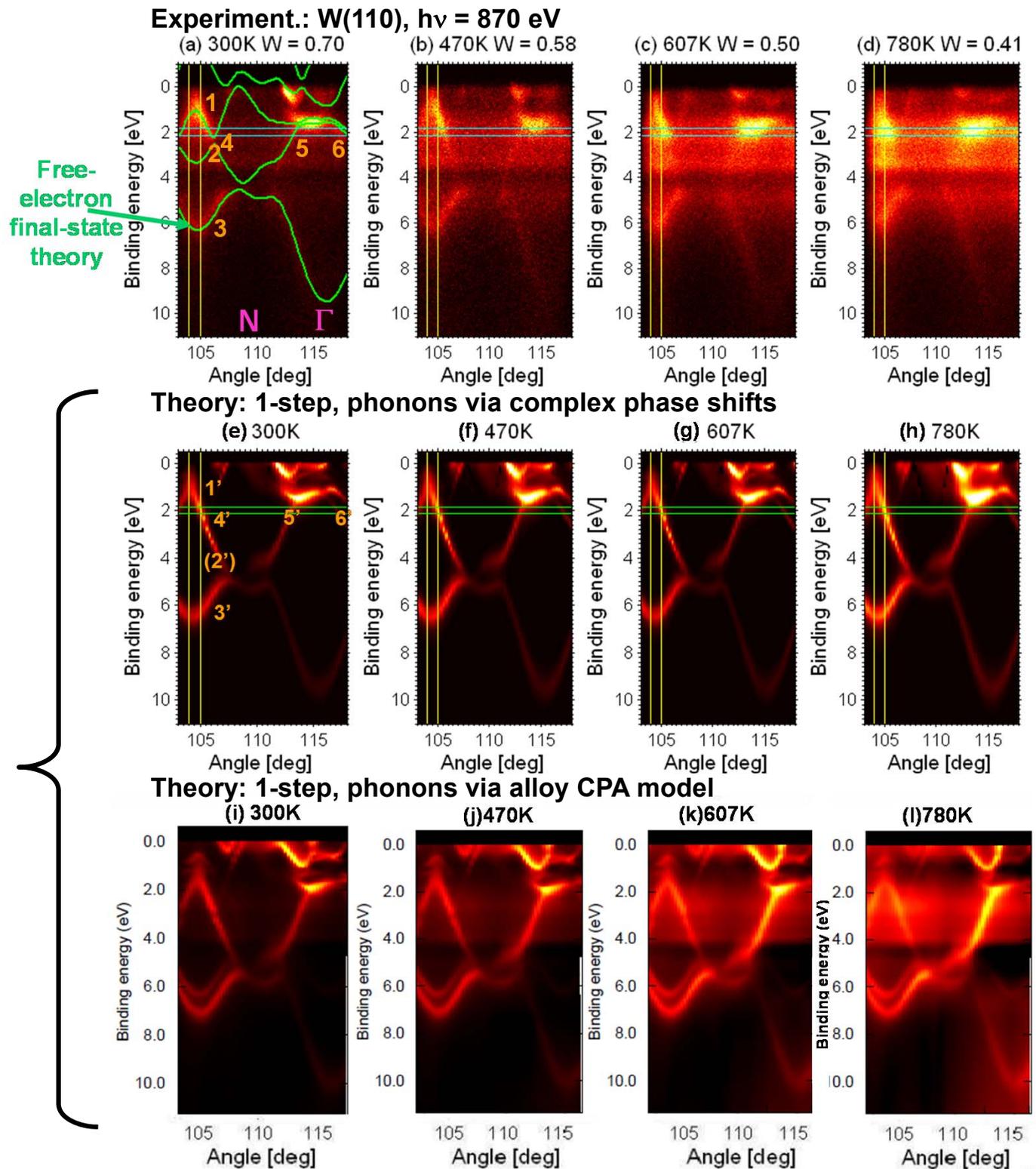
L. Plucinski, J. Minar, ...  
PRB 78, 035108 (2008)

One-step, t-reversed  
LEED, spin-polarized  
relativistic KKR:

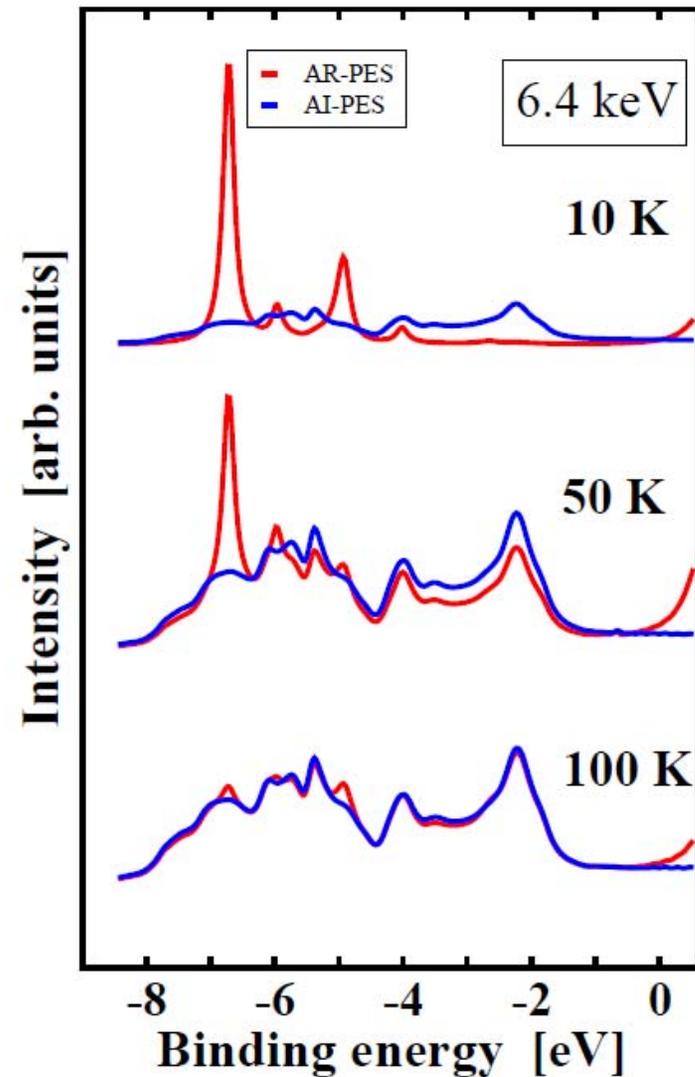
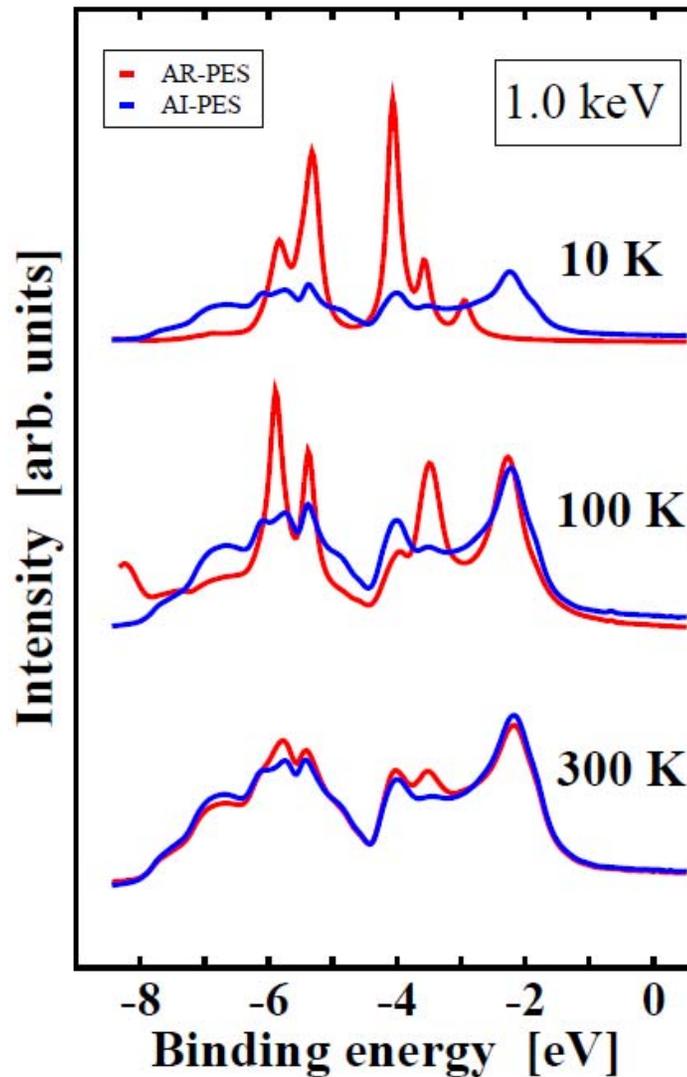
- Phonons via complex phase shifts

- Phonons via the coherent potential model

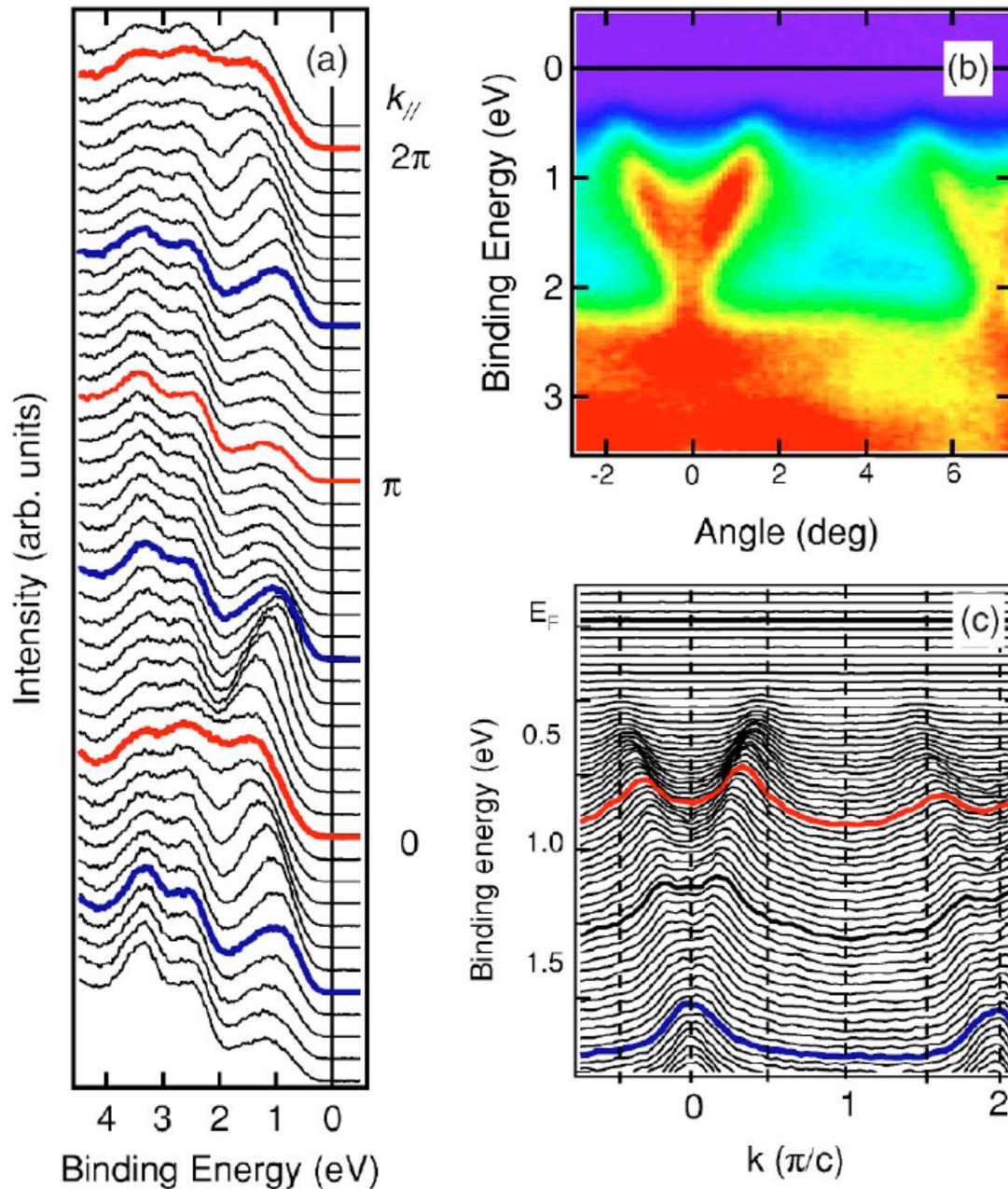
J. Braun, J. Minar, S. Mankovsky, L. Plucinski, Phys. Rev. B 88, 205409 (2013).



Calc. phonon effects in photoemission,  
Au soft and hard x-ray: Angle-resolved PES (ARPES)→Angle-integrated  
PES (XPS/MEWDOS)

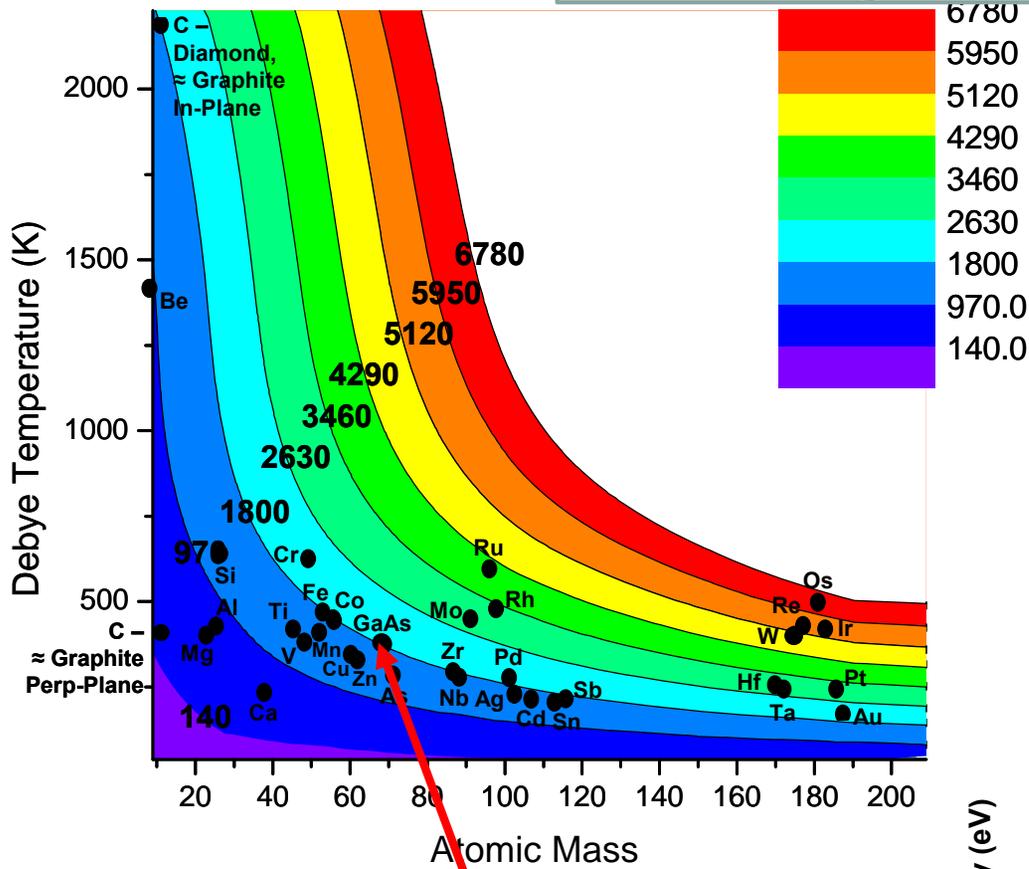


**A first real application of soft x-ray ARPES: Soft x-ray ARPES from SrCuO<sub>2</sub> at  $h\nu = 700$  eV and 300K, photoemission Debye-Waller factor of only 0.03-0.04**



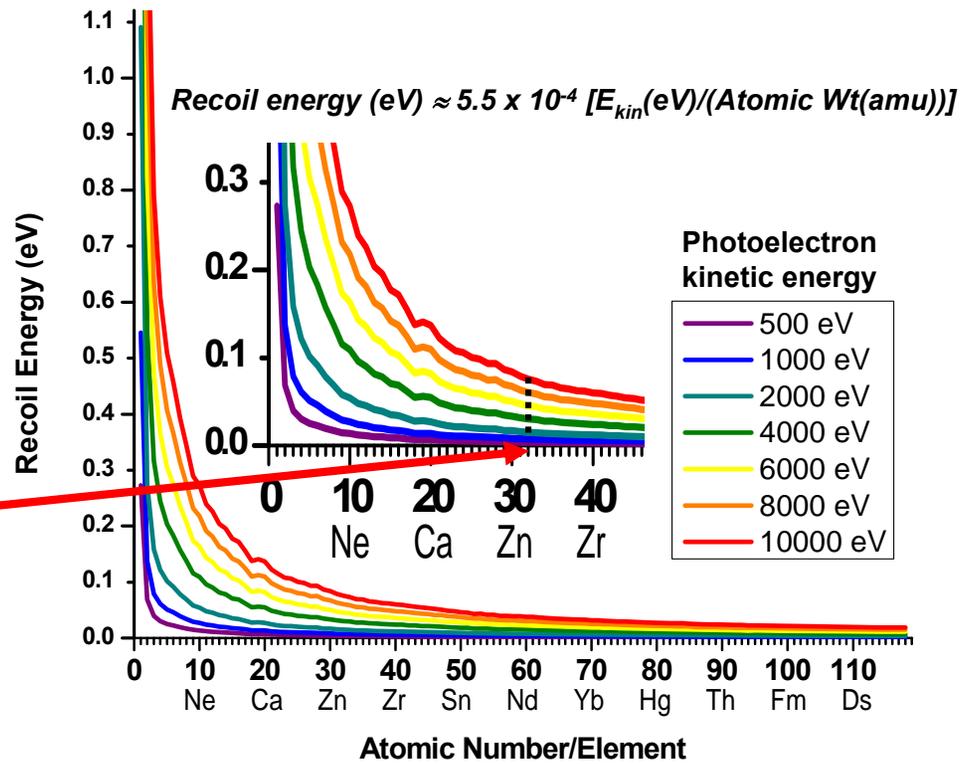
Photoemission DW factors can be too conservative for some systems (lack of correlated vibrations?)  
→ suggests a wider application of SARPES/HARPES

Photon energy for D-W  
= 0.5 @ 20K



**HARPES-How high can we go? Photoemission Debye-Waller Factors and Recoil Energies**

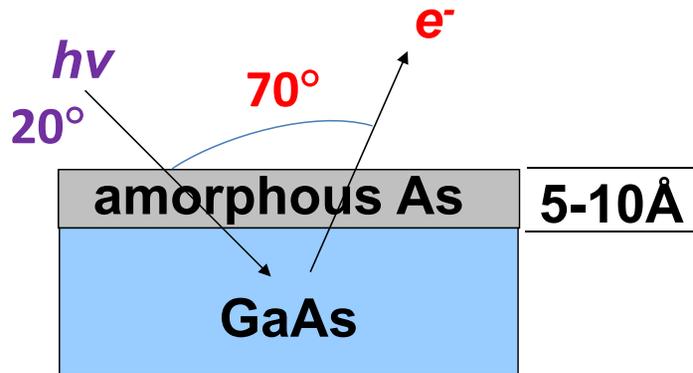
E.g.-GaAs



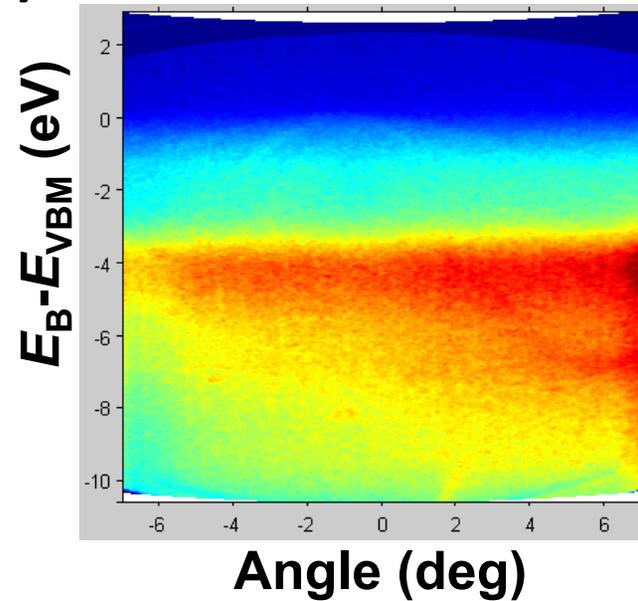
C. Papp, L. Plucinski, et al.,  
Phys. Rev. B 84, 045433 (2011)

# Looking through an amorphous layer to do ARPES: GaAs @ 11K

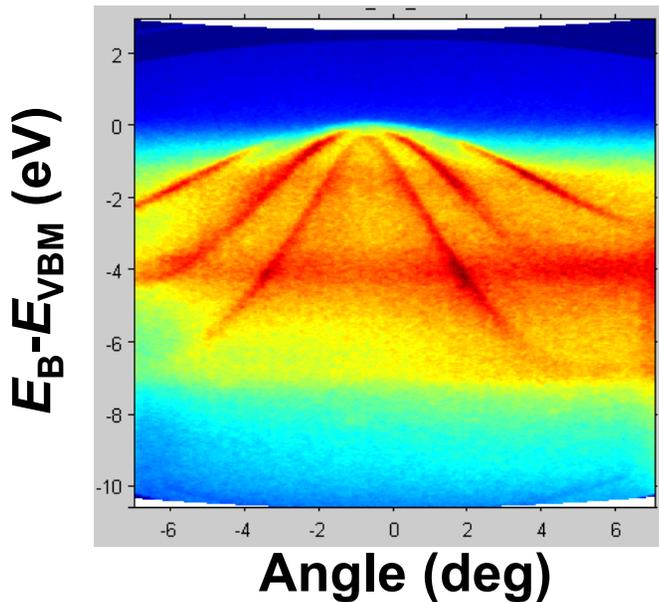
(a)



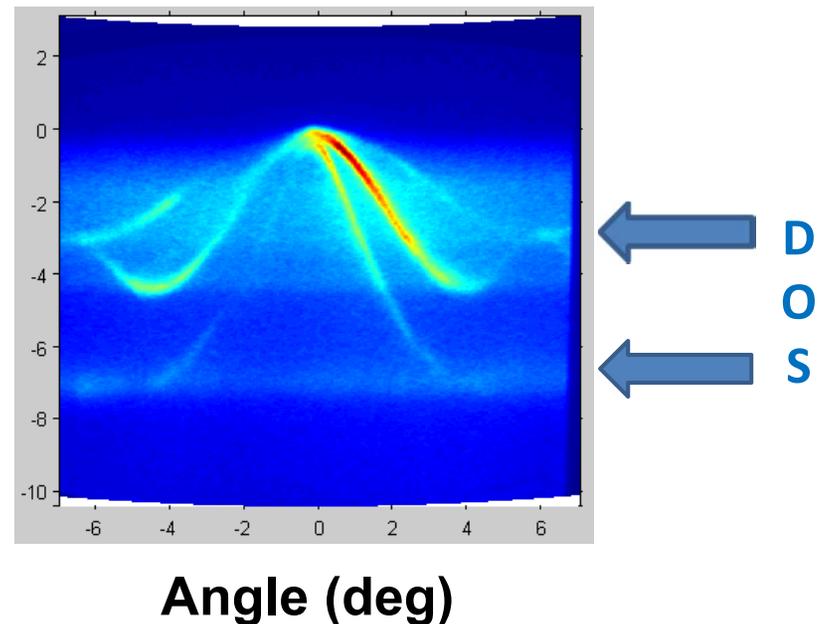
(b)  $h\nu = 287$  eV, D-W = 0.90



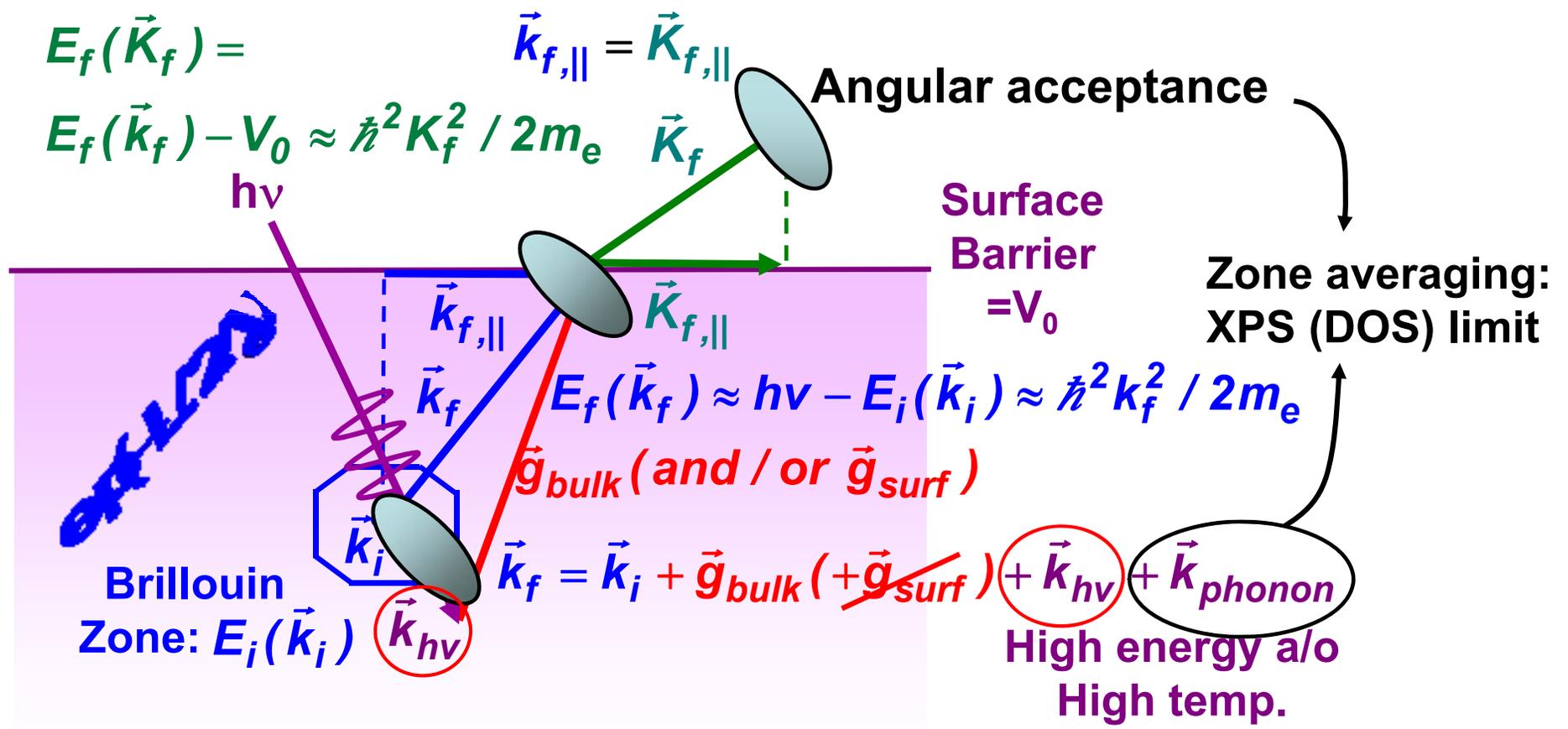
(c)  $h\nu = 453$  eV, D-W = 0.86



(d)  $h\nu = 892$  eV, D-W = 0.72



# ARPES—How high can we go in energy and temperature?



Fraction DTs  $\approx$  Debye-Waller factor =  $W(T) \approx \exp[-(k^f)^2 \langle u^2(T) \rangle]$   
 $\approx \exp[-C_1 (k^f)^2 T / (m \Theta_D^2)] \approx \exp(-C_2 E_{kin} T)$

$W \approx 1$

$W \approx 0.3$

$W \approx 0$

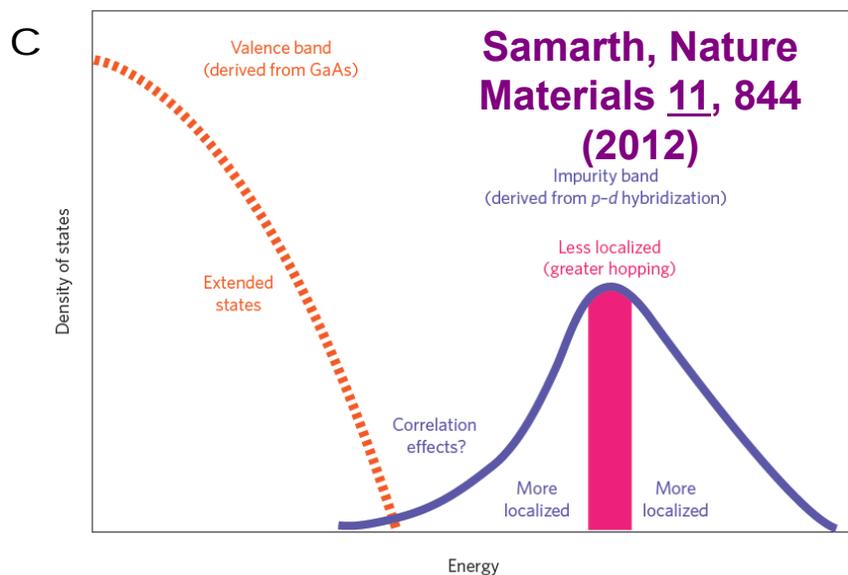
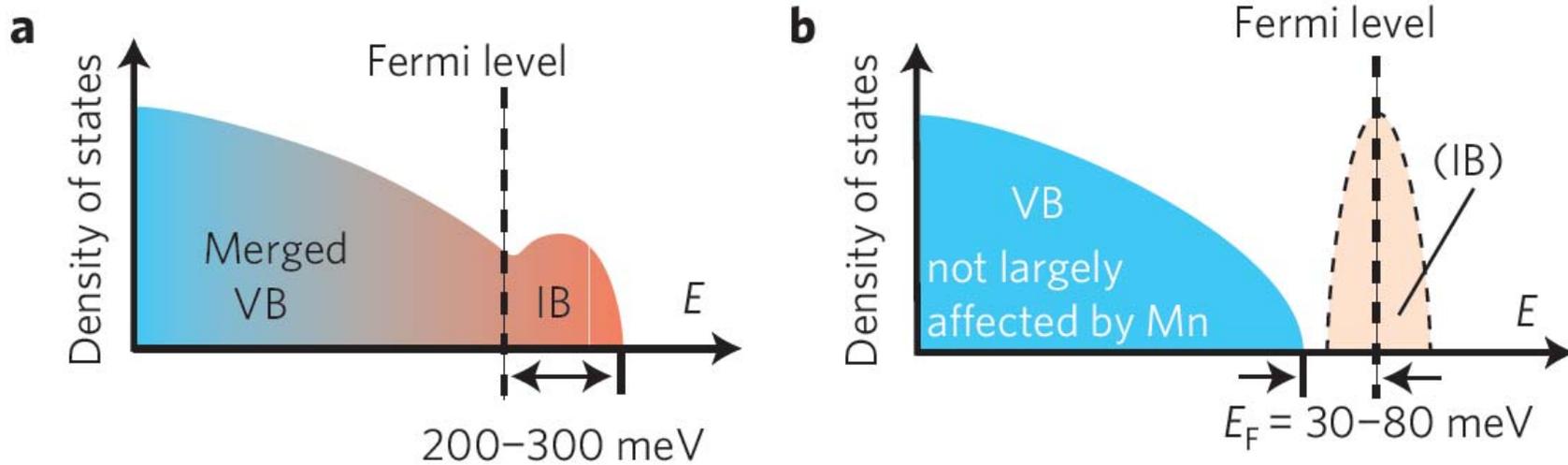
ARPES  $\rightarrow$  bands, quasiparticles  
 (Low  $h\nu$ , Low  $T$ , High angul. Res.)

XPS  $\rightarrow$  DOS + XPD  
 (High  $h\nu$ , High  $T$ , Low angul. Res.)

Shevchik, Phys. Rev. B 16, 3428 (1977)  
 Hussain....CF, Phys. Rev. B 34 (1986) 5226

# Hard x-ray ARPES--GaAs and the dilute magnetic semiconductor $\text{Ga}_{0.97}\text{Mn}_{0.03}\text{As}$

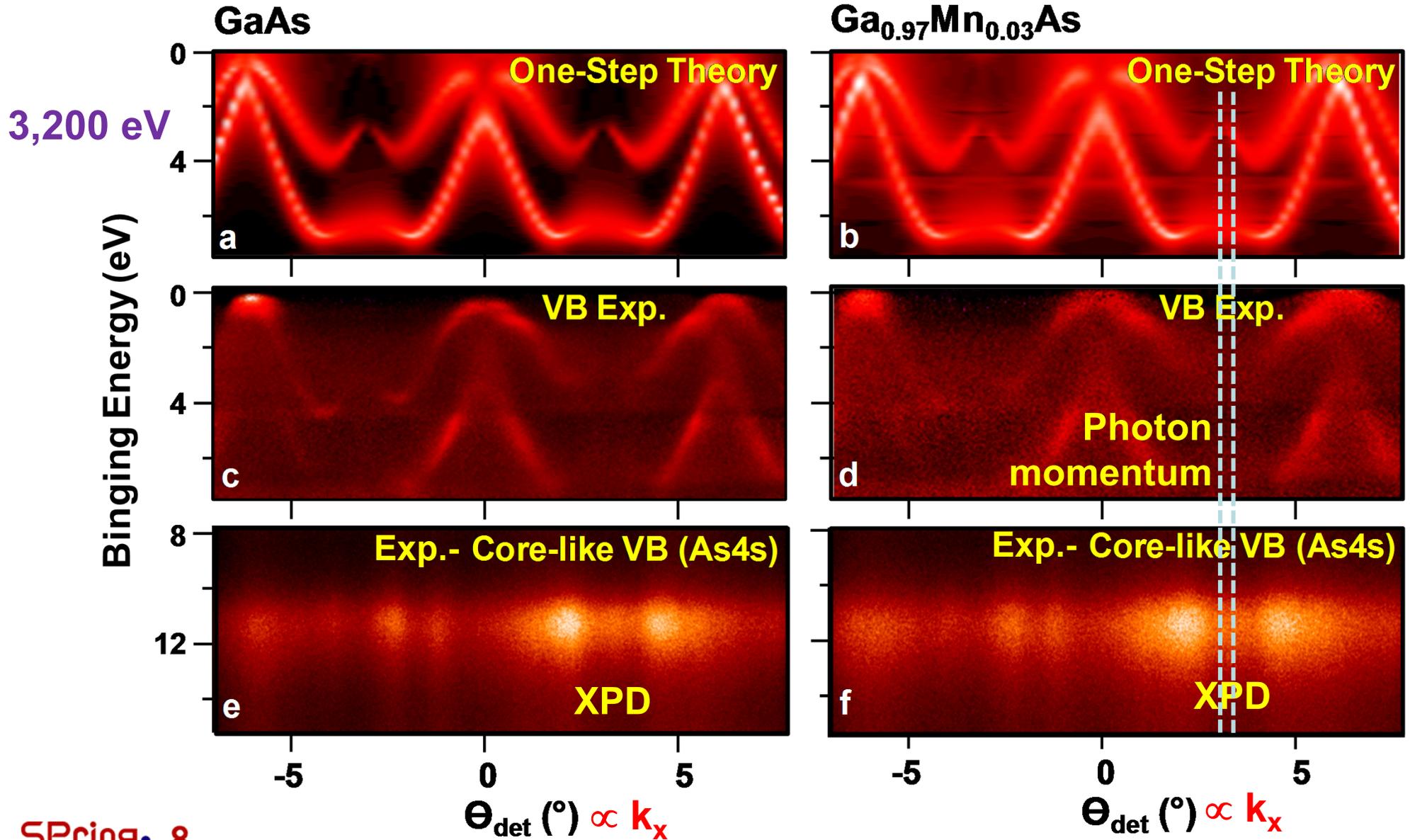
How does Mn alter the GaAs electronic structure so as to produce ferromagnetic coupling?  
Differing views: p-d exchange, double exchange?



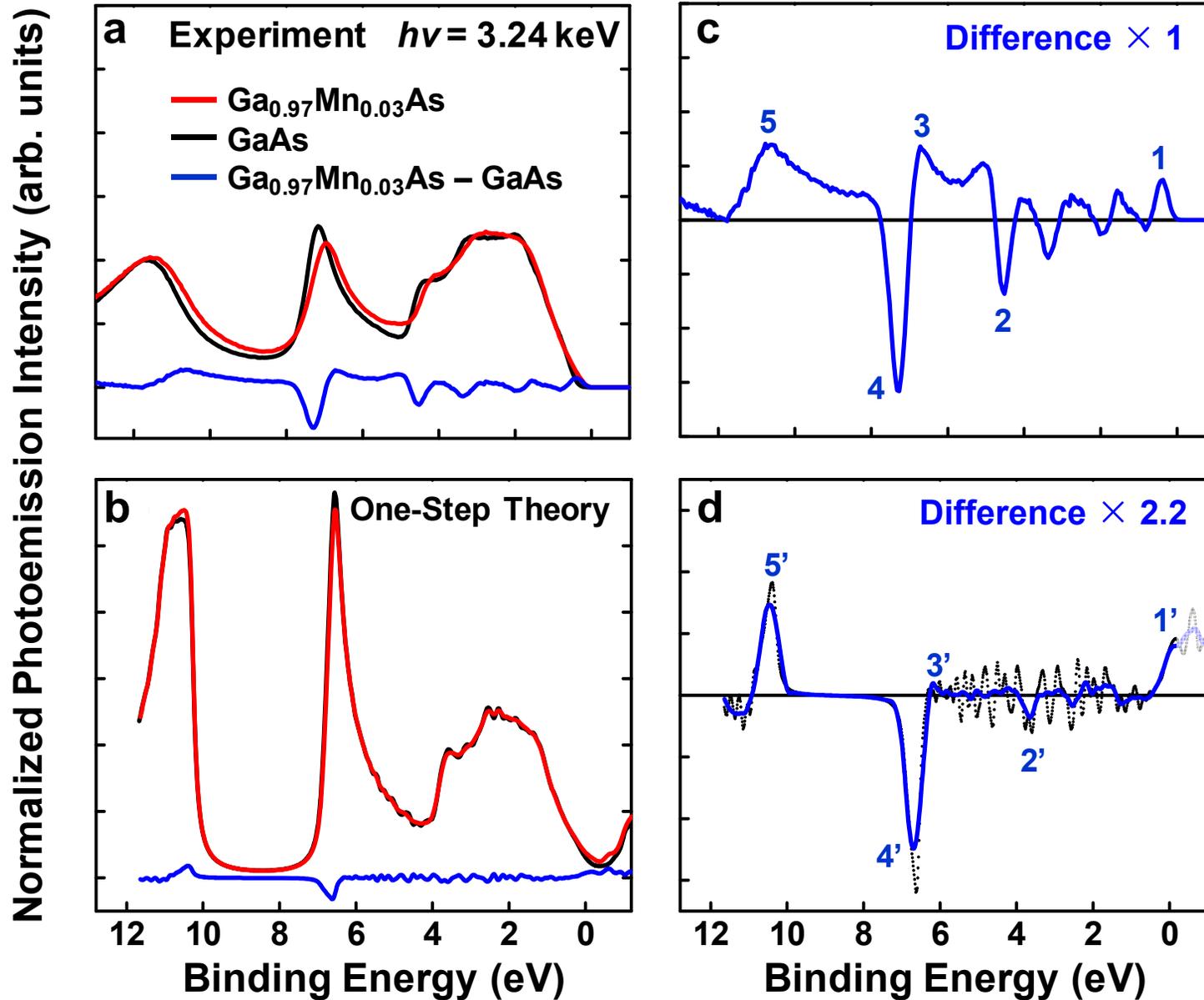
Ohya et al., Nature Physics 7, 342 (2011)



# Hard x-ray ARPES--GaAs and DMS $\text{Ga}_{0.97}\text{Mn}_{0.03}\text{As}$ Comparing Experiment (3.2 keV, 30K) and One-Step KKR Theory



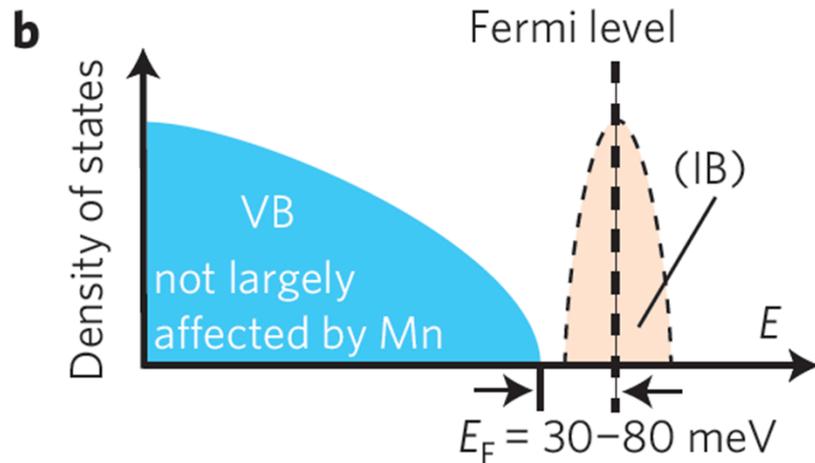
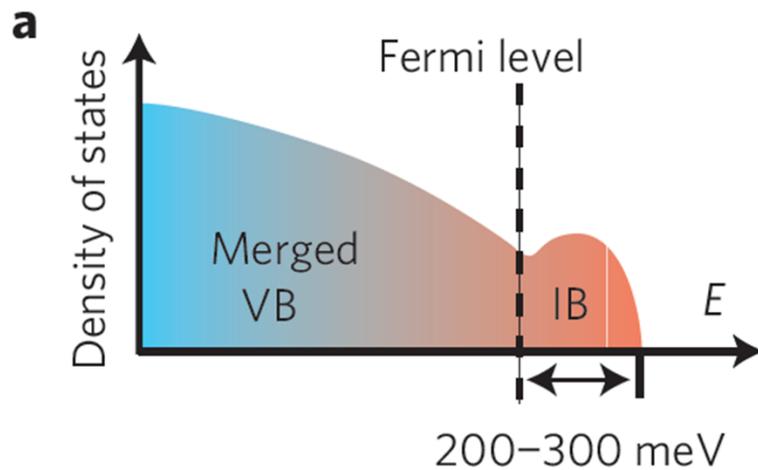
**GaAs and Ga<sub>0.97</sub>Mn<sub>0.03</sub>As**  
**Angle-Integrated Hard X-Ray ARPES @ 3.2 keV**  
**Experiment and One-Step KKR Theory**



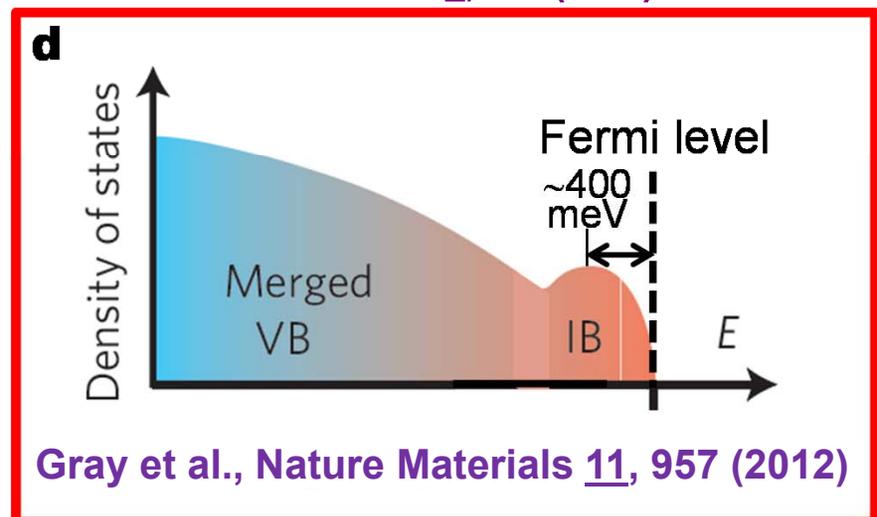
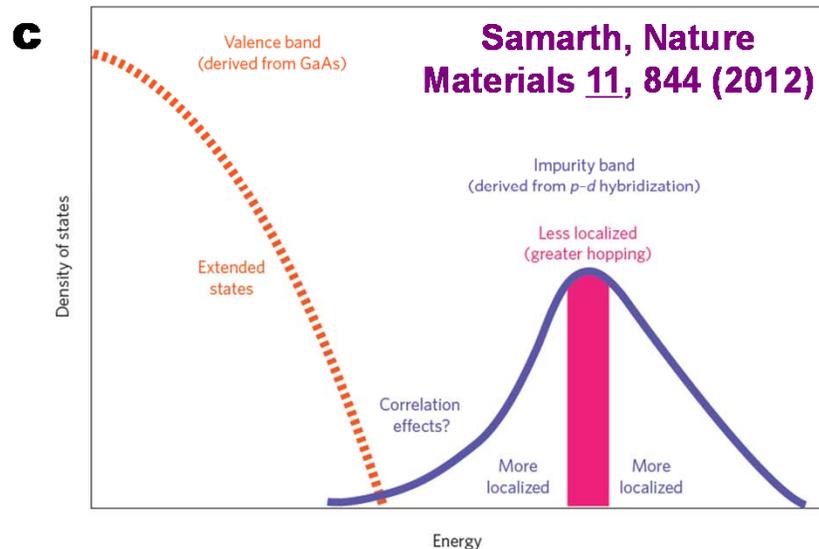
# Hard x-ray ARPES--GaAs and the dilute magnetic semiconductor $\text{Ga}_{0.97}\text{Mn}_{0.03}\text{As}$

How does Mn alter the electronic structure so as to produce ferromagnetic coupling?

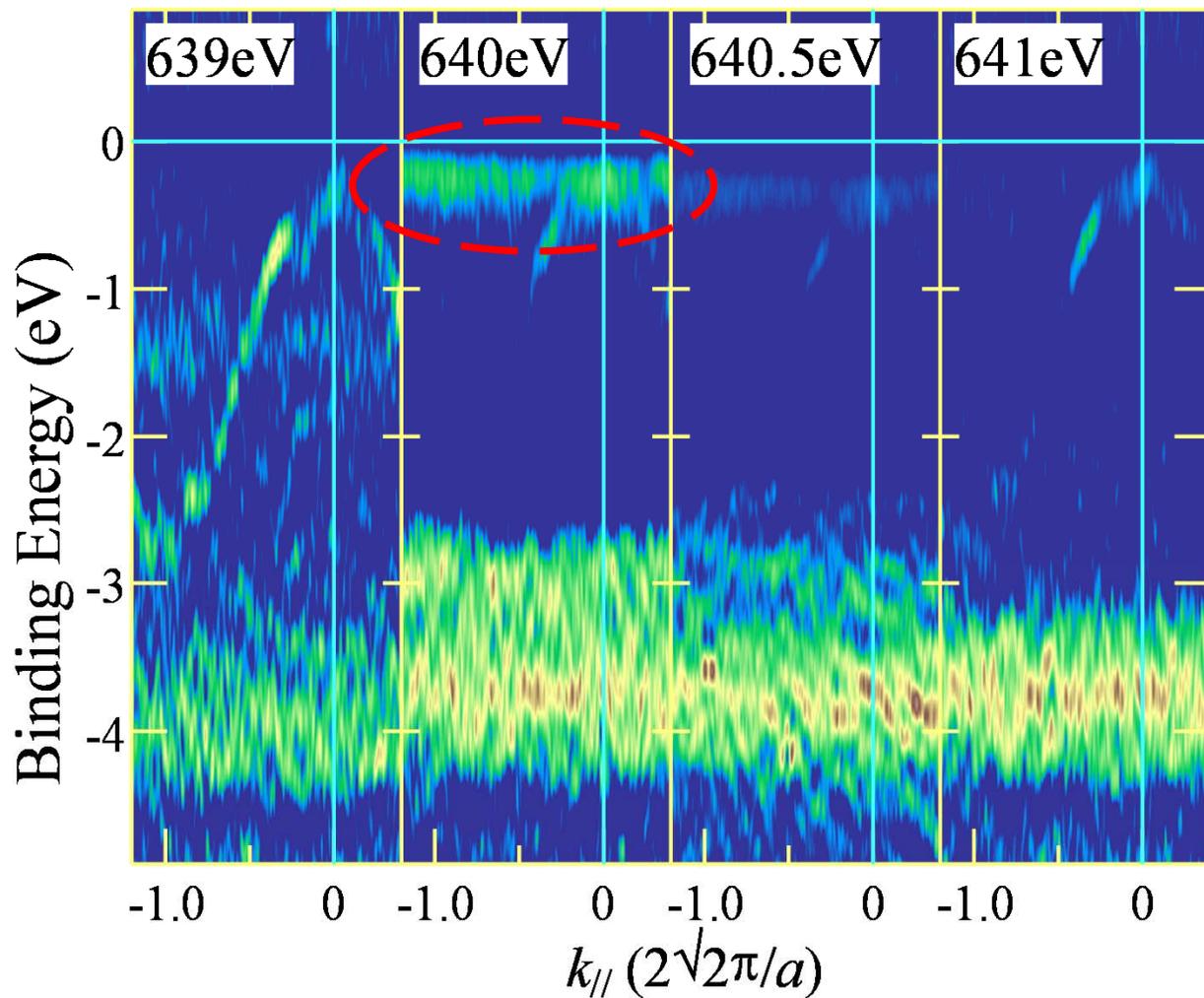
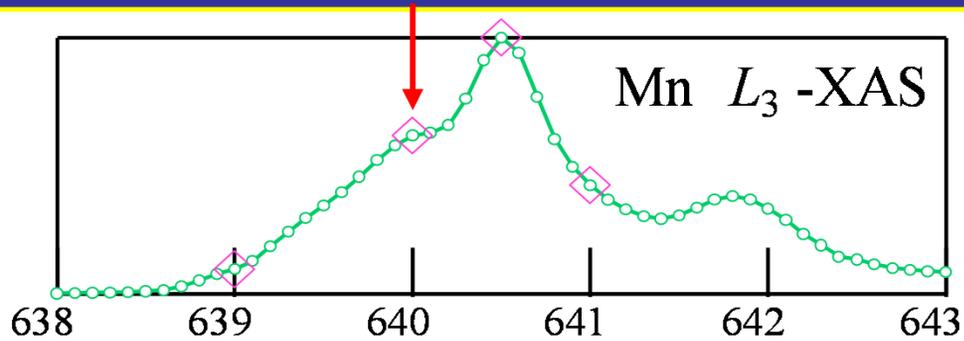
Differing views:



Ohya et al., *Nature Physics* **7**, 342 (2011)

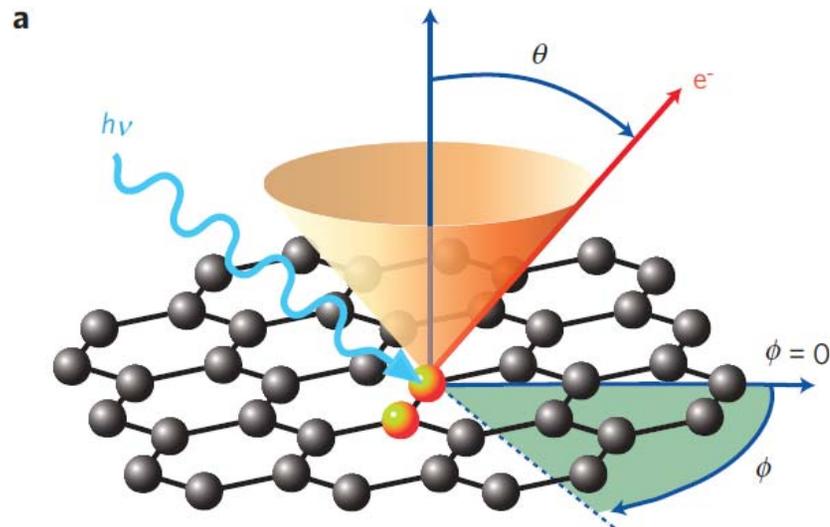


# $\text{Ga}_{0.975}\text{Mn}_{0.025}\text{As}$ : Resonant soft x-ray ARPES

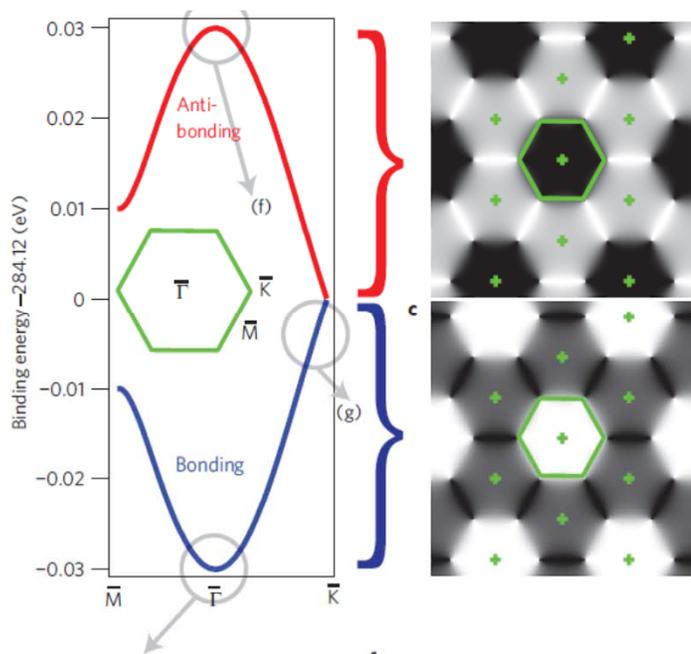


Kobayashi, Strosov, et al.,  
Phys Rev B 89, 205204 (2014)

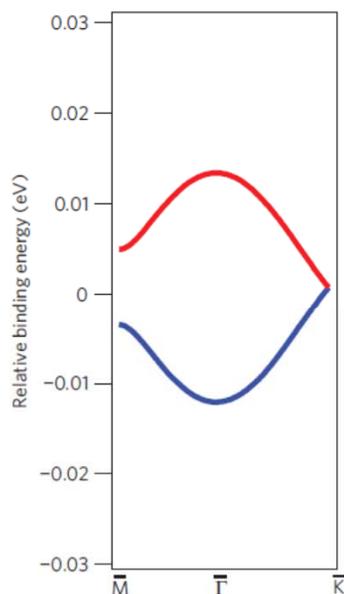
# Band structure in core levels!—C 1s from graphene



## Theory Tight-binding

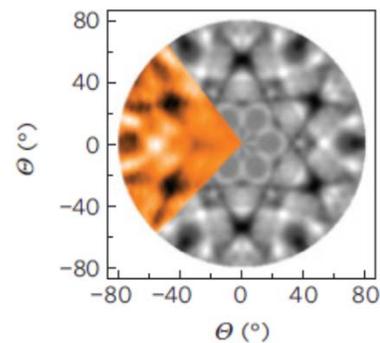


## All-electron

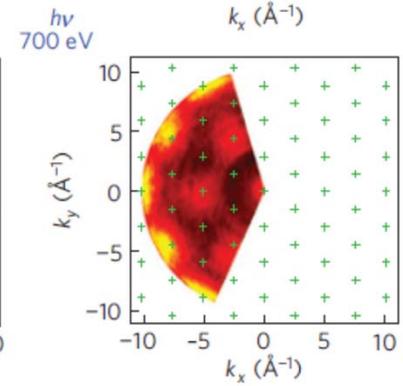
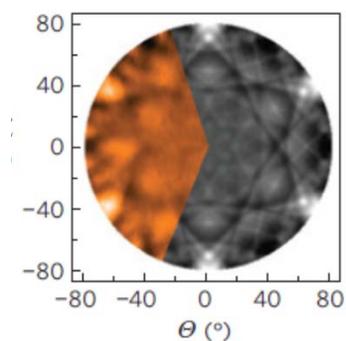
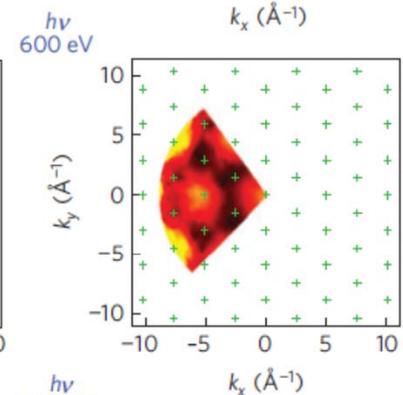
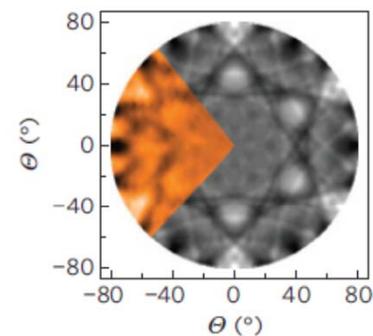
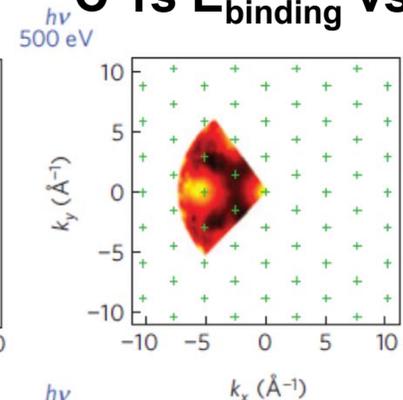


## Experiment

### C 1s XPD



### C 1s $E_{\text{binding}}$ vs $k_{\parallel}$



## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit - Covered already

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)



Photoemission with Standing Wave Excitation - See seminar

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit-Covered already

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation-See seminar

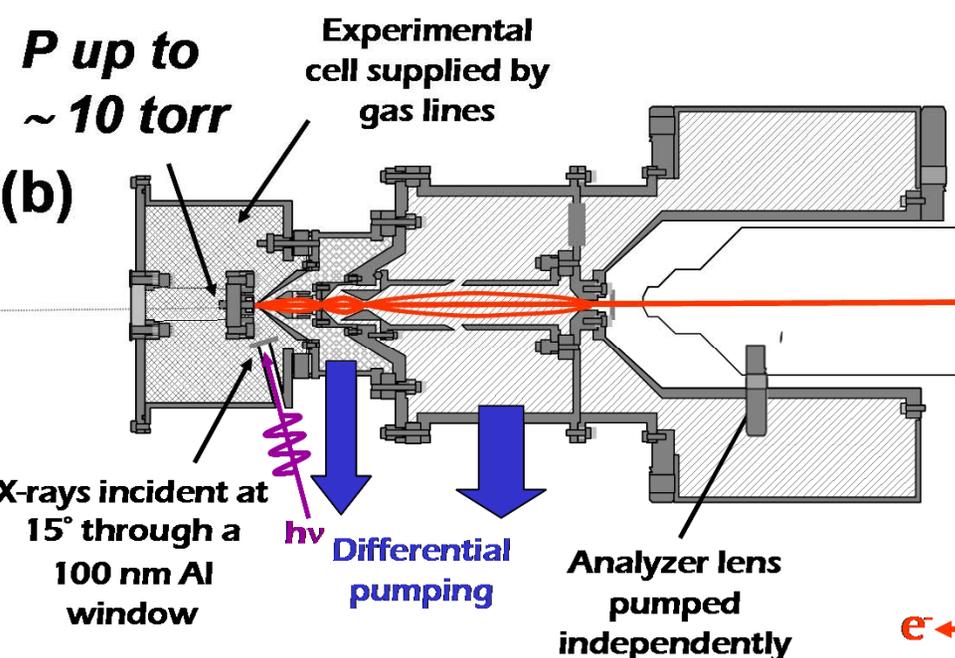
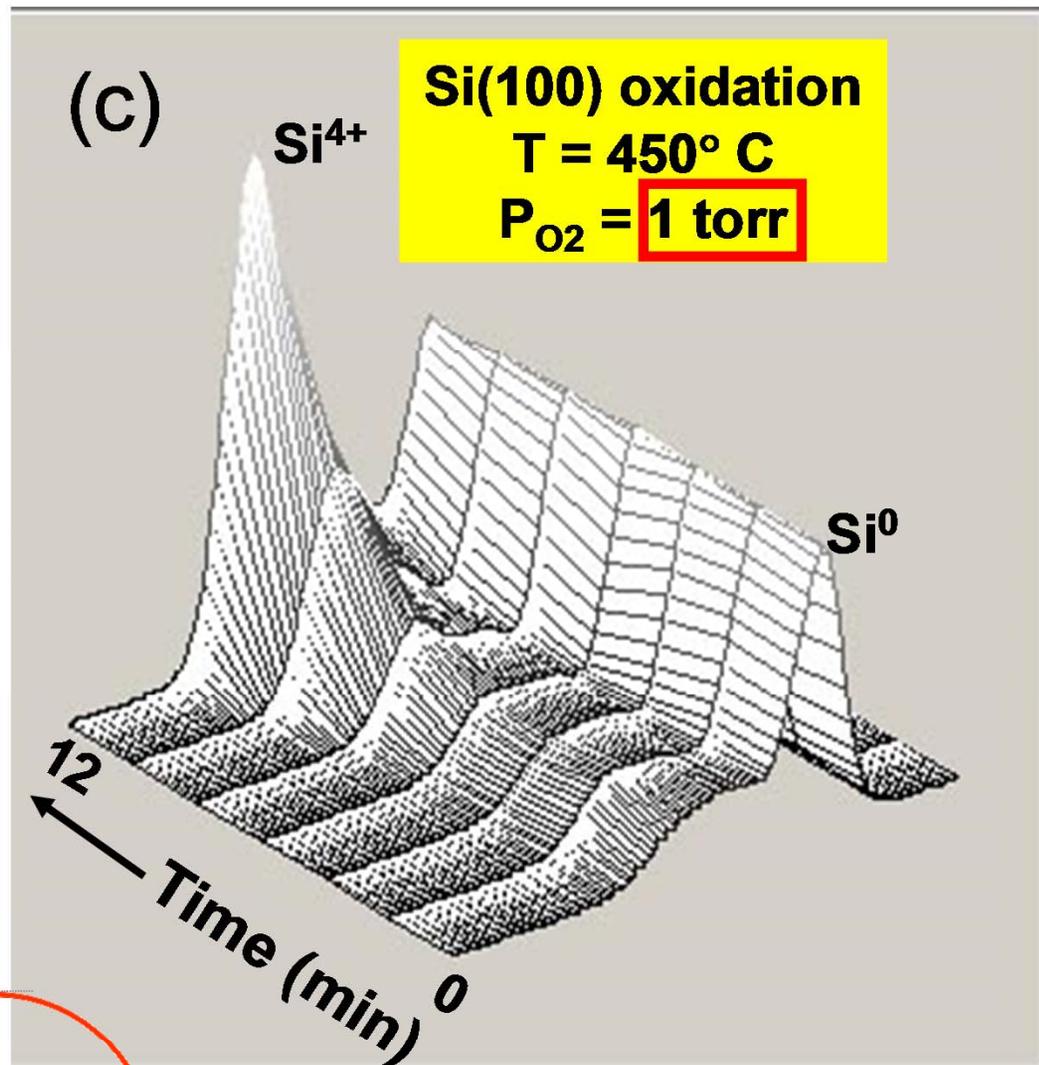
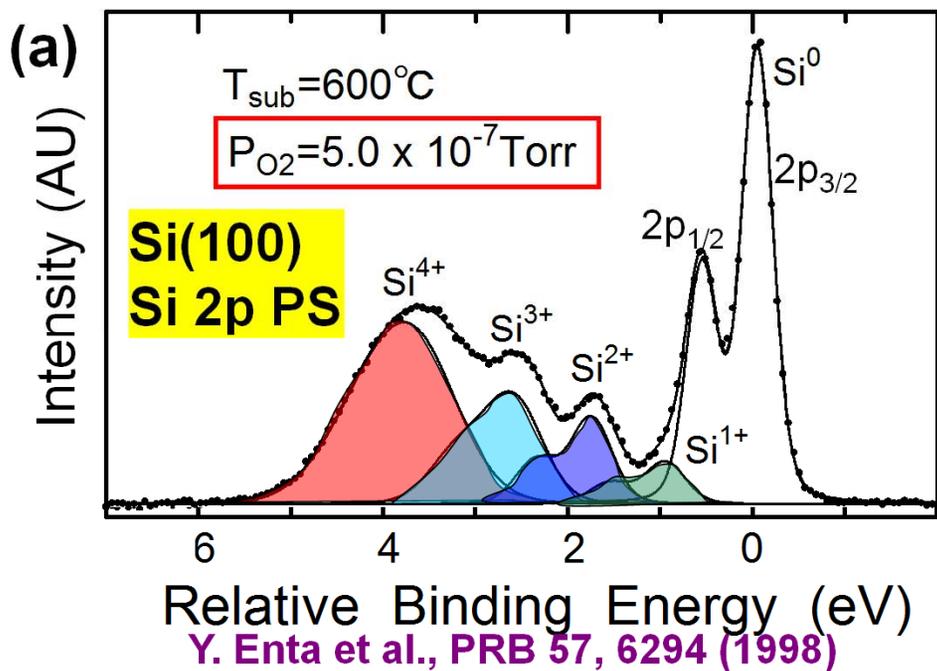


Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

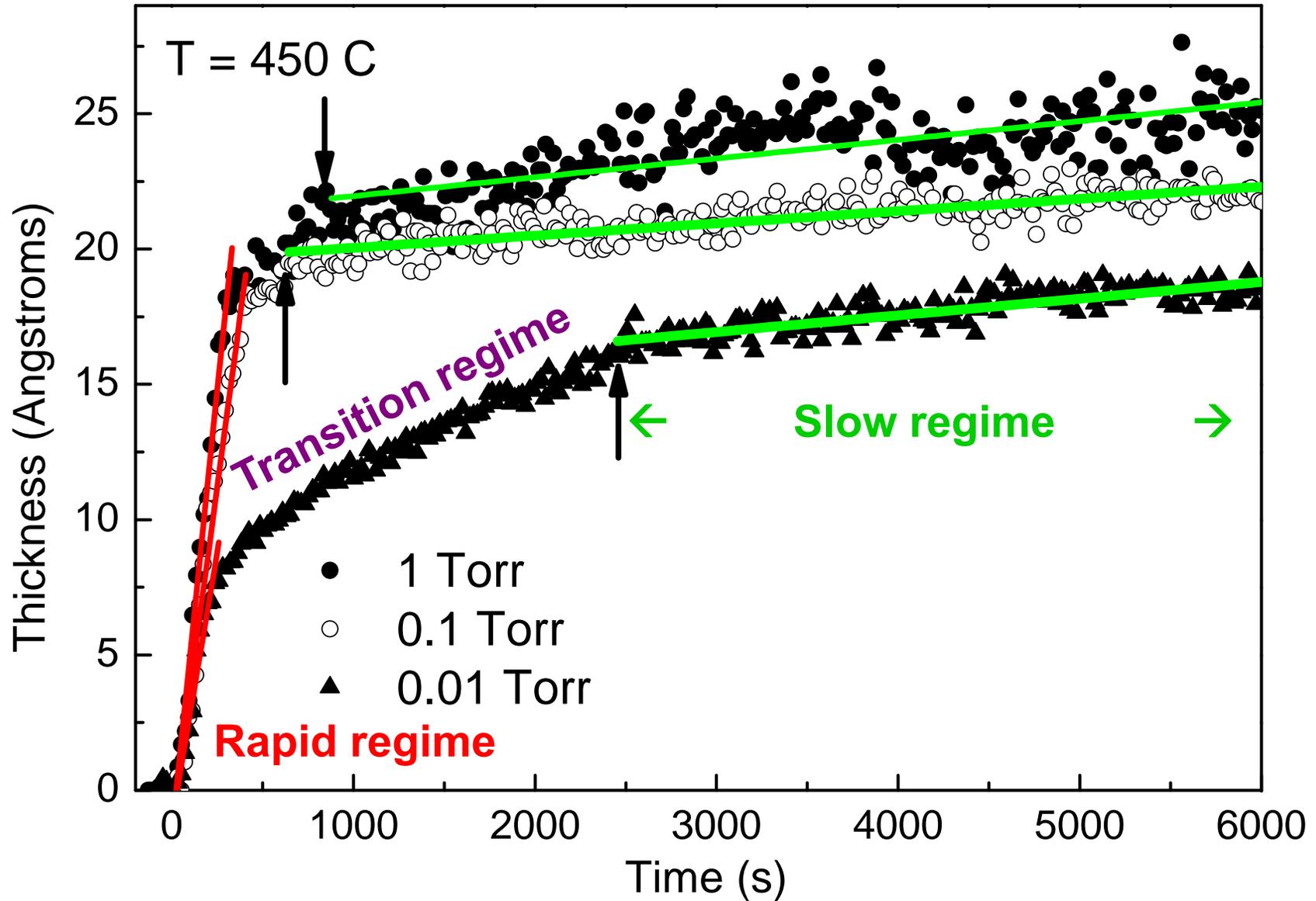
Temporal Resolution

# Ambient Pressure XPS-Bridging the Pressure Gap: CState- and Time- Resolved Oxidation of Si at Multi-Torr Pressures



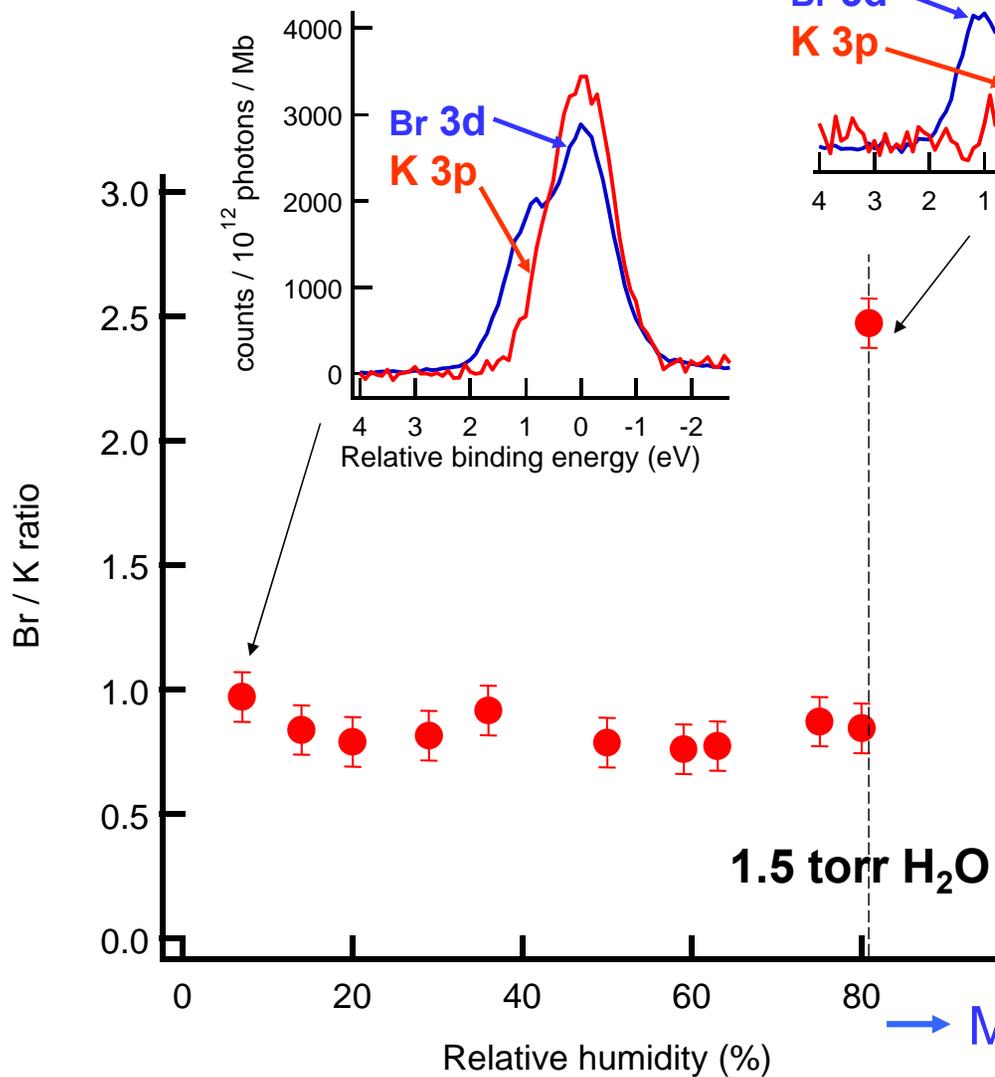
Energy Analysis  
P ≈ 10<sup>-7</sup> torr or better  
e<sup>-</sup>

# Watching the oxide grow in real time: constant P, variable T

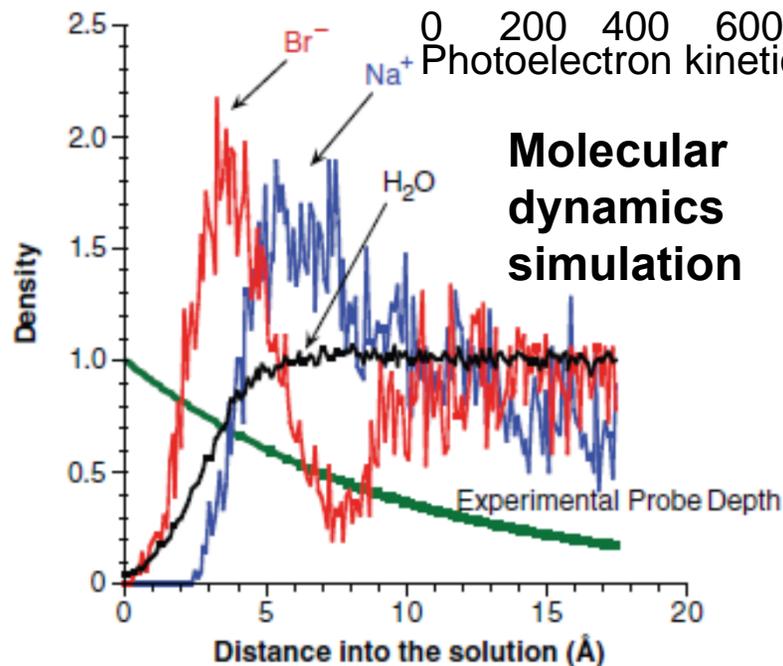
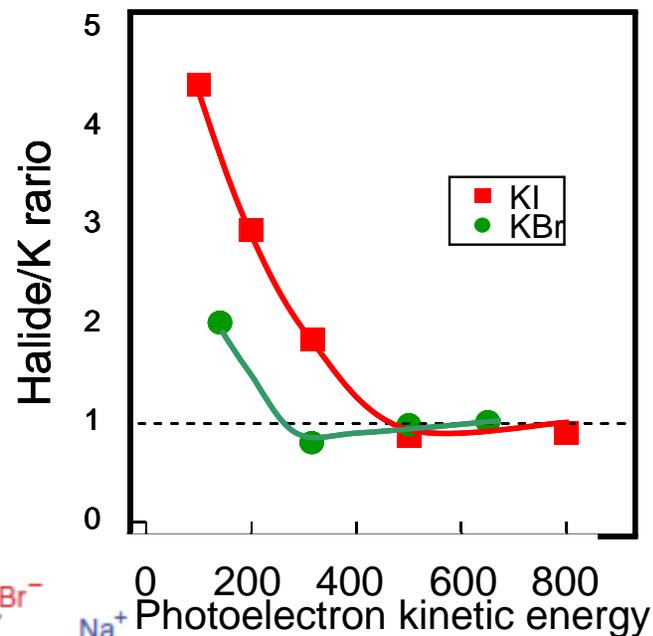
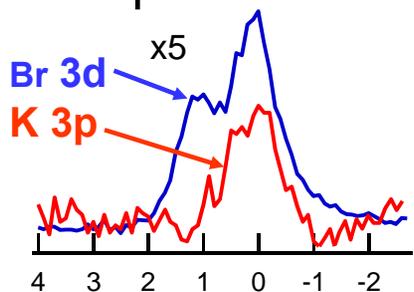


# Measuring the concentration profile of ions near an aqueous surface

**KBr (001)**  
 $h\nu = 200 \text{ eV}$



At deliquescence →  
droplet formation



→ More halide near surface—marked change

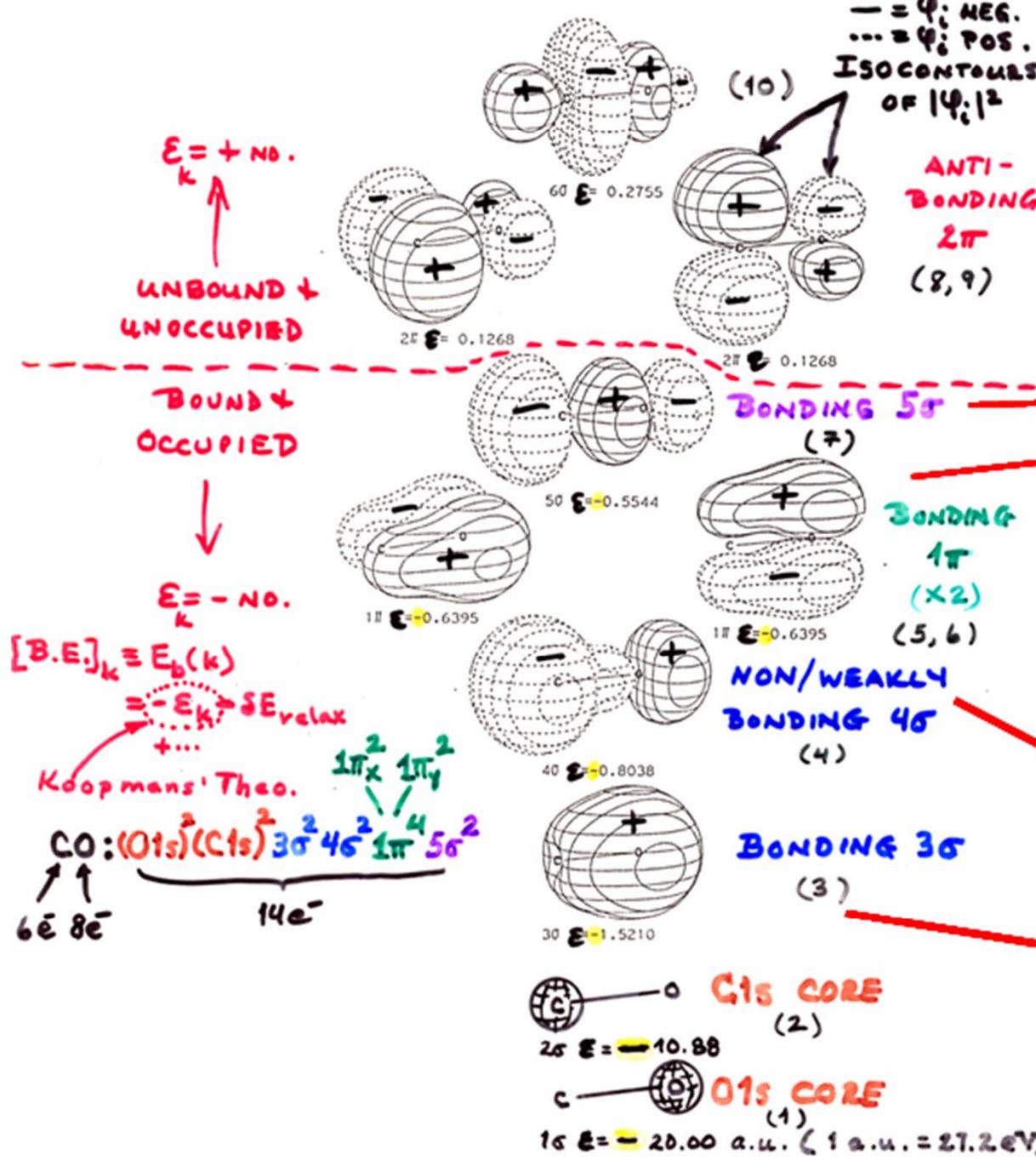
S. Ghosal, J.C. Hemminger, et al., Science 307, 5709 (2005)

# THE ELECTRONS IN CARBON MONOXIDE:

15. Carbon Monoxide

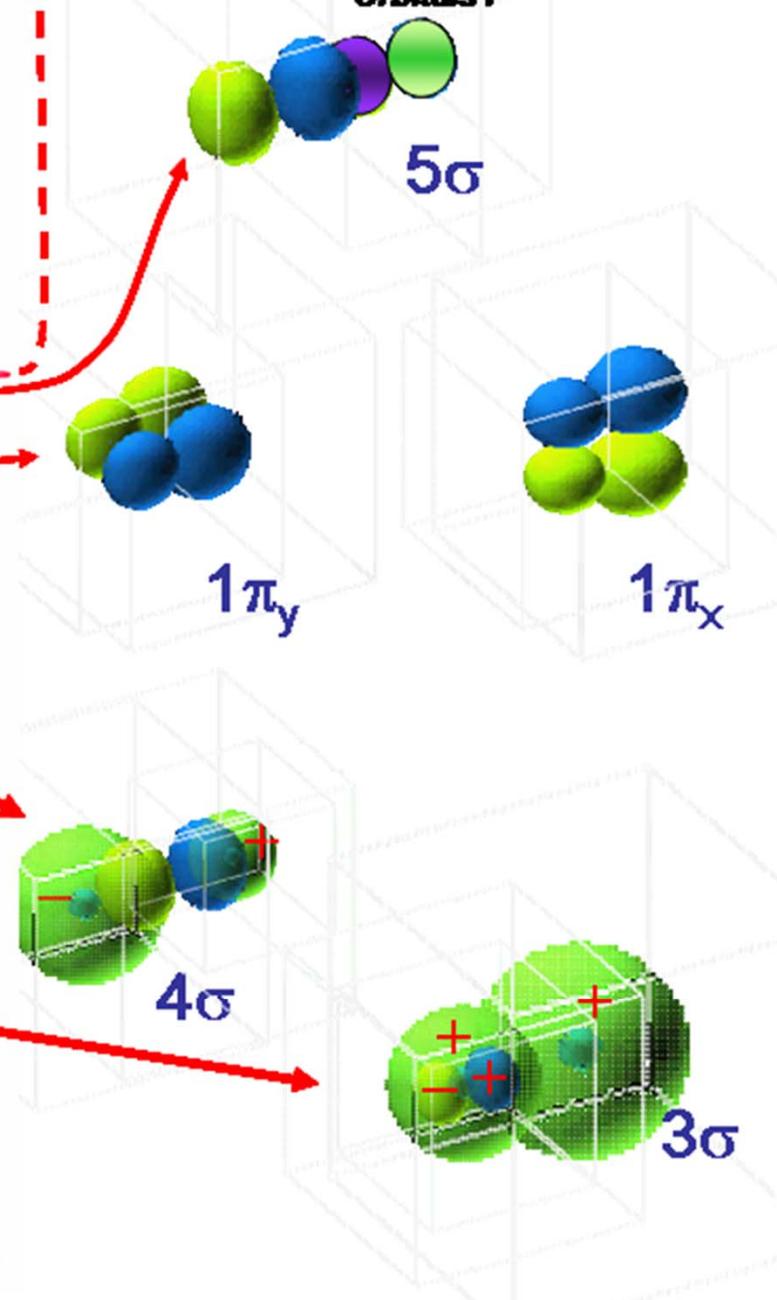
Symmetry:  $C_{\infty v}$

--- =  $\psi_i$ : NEG.  
 ... =  $\psi_i$ : POS.  
**ISOCONTOURS OF  $|\psi_i|^2$**

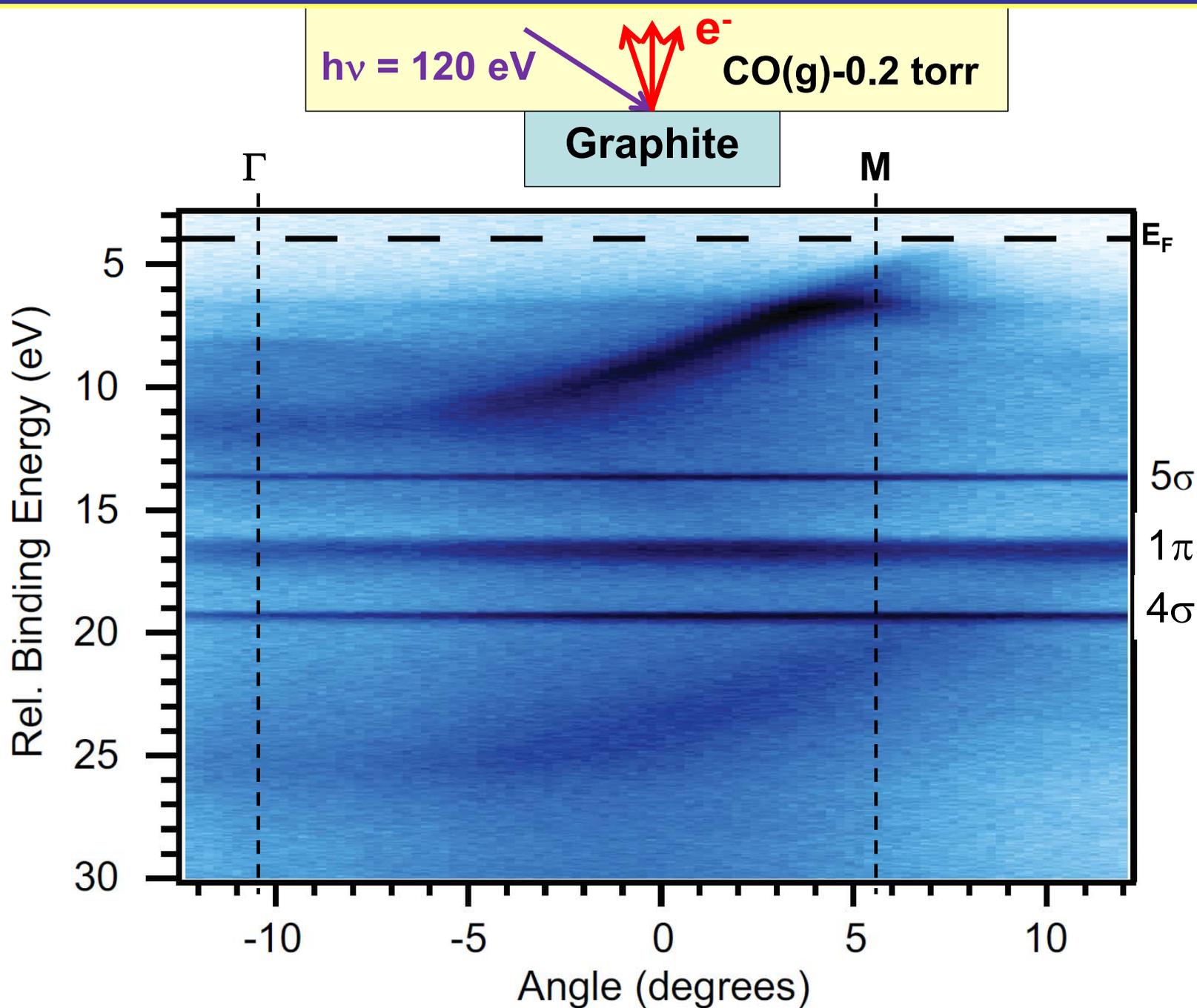


## Atomic orbital makeup

$$\phi_j^{MO}(\vec{r}) = \sum_{\text{Atoms } A} c_{Ai,j} \phi_{Ai}^{AO}(\vec{r})$$



# Seeing both bands and molecular states in ambient pressure XPS: CO above graphite



## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

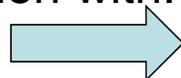
Densities of States in the X-Ray Photoemission Limit - Covered already

## Some New Directions

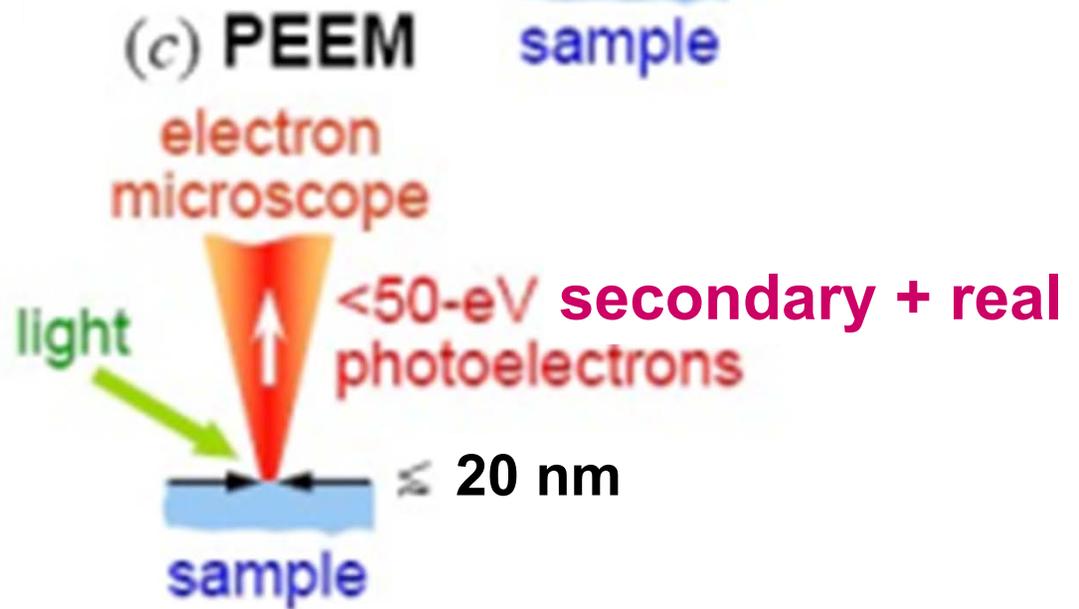
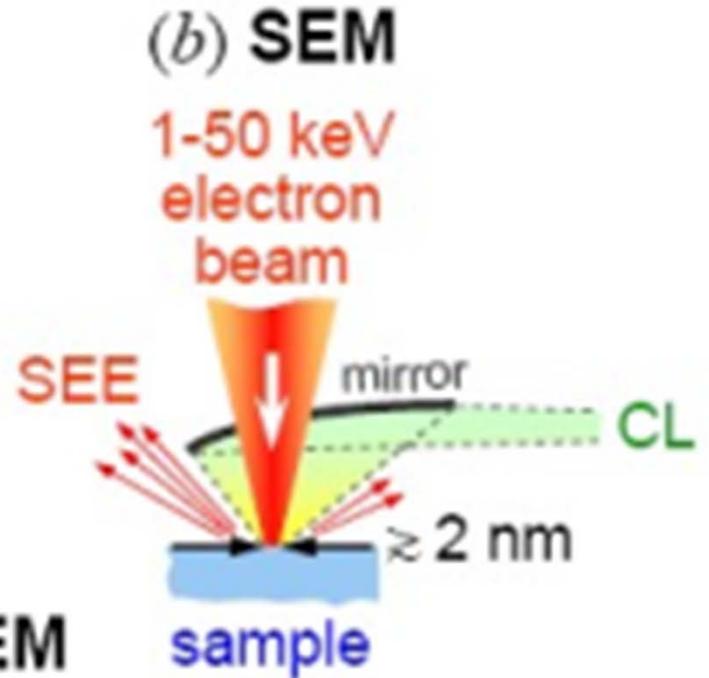
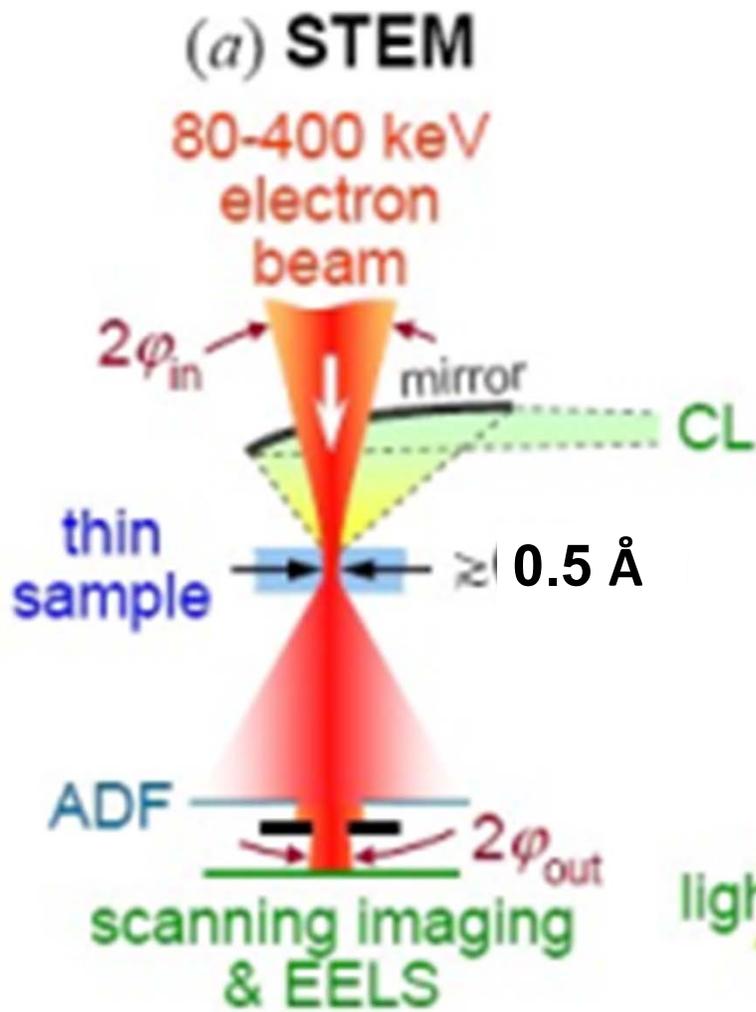
Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation - See seminar

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?



Spatial Resolution-Photoelectron Microscopy  
Temporal Resolution

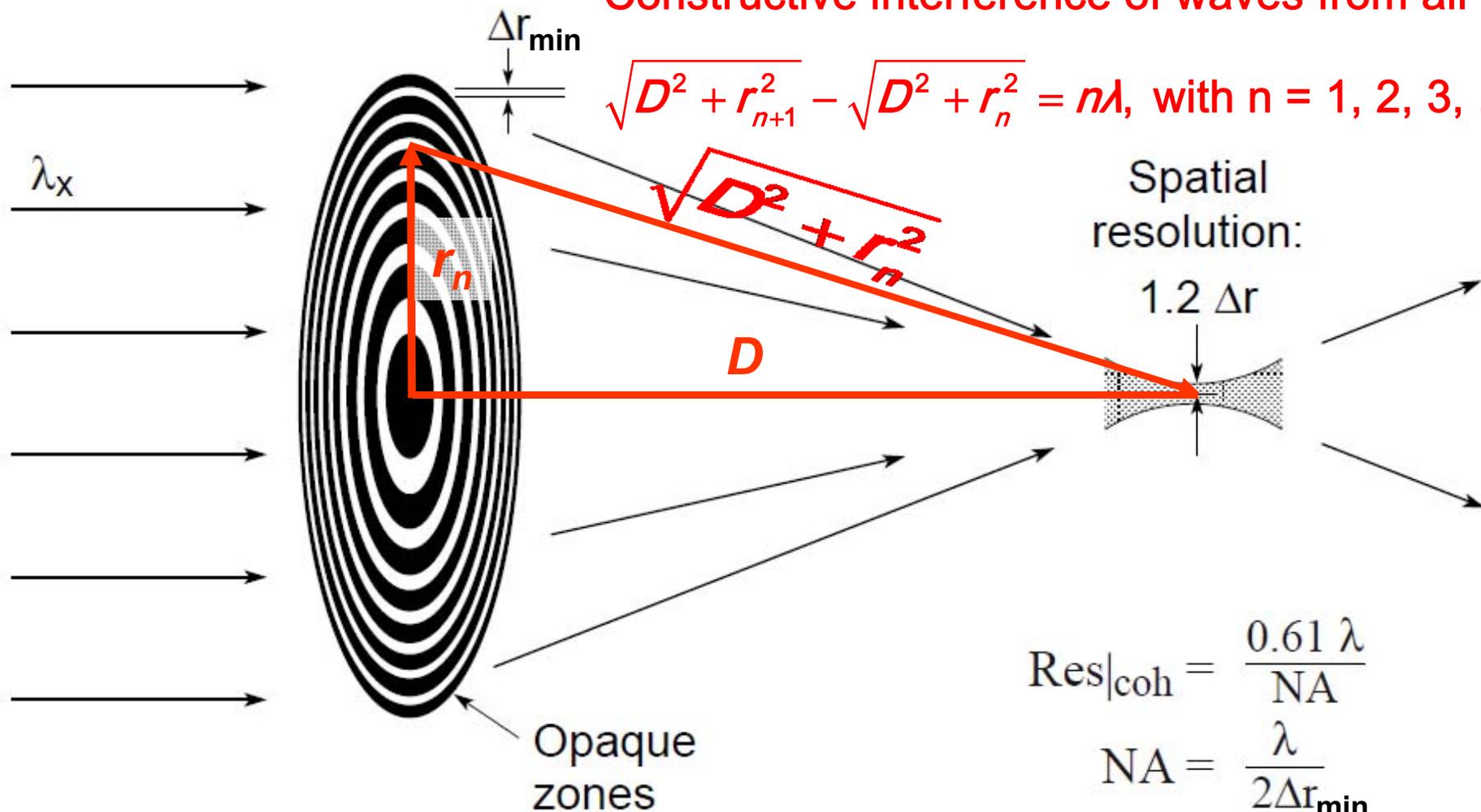




# Fresnel Zone Plate Lens for Diffractive Focusing of Spatially Coherent X-rays

Constructive interference of waves from all rings:

$$\sqrt{D^2 + r_{n+1}^2} - \sqrt{D^2 + r_n^2} = n\lambda, \text{ with } n = 1, 2, 3, \dots$$



$$\text{Res}_{|\text{coh}} = \frac{0.61 \lambda}{\text{NA}}$$

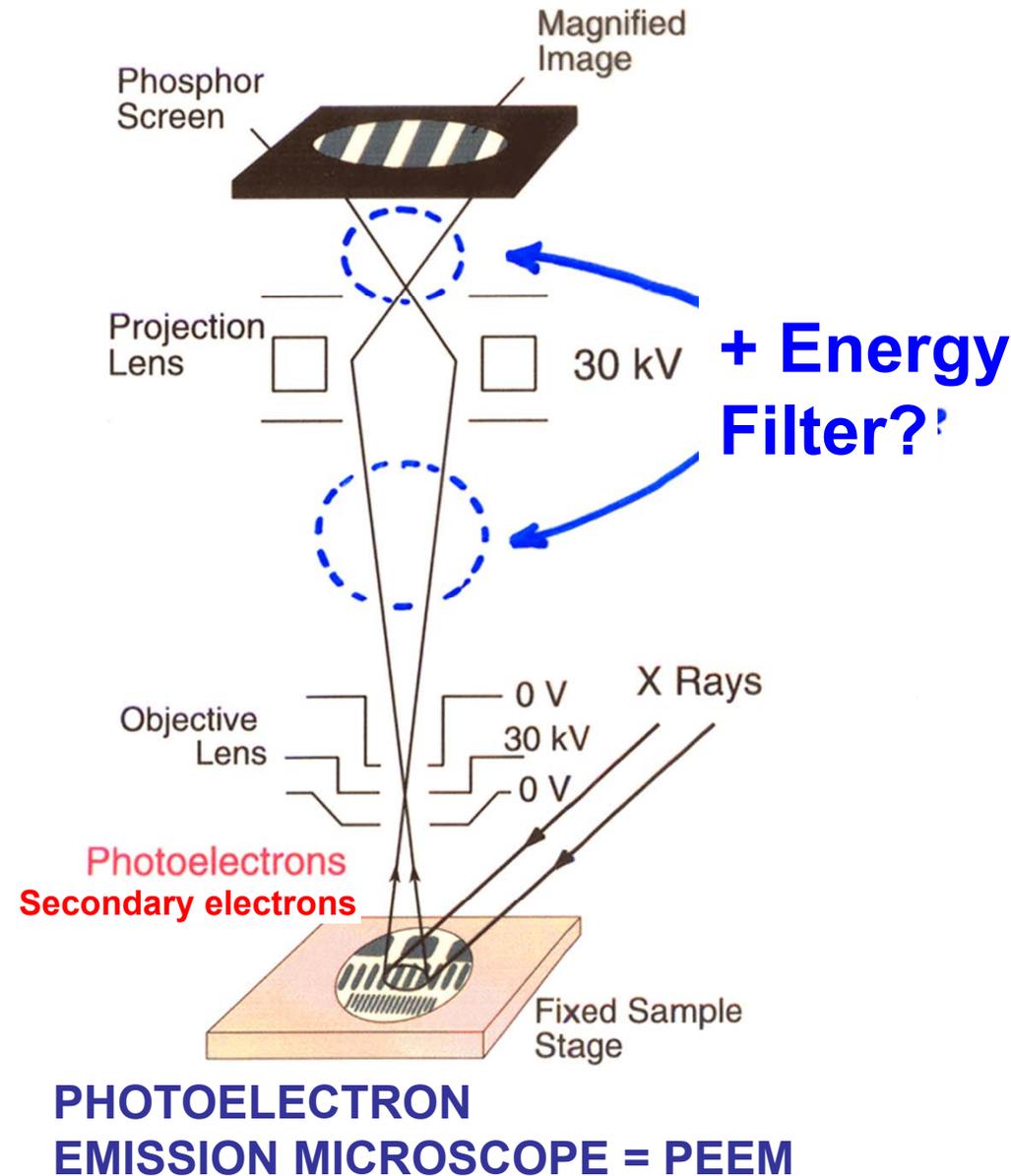
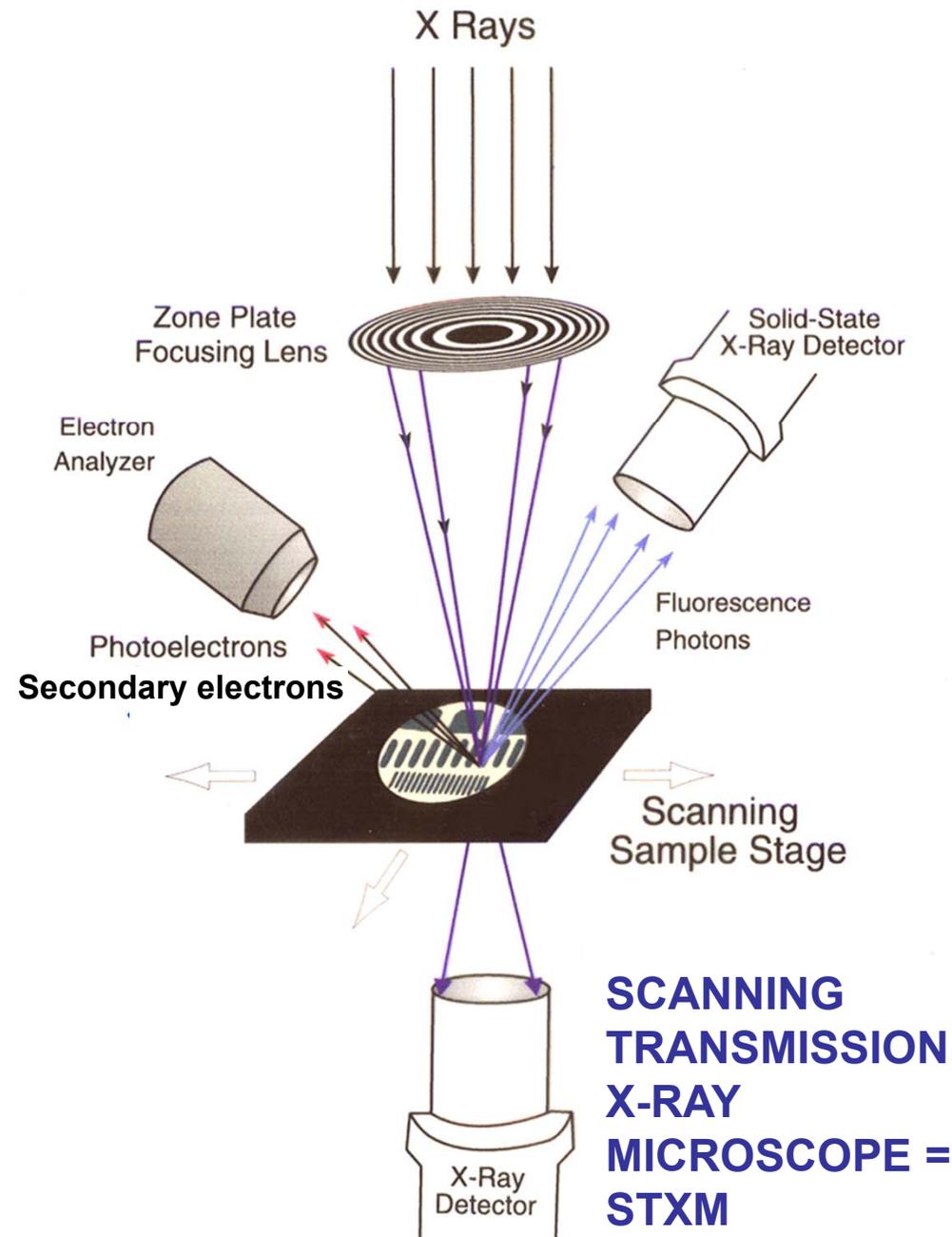
$$\text{NA} = \frac{\lambda}{2\Delta r_{\text{min}}}$$

$$\therefore \text{Res}_{|\text{coh}} = 1.22 \Delta r_{\text{min}}$$

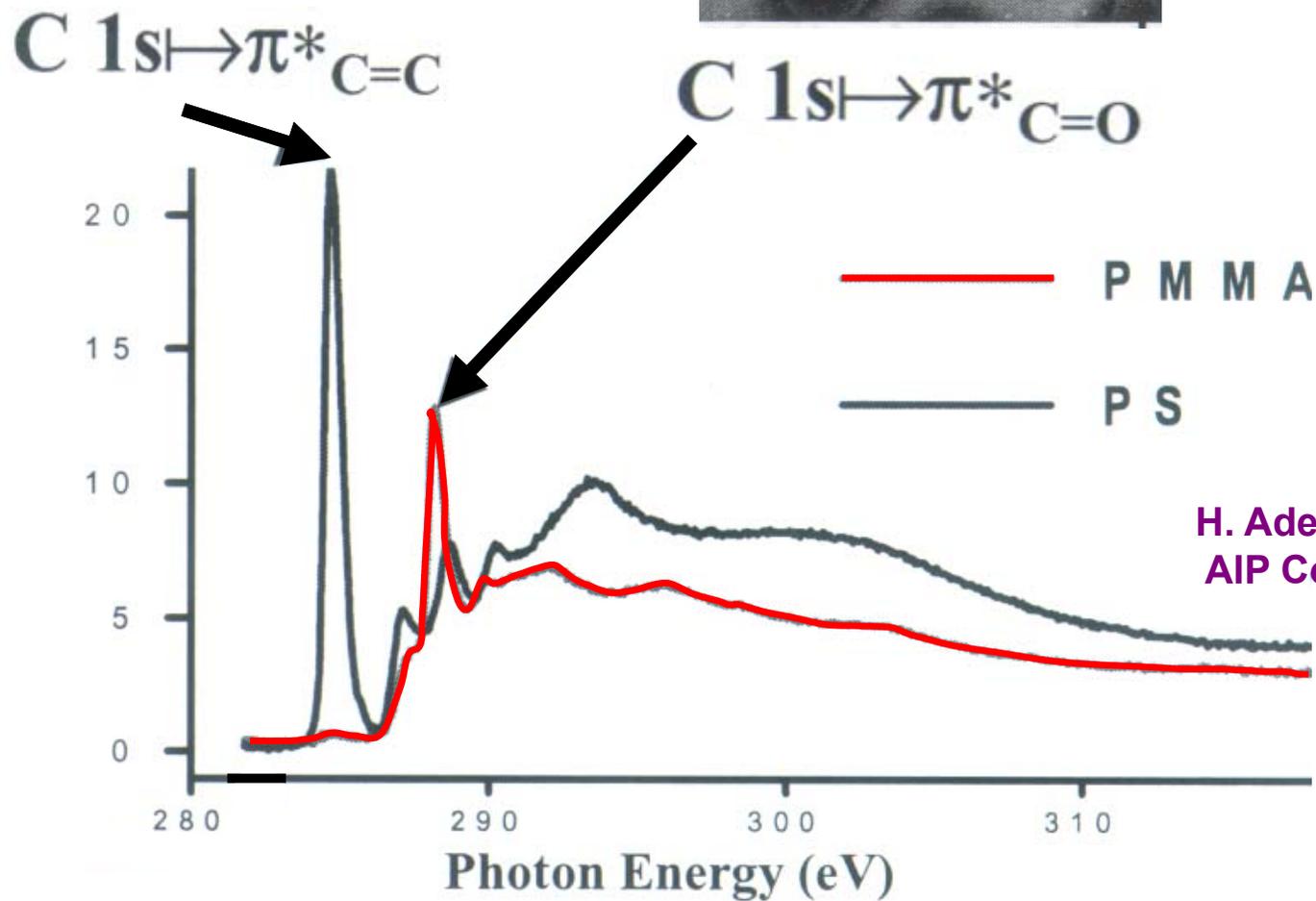
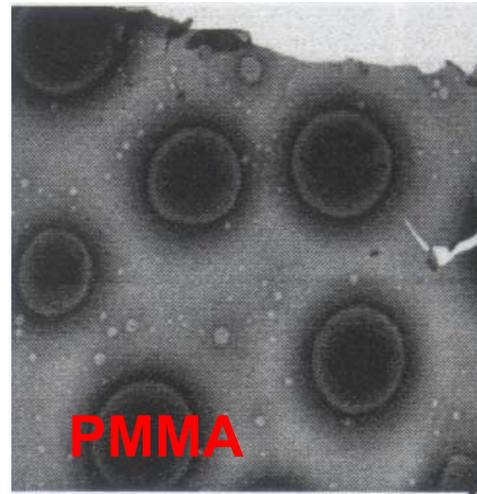
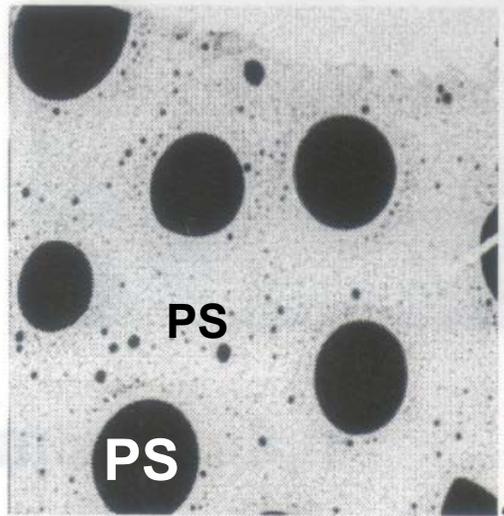
# Imaging with soft x-ray microscopes—three types

## 1. Scanning X-ray Microscopy

## 2. X-Ray Photoelectron Microscopy

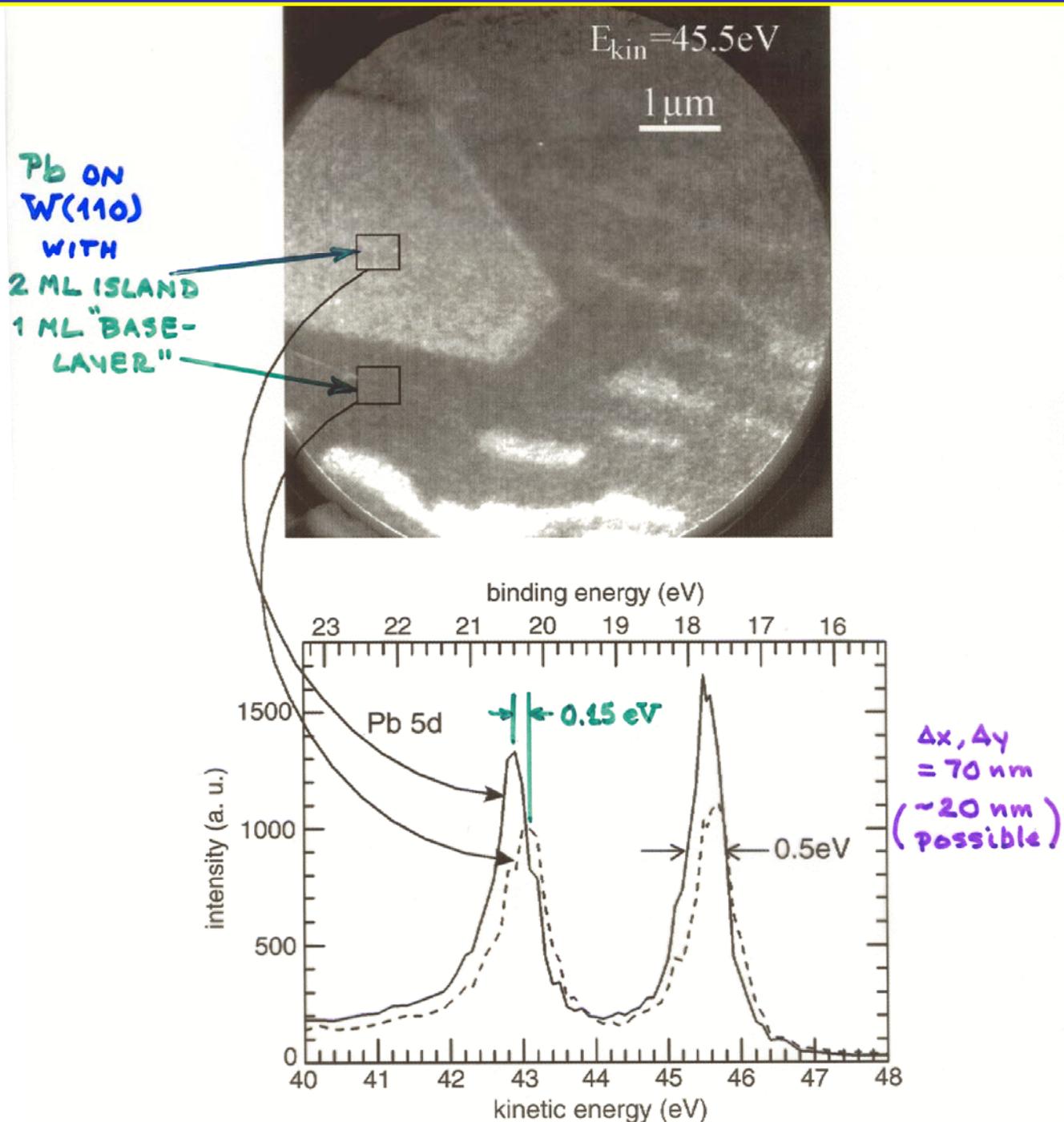


# SCANNING TRANSMISSION X-RAY MICROSCOPY OF POLYMER BLEND



H. Ade, X-ray Microscopy 99,  
AIP Conf. Proc. 507, p.197

# PHOTOELECTRON EMISSION MICROSCOPE (PEEM) USING PHOTOELECTRONS

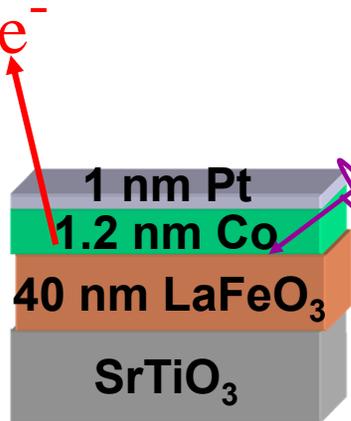
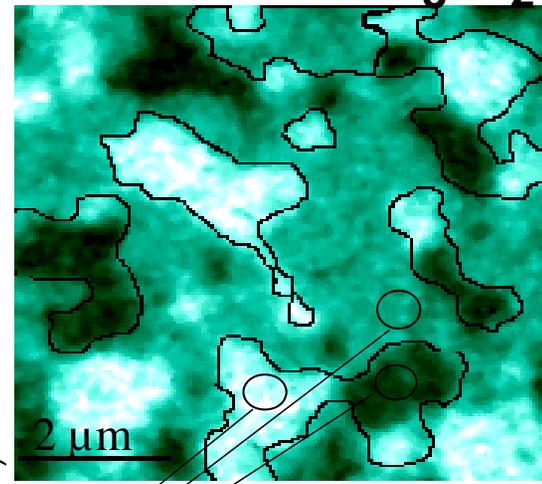
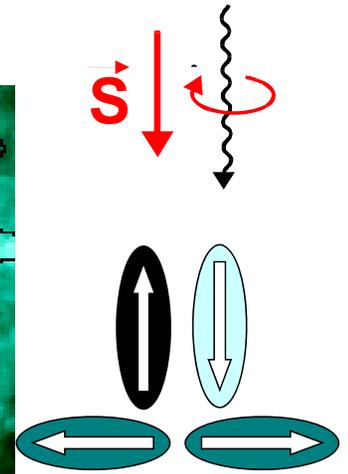
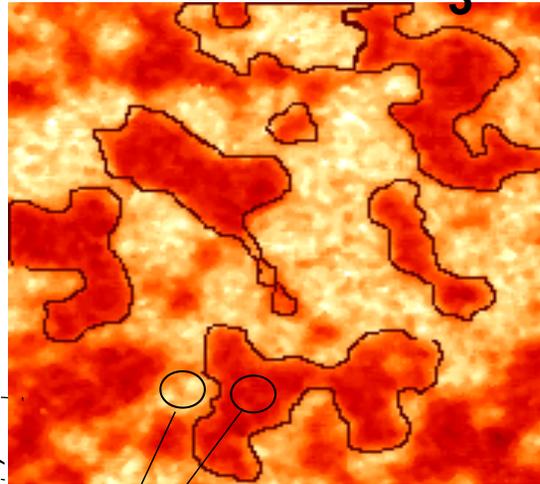
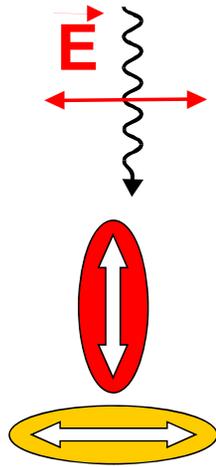


Sixth Int. Conf. On X-Ray Microscopy, (AIP Melville, New York, 2000) pp. 27-32

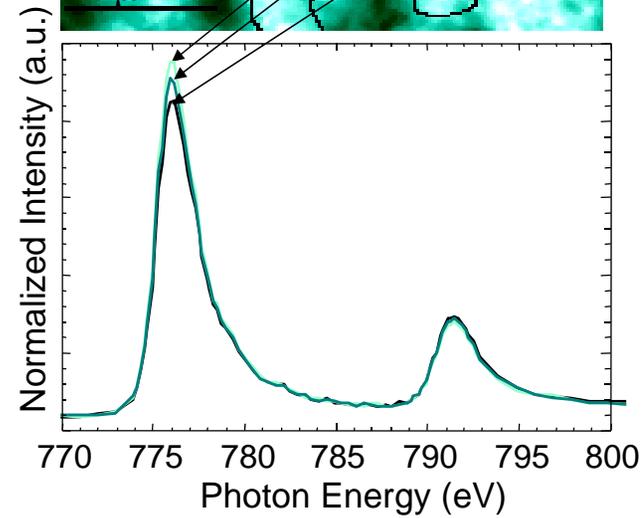
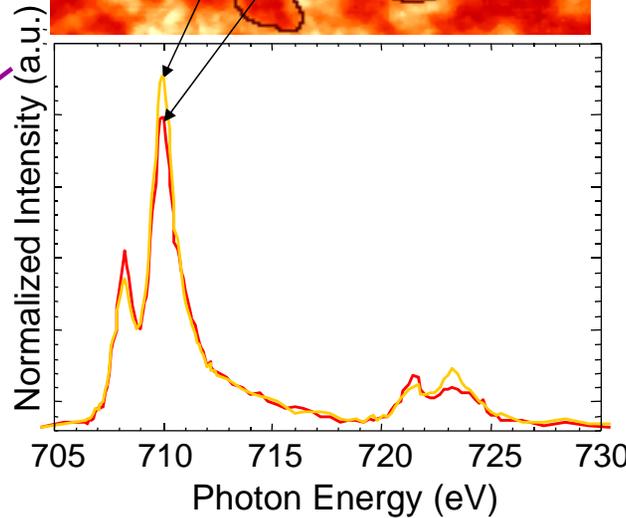
Schmidt et al. (ELETTRA)

**Antiferromagnetic**  
**LaFeO<sub>3</sub> layer**  
**XMLD Fe L<sub>3</sub>**

**Ferromagnetic**  
**Co layer**  
**XMCD Co L<sub>3</sub>/L<sub>2</sub>**

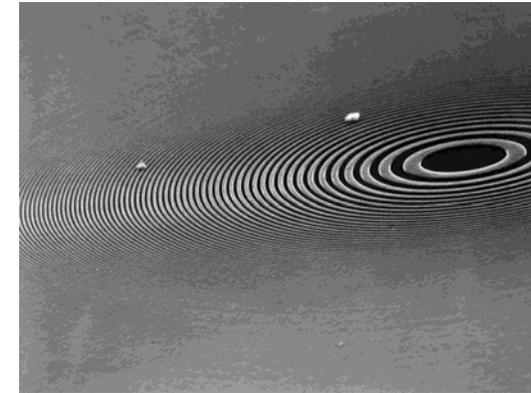
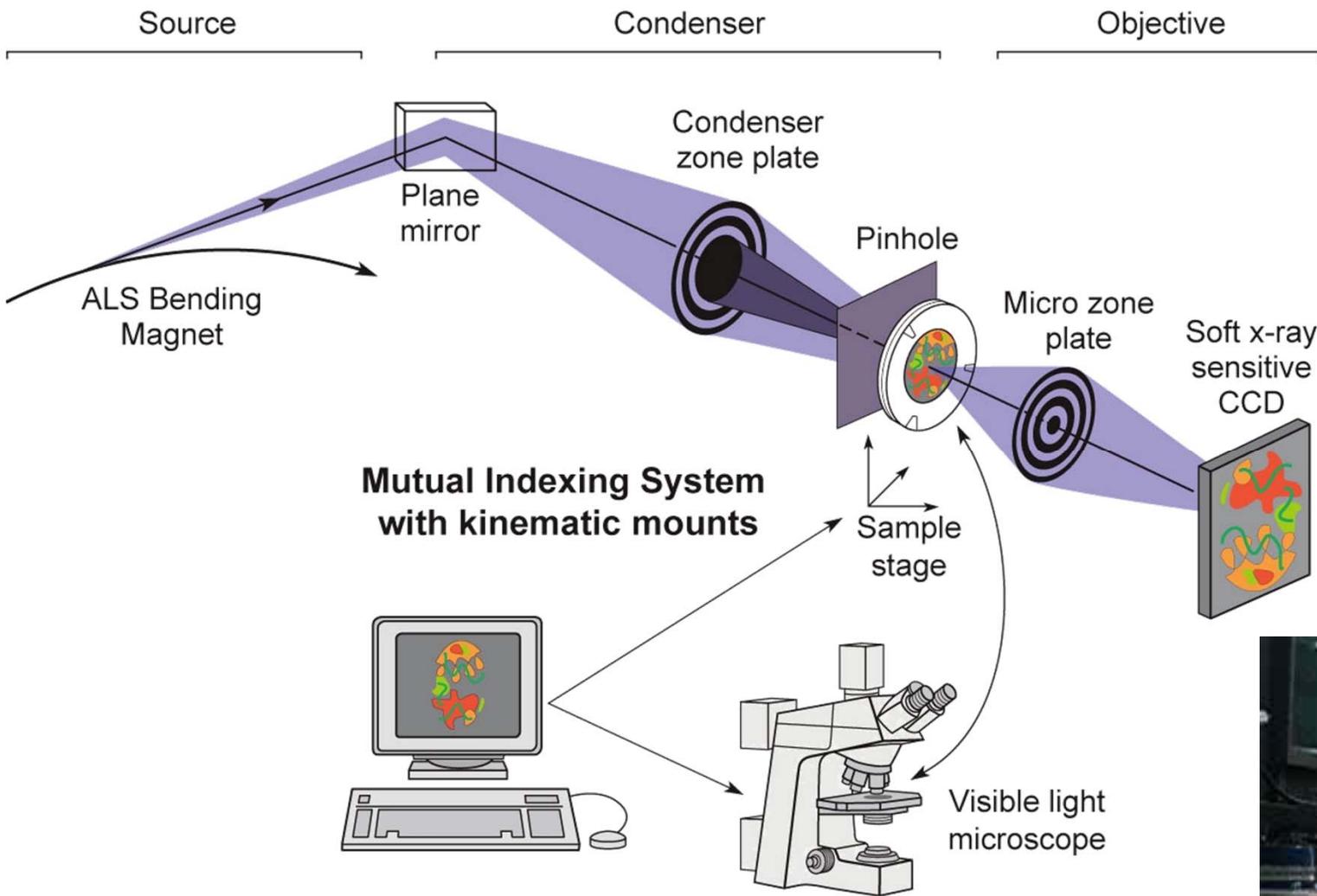


**As grown:**  
**bias not set**



**1:1 correlation of domain structure**

# Third type: Imaging Zone-Plate X-ray microscope: XM-1 @ ALS



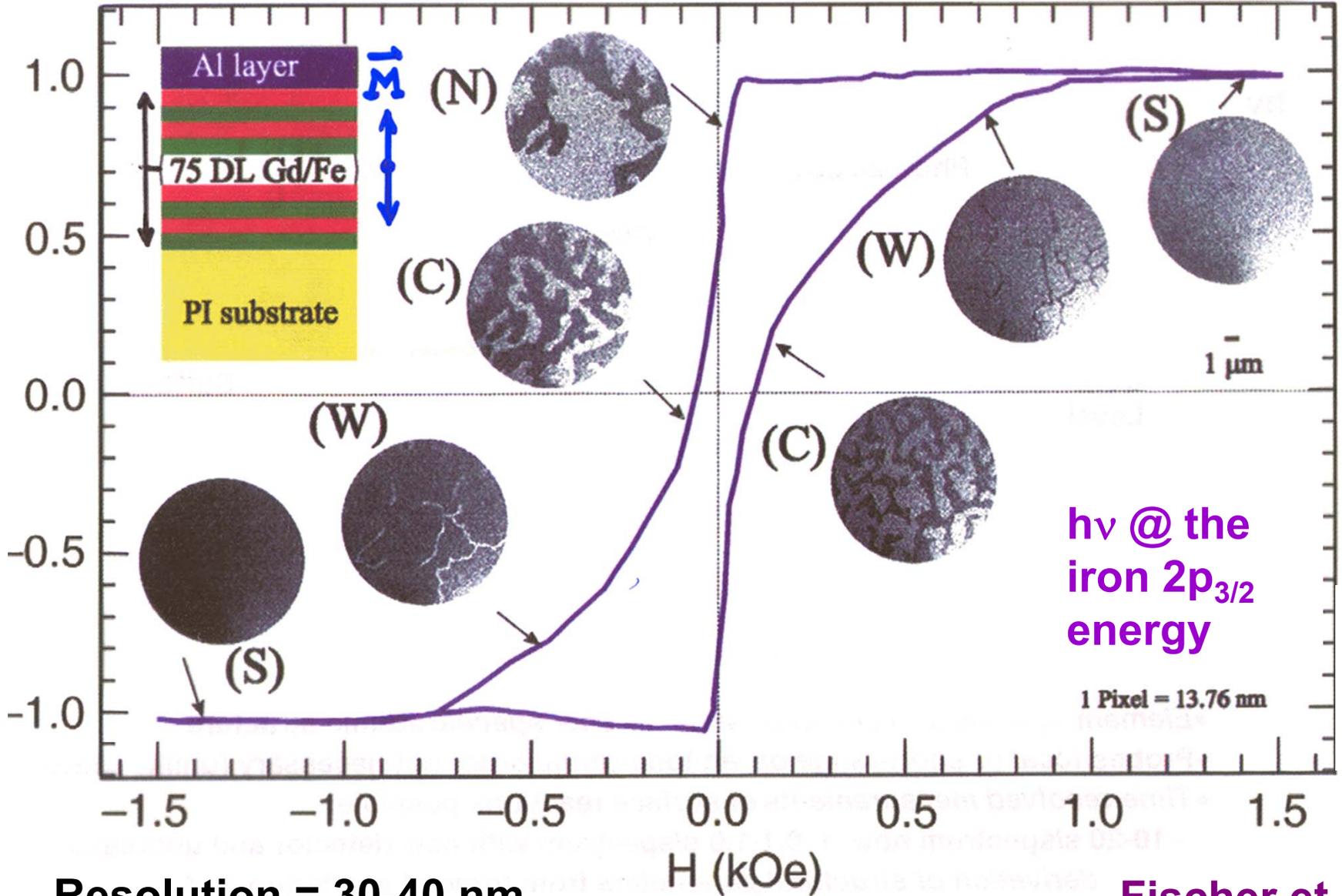
**X-ray lens = zone plate**  
**Outer rings 100 atoms apart**



Fischer et al.

# Imaging Iron Magnetic Domains with Circular-Polarized Light

Magnetization of the whole sample

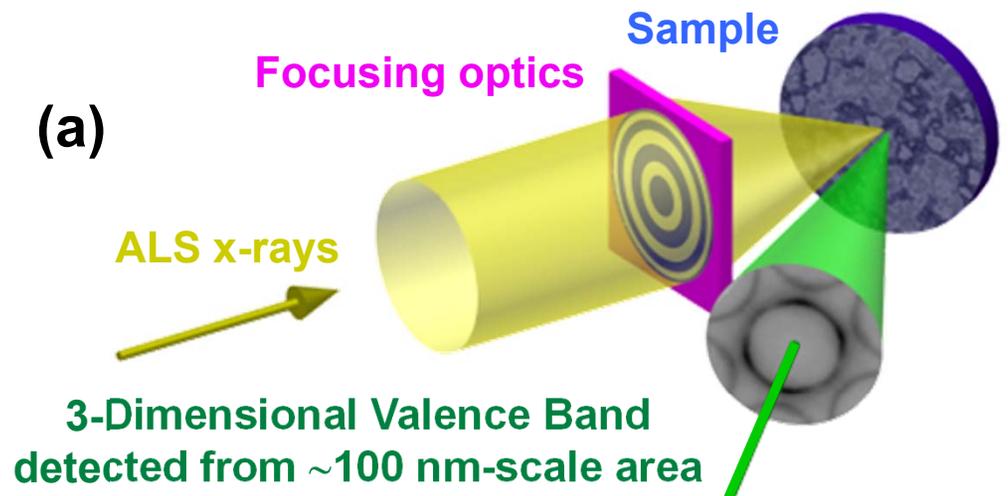


Resolution = 30-40 nm  
Now 15 nm → 10 nm

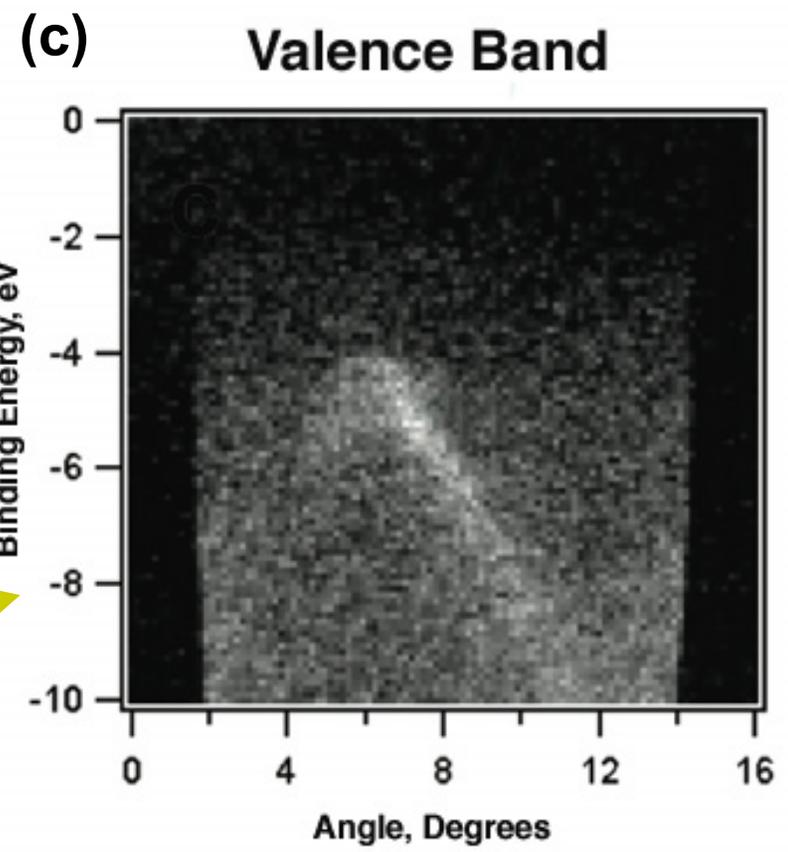
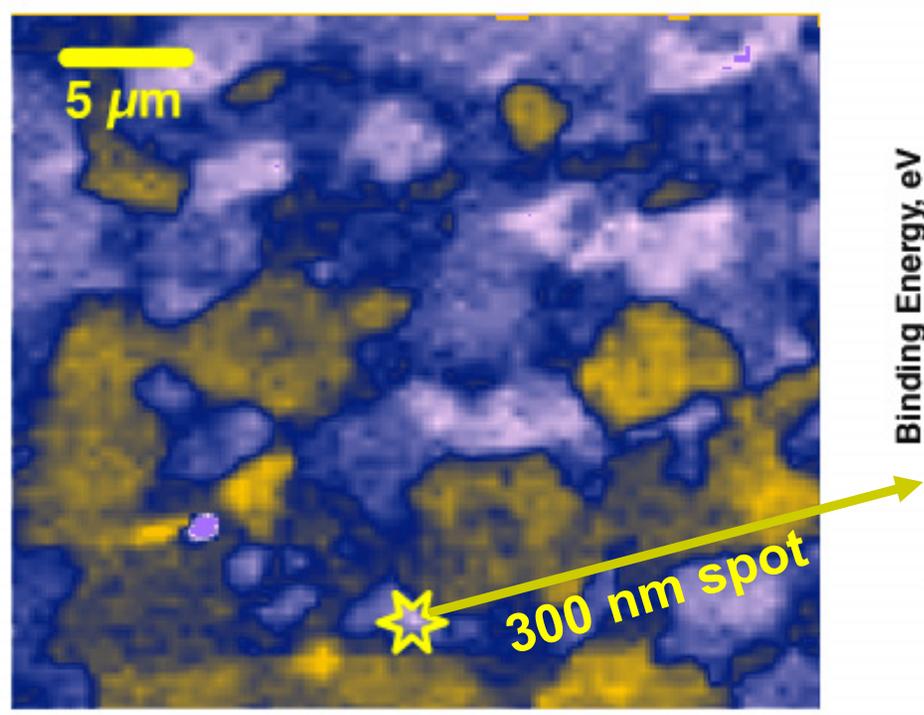
Magnetic Field

Fischer et al.

# Nanometer-Scale Angle-Resolved Photoemission



(b) HOPG Graphite Imaged with Valence Band Contrast



## Basic Concepts:

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## Core-Level Photoemission

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## Valence-Level Photoemission

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit-Covered already

## Some New Directions

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation-See seminar

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

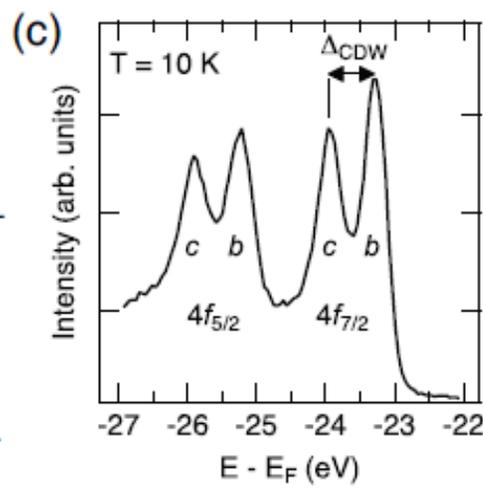
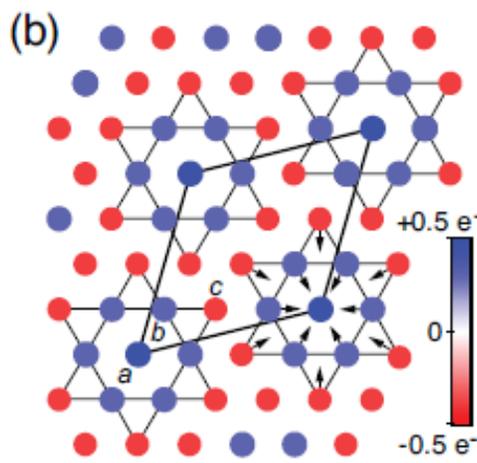
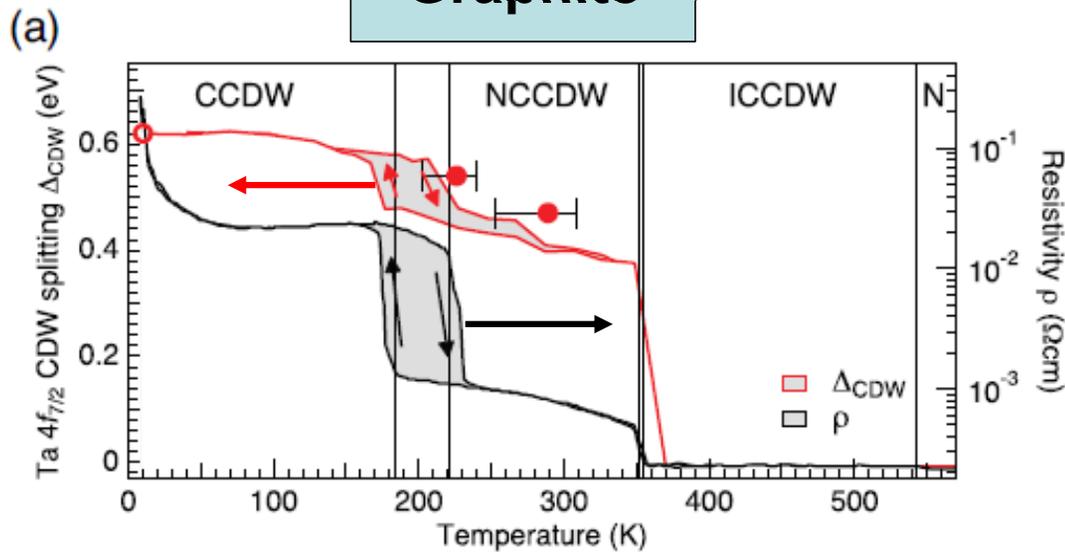


Temporal Resolution

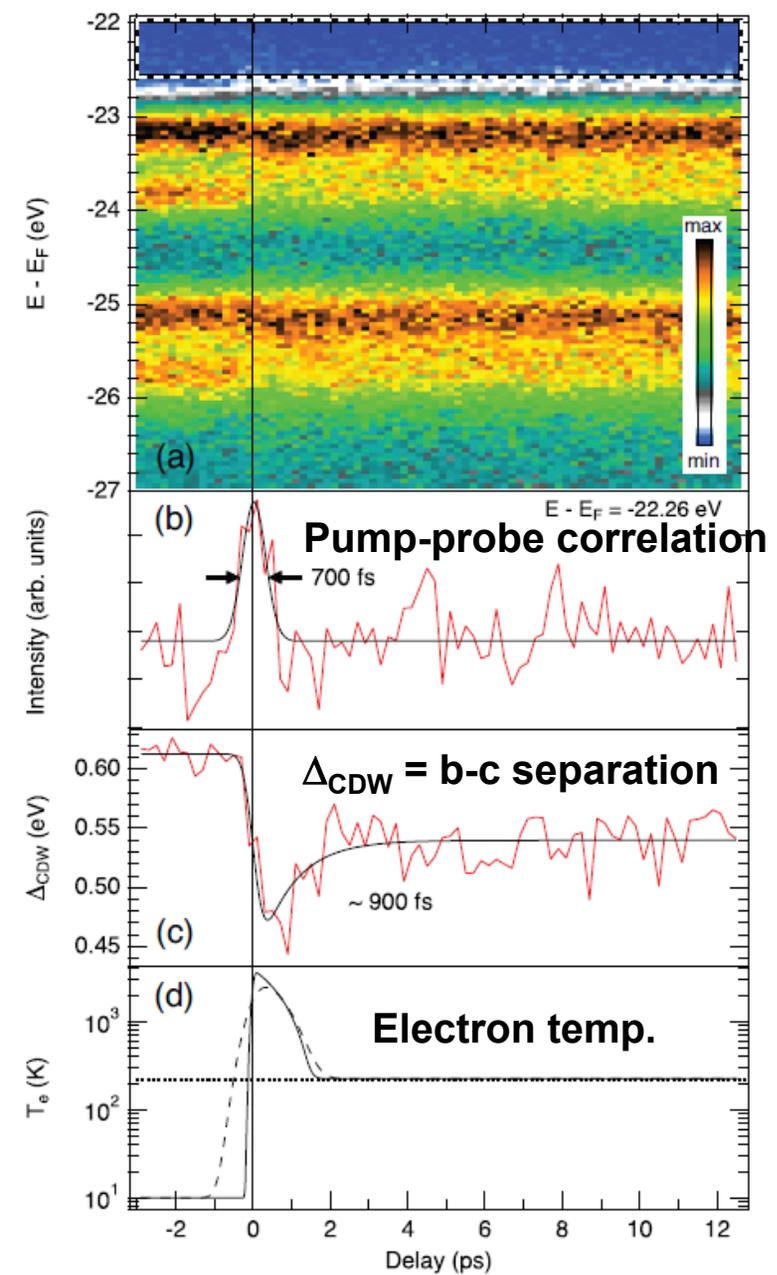
# Time-resolved core-level XPS as a monitor of a charge density wave in Mott insulator 1T-TaS<sub>2</sub>

Probe: 156 eV, 700 fs, FLASH FEL  
 Pump: 1.55 eV, 120 fs, laser

Graphite



~~a:b:c = 1:6:6~~



## **Basic Concepts:**

A Little Electronic Structure

The X-Ray-Based Experiments

X-Ray Sources, Synchrotron Radiation, Free Electron Lasers

## **Core-Level Photoemission**

Intensities and Quantitative Analysis, the 3-Step Model

Varying Surface and Bulk Sensitivity

Chemical Shifts

Multiplet Splittings

Electron Screening and Satellite Structure

Magnetic and Non-Magnetic Dichroism

Resonant Photoemission

Photoelectron Diffraction and Holography

## **Valence-Level Photoemission**

Band-Mapping in the Ultraviolet Photoemission Limit

Densities of States in the X-Ray Photoemission Limit

## **Some New Directions**

Photoemission with Hard X-Rays (throughout lectures)

Photoemission with Standing Wave Excitation-**See seminar**

Photoemission with: Higher Pressures → multi-Torr → Atmosphere?

Spatial Resolution-Photoelectron Microscopy

Temporal Resolution

