

# Outline

**Surface, interface, and nanoscience—short introduction**

**Some surface concepts and techniques→why photoemission?**

**Synchrotron radiation: experimental aspects**

**Electronic structure—a brief review**

**The basic synchrotron radiation techniques: more details**

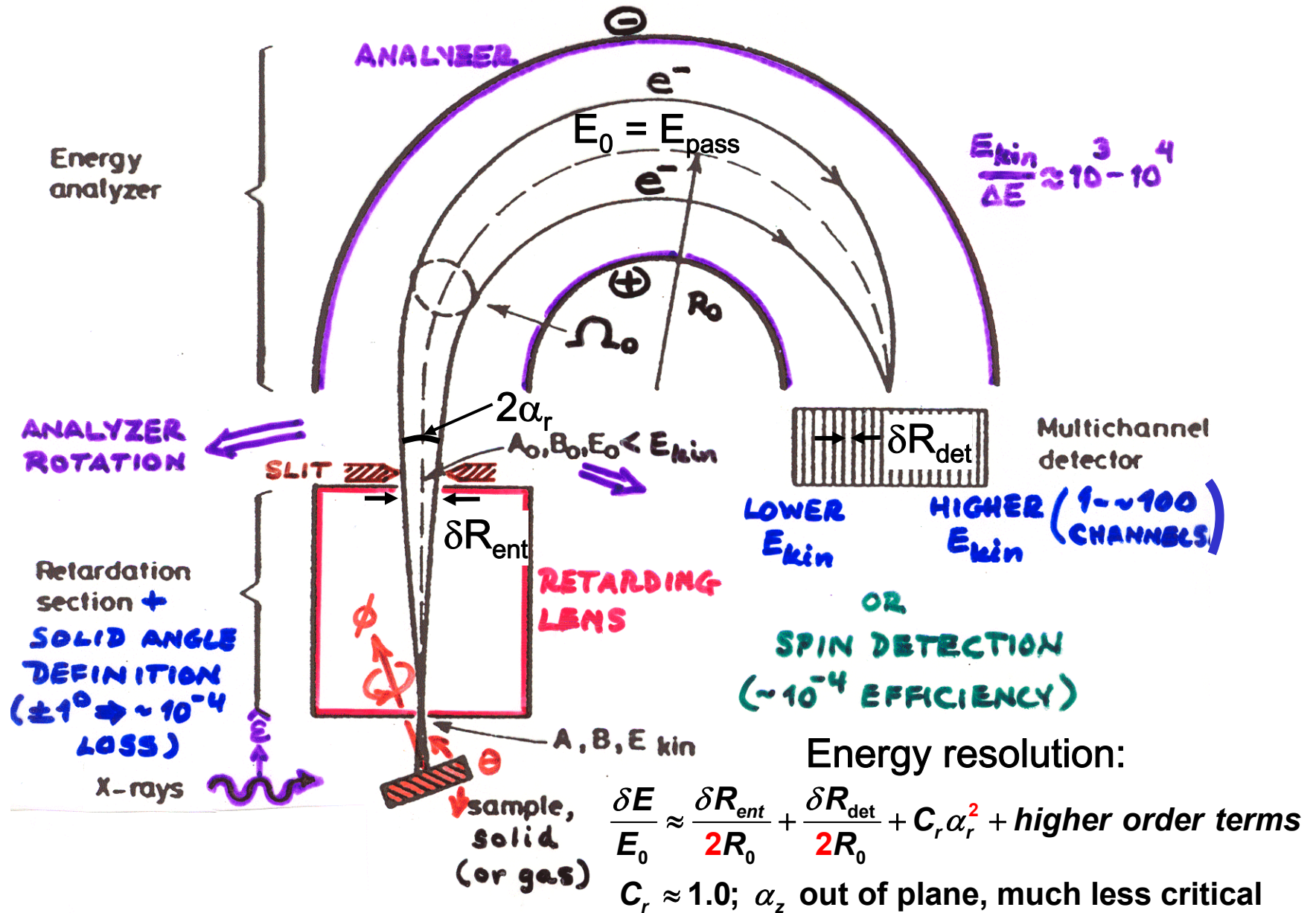
 **--Instrumentation for PS**

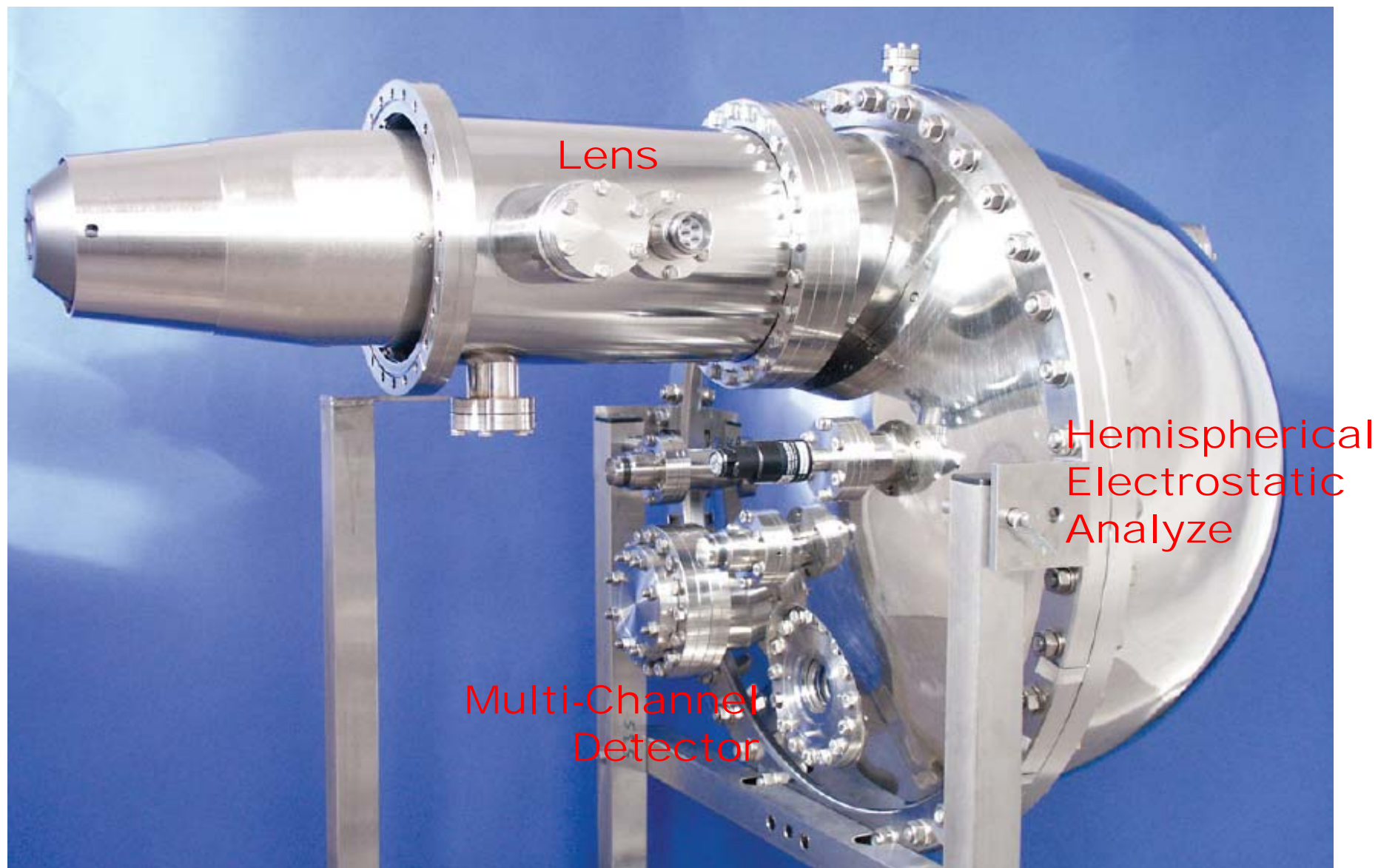
**Core-level photoemission**

**Valence-level photoemission**

**Microscopy with photoemission**

# Electron Spectroscopy—A typical configuration



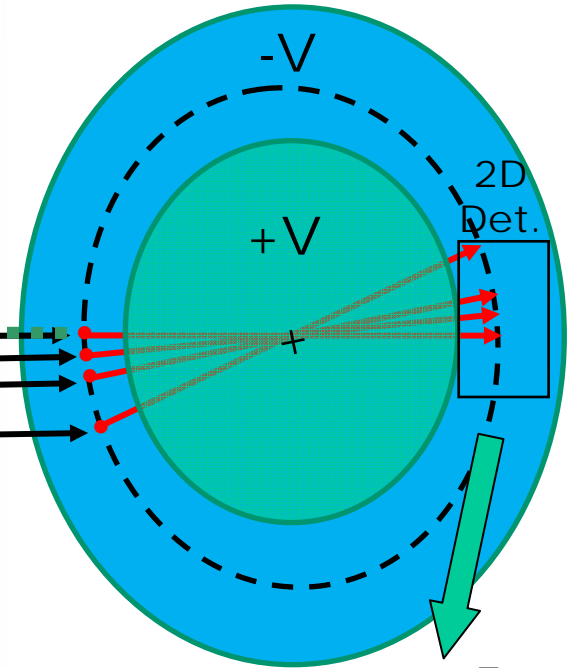
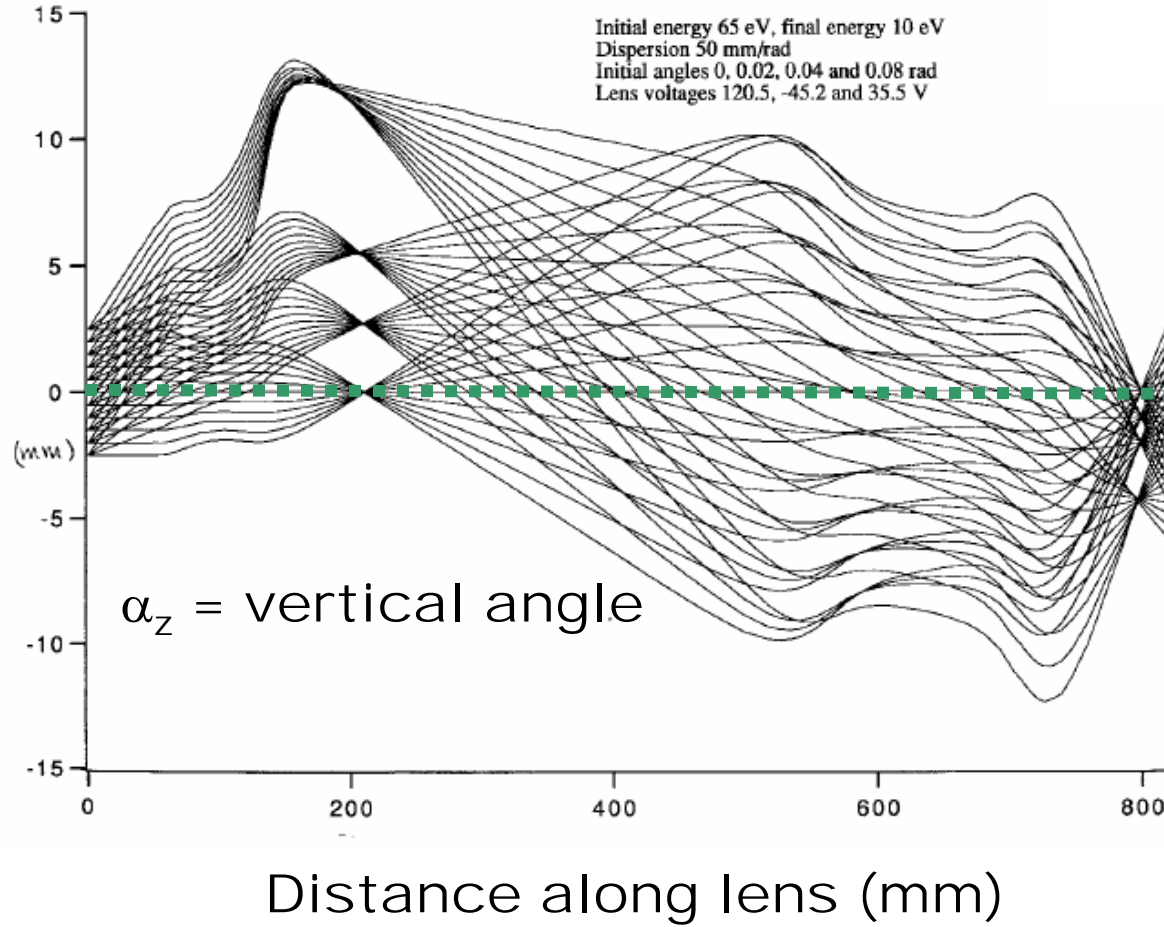


Nilsson et al., *Journal of Electron Spectroscopy and Related Phenomena* 70 (1994) 117-128

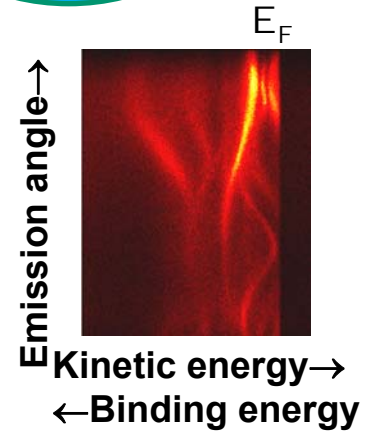
The Scienta R4000  
(plus SPECS, MBS)

With proper lens imaging in vertical angle-  
 an energy vs angle image at detector

Distance from sample center (mm)

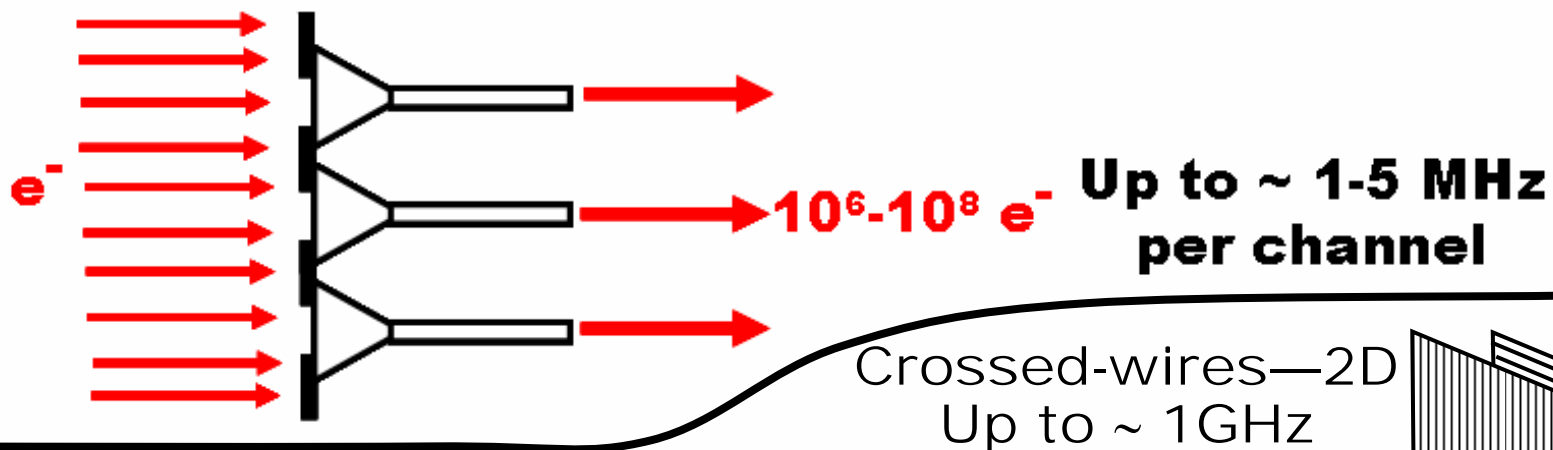


First Scienta, now others

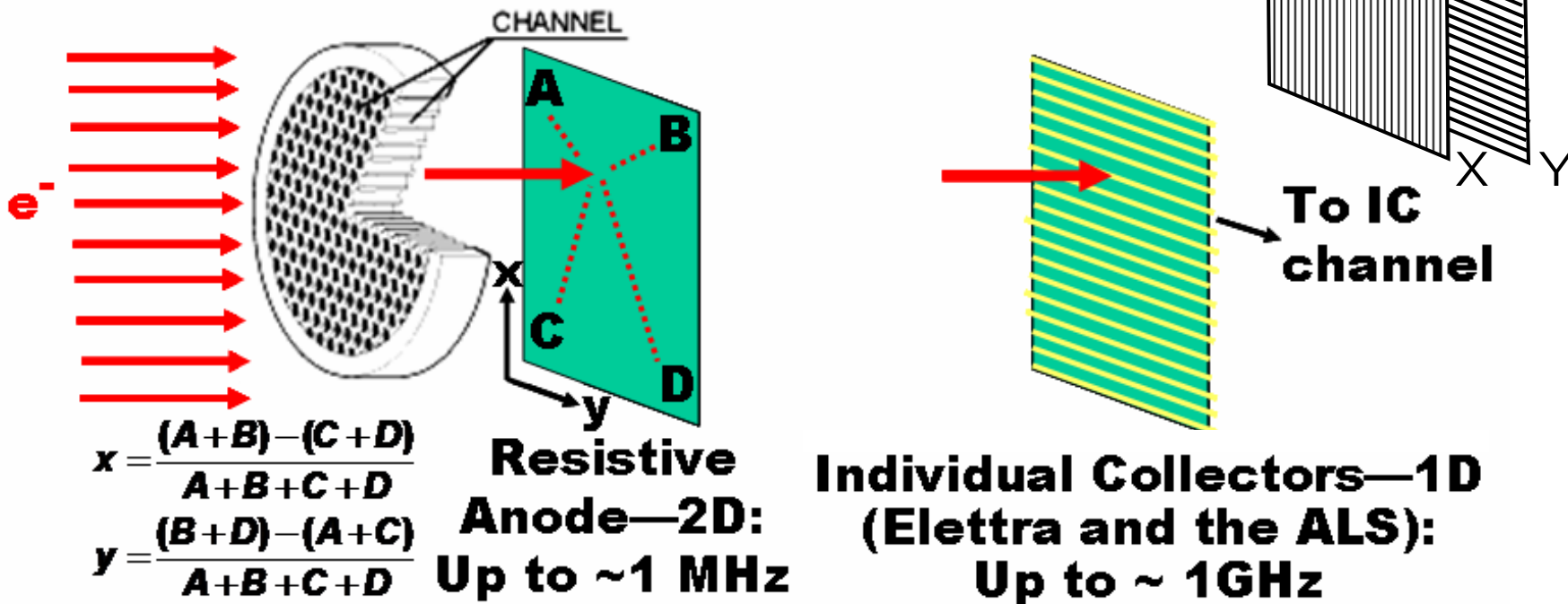


# MULTICHANNEL DETECTION GEOMETRIES

## Multiple channeltrons: brute force

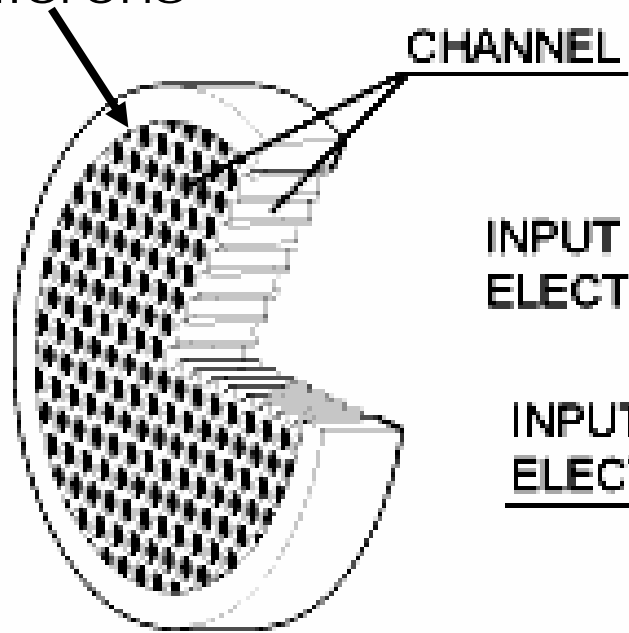


## Microchannel plates (MCPs) and

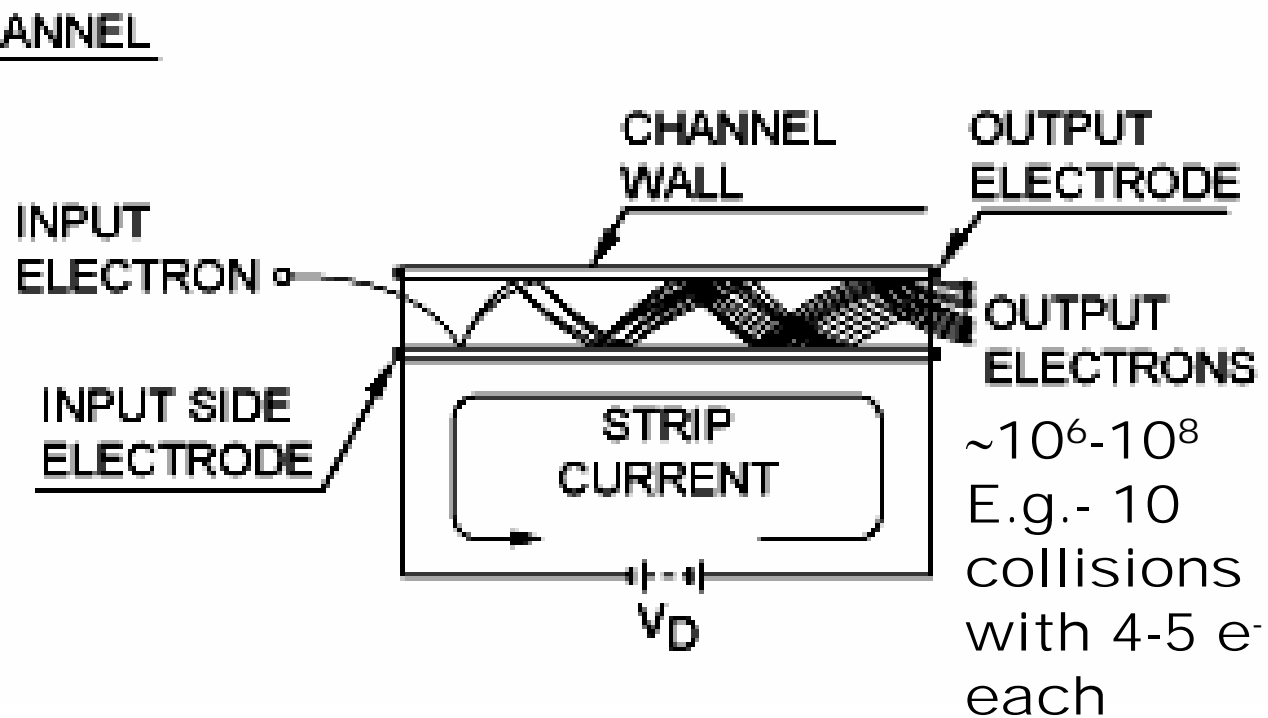


# The Microchannel Plate Electron (and Photon) Multiplier

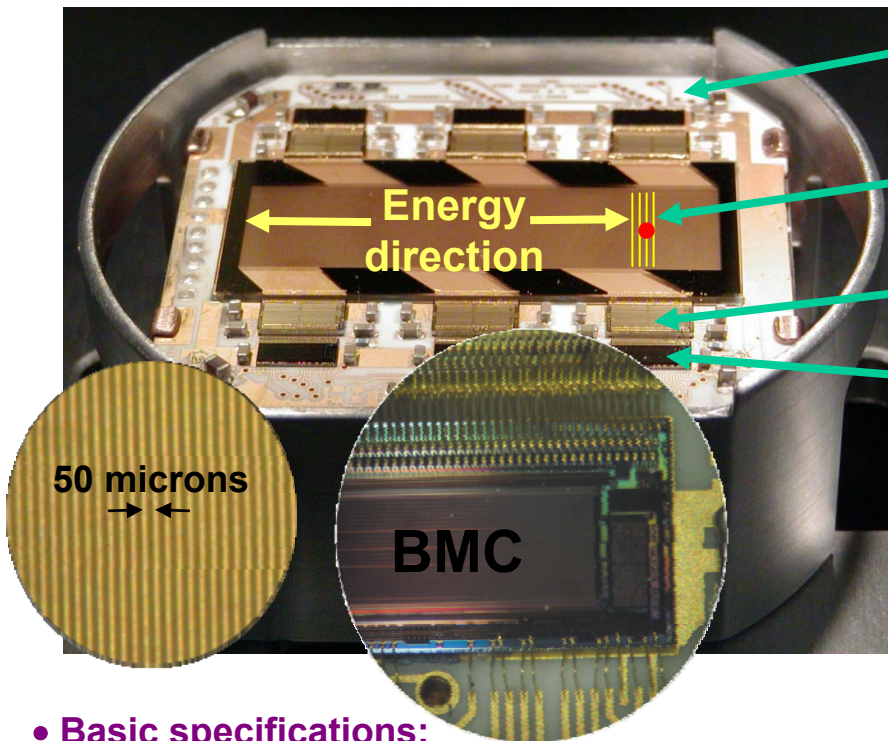
Diam.  
Down to 5  
microns



Pb-DOPED GLASS



# Next Generation Detection: ALS High-Speed Detector—1D



Ceramic substrate

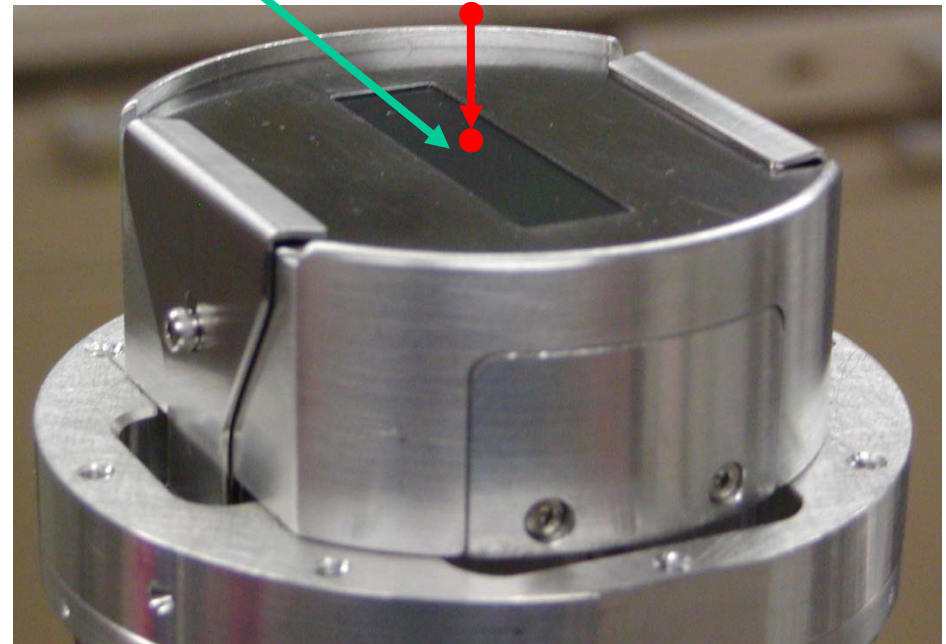
768 collector strips

Amplifier/discriminator chip (CAFE-M) from HEP

Buffered multichannel counter chip (BMC)

Microchannel plates

$e^-$  or  $h\nu$



- **Basic specifications:**

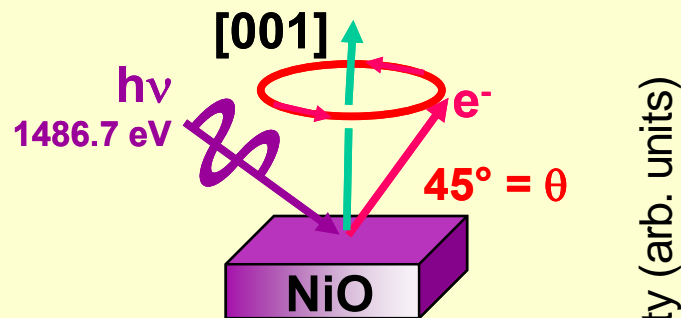
- 768 channels along one dimension
- ~75 micron spatial resolution
- >2 GHz overall linear count-rate→  
**100-1000x faster than present**
- spectral readout in as little as 200  $\mu$ s→  
**time-resolved measurements**
- programmable, robust

- Operating since July, 2003, final improvements underway: HV insulation, memory buffering

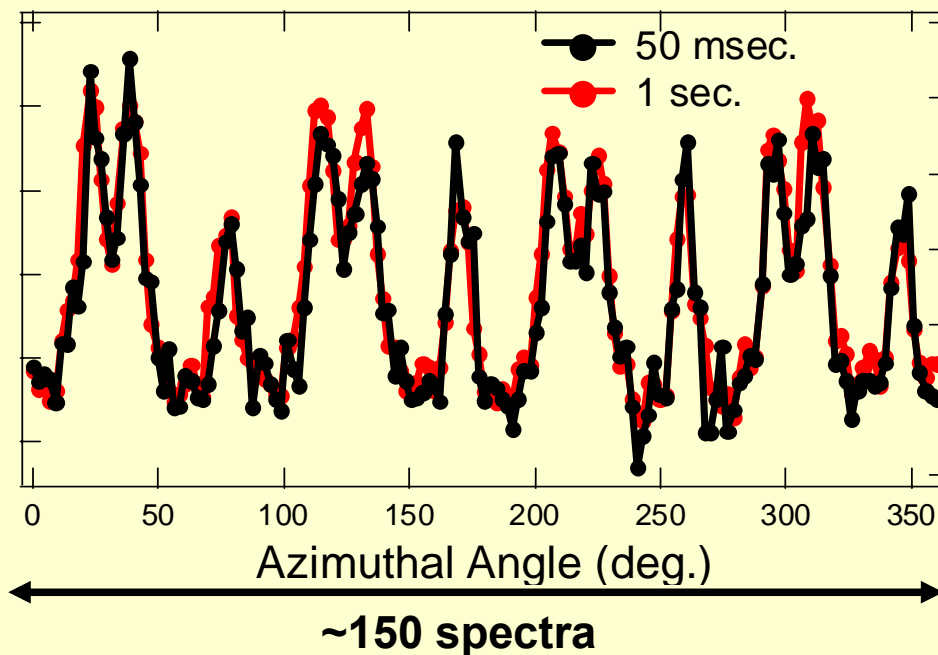
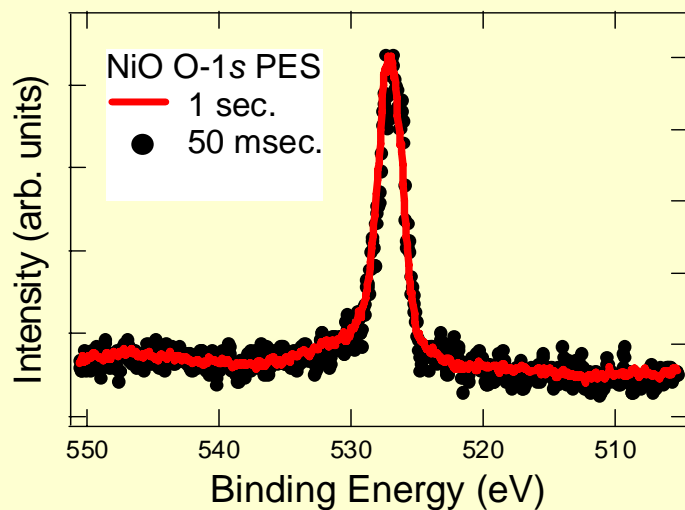
- Reinstallation for fulltime usage: 2008-09

# ALS High-Speed Detector: Some First Data in 2004

## Photoelectron Diffraction from NiO(001)



O 1s Spectrum



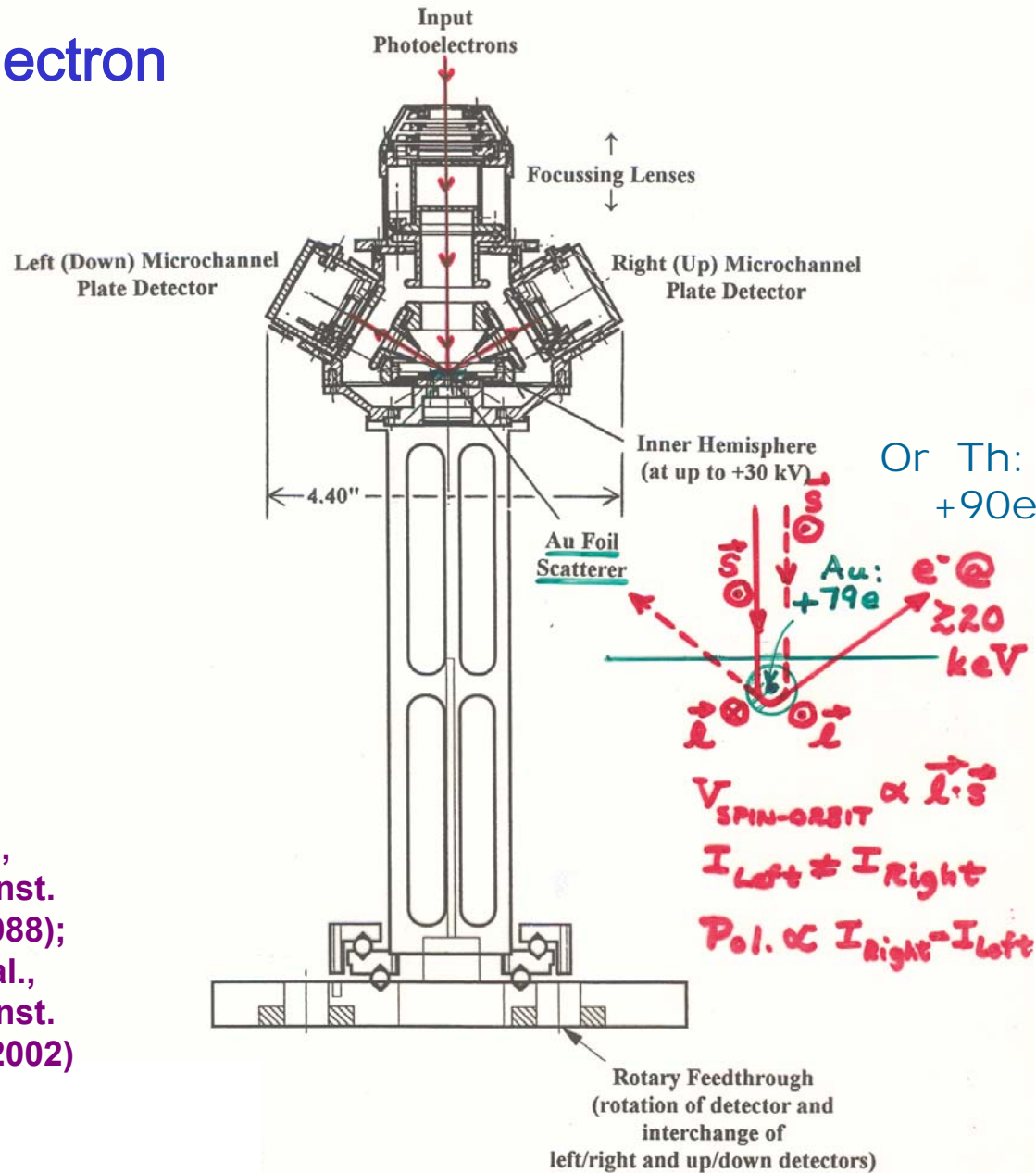
**Total 2 min. @ 50 msec/spectrum  
→ 7 sec. without CPU  
process time.  
With future data buffering:  
→ 30 ms total @ 200 μs/spectrum**

**To be reinstalled for permanent use in 2008-2009**



**MICROMOTT DETECTOR**  
(LBNL/Florida State Univ./UC Davis)

The MicroMott Electron Spin Detector



Tang et al.,  
Rev. Sci. Inst.  
59, 504 (1988);  
Huang et al.,  
Rev. Sci. Inst.  
73, 3778 (2002)

Light from ALS  
elliptically polarized  
undulator (80-1500 eV)

New refocussing  
mirror (August '07)

# Multi-Technique Spectrometer/ Diffractometer (Soft X-Ray/XUV)

5-axis sample  
manipulator:

New ultralow  
temp, ~6 K  
(June '07)

LHe

Sample prep.  
chamber: LEED,  
Knudsen cells, QCM,  
electromagnet,...

Permits using all  
relevant soft x-ray  
spectroscopies  
on a single  
sample: PS, PD,  
PH; XAS (e<sup>-</sup> or  
photon  
detection),  
XES/REXS/RIXS,  
with MCD, MLD

Loadlock  
for sample  
introduction

Diff.  
seal

X-ray  
tube

Electron  
spectrometer:  
Scienta SES "2002"

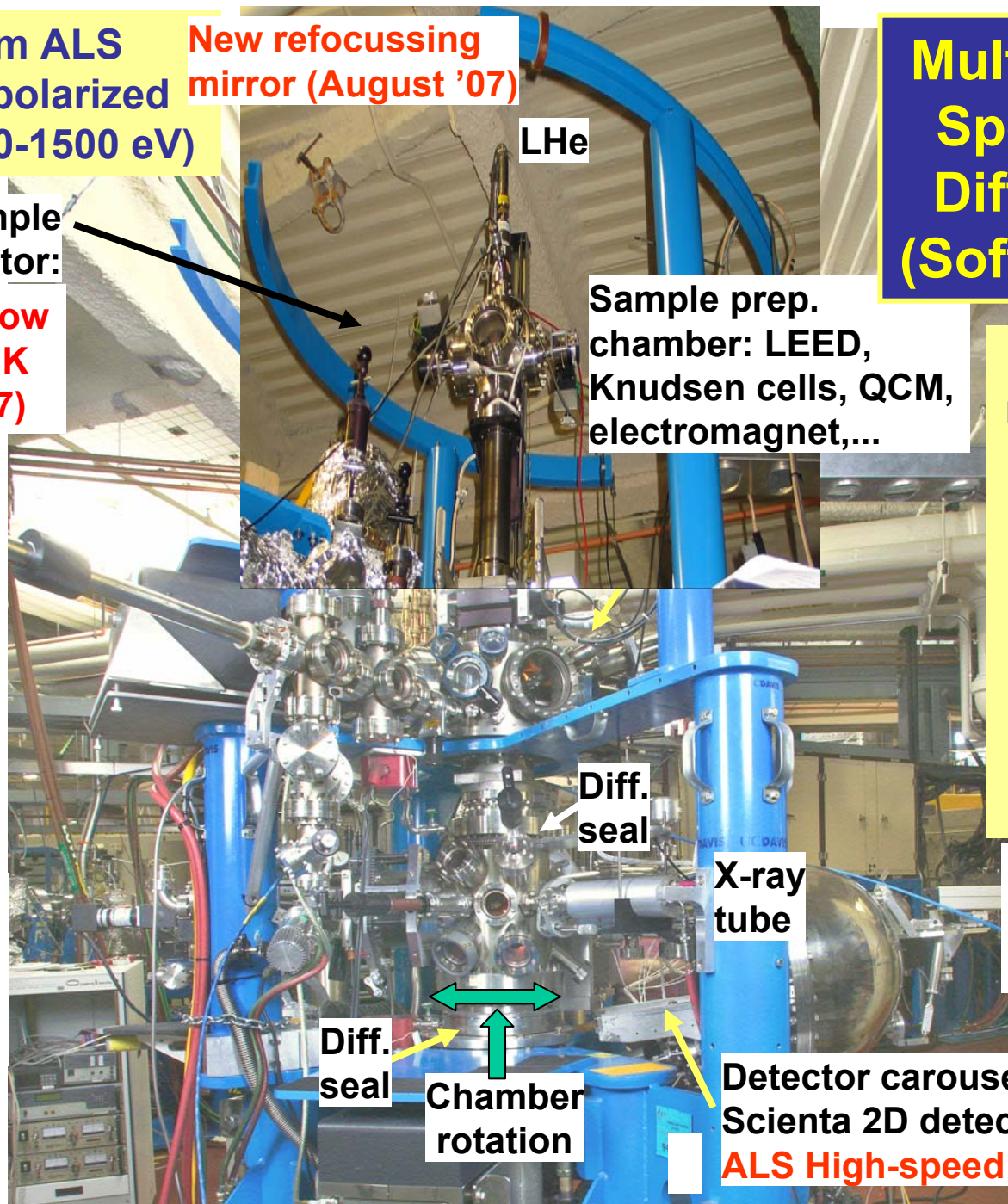
Soft x-ray  
spectrometer:  
Scienta  
XES 300

Diff.  
seal

Chamber  
rotation

Detector carousel:  
Scienta 2D detection—ARPES

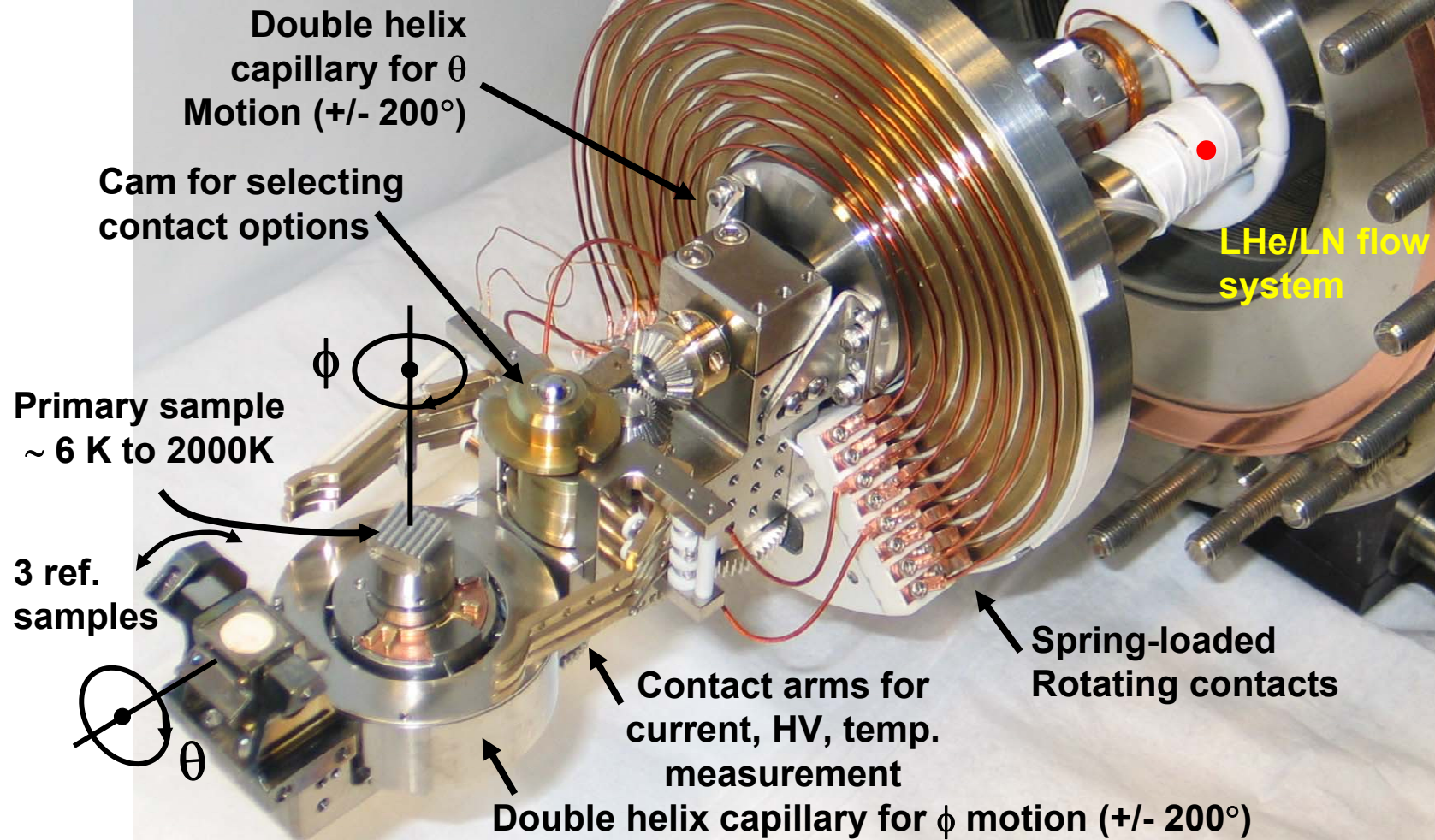
ALS High-speed 1D detector ('07-'08)



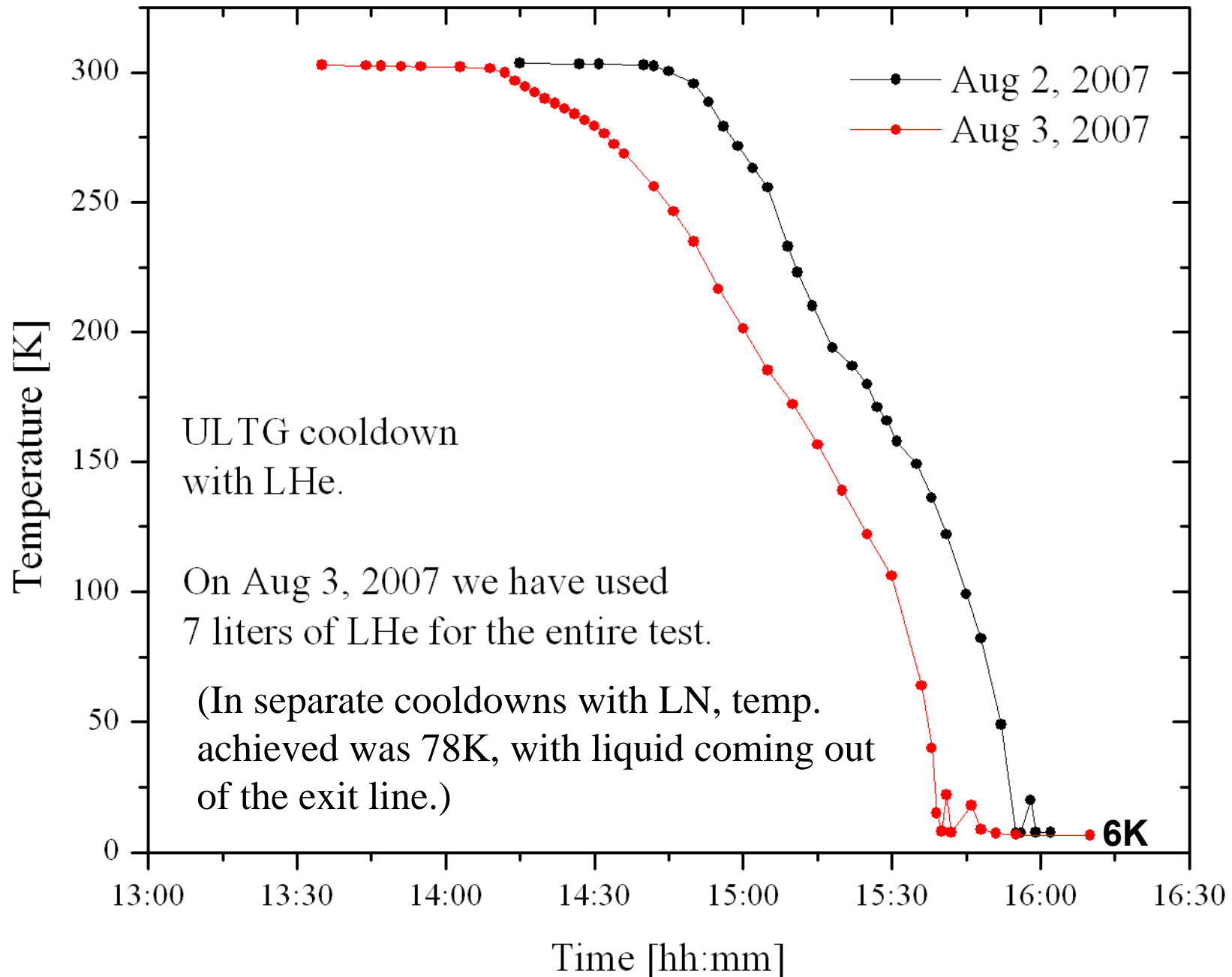
**Ultralow Temperature Goniometer  
Fadley Group**

**UC Davis: J. Thomson, D. Hemer,  
B.C. Sell**

**LBL: M.W. West, L. Plucinski,  
M. Malvestuto, I. Preda, M. Press**



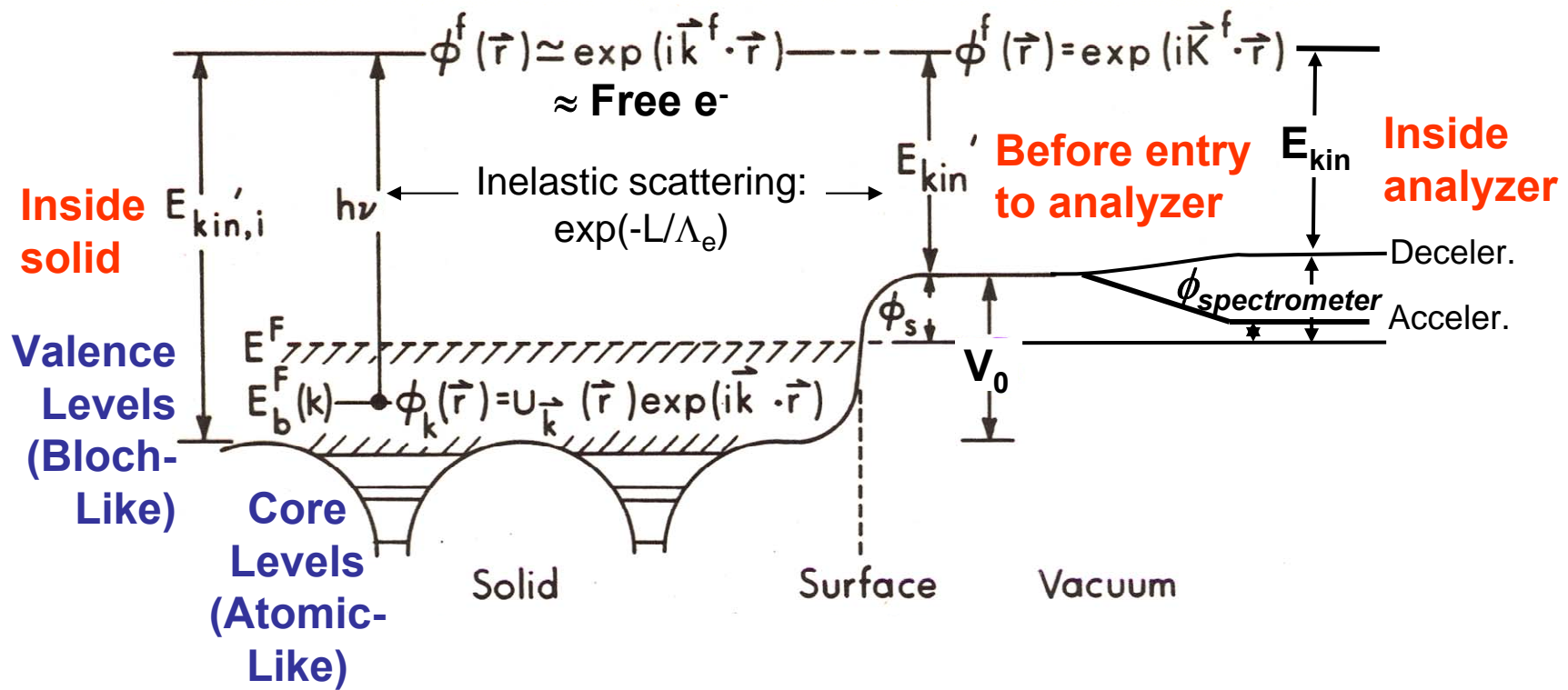
# FIRST COOLDOWN tests, temp. read with Si diode in contact with Cu cryogen reservoir just under sample



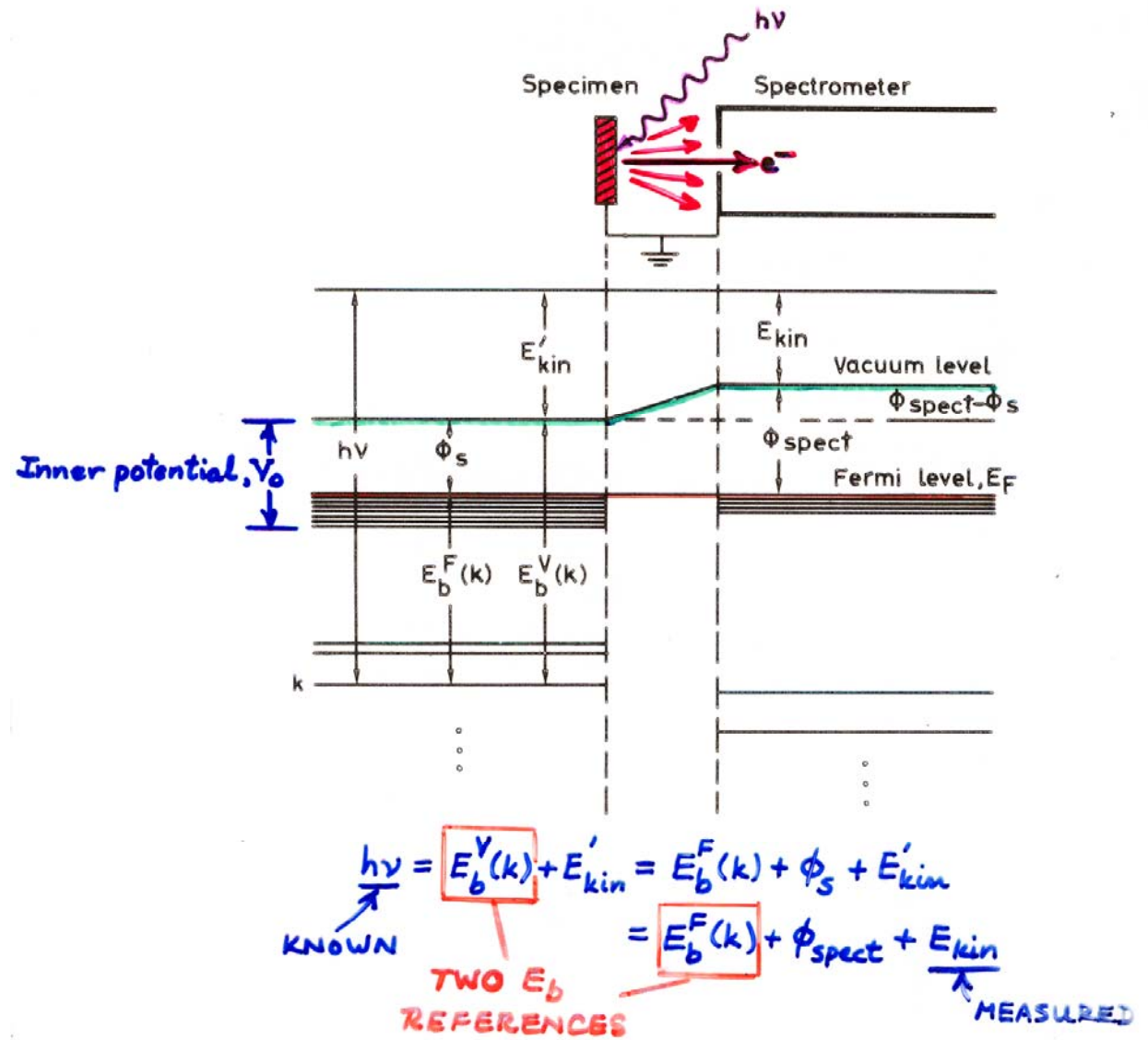
# Measuring Electron Binding Energies: Basic energetics

$$h\nu = E_{\text{binding}}^{\text{Vacuum}} + E_{\text{kinetic}} = E_{\text{binding}}^{\text{Fermi}} + \phi_{\text{spectrometer}} + E_{\text{kinetic}}$$

## One-Electron Picture of Photoemission from a Surface

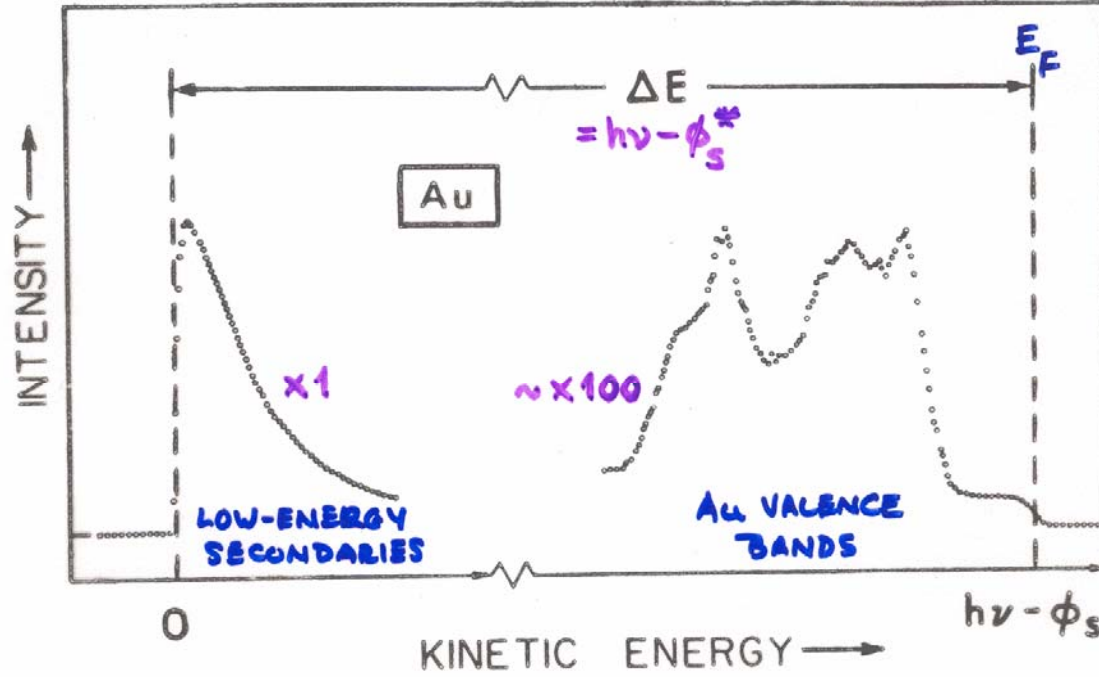


# Measuring Electron Binding Energies



“Basic Concepts of XPS”  
Figure 3

Figure 3 -- Energy level diagram for a metallic specimen in electrical equilibrium with an electron spectrometer. The closely spaced levels near the Fermi level  $E_F$  represent the filled portions of the valence bands in specimen and spectrometer. The deeper levels are core levels. An analogous diagram also applies to semiconducting or insulating specimens, with the only difference being that  $E_F$  lies somewhere between the filled valence bands and the empty conduction bands above.



\* PROVIDED  $\phi_s > \phi_{\text{spect}}$  OR,  
 IF  $\phi_s < \phi_{\text{spect}}$ , SAMPLE  
 BIASED NEGATIVELY BY  
 $V_{\text{BIAS}} > \phi_{\text{spect}} - \phi_s$   
 (-)

Figure 4 -- Full XPS spectral scan for a polycrystalline Au specimen, showing both the cutoff of the secondary electron peak at zero kinetic energy and the high-energy cutoff for emission from levels at the metal Fermi level. The measurable distance  $\Delta E$  thus equals  $h\nu - \phi_s$ , provided that suitable specimen biasing has been utilized. For this case,  $h\nu$  was 1253.6 eV and  $\phi_s$  was 5.1 eV. (From Baer, reference 56).

“Basic Concepts of XPS”  
 Figure 3

## Work functions of the Elements [eV]

After L. Ley and M. Cardona,  
"Photoemission in Solids", Springer 1979

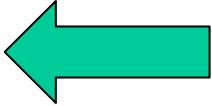
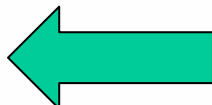
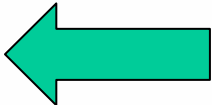
1 <b>H</b> -																	2 <b>He</b> -
3 <b>Li</b> 2.4	4 <b>Be</b> 1.5											5 <b>B</b> 4.5	6 <b>C</b> 4.7	7 <b>N</b> -	8 <b>O</b> -	9 <b>F</b> -	10 <b>Ne</b> -
11 <b>Na</b> 2.35	12 <b>Mg</b> 3.6											13 <b>Al</b> 4.25	14 <b>Si</b> 4.8	15 <b>P</b> -	16 <b>S</b> -	17 <b>Cl</b> -	18 <b>Ar</b> -
19 <b>K</b> 2.2	20 <b>Ca</b> 2.8	21 <b>Sc</b> 3.3	22 <b>Ti</b> 3.95	23 <b>V</b> 4.1	24 <b>Cr</b> 4.6	25 <b>Mn</b> 3.8	26 <b>Fe</b> 4.3	27 <b>Co</b> 4.4	28 <b>Ni</b> 4.5	29 <b>Cu</b> 4.4	30 <b>Zn</b> 4.2	31 <b>Ga</b> 4.0	32 <b>Ge</b> 4.8	33 <b>As</b> 5.1	34 <b>Se</b> 4.7	35 <b>Br</b> -	36 <b>Kr</b> -
37 <b>Rb</b> 2.2	38 <b>Sr</b> 2.35	39 <b>Y</b> 3.3	40 <b>Zr</b> 3.9	41 <b>Nb</b> 4.0	42 <b>Mo</b> 4.3	43 <b>Tc</b> -	44 <b>Ru</b> 4.6	45 <b>Rh</b> 4.75	46 <b>Pd</b> 4.8	47 <b>Ag</b> 4.3	48 <b>Cd</b> 4.1	49 <b>In</b> 3.8	50 <b>Sn</b> 4.4	51 <b>Sb</b> 4.1	52 <b>Te</b> 4.7	53 <b>I</b> -	54 <b>Xe</b> -
55 <b>Cs</b> 1.8	56 <b>Ba</b> 2.5	57 <b>La</b> 3.3	72 <b>Hf</b> 3.5	73 <b>Ta</b> 4.1	74 <b>W</b> 4.5	75 <b>Re</b> 5.0	76 <b>Os</b> 4.7	77 <b>Ir</b> 5.3	78 <b>Pt</b> 5.3	79 <b>Au</b> 4.3	80 <b>Hg</b> 4.5	81 <b>Tl</b> 3.7	82 <b>Pb</b> 4.0	83 <b>Bi</b> 4.4	84 <b>Po</b> -	85 <b>At</b> -	86 <b>Rn</b> -
87 <b>Fr</b> -	88 <b>Ra</b> -	89 <b>Ac</b> -	<b>High</b>														
			58 <b>Ce</b> 2.7	59 <b>Pr</b> -	60 <b>Nd</b> -	61 <b>Pm</b> -	62 <b>Sm</b> -	63 <b>Eu</b> -	64 <b>Gd</b> -	65 <b>Tb</b> -	66 <b>Dy</b> -	67 <b>Ho</b> -	68 <b>Er</b> -	69 <b>Tm</b> -	70 <b>Yb</b> -	71 <b>Lu</b> -	
			90 <b>Th</b> 3.3	91 <b>Pa</b> -	92 <b>U</b> 3.3	93 <b>Np</b>	94 <b>Pu</b>	95 <b>Am</b>	96 <b>Cm</b>	97 <b>Bk</b>	98 <b>Cf</b>	99 <b>Es</b>	100 <b>Fm</b>	101 <b>Md</b>	102 <b>No</b>	103 <b>Lr</b>	



# Electron Work Functions of the Elements

From the CRC-Handbook, 73rd edition (1993)

Element	Surface crystallographic orientation	Work function (eV)
Ag	polycrystalline	4.26
	(100)	4.64
	(110)	4.52
	(111)	4.74
Al	polycrystalline	4.28
	(100)	4.41
	(110)	4.06
	(111)	4.24
As		3.75
Au	polycrystalline	5.1
	(100)	5.47
	(110)	5.37
	(111)	5.31
B		4.45
Ba		2.7
Be		4.98
Bi		4.22
C		5.0



**Depends on surface orientation**

# Measuring Electron Binding Energies: Charging Effects For Insulators

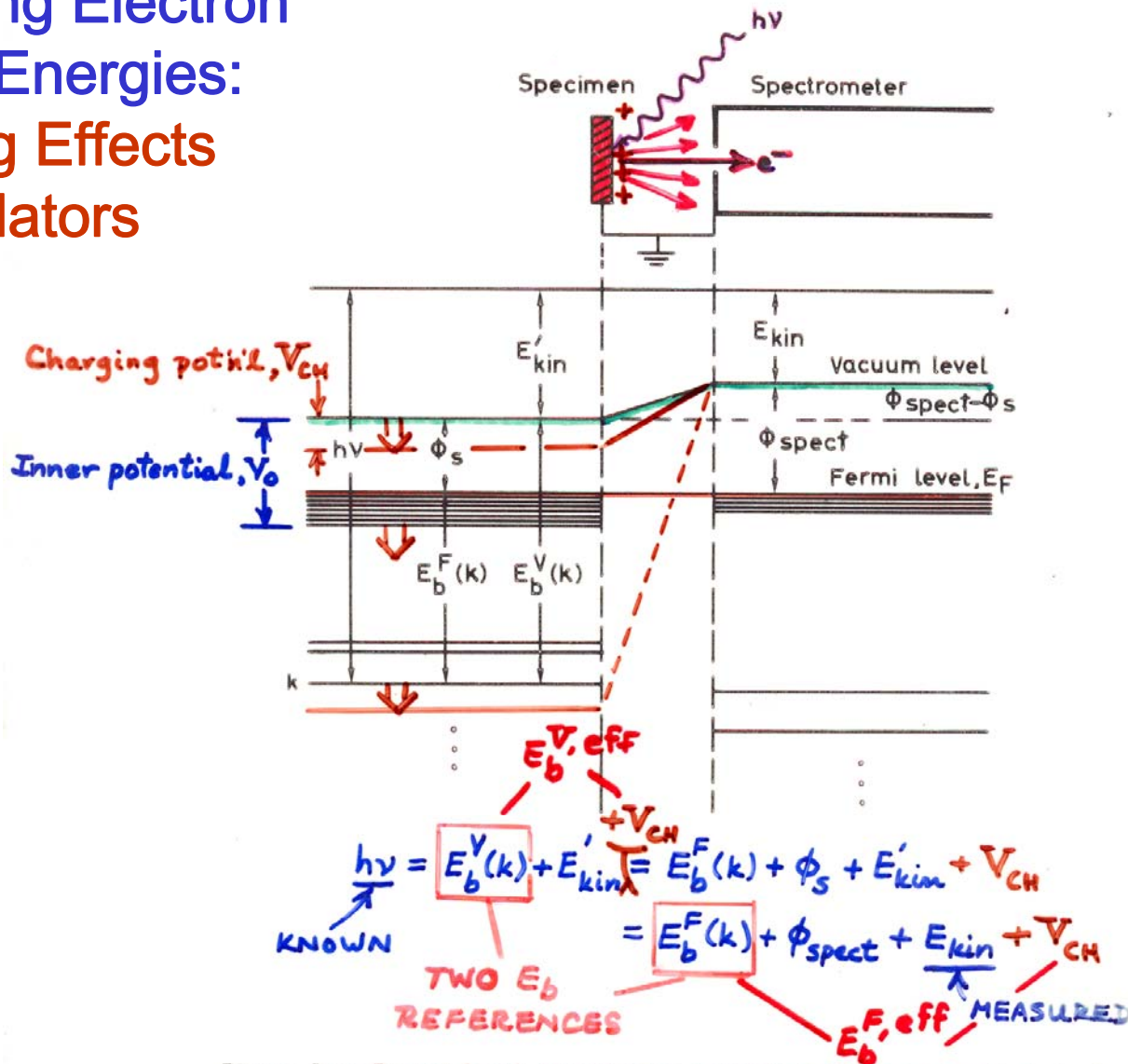
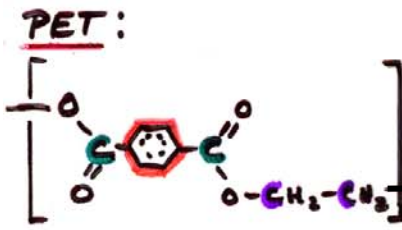
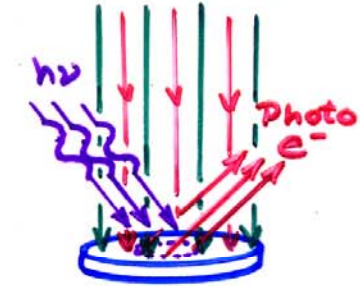


Figure 3 -- Energy level diagram for a metallic specimen in electrical equilibrium with an electron spectrometer. The closely spaced levels near the Fermi level  $E_F$  represent the filled portions of the valence bands in specimen and spectrometer. The deeper levels are core levels. An analogous diagram also applies to semiconducting or insulating specimens, with the only difference being that  $E_F$  lies somewhere between the filled valence bands and the empty conduction bands above.

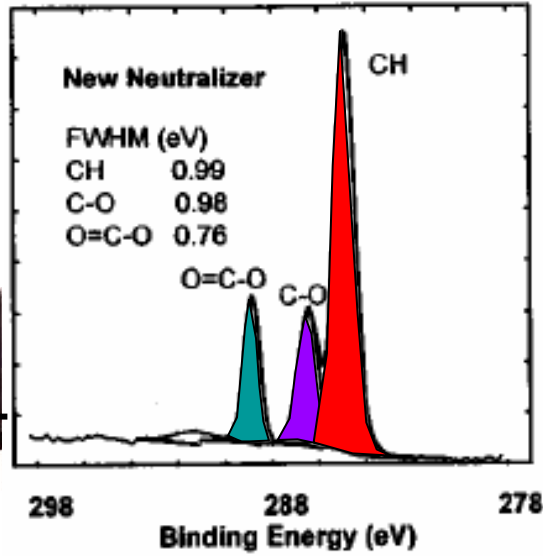
“Basic Concepts of XPS”  
Figure 3

Flood  $e^-$ : 1 eV  
 Ar $^+$ : 5-10 eV

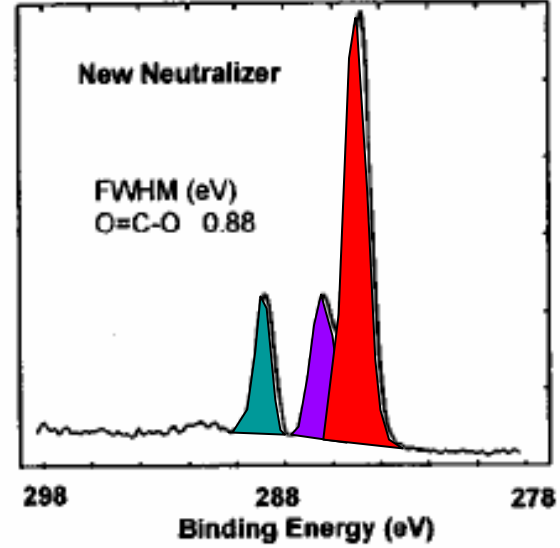
# BEST CURRENT SOLUTION TO AN OLD PROBLEM: CHARGING IN INSULATORS



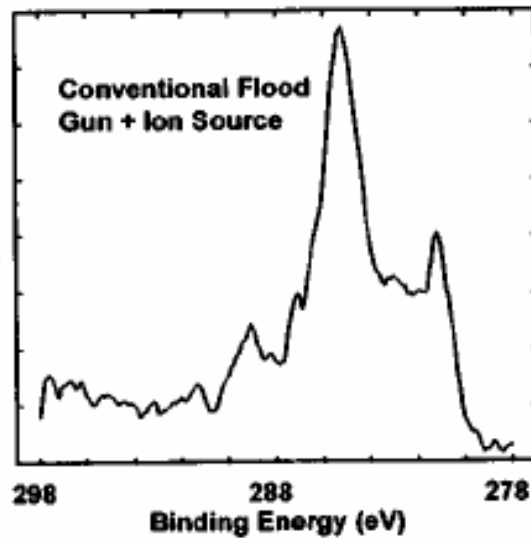
(a) 100  $\mu\text{m}$  x 800  $\mu\text{m}$  Scanned Line



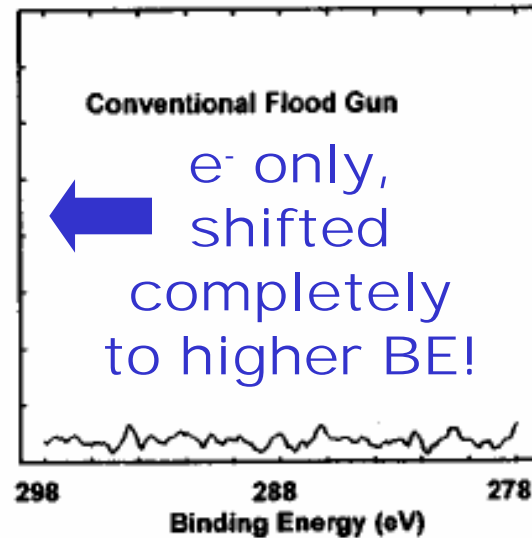
b) 20  $\mu\text{m}$  static point



c) 20  $\mu\text{m}$  static point



d) 20  $\mu\text{m}$  Static Point

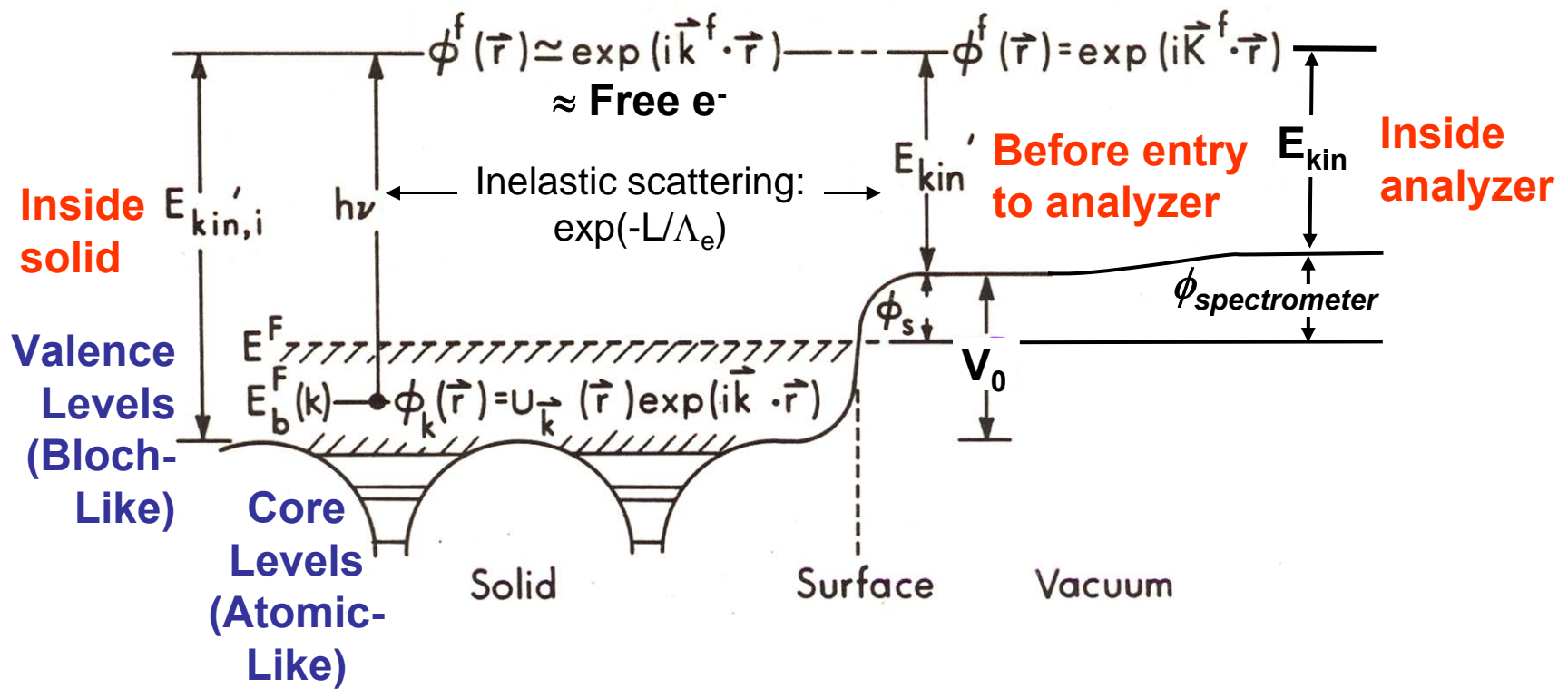


P. LARSON,  
 M. KELLY,  
 J. VAC.  
 SCI. TECH.  
 16, 3483  
 ('98)

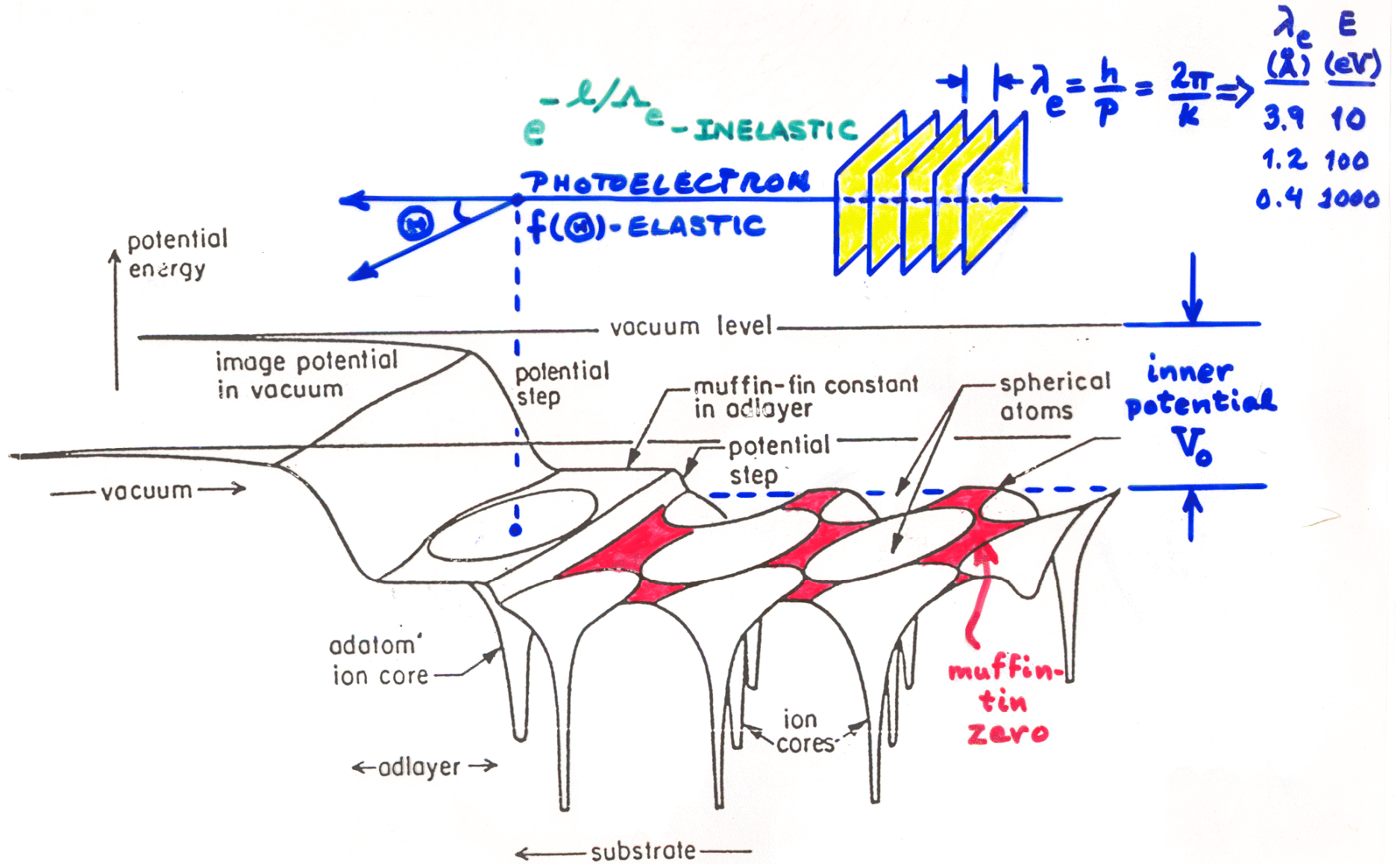
# Basic energetics

$$h\nu = E_{\text{binding}}^{\text{Vacuum}} + E_{\text{kinetic}} = E_{\text{binding}}^{\text{Fermi}} + \phi_{\text{spectrometer}} + E_{\text{kinetic}}$$

## One-Electron Picture of Photoemission from a Surface



# One-Electron Picture of Photoemission from a Surface—3D



## CALCULATION OF $V_0$ FOR AN IDEAL METAL

Fig. 4.2. Electron density profile at a jellium surface for two choices of the background density,  $r_s$  (Lang & Kohn, 1970).

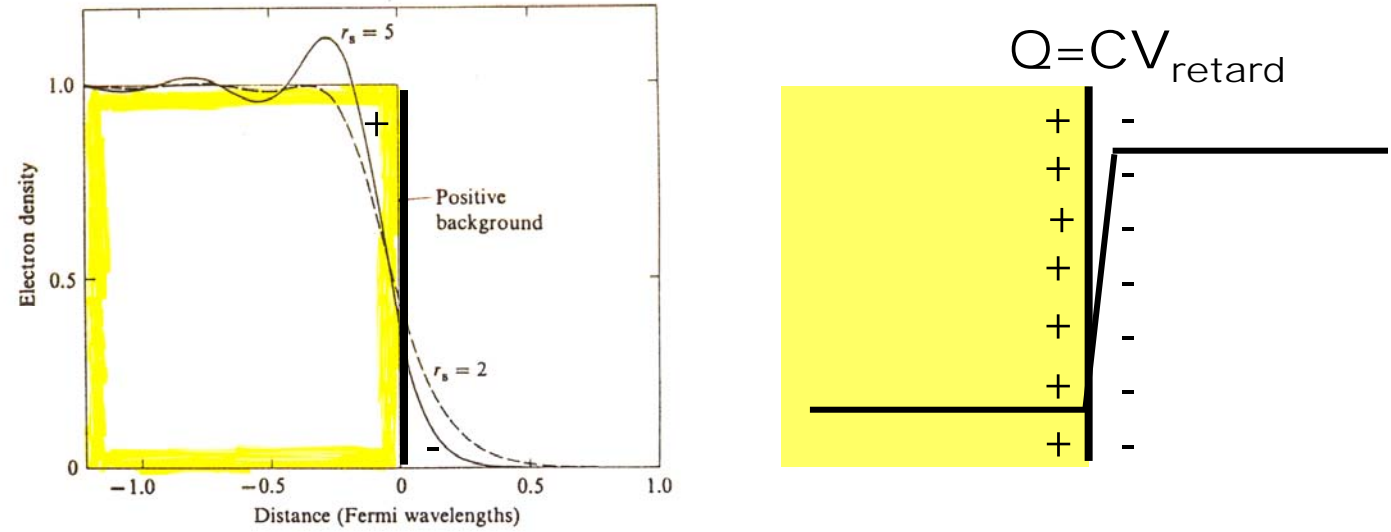
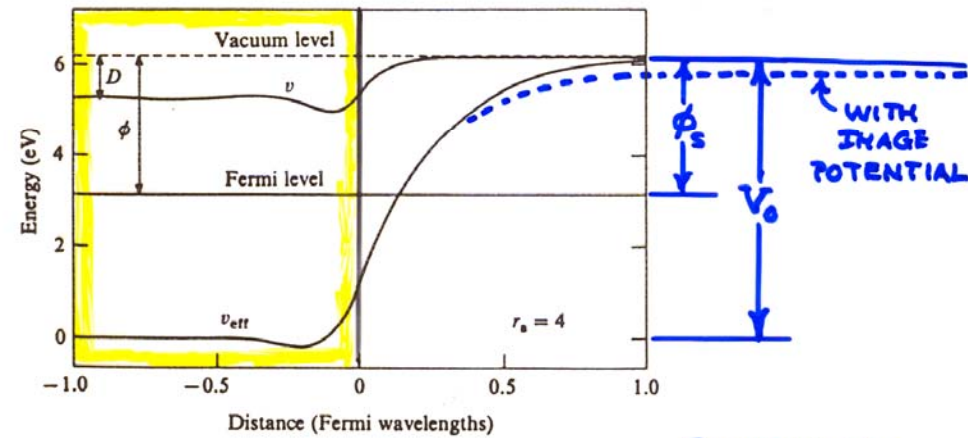


Fig. 4.3. Electrostatic potential,  $v(z)$ , and total effective one-electron potential,  $v_{\text{eff}}(z)$ , near a jellium surface (Lang & Kohn, 1970).



ZANGWILL,  
"SURFACE  
PHYSICS"

Vacuum level-

# The electronic structure of a transition metal—fcc Cu

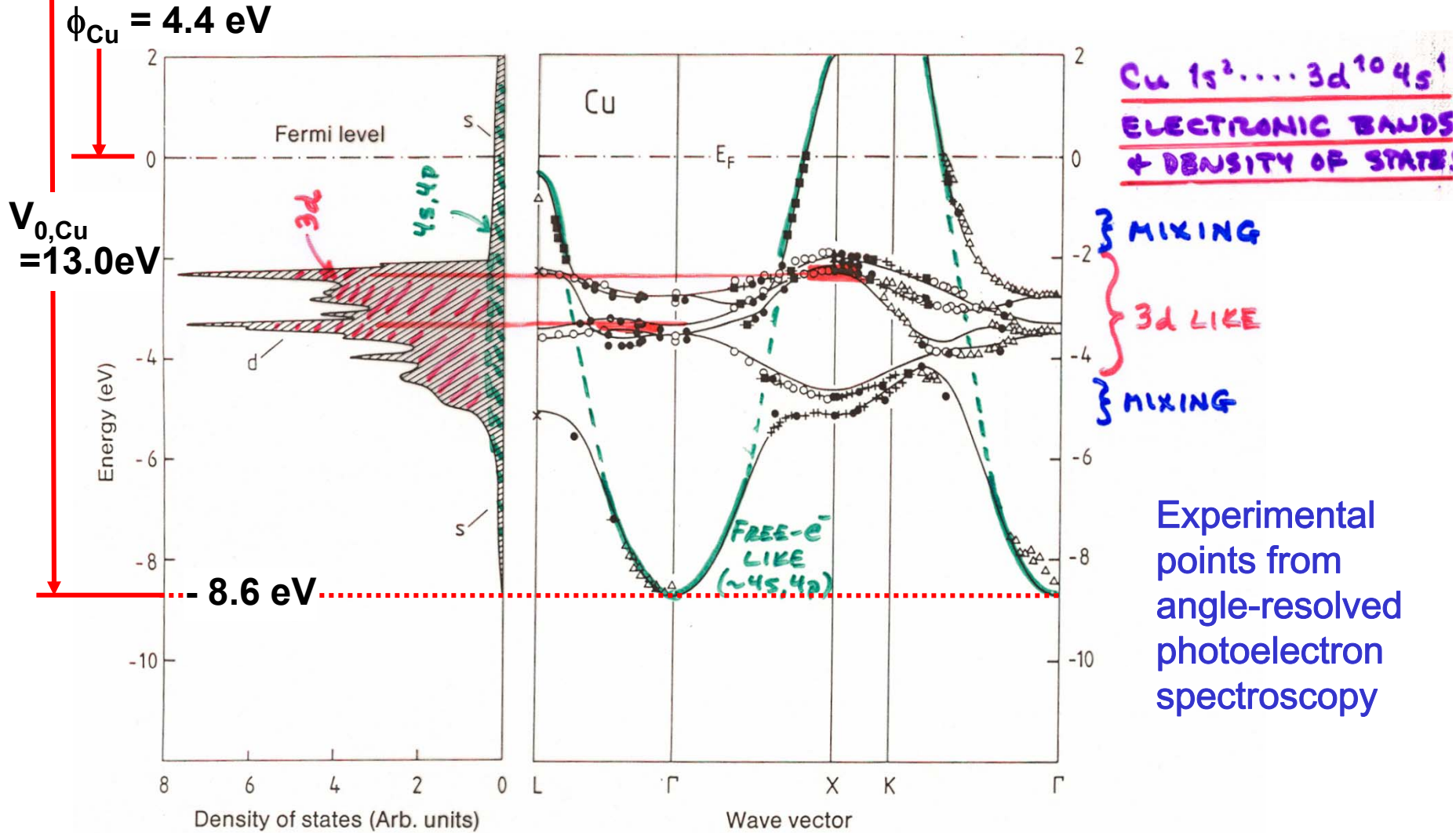


Fig. 7.12. Bandstructure  $E(k)$  for copper along directions of high crystal symmetry (right). The experimental data were measured by various authors and were presented collectively by Courths and Hüfner [7.4]. The full lines showing the calculated energy bands and the density of states (left) are from [7.5]. The experimental data agree very well, not only among themselves, but also with the calculation

# Outline

**Surface, interface, and nanoscience—short introduction**

**Some surface concepts and techniques→photoemission**

**Synchrotron radiation: experimental aspects**

**Electronic structure—a brief review**

**The basic synchrotron radiation techniques**

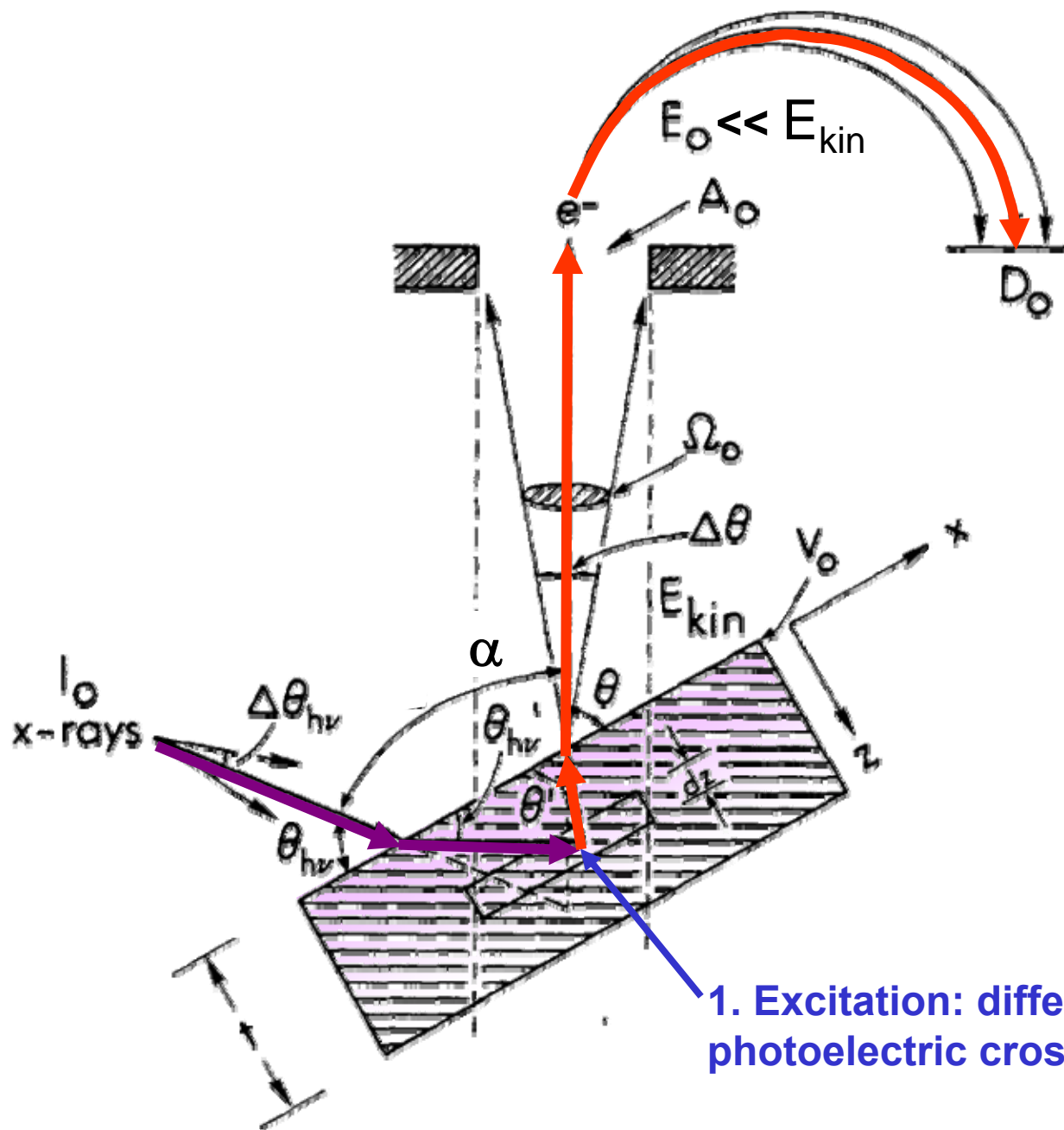
 **Core-level photoemission:  
peak intensities and surface analysis**

**Valence-level photoemission**

**Microscopy with photoemission**



# PHOTOELECTRON INTENSITIES—THE 3-STEP MODEL



1. Excitation: differential photoelectric cross section ( $d\sigma/d\Omega$ )

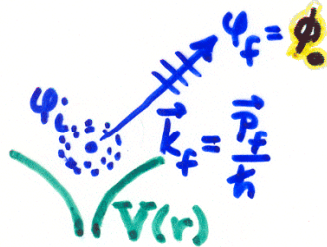
# PHOTOELECTRON EMISSION-

## BASIC MATRIX ELEMENTS + SELECTION RULES:

● ATOMIC-LIKE (LOCALIZED) STATES ⇒ CORE:

PLUS SPIN:

$$\psi_i(\vec{r}) = \psi_{n_i l_i m_i}(r, \theta, \phi) = R_{n_i l_i}(r) Y_{l_i m_i}(\theta, \phi) \begin{cases} \alpha(\sigma) = m_{s_i} = +1/2 = \uparrow \\ \beta(\sigma) = m_{s_i} = -1/2 = \downarrow \end{cases}$$



$$\psi_f(\vec{r}, \vec{k}_f) = \psi_{E_f}(\vec{r}, \vec{k}_f) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

$$= 4\pi \sum_{l_f, m_f} i^{l_f} e^{-i\delta_{l_f}} Y_{l_f m_f}^*(\theta, \phi) Y_{l_f m_f}(\theta, \phi) R_{E_f, l_f}(r) \begin{cases} \alpha(\sigma) \\ \beta(\sigma) \end{cases}$$

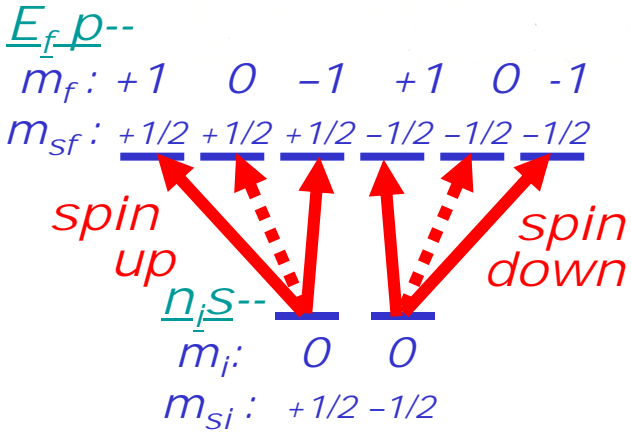
PHASE SHIFT OF  $l_f$  WAVE IN  $V(r)$

DIPOLE: INT.  $\propto |\langle \psi_f | \hat{E} \cdot \vec{r} | \psi_i \rangle|^2 = |\hat{E} \cdot \langle \psi_f | \vec{r} | \psi_i \rangle|^2 \Rightarrow$

EQUIVALENT WITHIN CONSTANT FACTOR



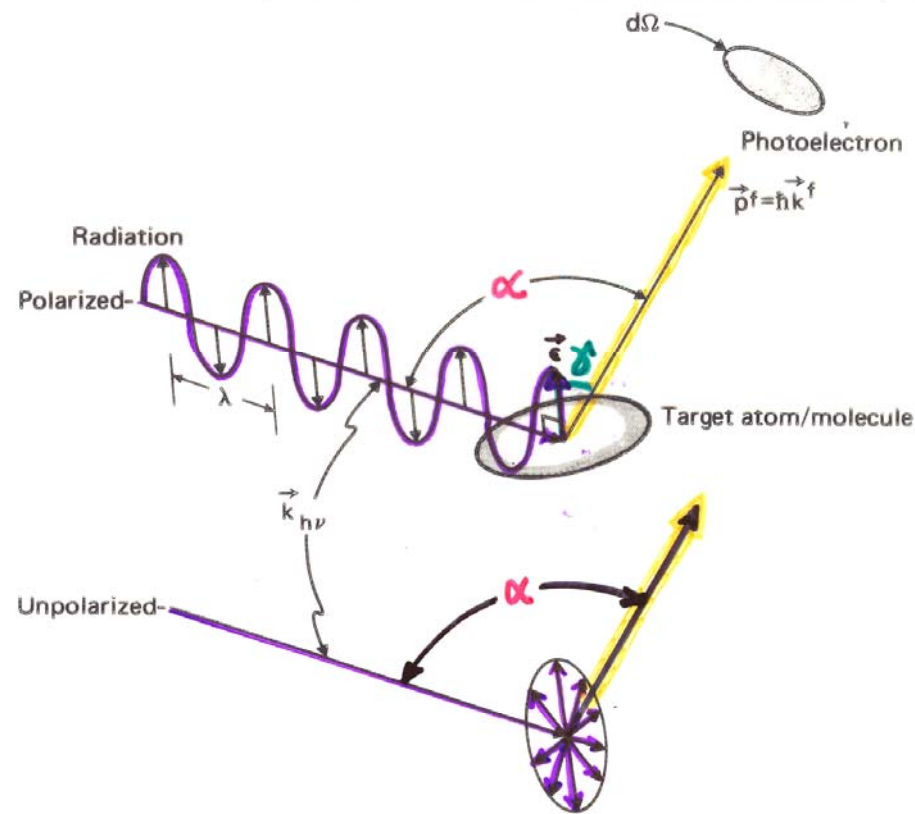
- $\langle \Delta l = l_f - l_i = \pm 1$   
TWO CHANNELS
  - $\langle \Delta m = m_f - m_i = 0, \pm 1$   
LINEAR POLARIZ.
  - $\langle \Delta m = \pm 1$ , CIRCULAR POLARIZATION
- $\Delta m_s = m_{s_f} - m_{s_i} = 0!$



FOR A GIVEN  $n_i/l_i/m_i/m_{s_i}$ : SUM OVER DEGENERATE INITIAL STATES  $m_i/m_{s_i}$  AND AVERAGE OVER FINAL STATES  $E_f/l_f/m_f/m_{s_f}$  ACCESSED FROM EACH  $m_i$  TO YIELD DIFFERENTIAL SUBSHELL PHOTOELECTRIC CROSS SECTION:

$$d\sigma_{n_i l_i} / d\Omega$$

$\propto$  PROBABILITY PER UNIT SOLID ANGLE OF EXCITING ONE ELECTRON FROM SUBSHELL  $n_i/l_i$  INTO THE DIRECTION  $k_f$



**FOR ATOMIC-LIKE EMISSION:**

LIN.

**POLARIZED:** 
$$\frac{d\sigma_{nl}(E_f)}{d\Omega} = \frac{\sigma_{nl}(E_f)}{4\pi} \left[ 1 + \beta_{nl}(E_f) \left( \frac{3}{2} \cos^2 \gamma - \frac{1}{2} \right) \right]$$

**UNPOLARIZED:** 
$$\frac{d\sigma_{nl}(E_f)}{d\Omega} = \frac{\sigma_{nl}(E_f)}{4\pi} \left[ 1 + \frac{1}{2} \beta_{nl}(E_f) \left( \frac{3}{2} \sin^2 \alpha - 1 \right) \right]$$

Figure 7 -- General geometry for defining the differential cross section  $d\sigma/d\Omega$ , showing both polarized and unpolarized incident radiation. The polarization vector  $\vec{e}$  is parallel to the electric field  $\vec{E}$  of the radiation. In order for the dipole approximation to be valid, the radiation wave length  $\lambda$  should be much larger than typical target dimensions (that is, the opposite of what is shown here).

WITH:

$\sigma_{nl}$  = TOTAL CROSS SECTION

$\beta_{nl}$  = ASYMMETRY PARAMETER

$\sigma_{nl}, \beta_{nl}$  TABULATIONS IN: GOLDBERG ET AL., J. ELECT. SPECT. & YEH, LINDAU, AT. NUC. DATA 22, 1 ('85) \ 21, 285 ('91)

TOTAL SUBSHELL CROSS SECTION:  $\int \frac{d\sigma_{nl}}{d\Omega} d\Omega =$

$$\sigma_{nl}(E^f) = \frac{4\pi\alpha_0 a_0^2}{3} (h\nu) [lR_{l-1}^2(E^f) + (l+1)R_{l+1}^2(E^f)]$$

= SUM OVER ALL  $m_l, m_s$  IN SUBSHELL  $nl$

RADIAL MATRIX ELEMENTS TO  $l \pm 1$  CHANNELS:

$$R_{l \pm 1}(E^f) = \int_0^\infty R_{nl}(r) r R_{E^f, l \pm 1}(r) r^2 dr = \int_0^\infty P_{nl}(r) r P_{E^f, l \pm 1}(r) dr$$

DIFFERENTIAL CROSS SECTION: UNPOLARIZED

$$\frac{d\sigma_{nl}}{d\Omega}(E^f) = \frac{\sigma_{nl}}{4\pi} [1 - \frac{1}{2}\beta_{nl}(E^f)P_2(\cos \alpha)]$$

$$= \frac{\sigma_{nl}}{4\pi} [1 + \frac{1}{2}\beta_{nl}(E^f)(\frac{3}{2}\sin^2 \alpha - 1)]$$

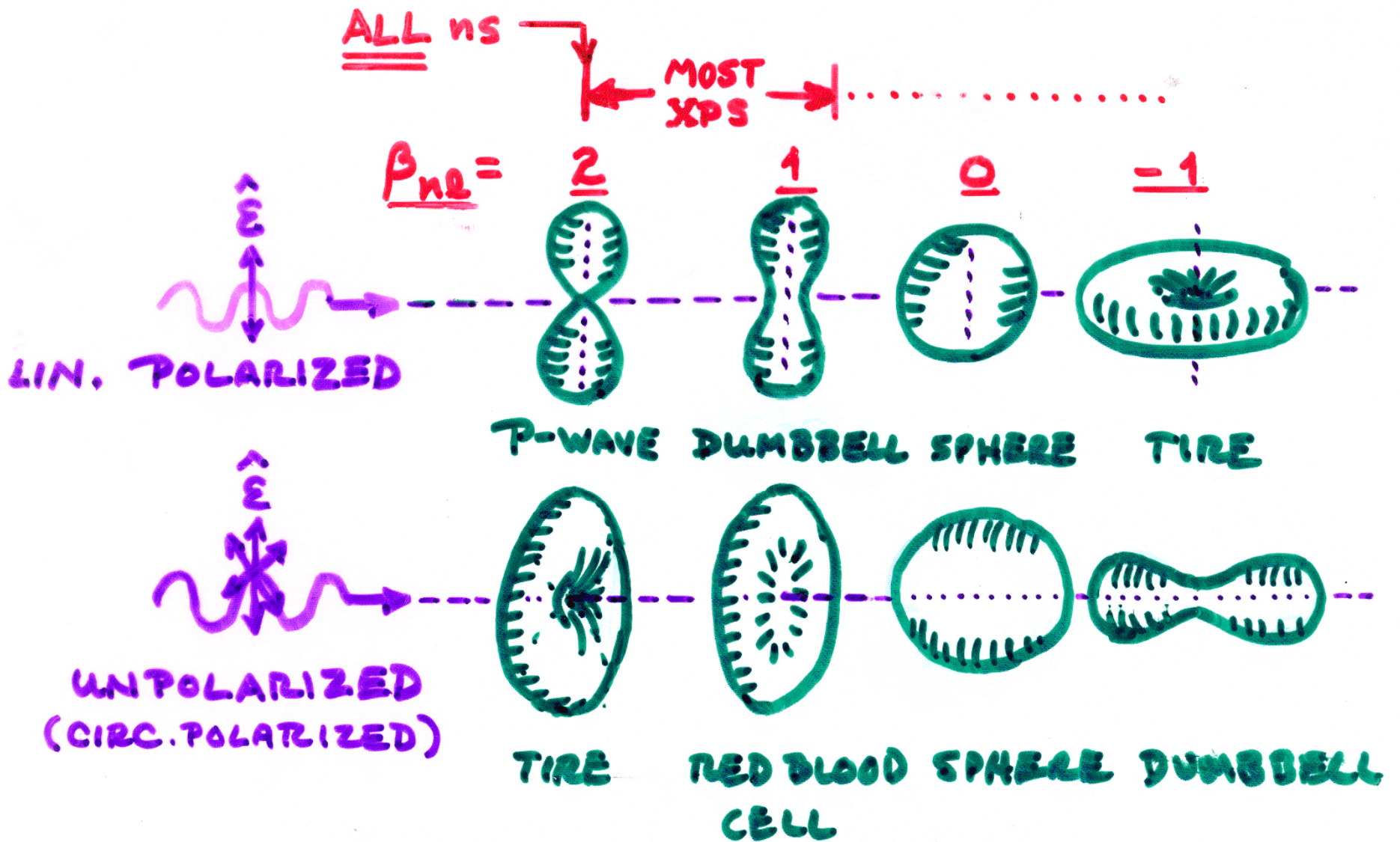
$$= A + B \sin^2 \alpha$$

ASYMMETRY PARAMETER:

TERM FOR  
 $l \pm 1$  INTERFERENCE

$$\beta_{nl}(E^f) = \frac{\{l(l-1)R_{l-1}^2(E^f) + (l+1)(l+2)R_{l+1}^2(E^f) - 6l(l+1)R_{l+1}(E^f)R_{l-1}(E^f) \cos [\delta_{l+1}(E^f) - \delta_{l-1}(E^f)]\}}{(2l+1)[lR_{l-1}^2(E^f) + (l+1)R_{l+1}^2(E^f)]}$$

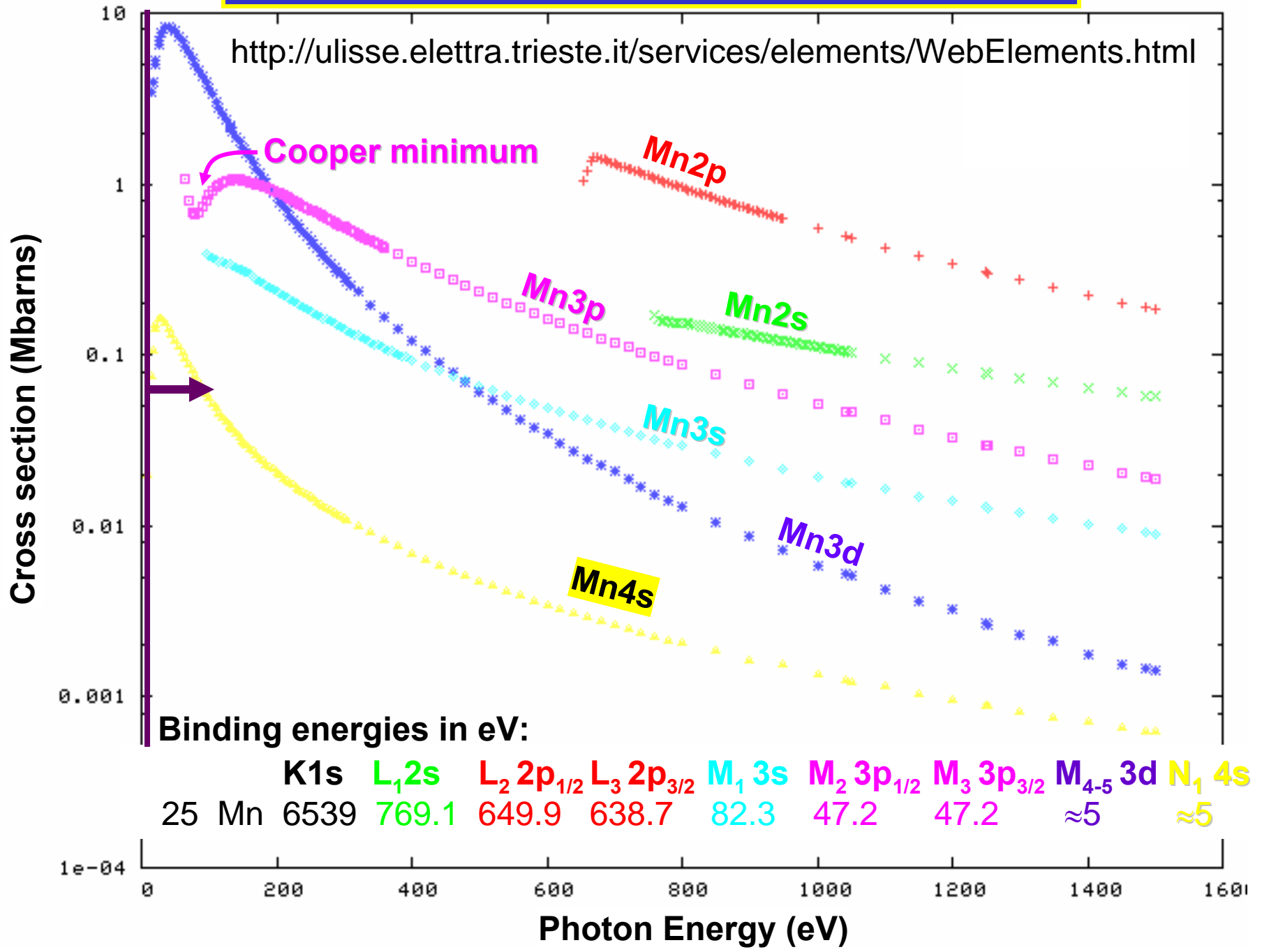
$\delta_{l \pm 1}(E^f) =$  CONTINUUM ORBITAL PHASE SHIFTS  
IN ATOMIC POTENTIAL  $V(r)$



RANGE OF SHAPES OF  $\frac{d\sigma}{d\Omega}$

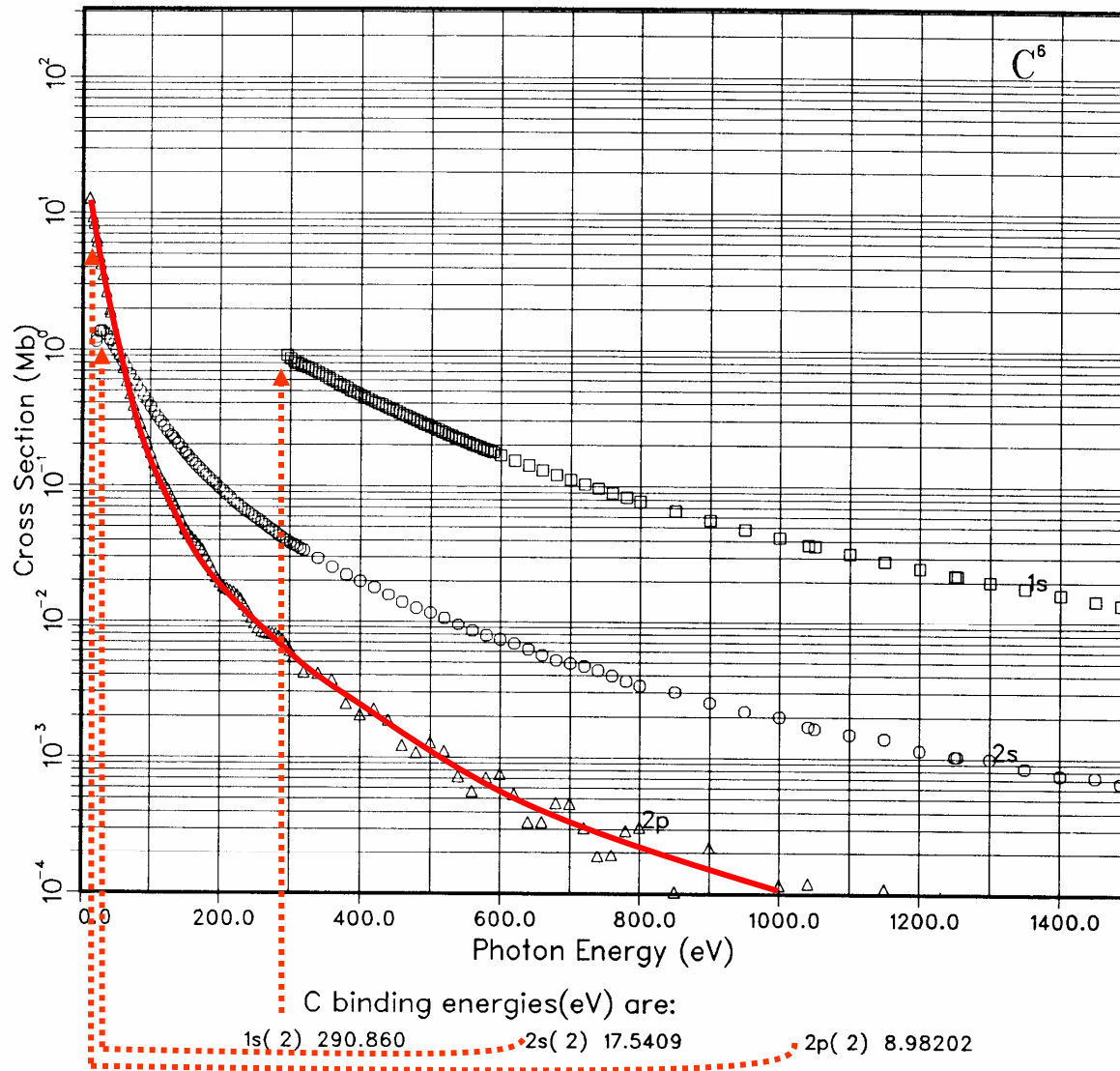
# PHOTOELECTRIC CROSS SECTIONS FOR Mn

<http://ulisse.elettra.trieste.it/services/elements/WebElements.html>



GRAPH I. Atomic Subshell Photoionization Cross Sections for 0–1500 eV,  $1 \leq Z \leq 103$   
See page 6 for Explanation of Graphs

# PHOTOELECTRIC CROSS SECTIONS FOR C



Plus other Examples from Yeh and Lindau in Sec. 1.5 of X-Ray Data Booklet, and plots for all elements at: <http://ulisse.elettra.trieste.it/elements/WebElements.html>

WebCrossSections - Microsoft Internet Explorer

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Address http://ulisse.elettra.trieste.it/elements/WebElements.html

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# Atomic Calculation of Photoionization Cross-Sections and Asymmetry Parameters

This periodic table interface was developed to easily access the calculated atomic cross sections for photoionization and the related asymmetry parameters. The data are taken from: J.J. Yeh, *Atomic Calculation of Photoionization Cross-Sections and Asymmetry Parameters*, Gordon and Breach Science Publishers, Langhorne, PE (USA), 1993 and from J.J. Yeh and I.Lindau, *Atomic Data and Nuclear Data Tables*, **32**, 1-155 (1985). The data shown here are those calculated in the dipole length approximation.

This is a beta version: [comments](#) are welcome.

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
	1A	2A	3B	4B	5B	6B	7B	8B			1B	2B	3A	4A	5A	6A	7A	8A
Period																		
1	1 <a href="#">H</a>																	2 <a href="#">He</a>
2	3 <a href="#">Li</a>	4 <a href="#">Be</a>											5 <a href="#">B</a>	6 <a href="#">C</a>	7 <a href="#">N</a>	8 <a href="#">O</a>	9 <a href="#">F</a>	10 <a href="#">Ne</a>
3	11 <a href="#">Na</a>	12 <a href="#">Mg</a>											13 <a href="#">Al</a>	14 <a href="#">Si</a>	15 <a href="#">P</a>	16 <a href="#">S</a>	17 <a href="#">Cl</a>	18 <a href="#">Ar</a>
4	19 <a href="#">K</a>	20 <a href="#">Ca</a>	21 <a href="#">Sc</a>	22 <a href="#">Ti</a>	23 <a href="#">V</a>	24 <a href="#">Cr</a>	25 <a href="#">Mn</a>	26 <a href="#">Fe</a>	27 <a href="#">Co</a>	28 <a href="#">Ni</a>	29 <a href="#">Cu</a>	30 <a href="#">Zn</a>	31 <a href="#">Ga</a>	32 <a href="#">Ge</a>	33 <a href="#">As</a>	34 <a href="#">Se</a>	35 <a href="#">Br</a>	36 <a href="#">Kr</a>
	27	29	20	40	41	42	42	44	45	46	47	49	40	50	51	52	52	54

Internet



Graph - Microsoft Internet Explorer

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Address [http://ulisse.elettra.trieste.it/elements/mnu\\_elem.cgi?ACTION=SHOWGRAPH&ELEMENT=c&C0=1s&C1=2p&C2=2s](http://ulisse.elettra.trieste.it/elements/mnu_elem.cgi?ACTION=SHOWGRAPH&ELEMENT=c&C0=1s&C1=2p&C2=2s) Go Links

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Media

Energy (eV)	Cross o1s (Mbarn)	Cross o2p (Mbarn)	Cross o2s (Mbarn)
0	-	10	10
50	-	1	1
100	-	0.1	0.1
200	-	0.01	0.01
300	1	0.003	0.003
400	0.3	0.001	0.001
600	0.1	0.0003	0.0003
800	0.03	0.0001	0.0001
1000	0.01	3e-05	3e-05
1200	0.003	1e-05	1e-05
1400	0.001	3e-06	3e-06
1600	0.0003	1e-06	1e-06

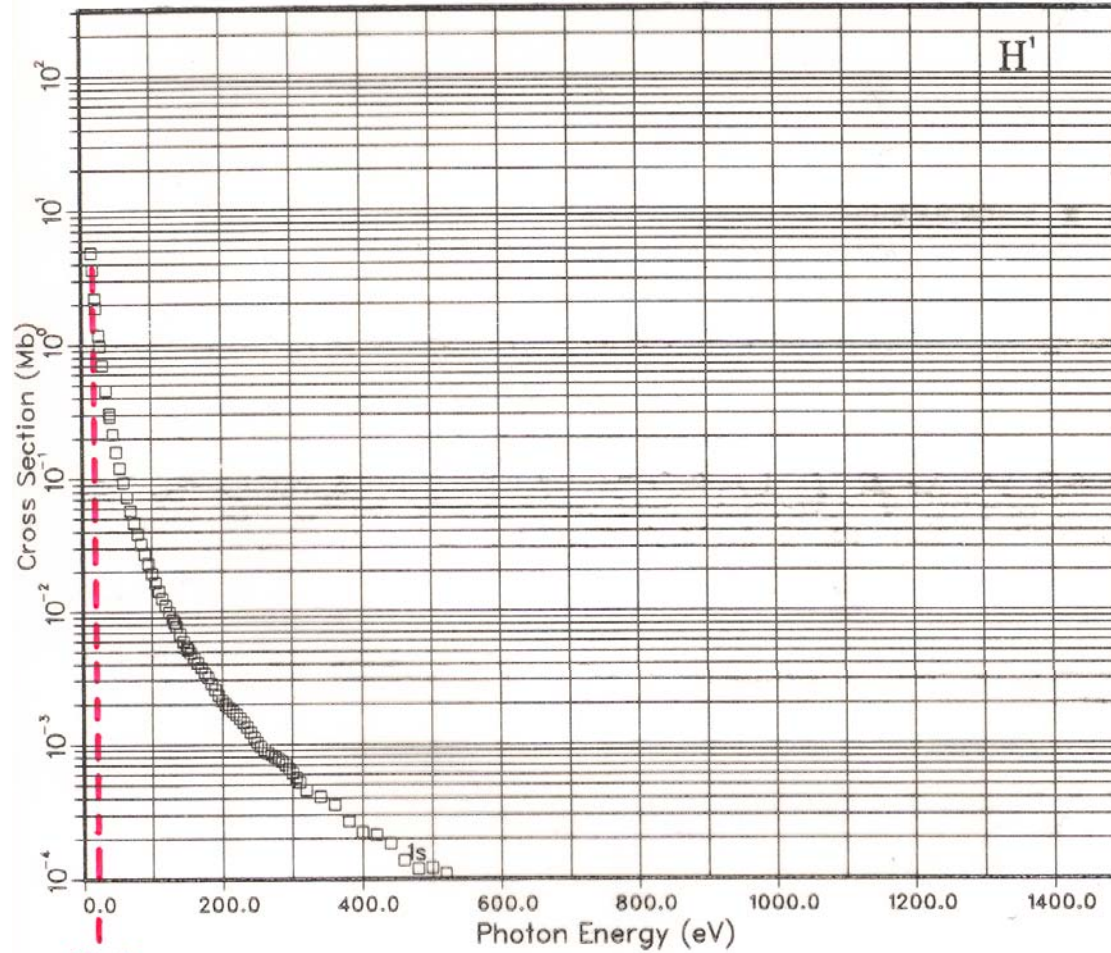
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Start

11:17 AM

GRAPH I. Atomic Subshell Photoionization Cross Sections for 0-1500 eV,  $1 \leq Z \leq 103$   
See page 6 for Explanation of Graphs

# PHOTOELECTRIC CROSS SECTIONS FOR H

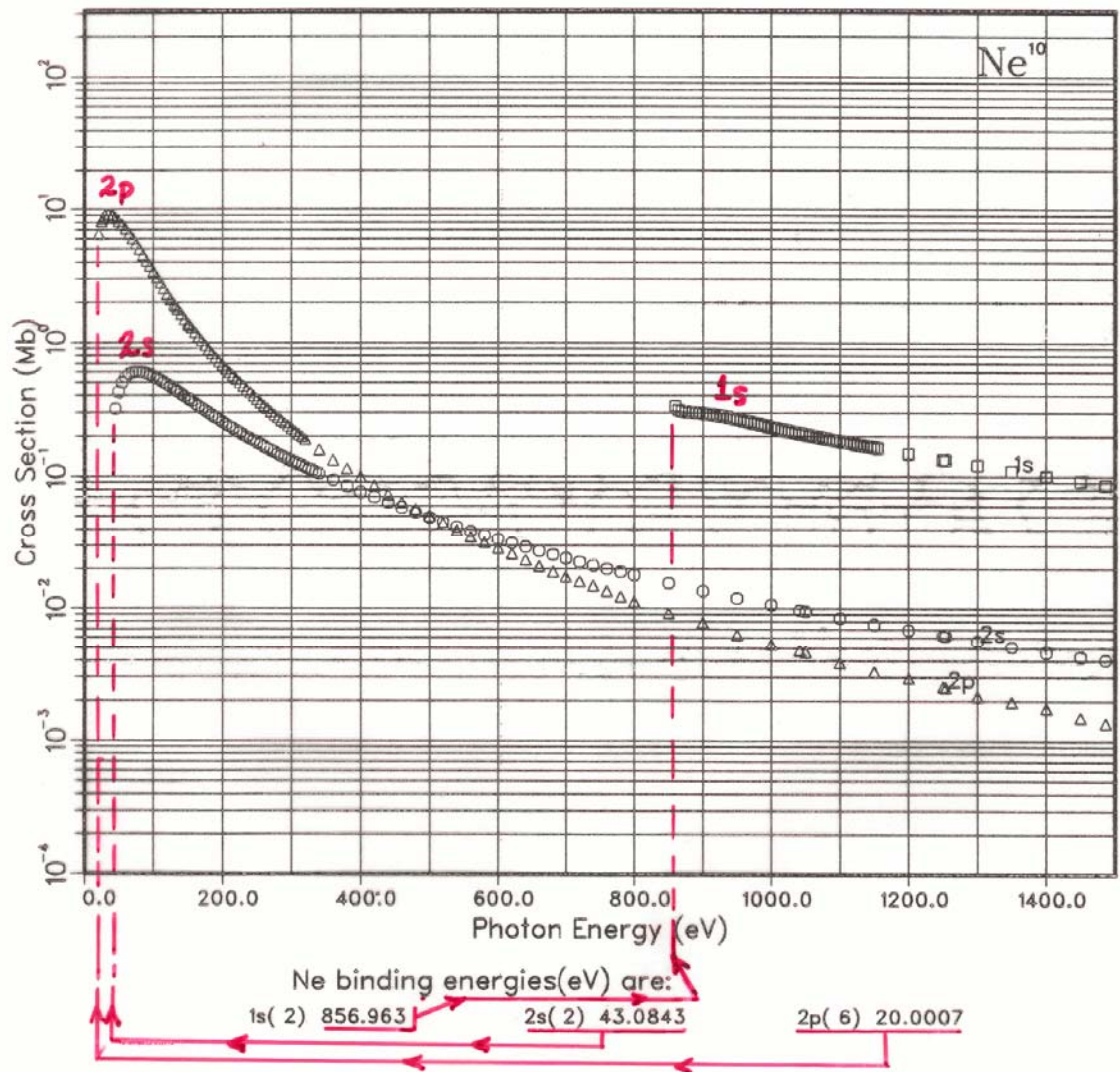


13.6  
eV  
= THRESHOLD  
FOR  
e<sup>-</sup> EMISSION

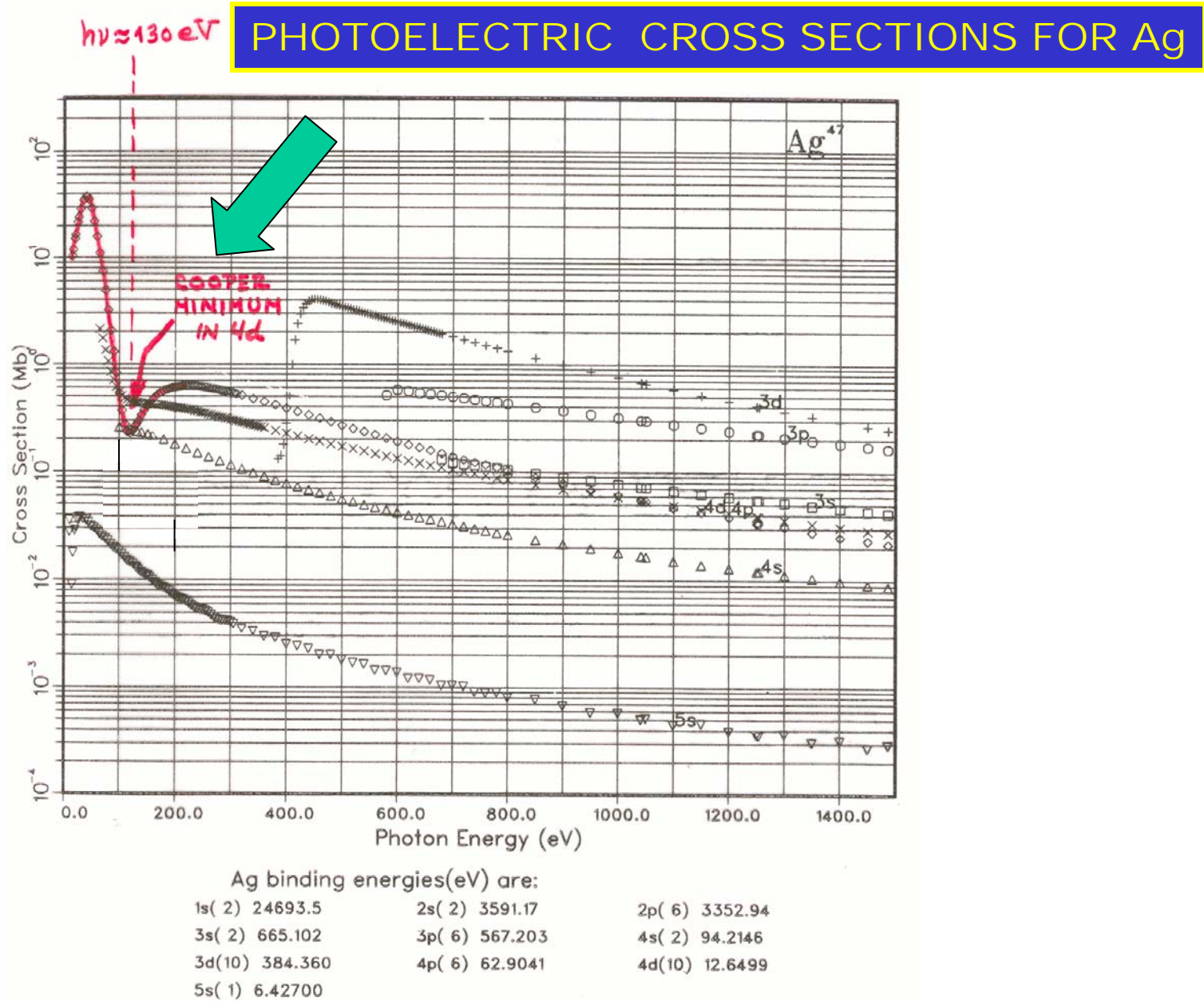
H binding energies(eV) are:  
1s( 1) 13.6050

GRAPH I. Atomic Subshell Photoionization Cross Sections for 0–1500 eV,  $1 \leq Z \leq 103$   
 See page 6 for Explanation of Graphs

# PHOTOELECTRIC CROSS SECTIONS FOR Ne



GRAPH I. Atomic Subshell Photoionization Cross Sections for 0-1500 eV,  $1 \leq Z \leq 103$   
See page 6 for Explanation of Graphs



COOPER MINIMUM IN Ag 4d (Z = 47) CROSS SECTION : Expt. & Theory

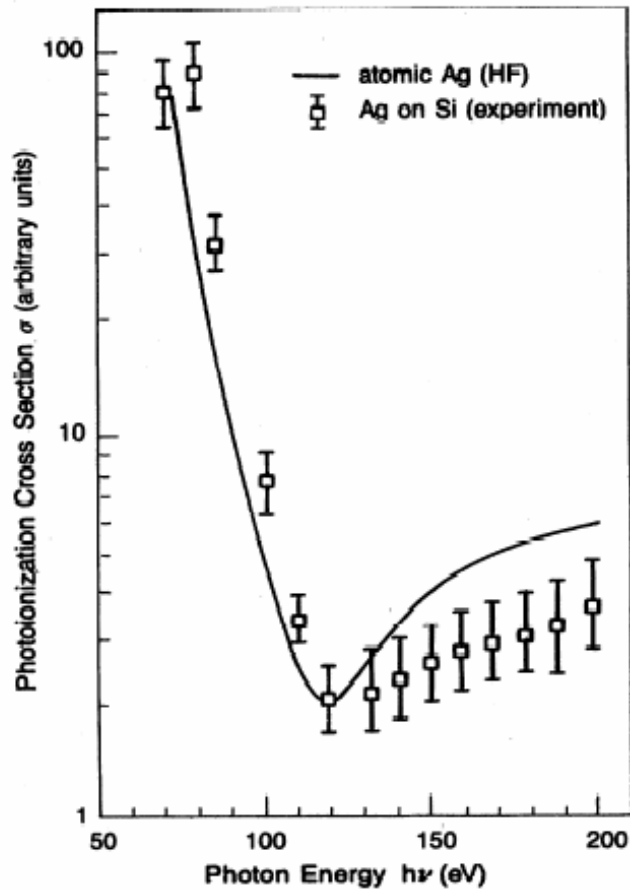


FIG. 5. Partial photoionization cross section for 4d electrons of Ag in logarithmic scale. Our experimental data for the Ag/Si interface (squares) are compared with the Hartree-Fock results for atomic Ag by Yeh and Lindau (solid line). Note that our experimental data are normalized at the minimum to the theoretical value.

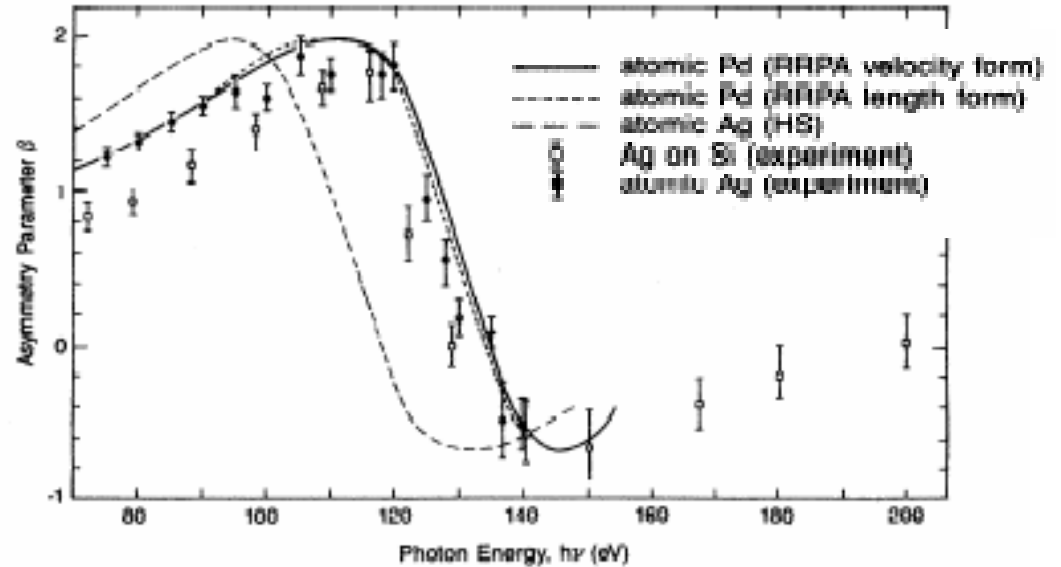


FIG. 6. Asymmetry parameter for 4d electrons of Ag. Our experimental data for the Ag/Si interface (squares) are compared with the data for atomic Ag (circles), the RRPA prediction for atomic Pd by Radojevic and Johnson (solid line, velocity form; short-dashed line, length form), and the HS calculations for atomic Ag by Manson (long-dashed line).

TOTAL SUBSHELL CROSS SECTION:  $\int \frac{d\sigma_{nl}}{d\Omega} d\Omega =$

$$\sigma_{nl}(E^f) = \frac{4\pi\alpha_0 a_0^2}{3} (h\nu) [lR_{l-1}^2(E^f) + (l+1)R_{l+1}^2(E^f)]$$

= SUM OVER ALL  $m_l, m_s$  IN SUBSHELL  $nl$

RADIAL MATRIX ELEMENTS TO  $l \pm 1$  CHANNELS:

$$R_{l \pm 1}(E^f) = \int_0^\infty R_{nl}(r) r R_{E^f, l \pm 1}(r) r^2 dr = \int_0^\infty P_{nl}(r) r P_{E^f, l \pm 1}(r) dr$$

DIFFERENTIAL CROSS SECTION: UNPOLARIZED

$$\frac{d\sigma_{nl}}{d\Omega}(E^f) = \frac{\sigma_{nl}}{4\pi} [1 - \frac{1}{2}\beta_{nl}(E^f)P_2(\cos \alpha)]$$

$$= \frac{\sigma_{nl}}{4\pi} [1 + \frac{1}{2}\beta_{nl}(E^f)(\frac{3}{2}\sin^2 \alpha - 1)]$$

$$= A + B \sin^2 \alpha$$

ASYMMETRY PARAMETER:

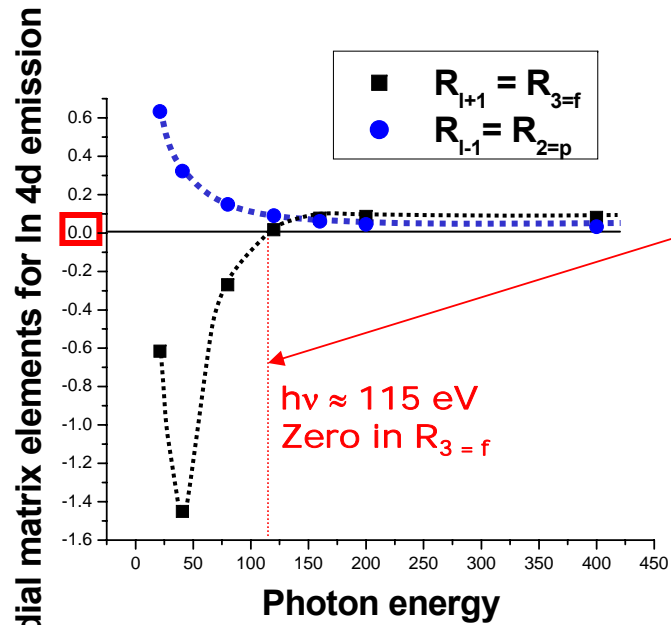
TERM FOR  
 $l \pm 1$  INTERFERENCE

$$\beta_{nl}(E^f) = \frac{\{l(l-1)R_{l-1}^2(E^f) + (l+1)(l+2)R_{l+1}^2(E^f) - 6l(l+1)R_{l+1}(E^f)R_{l-1}(E^f) \cos [\delta_{l+1}(E^f) - \delta_{l-1}(E^f)]\}}{(2l+1)[lR_{l-1}^2(E^f) + (l+1)R_{l+1}^2(E^f)]}$$

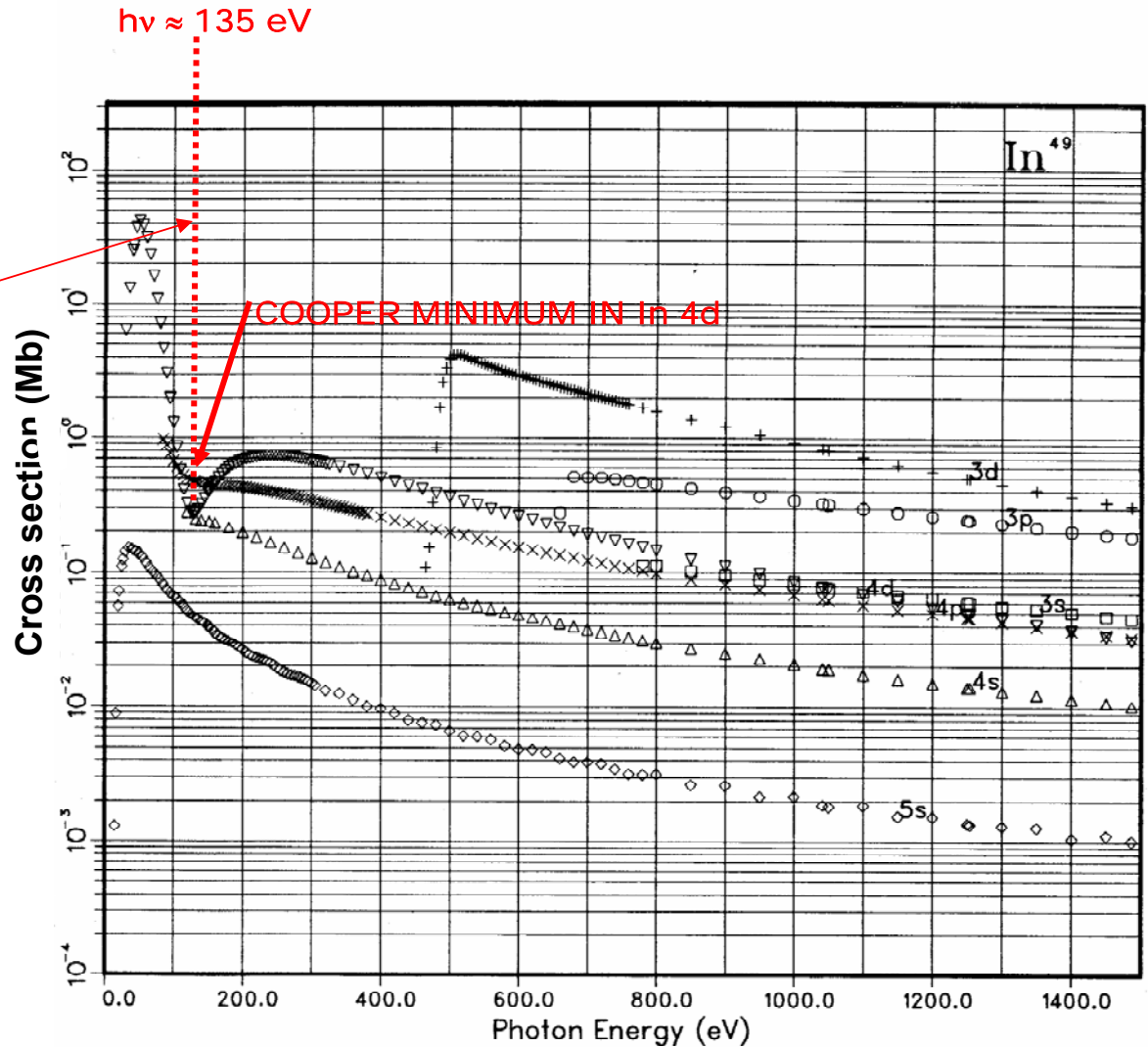
$\delta_{l \pm 1}(E^f)$  = CONTINUUM ORBITAL PHASE SHIFTS  
IN ATOMIC POTENTIAL  $V(r)$

# COOPER MINIMUM IN In 4d (Z = 49) CROSS SECTION—Radial Matrix Element Variation

GRAPH I. Atomic Subshell Photoionization Cross Sections for 0–1500 eV,  $1 \leq Z \leq 103$   
See page 6 for Explanation of Graphs



Goldberg, Kono, Fadley  
J. Elect. Spect. 21, 285 ('81)



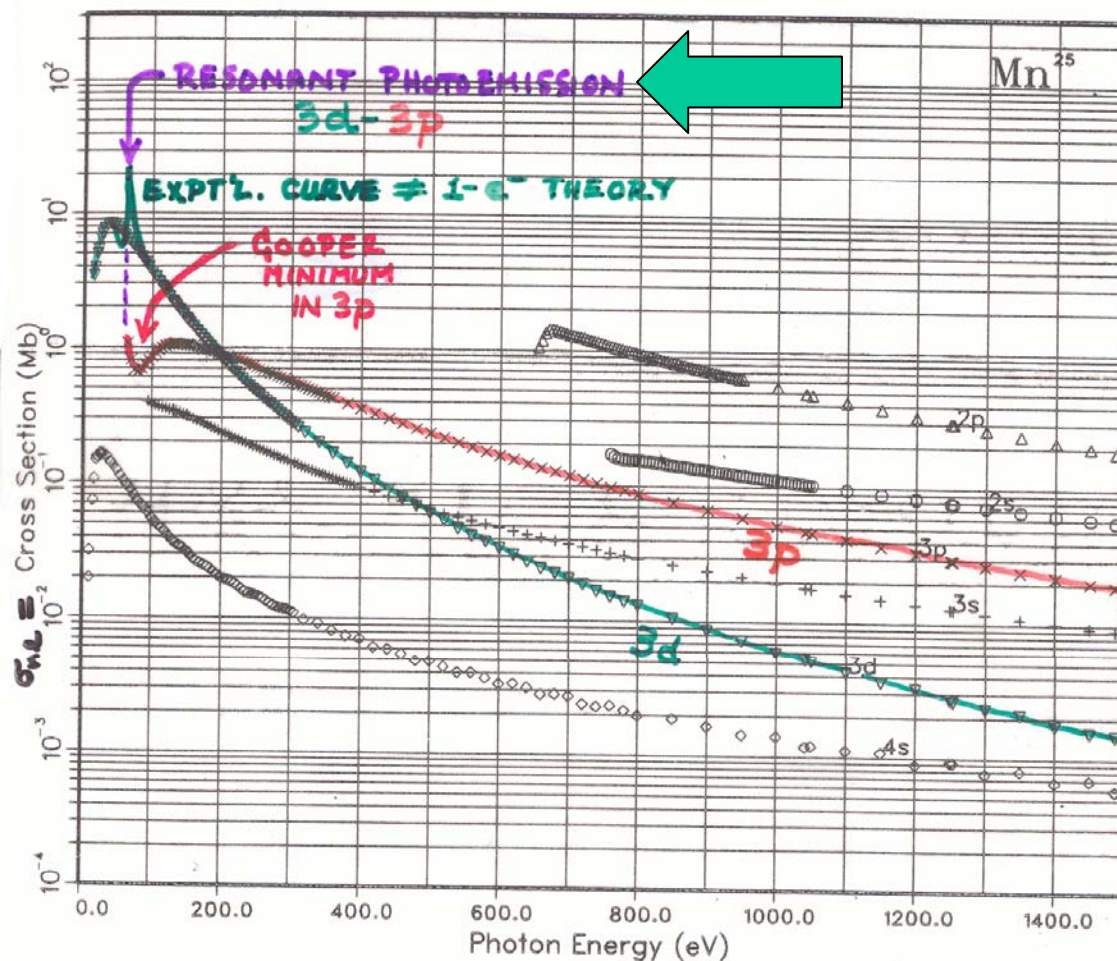
In binding energies(eV) are:

1s( 2) 26971.5	2s( 2) 3983.01	2p( 6) 3731.41
3s( 2) 764.232	3p( 6) 659.286	4s( 2) 118.953
3d(10) 462.909	4p( 6) 84.0558	5s( 2) 10.1384
4d(10) 26.2168	5p( 1) 4.69781	

ATOMIC & NUCLEAR DATA TABLES 32, 45 (1985)

GRAPH I. Atomic Subshell Photoionization Cross Sections for 0-1500 eV,  $1 \leq Z \leq 103$   
See page 6 for Explanation of Graphs

PHOTOELECTRIC CROSS SECTIONS FOR Mn



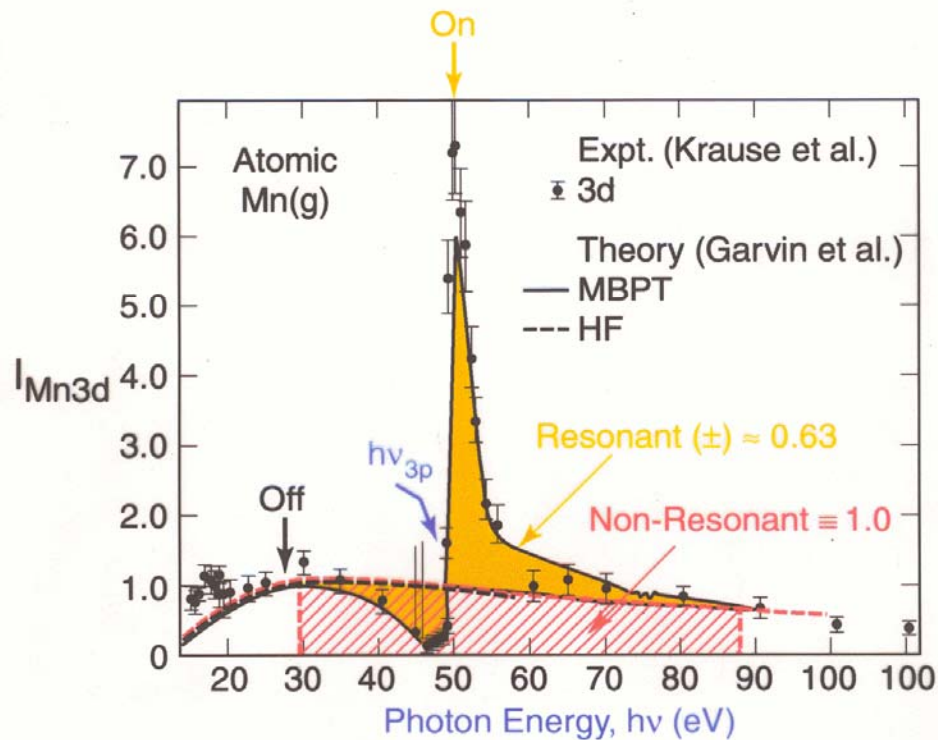
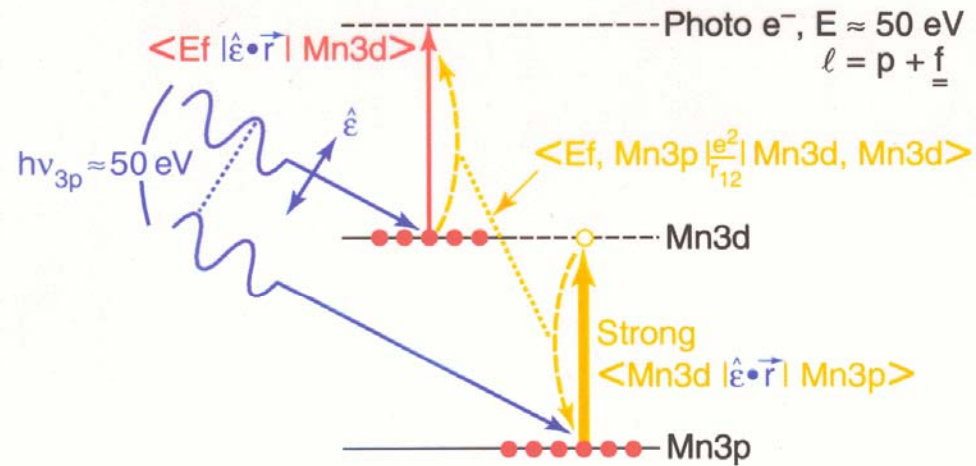
Mn binding energies(eV) are:

1s (2) 6455.26	2s (2) 755.155	2p (6) 653.681
3s (2) 90.8814	3p (6) 60.9150	4s (2) 7.14671
3d (5) 12.0486		



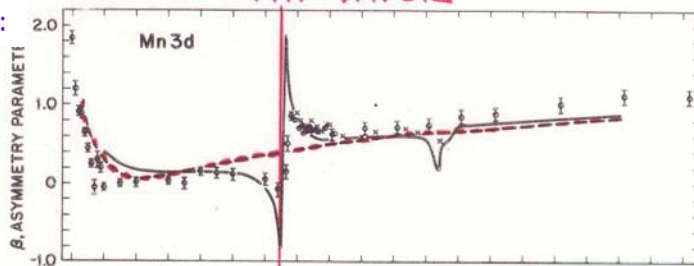
# RESONANT PHOTOEMISSION FOR Mn-A MANY-ELECTRON EFFECT

Ex. – Mn atom: Mn3d emission, resonance with Mn3p

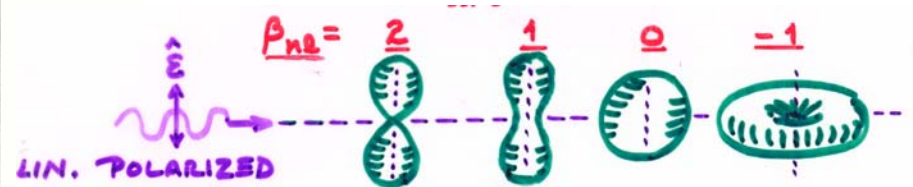
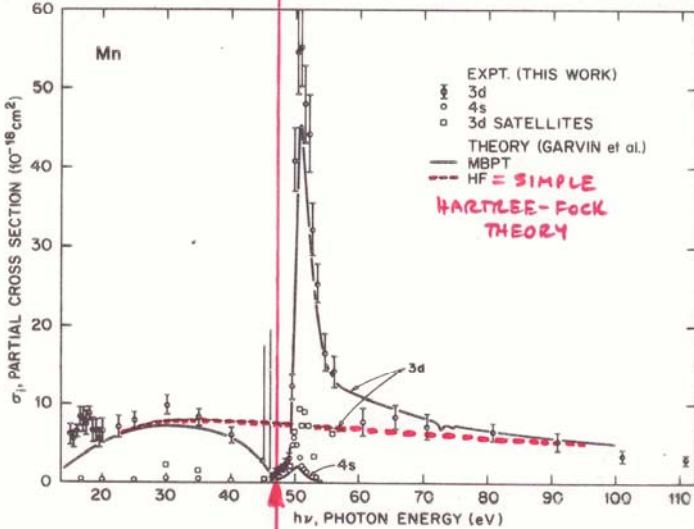


SINGLE-ATOM  
RESONANT  
PHOTOEMISSION:

$\beta_{3d}$



$\sigma_{3d}$



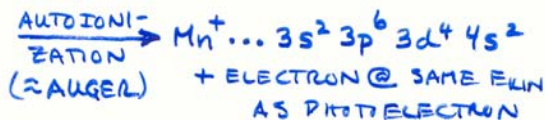
KRAUSE  
ET AL.,  
P.R.A  
30, 1316  
(84)

FIG. 2. Angular distribution parameter  $\beta$  of 3d photoelectrons (upper panel) and partial cross sections of 4s, 3d and satellite peaks (lower panel). Crosses ( $\times$ ) for  $\beta$  are from Ref. 3, theory from Ref. 6. The resonance near 50 eV is due to the  $3p \rightarrow 3d$  excitation into the partially filled 3d subshell of Mn.

$$h\nu = E_b^V(\text{Mn}3p)$$

RESONANT PROCESS:

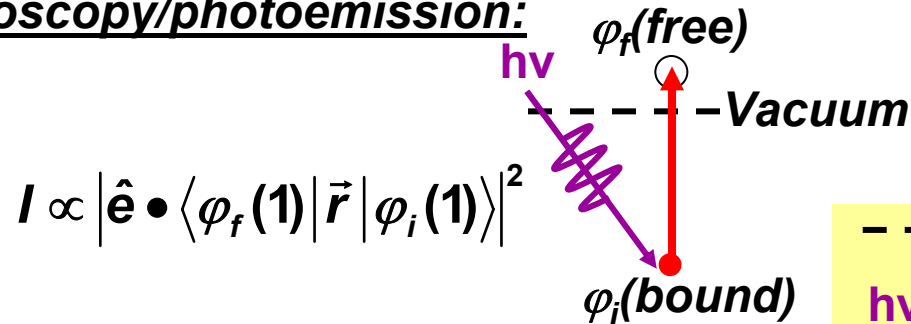
IF  $h\nu \approx E_b$  OF  $n\ell'$  SUBSHELL INSIDE OF  $n\ell$  SUBSHELL OF INTEREST (E.G., 3p FOR 3d), TWO "CHANNELS" COUPLE-



|| COUPLING MUCH ENHANCES CROSS SECTION ||

# MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: DIPOLE LIMIT

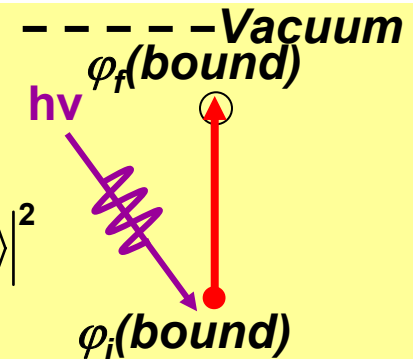
- Photoelectron spectroscopy/photoemission:



$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$

- Near-edge x-ray absorption:

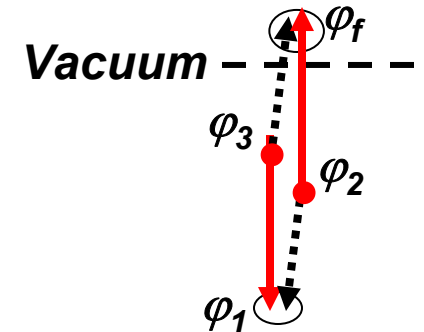
$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$



- Auger electron emission:

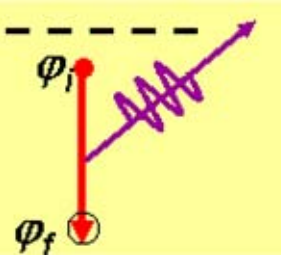
$$I \propto \left| \langle \varphi_f(\mathbf{1})\varphi_1(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_3(\mathbf{1})\varphi_2(\mathbf{2}) \rangle - \langle \varphi_1(\mathbf{1})\varphi_f(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_3(\mathbf{1})\varphi_2(\mathbf{2}) \rangle \right|^2$$

Direct Exchange



- X-ray emission:

$$I \propto |\hat{\mathbf{e}} \cdot \langle \varphi_f(\mathbf{1}) | \vec{r} | \varphi_i(\mathbf{1}) \rangle|^2$$

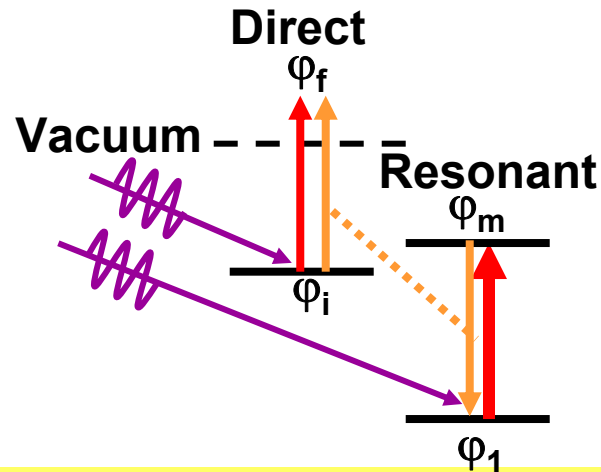


## MATRIX ELEMENTS IN THE SOFT X-RAY SPECTROSCOPIES: RESONANT EFFECTS

- Resonant photoemission:

$$I \propto \left| \langle \varphi_f(\mathbf{1}) | \hat{\mathbf{e}} \cdot \vec{r} | \varphi_i(\mathbf{1}) \rangle + \sum_m \langle \varphi_f(\mathbf{1}) \varphi_1(\mathbf{2}) | \frac{e^2}{r_{12}} | \varphi_i(\mathbf{1}) \varphi_m(\mathbf{2}) \rangle \langle \varphi_m(\mathbf{1}) | \hat{\mathbf{e}} \cdot \vec{r} | \varphi_1(\mathbf{1}) \rangle \right|^2$$

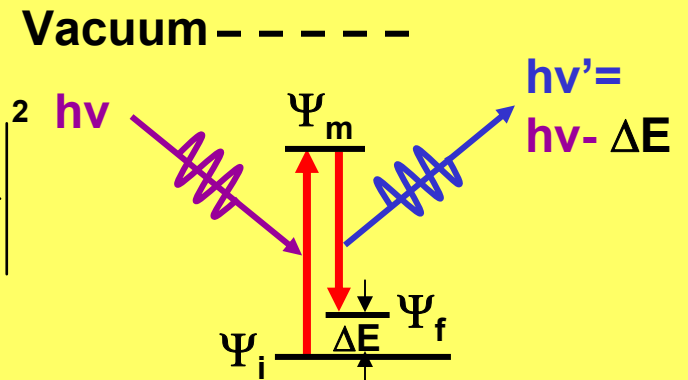
$$\times \delta(h\nu - (E_m - E_1))$$



- Resonant inelastic x-ray scattering:

$$I \propto \sum_f \left| \sum_m \frac{\langle \Psi_f(N) | \hat{\mathbf{e}} \cdot \vec{r} | \Psi_m(N) \rangle \langle \Psi_m(N) | \hat{\mathbf{e}} \cdot \vec{r} | \Psi_i(N) \rangle}{h\nu + E_i(N) - E_m(N) - i\Gamma} \right|^2$$

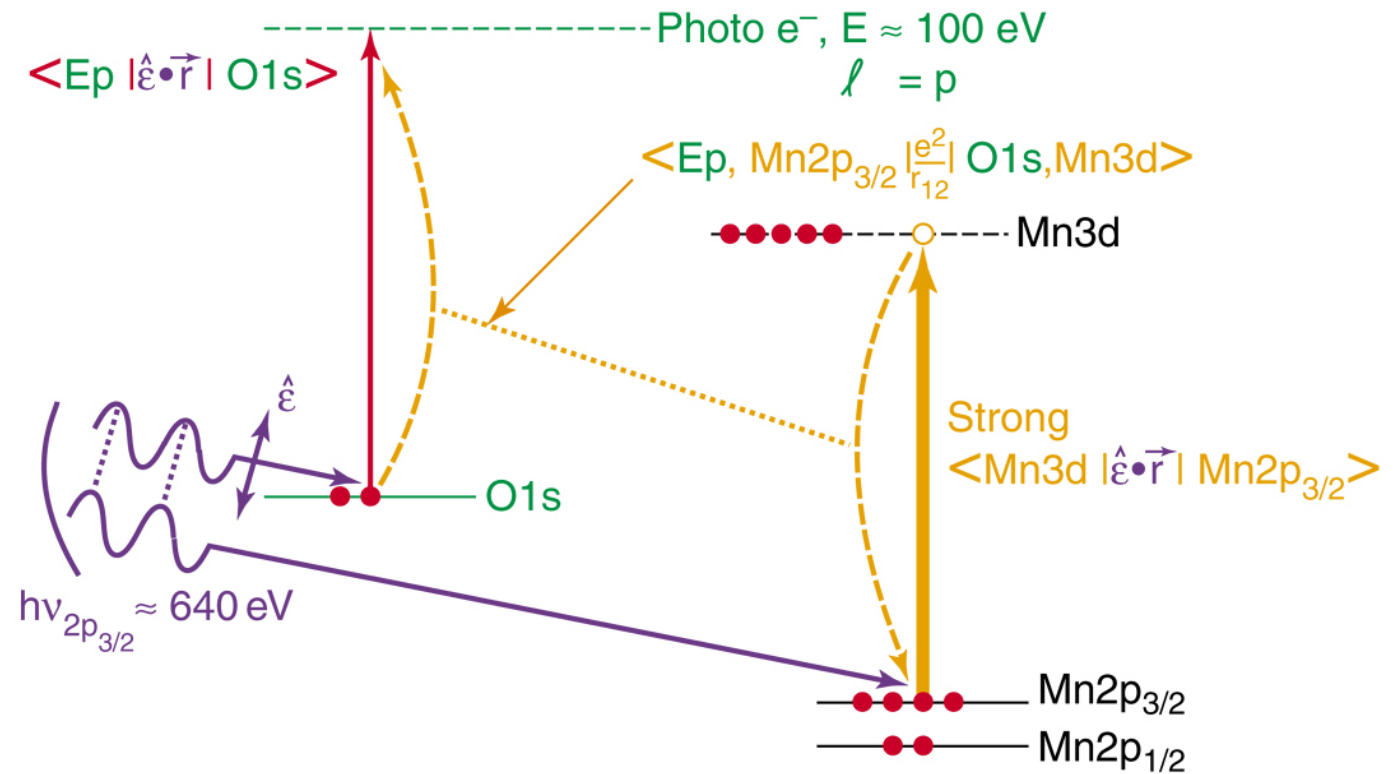
$$\times \delta(h\nu - (E_m(N) - E_i(N)))$$



# Multi-Atom Resonant Photoemission

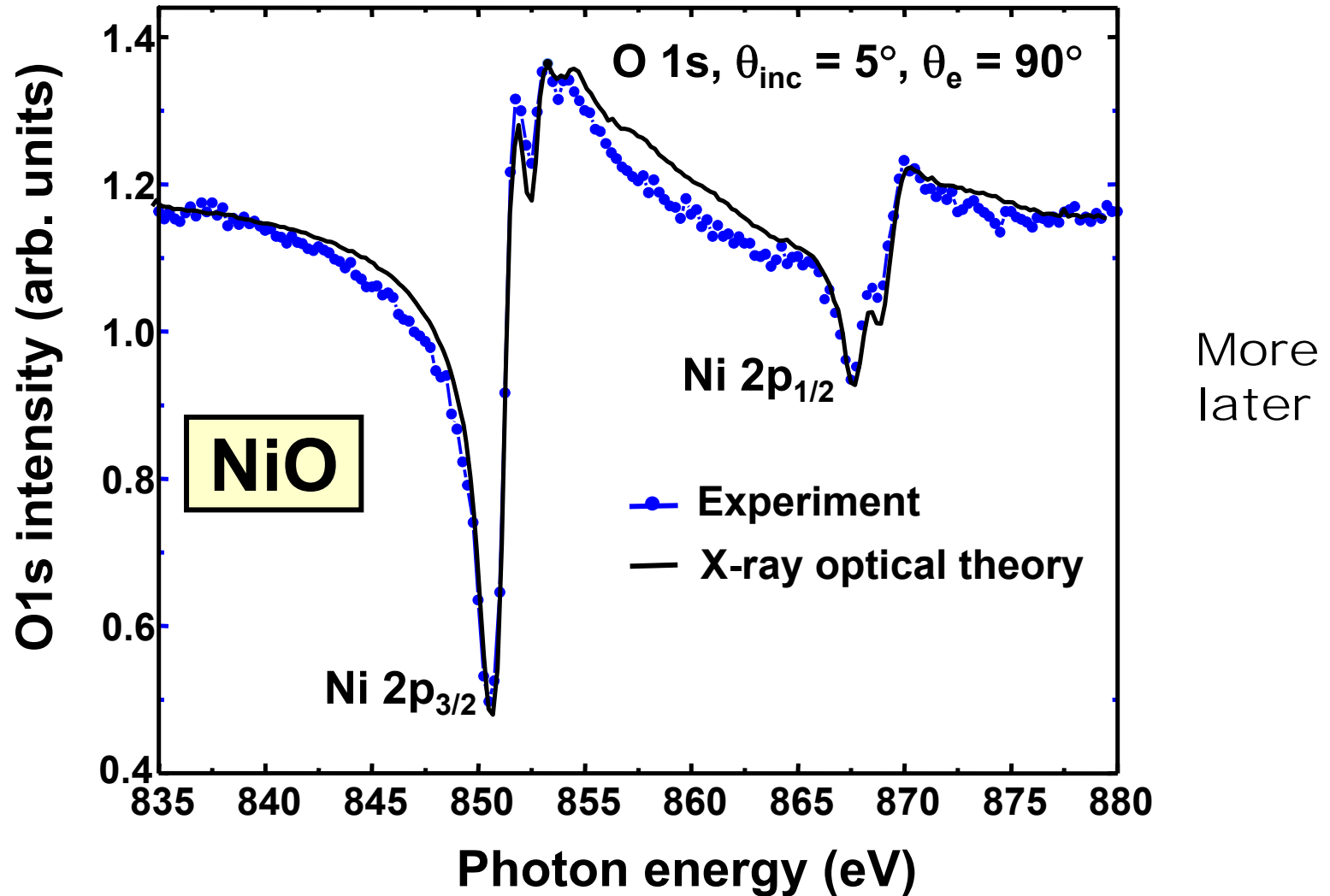
*Microscopic  
Q.M. picture*

Ex. – MnO(001): O1s emission, resonance with Mn2p<sub>3/2</sub>



Kay et al.,  
Science 281, 679 ('98);  
Corrected picture in  
PRB 61, 5119 ('01)←

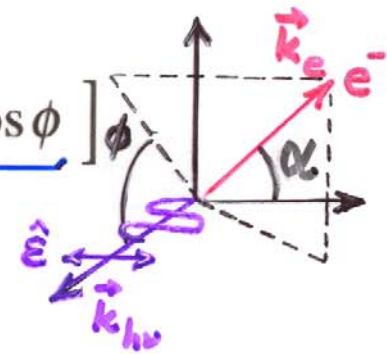
# Multi-Atom Resonant Photoemission— O 1s emission from NiO(001)



# Effects beyond the dipole approximation

The differential cross section for photoionization of randomly oriented target atoms by 100% linearly polarized photons has the form:

$$\frac{d\sigma}{d\Omega} = \left( \frac{\sigma}{4\pi} \right) \left[ \underbrace{1 + \beta P_2(\cos \alpha)}_{\text{DIPOLE}} + \underbrace{(\delta + \gamma \cos^2 \alpha) \sin \alpha \cos \phi}_{\text{NON-DIPOLE}} \right]$$



with:

$$P_2(\cos \alpha) = \frac{1}{2} (3 \cos^2 \alpha - 1)$$

$\sigma$ : angle integrated cross section

$\gamma$ : pole electron anisotropy parameter

$\beta$ : electron anisotropy parameter

$\delta$ : non-dipole electron anisotropy parameter

$$\exp(i \vec{k}_{h\nu} \cdot \vec{r}) = \underbrace{1}_{\text{DIPOLE}} + \underbrace{i \vec{k}_{h\nu} \cdot \vec{r} - \frac{1}{2} (\vec{k}_{h\nu} \cdot \vec{r})^2 + \dots}_{\text{NON-DIPOLE}}$$

Krause et al.  
Lindle et al.  
Krässig et al.

$$k_{h\nu} = 2\pi/\lambda_{h\nu} = 0.75 \text{ \AA}^{-1} @ 1.49 \text{ keV} \rightarrow k_{h\nu} \cdot [\langle r_{nl} \rangle \approx 1 \text{ \AA}] \approx 0.75 \text{—Non-dipole imp?}$$

$$0.075 \text{ \AA}^{-1} @ 149 \text{ eV} \rightarrow k_{h\nu} \cdot [\langle r_{nl} \rangle \approx 1 \text{ \AA}] \approx 0.075 \text{—Dipole ~OK}$$

**BEYOND THE DIPOLE APPROXIMATION?  
FREE-ATOM DIFFERENTIAL CROSS SECTIONS  
( KRAUSE, PHYS. REV. 177, 151 ('69)**

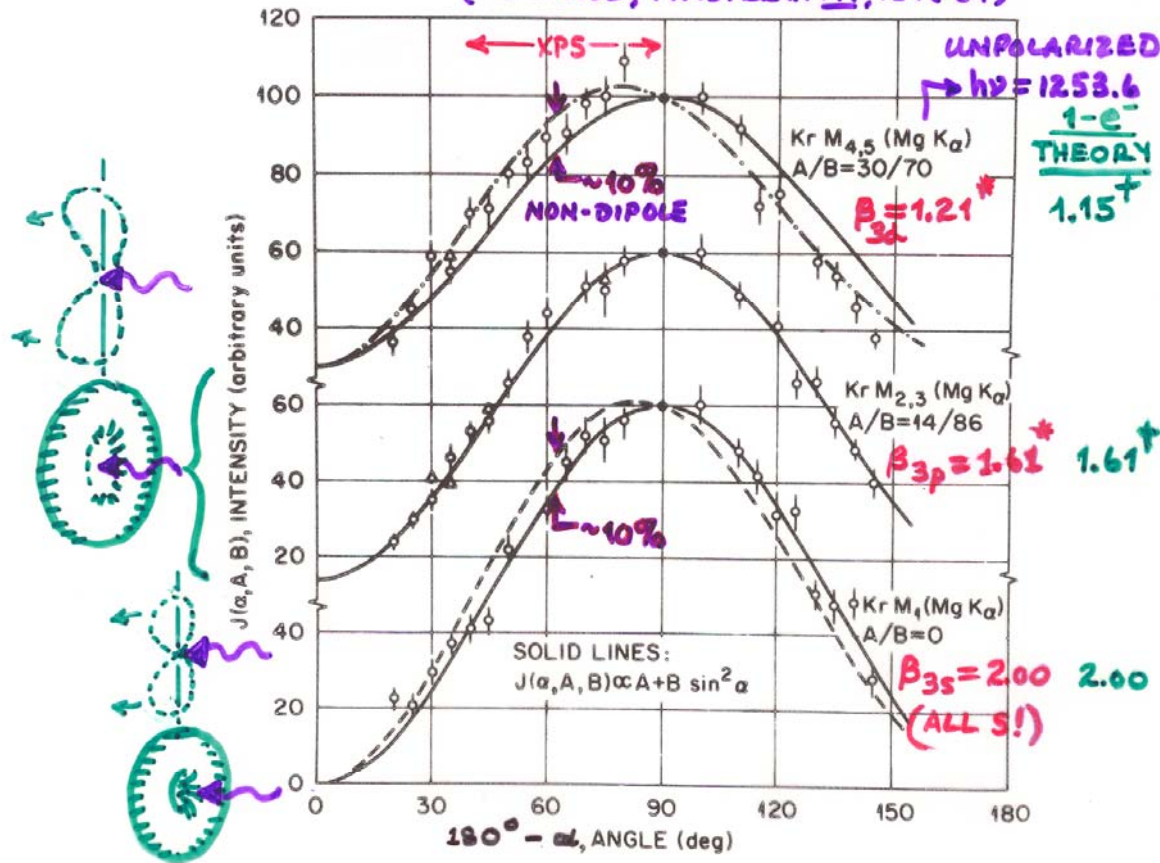


Figure 10 -- Experimental angular distributions of 3s (=  $M_1$ ), 3p (=  $M_{2,3}$ ), and 3d (=  $M_{4,5}$ ) photoelectrons excited from gaseous Kr with MgK $\alpha$  X-rays. The curves represent least-squares fits to the data points of a relationship of the form of Equation (93), in which A and B were treated as empirical constants. (From Krause, reference 142.)

\* FROM:  $\beta_{nl} = \frac{4B}{(3A+2B)}$   
 $= \frac{4}{(3A/B+2)}$

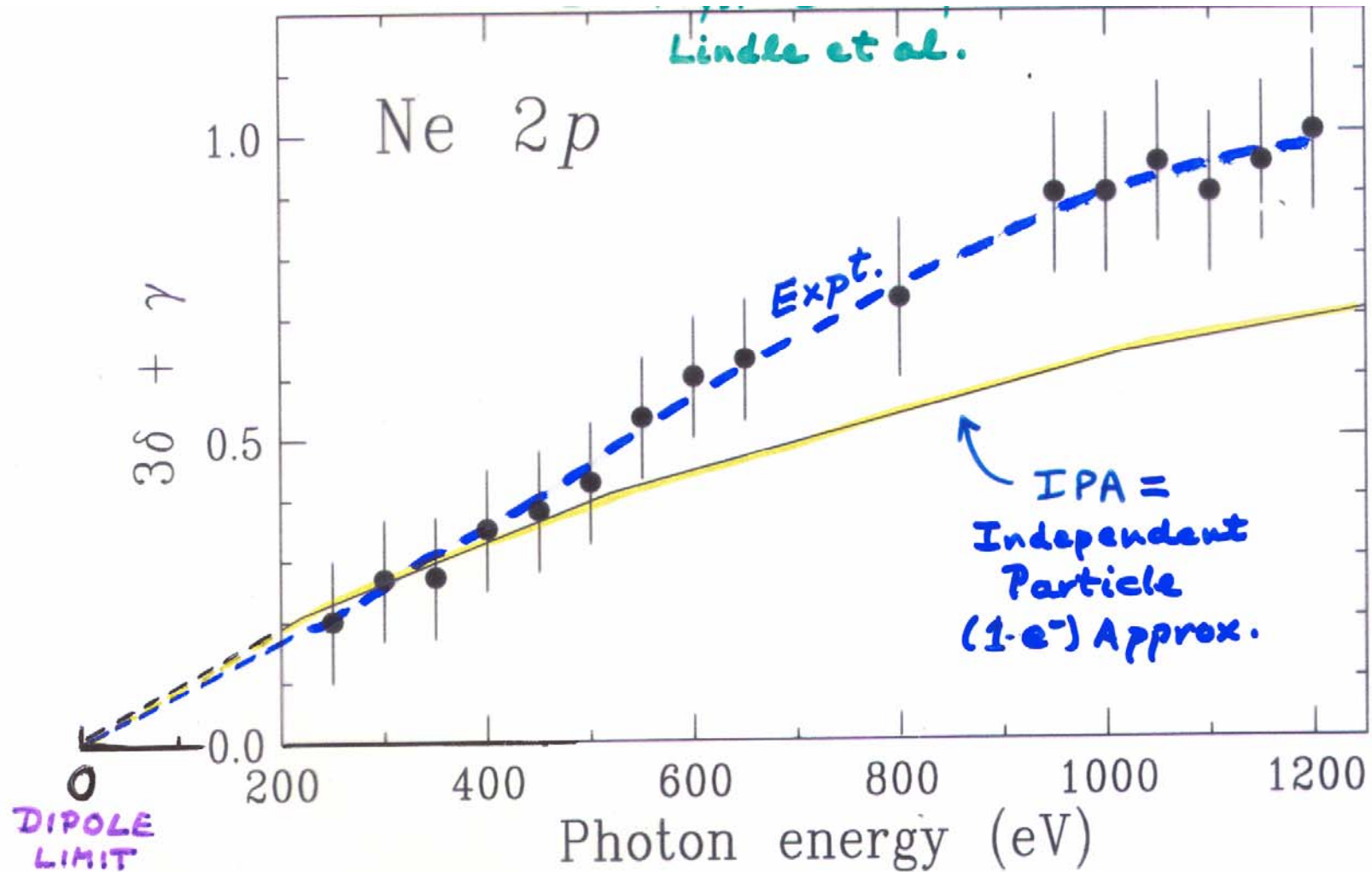
NEAR EQ. 93;  
 FADLEY, "BASIC  
 CONCEPTS OF XPS"

† FROM YEH  
 & LINDAU  
 TABLES

"Basic Concepts of XPS"  
 Figure 10

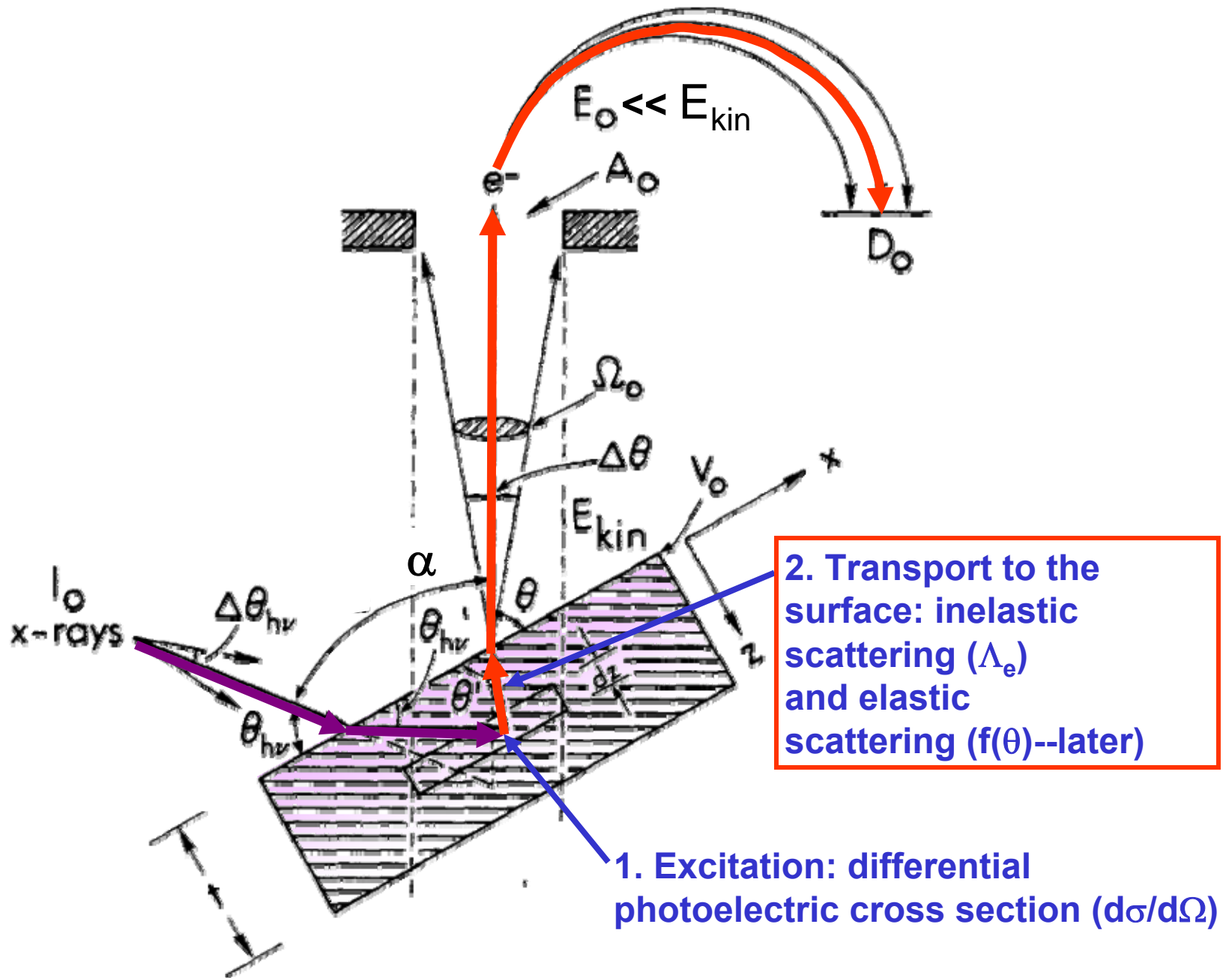


# Non-dipole effects in 2p emission from Ne



+ see Phys. Rev. Lett. 78, 4553 (1997): Lindle et al.  
" " " 75, 4736 (1995): Krässig et al.

# PHOTOELECTRON INTENSITIES—THE 3-STEP MODEL

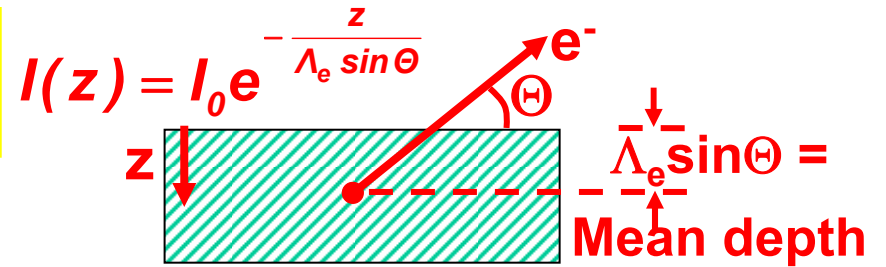
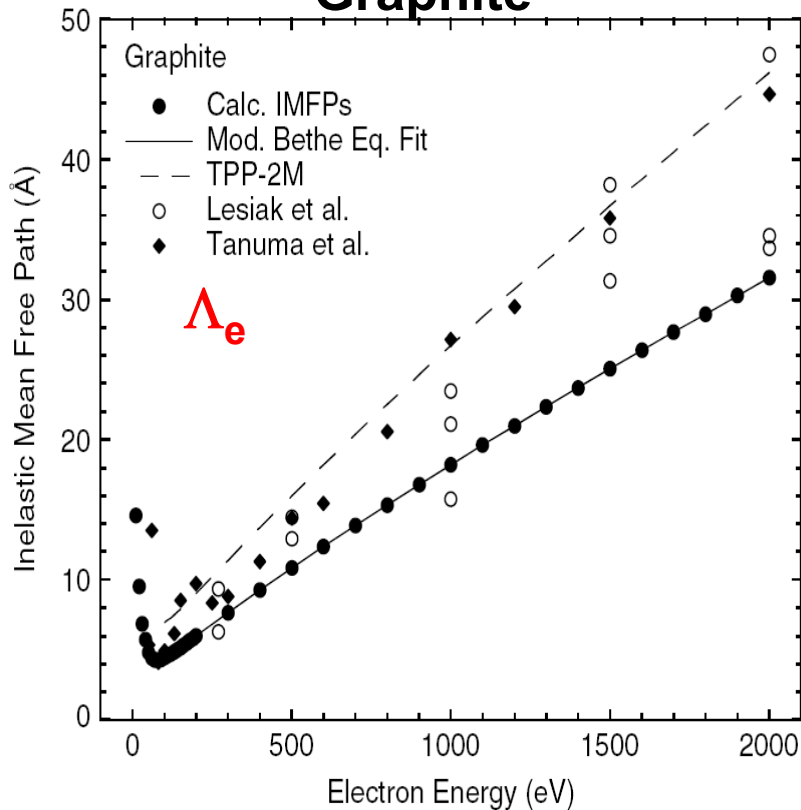


# Electron inelastic attenuation length in solids—the “universal curve”

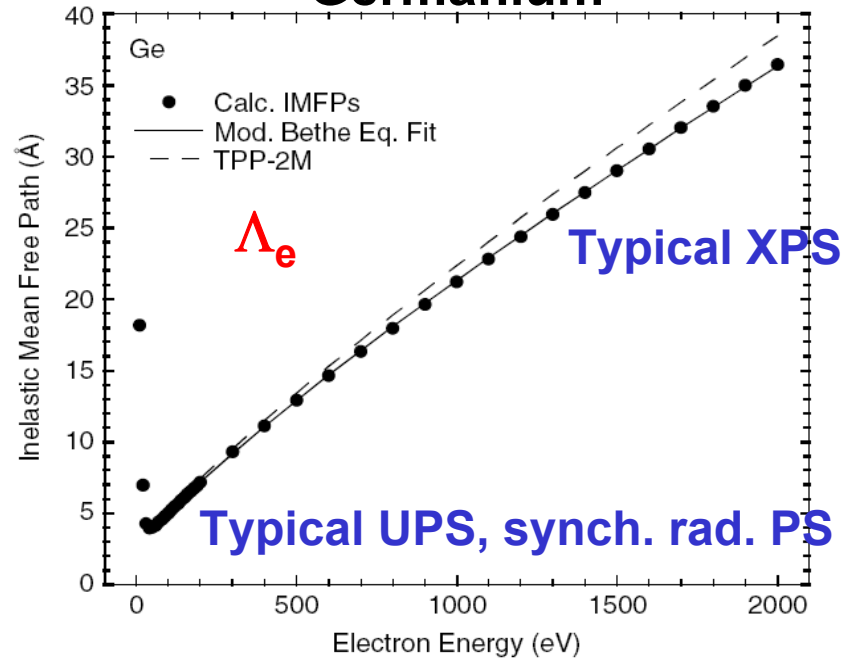
## Photoemission is a surface sensitive experiment

Changing angle:  
1st way to vary surface sensitivity

### Graphite



### Germanium



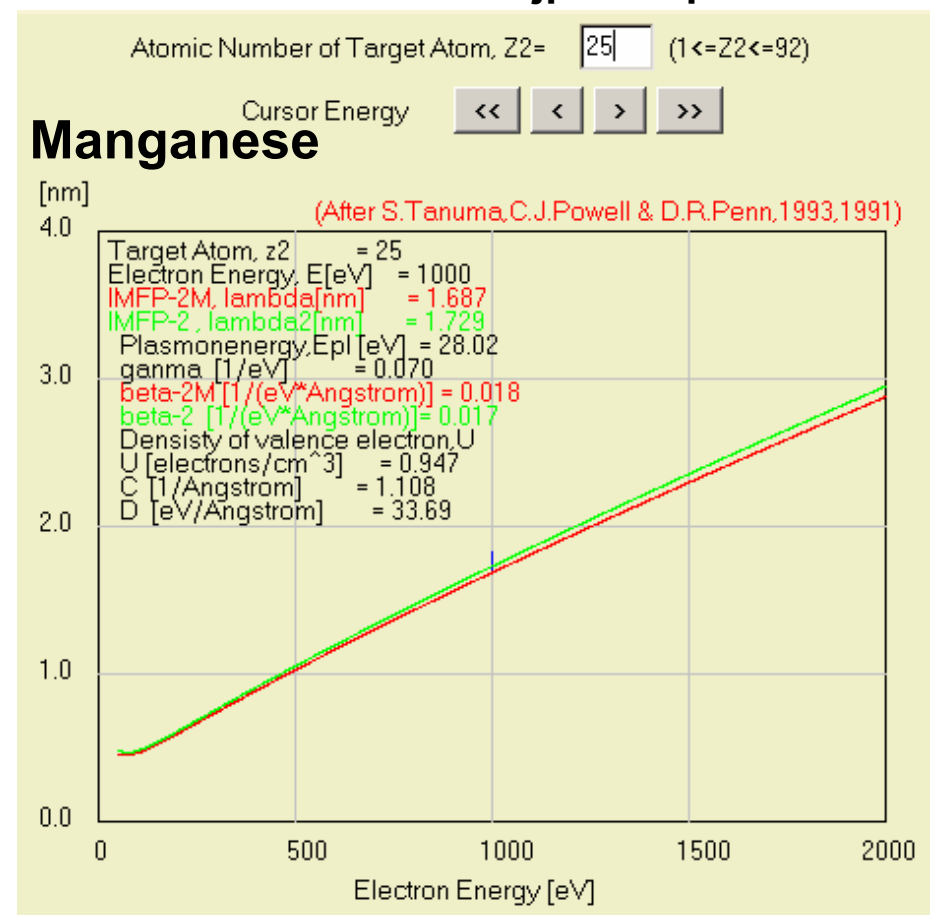
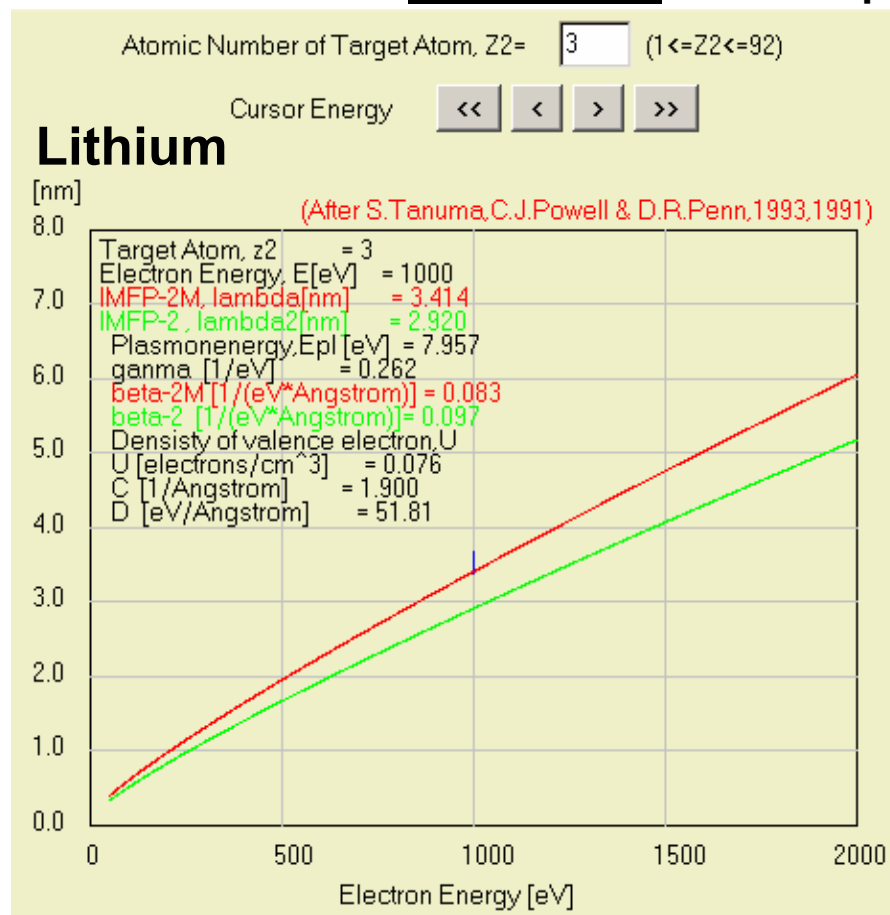
Changing photon energy:  
2nd way to vary surface sensitivity

# Inelastic mean free paths in solids

Database of experimental and theoretically estimated mean free paths at <http://www.nist.gov/srd/webguide/nist71/71imfp.htm#elements>

Plus estimation with the **TPP-2M** (TPP-2) formula of Tanuma, Powell, Penn:

Web calculation for elements from: <http://www.ss.teen.setsunan.ac.jp/e-imfp2.html>



# Inelastic mean free paths in solids

*Estimation from the **TPP-2M** formula: any compound*

$$\Lambda_e \approx \lambda = \frac{E}{E_p^2 [\beta \ln(\gamma E) - (C/E) + (D/E^2)]}$$

where

$$\beta = -0.10 + 0.944/(E_p^2 + E_g^2)^{1/2} + 0.069\rho^{0.1}$$

$$\gamma = 0.191\rho^{-0.50}$$

$$C = 1.97 - 0.91U$$

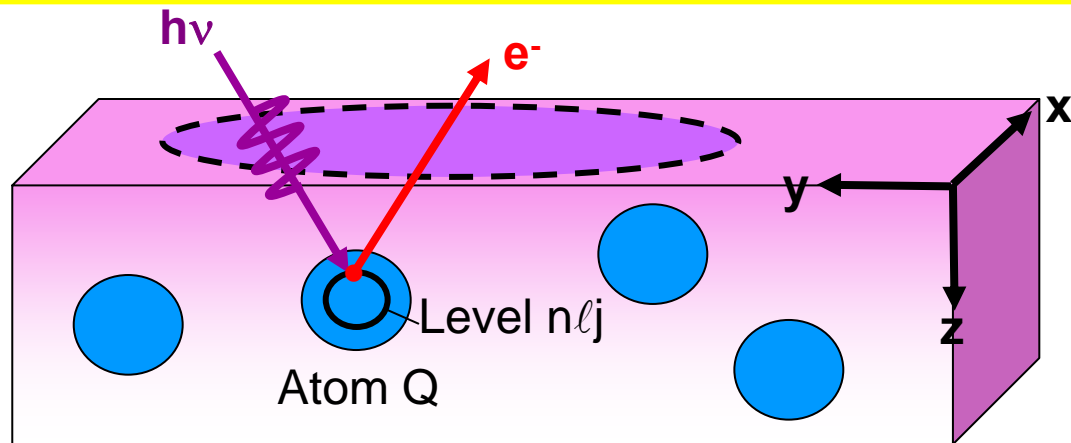
$$D = 53.4 - 20.8U$$

$$U = N_v \rho / M = E_p^2 / 829.4$$

and  $E_p = 28.8 (N_v \rho / M)^{1/2}$  is the free-electron plasmon energy (in eV),  $\rho$  is the density (in g cm<sup>-3</sup>),  $N_v$  is the number of valence electrons per atom (for an element) or molecule (for a compound),  $M$  is the atomic or molecular weight, and  $E_g$  is the bandgap energy (in eV). These equations are collectively known as the **TPP-2M** equation.

Tanuma, Powell, Penn, Surf. Interface Anal. 21, 165 (1994)

# CORE PHOTOELECTRON INTENSITIES AND COMPOSITION



$$I(Qn\ell j) =$$

$$C \int_0^{\infty} I_0(x,y,z) \rho_Q(x,y,z) \frac{d\sigma_{Qn\ell j}(h\nu)}{d\Omega} \exp\left[-\frac{z}{\Lambda_e \sin\theta}\right] \Omega(h\nu, x, y) dx dy dz$$

$$I_{h\nu}(x,y,z) = \text{x-ray flux}$$

$\rho_Q(x,y,z)$  = density of atoms Q → quantitative analysis

$$\frac{d\sigma_{Qn\ell j}(h\nu)}{d\Omega} = \text{differential photoelectric cross section for subshell } Qn\ell j$$

$\Lambda_e$  = inelastic attenuation length

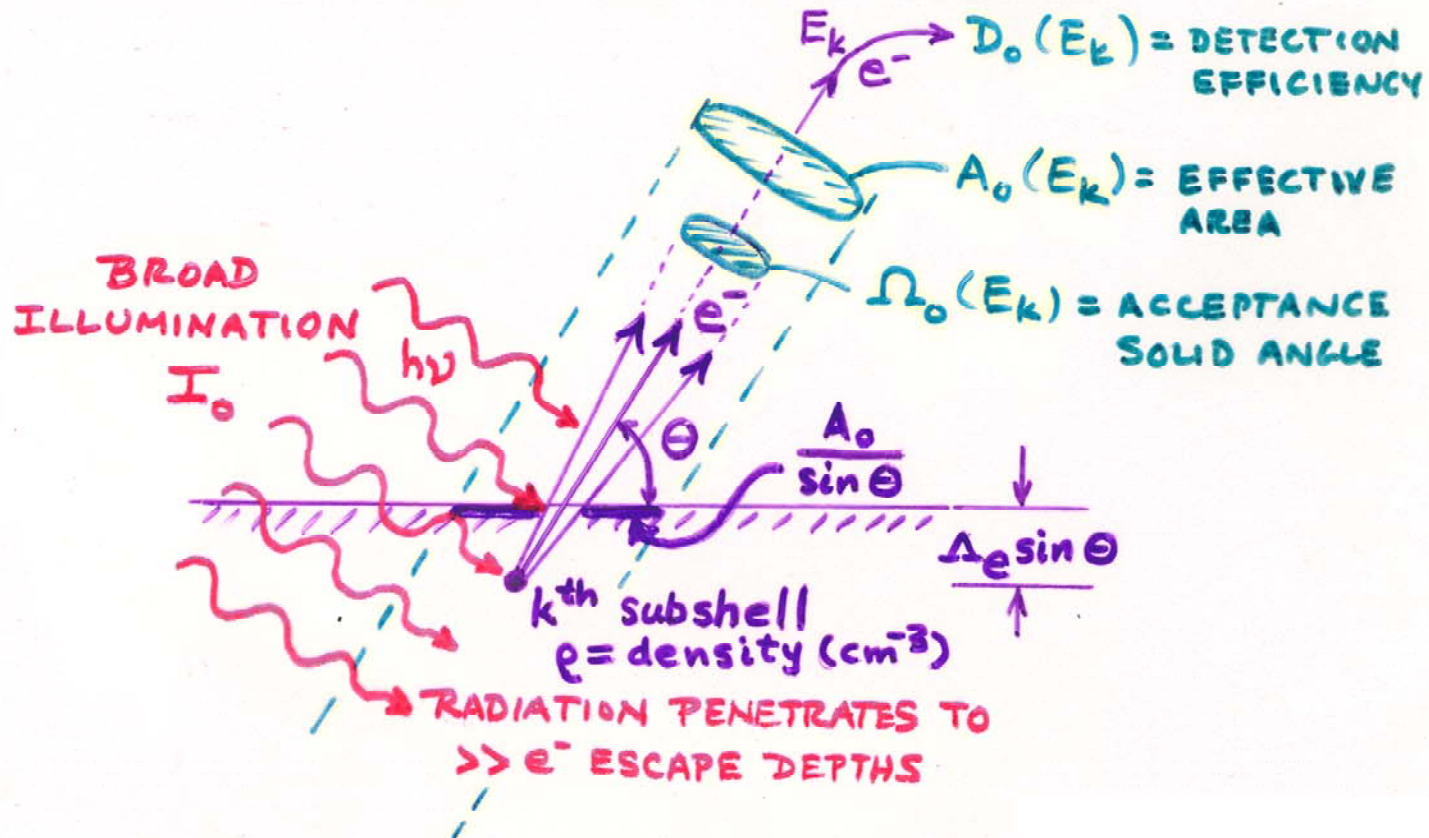
$\Omega(h\nu, x, y)$  = spectrometer acceptance solid angle

## PHOTOELECTRON INTENSITIES FOR SOME USEFUL CASES

(a) Semi-infinite specimen, atomically clean surface, peak  $k$  with  $E_{kin} \equiv E_k$ :

$$N_k(\theta) = I_0 \Omega_0(E_k) A_0(E_k) D_0(E_k) \rho \, d\sigma_k/d\Omega \, \Lambda_e(E_k) \quad \left( \begin{array}{c} \text{NO} \\ \Theta \\ \text{DEP.} \end{array} \right) \quad (115)$$

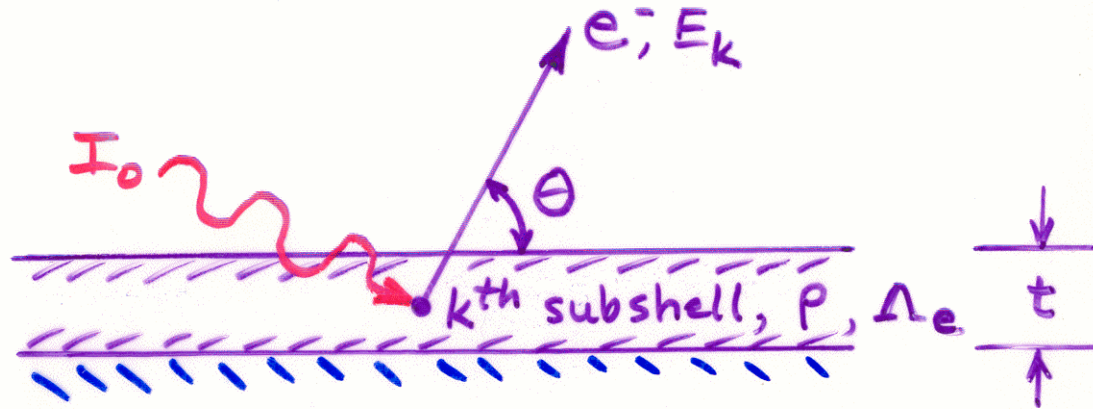
This case corresponds to an optimal measurement on a homogeneous specimen for which no surface contaminant layer is present.



(b) Specimen of thickness  $t$ , atomically clean surface, peak  $k$  with  $E_{\text{kin}} \equiv E_k$ :

$$N_k(\theta) = I_0 \Omega_0(E_k) A_0(E_k) D_0(E_k) \rho \frac{d\sigma_k}{d\Omega} \Lambda_e(E_k) \times [1 - \exp(-t/\Lambda_e(E_k) \sin \theta)] \quad (116)$$

Here, the intensity of a peak originating in a specimen of finite thickness is predicted to increase with decreasing  $\theta$ .





(c) Semi-infinite substrate with uniform overlayer of thickness  $t$  -  
 Peak  $k$  from substrate with  $E_{k1n} \equiv E_k$ :

$$N_k(\theta) = I_0 \Omega_0(E_k) A_0(E_k) D_0(E_k) \rho \, d\sigma_k/d\Omega \, \Lambda_e(E_k) \times \exp(-t/\Lambda_e'(E_k) \sin \theta) \quad (117)$$

Peak  $l$  from overlayer with  $E_{l1n} \equiv E_l$ :

$$N_l(\theta) = I_0 \Omega_0(E_l) A_0(E_l) D_0(E_l) \rho' \, d\sigma_l/d\Omega \, \Lambda_e'(E_l) \times [1 - \exp(-t/\Lambda_e'(E_l) \sin \theta)] \quad (118)$$

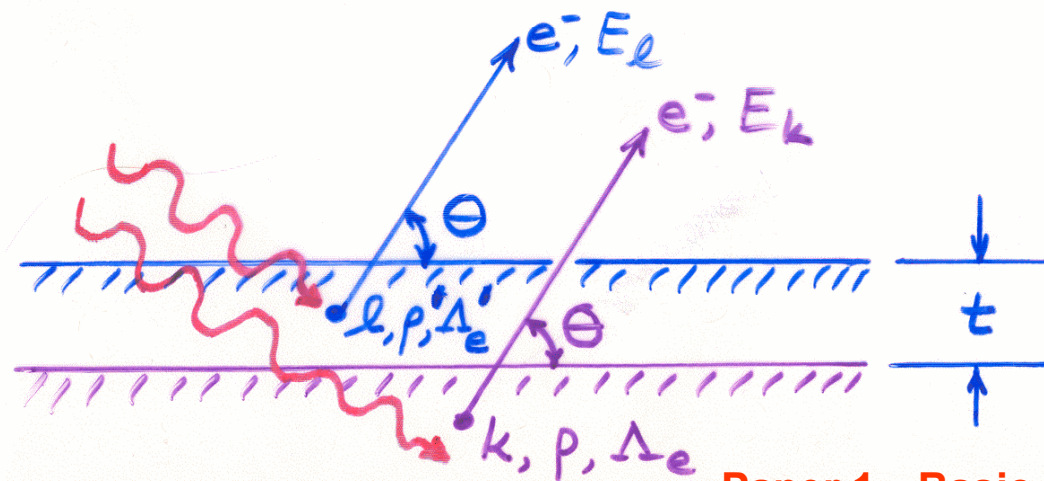
where

$\Lambda_e(E_k)$  = an attenuation length in the substrate

$\Lambda_e'(E_k)$  = an attenuation length in the overlayer

$\rho$  = an atomic density in the substrate

$\rho'$  = an atomic density in the overlayer.



(d) Semi-infinite substrate with a non-attenuating overlayer at fractional monolayer coverage—Peak  $k$  from substrate: Eq. (115).

Peak  $l$  from overlayer:

$$N_l(\theta) = I_0 \Omega_0(E_l) A_0(E_l) D_0(E_l) s' (d\sigma_l/d\Omega) (\sin \theta)^{-1} \quad (120a)$$

Overlayer/substrate ratio:

$$\begin{aligned} \frac{N_l(\theta)}{N_k(\theta)} &= \frac{\Omega_0(E_l) A_0(E_l) D_0(E_l) s' (d\sigma_l/d\Omega)}{\Omega_0(E_k) A_0(E_k) D_0(E_k) s (d\sigma_k/d\Omega) (\Lambda_e(E_k) \sin \theta/d)} \\ &= \left[ \frac{s'}{s} \right] \cdot \frac{D_0(E_l) \Omega_0(E_l) A_0(E_l) (d\sigma_l/d\Omega) d}{D_0(E_k) \Omega_0(E_k) A_0(E_k) (d\sigma_k/d\Omega) \Lambda_e \sin \theta} \end{aligned} \quad (120b)$$

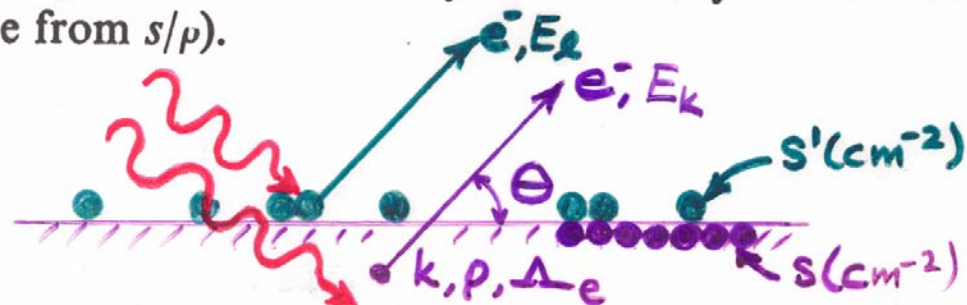
with

$s'$  = the mean surface density of atoms in which peak  $l$  originates in  $\text{cm}^{-2}$

$s$  = the mean surface density of substrate atoms in  $\text{cm}^{-2} \equiv \rho_s$

$s'/s$  = the fractional monolayer coverage of the atomic species in which peak  $l$  originates

$d$  = the mean separation between layers of density  $s$  in the substrate (calculable from  $s/\rho$ ).



**Table 4 Density and atomic concentration**

The data are given at atmospheric pressure and room temperature, or at the stated temperature in deg K. (Crystal modifications as for Table 3.)

<b>H</b> <sup>4K</sup> 0.088																	<b>He</b> <sup>2K</sup> 0.205 (at 37 atm)																																																																																																																
<b>Li</b> <sup>78K</sup> 0.542 4.700 3.023	<b>Be</b> 1.82 12.1 2.22	<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="border: 1px solid black; background-color: yellow; padding: 5px;"> <b>Atomic radius</b>  <math>= r_{MT}</math>  <math>= 0.5 \text{ n-n dist.}</math> </div> <div style="border: 1px solid black; background-color: yellow; padding: 5px;"> <b>Average surface density</b>  <math>= \rho_S = (\rho_V)^{2/3}</math> </div> </div>										<b>B</b> 2.47 13.0	<b>C</b> 3.516 17.6 1.54	<b>N</b> <sup>20K</sup> 1.03	<b>O</b>	<b>F</b> 1.44	<b>Ne</b> <sup>4K</sup> 1.51 4.36 3.16																																																																																																																
<b>Na</b> <sup>5K</sup> 1.013 2.652 3.659	<b>Mg</b> 1.74 4.30 3.20	Density in g cm <sup>-3</sup> (10 <sup>3</sup> kg m <sup>-3</sup> ) Concentration in 10 <sup>22</sup> cm <sup>-3</sup> (10 <sup>28</sup> m <sup>-3</sup> ) Nearest-neighbor distance, in Å (10 <sup>-10</sup> m)										<b>Al</b> 2.70 6.02 2.86	<b>Si</b> 2.33 5.00 2.35	<b>P</b>	<b>S</b>	<b>Cl</b> <sup>93K</sup> 2.03 2.02	<b>Ar</b> <sup>4K</sup> 1.77 2.66 3.76																																																																																																																
<b>K</b> <sup>5K</sup> 0.910 1.402 4.525	<b>Ca</b> 1.53 2.30 3.95	<b>Sc</b> 2.99 4.27 3.25	<b>Ti</b> 4.51 5.66 2.89	<b>V</b> 6.09 7.22 2.62	<b>Cr</b> 7.19 8.33 2.50	<b>Mn</b> 7.47 8.18 2.24	<b>Fe</b> 7.87 8.50 2.48	<b>Co</b> 8.9 8.97 2.50	<b>Ni</b> 8.91 9.14 2.49	<b>Cu</b> 8.93 8.45 2.56	<b>Zn</b> 7.13 6.55 2.66	<b>Ga</b> 5.91 5.10 2.44	<b>Ge</b> 5.32 4.42 2.45	<b>As</b> 5.77 4.65 3.16	<b>Se</b> 4.81 3.67 2.32	<b>Br</b> <sup>123K</sup> 4.05 2.36	<b>Kr</b> <sup>4K</sup> 3.09 2.17 4.00																																																																																																																
<b>Rb</b> <sup>5K</sup> 1.629 1.148 4.837	<b>Sr</b> 2.58 1.78 4.30	<b>Y</b> 4.48 3.02 3.55	<b>Zr</b> 6.51 4.29 3.17	<b>Nb</b> 8.58 5.56 2.86	<b>Mo</b> 10.22 6.42 2.72	<b>Tc</b> 11.50 7.04 2.71	<b>Ru</b> 12.36 7.36 2.65	<b>Rh</b> 12.42 7.26 2.69	<b>Pd</b> 12.00 6.80 2.75	<b>Ag</b> 10.50 5.85 2.89	<b>Cd</b> 8.65 4.64 2.98	<b>In</b> 7.29 3.83 3.25	<b>Sn</b> 5.76 2.91 2.81	<b>Sb</b> 6.69 3.31 2.91	<b>Te</b> 6.25 2.94 2.86	<b>I</b> 4.95 2.36 3.54	<b>Xe</b> <sup>4K</sup> 3.78 1.64 4.34																																																																																																																
<b>Cs</b> <sup>5K</sup> 1.997 0.905 5.235	<b>Ba</b> 3.59 1.60 4.35	<b>La</b> 6.17 2.70 3.73	<b>Hf</b> 13.20 4.52 3.13	<b>Ta</b> 16.66 5.55 2.86	<b>W</b> 19.25 6.30 2.74	<b>Re</b> 21.03 6.80 2.74	<b>Os</b> 22.58 7.14 2.68	<b>Ir</b> 22.55 7.06 2.71	<b>Pt</b> 21.47 6.62 2.77	<b>Au</b> 19.28 5.90 2.88	<b>Hg</b> <sup>227</sup> 14.26 4.26 3.01	<b>Tl</b> 11.87 3.50 3.46	<b>Pb</b> 11.34 3.30 3.50	<b>Bi</b> 9.80 2.82 3.07	<b>Po</b> 9.31 2.67 3.34	<b>At</b> —	<b>Rn</b> —																																																																																																																
<b>Fr</b> —	<b>Ra</b> —	<b>Ac</b> 10.07 2.66 3.76	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th>Ce</th><th>Pr</th><th>Nd</th><th>Pm</th><th>Sm</th><th>Eu</th><th>Gd</th><th>Tb</th><th>Dy</th><th>Ho</th><th>Er</th><th>Tm</th><th>Yb</th><th>Lu</th> </tr> </thead> <tbody> <tr> <td>6.77</td><td>6.78</td><td>7.00</td><td>—</td><td>7.54</td><td>5.25</td><td>7.89</td><td>8.27</td><td>8.53</td><td>8.80</td><td>9.04</td><td>9.32</td><td>6.97</td><td>9.84</td> </tr> <tr> <td>2.91</td><td>2.92</td><td>2.93</td><td>—</td><td>3.03</td><td>2.04</td><td>3.02</td><td>3.22</td><td>3.17</td><td>3.22</td><td>3.26</td><td>3.32</td><td>3.02</td><td>3.39</td> </tr> <tr> <td>3.65</td><td>3.63</td><td>3.66</td><td>—</td><td>3.59</td><td>3.96</td><td>3.58</td><td>3.52</td><td>3.51</td><td>3.49</td><td>3.47</td><td>3.54</td><td>3.88</td><td>3.43</td> </tr> <tr> <th>Th</th><th>Pa</th><th>U</th><th>Np</th><th>Pu</th><th>Am</th><th>Cm</th><th>Bk</th><th>Cf</th><th>Es</th><th>Fm</th><th>Md</th><th>No</th><th>Lr</th> </tr> <tr> <td>11.72</td><td>15.37</td><td>19.05</td><td>20.45</td><td>19.81</td><td>11.87</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td> </tr> <tr> <td>3.04</td><td>4.01</td><td>4.80</td><td>5.20</td><td>4.26</td><td>2.96</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td> </tr> <tr> <td>3.60</td><td>3.21</td><td>2.75</td><td>2.62</td><td>3.1</td><td>3.61</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td> </tr> </tbody> </table>															Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu	6.77	6.78	7.00	—	7.54	5.25	7.89	8.27	8.53	8.80	9.04	9.32	6.97	9.84	2.91	2.92	2.93	—	3.03	2.04	3.02	3.22	3.17	3.22	3.26	3.32	3.02	3.39	3.65	3.63	3.66	—	3.59	3.96	3.58	3.52	3.51	3.49	3.47	3.54	3.88	3.43	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr	11.72	15.37	19.05	20.45	19.81	11.87	—	—	—	—	—	—	—	—	3.04	4.01	4.80	5.20	4.26	2.96	—	—	—	—	—	—	—	—	3.60	3.21	2.75	2.62	3.1	3.61	—	—	—	—	—	—	—	—
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu																																																																																																																				
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# Surface sensitivity enhancement for grazing exit angles

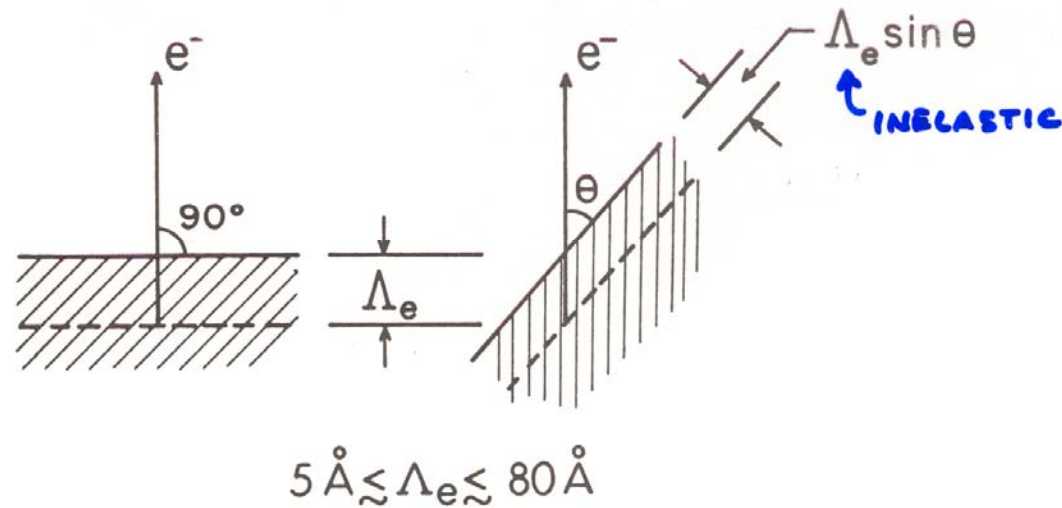


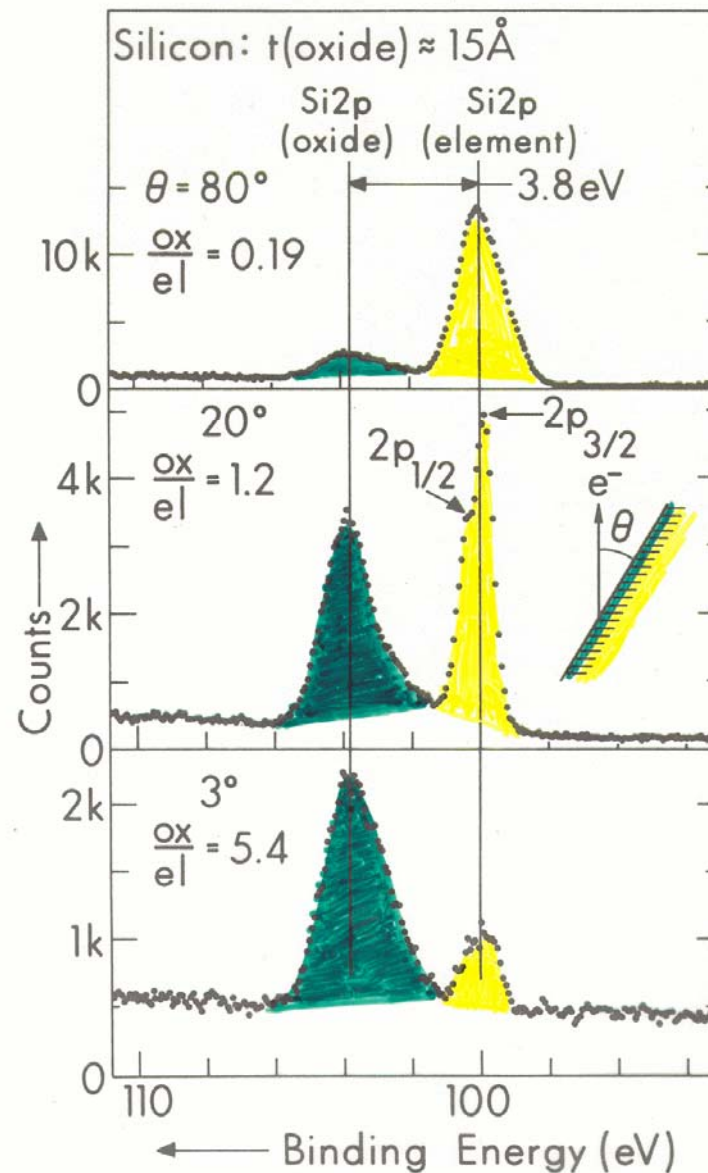
Fig. 5. Illustration of the basic mechanism producing surface sensitivity enhancement for low electron exit angles  $\theta$ . The average depth for no-loss emission as measured perpendicular to the surface is  $\Lambda_e \sin \theta$ .

E.g. -  $\Lambda_e = 28 \text{ \AA}$  in Au(s) at 1400 eV

$\theta$	Mean Depth	No. layers
"BULK" $\rightarrow 90^\circ$	28 $\text{\AA}$	$\sim 9$
"SURFACE" $\rightarrow 10^\circ$	$\sim 4.4 \text{ \AA}$	$\sim 1.5$

... BUT REFRACTION AT SURFACE AND ELASTIC SCATTERING CAN REDUCE SURFACE ENHANCEMENT, ESP. AT LOW  $\theta \leq 30^\circ$

**Surface  
sensitivity  
enhancement  
for grazing exit  
angles**



**Fadley, Progress in Surface Science, 16, 275 ('84)**

Fig. 7. Si<sub>2p</sub> spectra at three electron exit angles for a Si specimen with a 15-Å thick oxide overlayer. Note the complete reversal of the relative intensities of oxide and element between high and low  $\theta$ . (From Hill et al., ref. (19).)

# Surface sensitivity enhancement for grazing exit angles

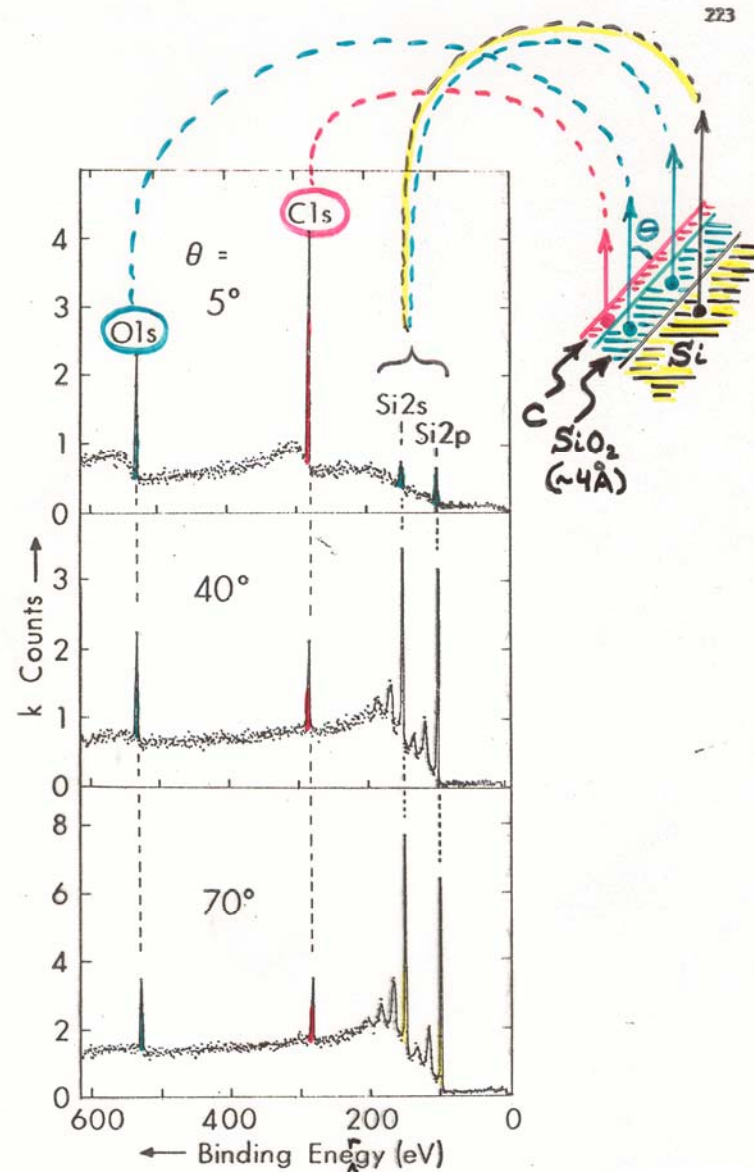
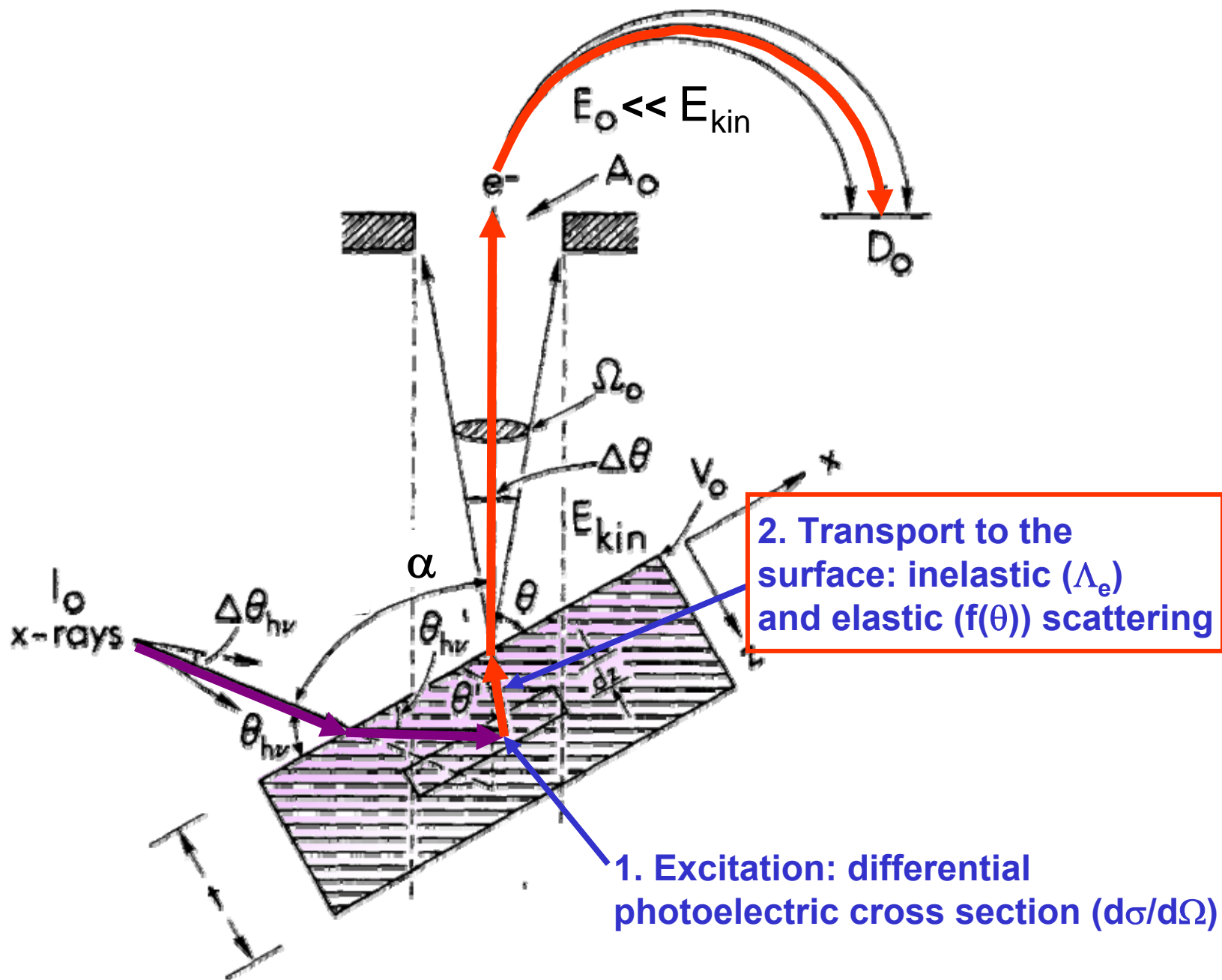


Figure 44 -- Broad-scan core spectra at low and high exit angles for a Si specimen with a thin oxide overlayer ( $\sim 4\text{\AA}$ ) and an outermost carbon contaminant overlayer approximately 1-2 monolayers in thickness. The C1s and O1s signals are markedly enhanced in relative intensity at low  $\theta$  due to the general effect presented in Figure 43. (From Falley, reference 17.)

# PHOTOELECTRON INTENSITIES—THE 3-STEP MODEL



EFFECTS OF ELASTIC SCATTERING ON ANGULAR DISTRIBUTIONS: POLYCRYSTALLINE OR AMORPHOUS SAMPLE

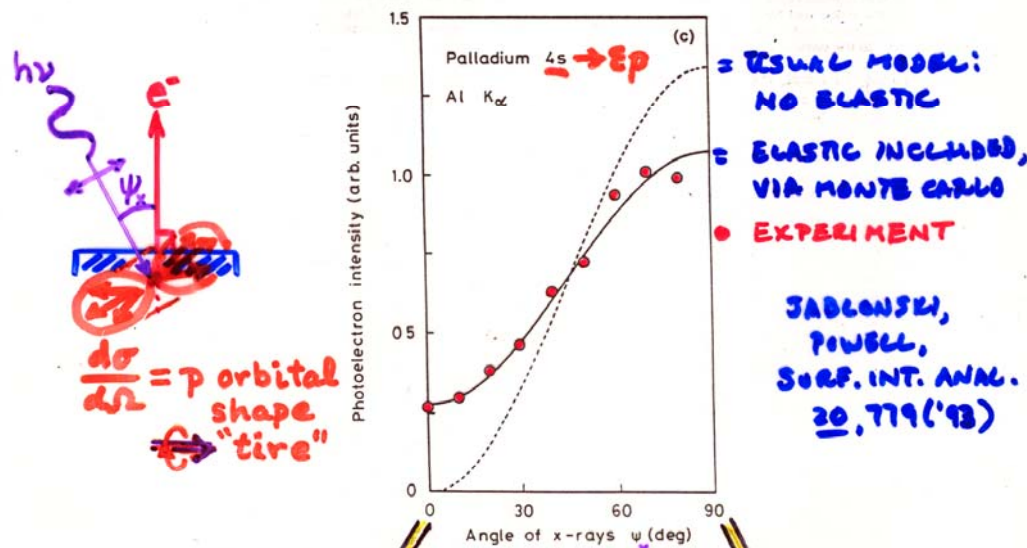
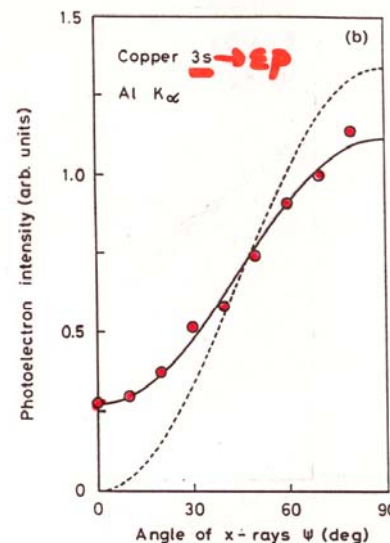
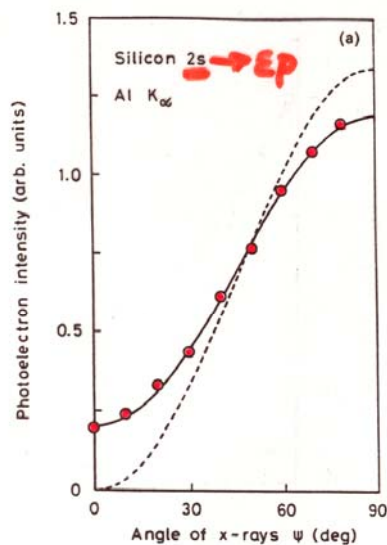
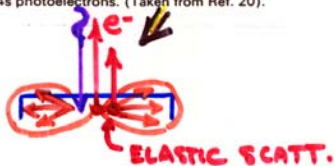
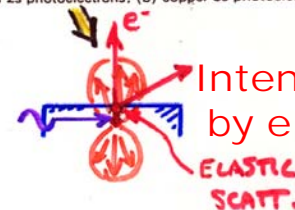


Figure 4. Dependence of the photoelectron intensity emitted normal to the surface on the angle of Al  $K_{\alpha}$  x-rays with respect to the direction of analysis. Circles and solid line: Monte Carlo calculations accounting for elastic collisions of photoelectrons; dashed line: result of common simple formalism of XPS in which elastic collisions are neglected. (a) Silicon 2s photoelectrons; (b) copper 3s photoelectrons; (c) palladium 4s photoelectrons. (Taken from Ref. 20).

Intensity increased by elastic scattering

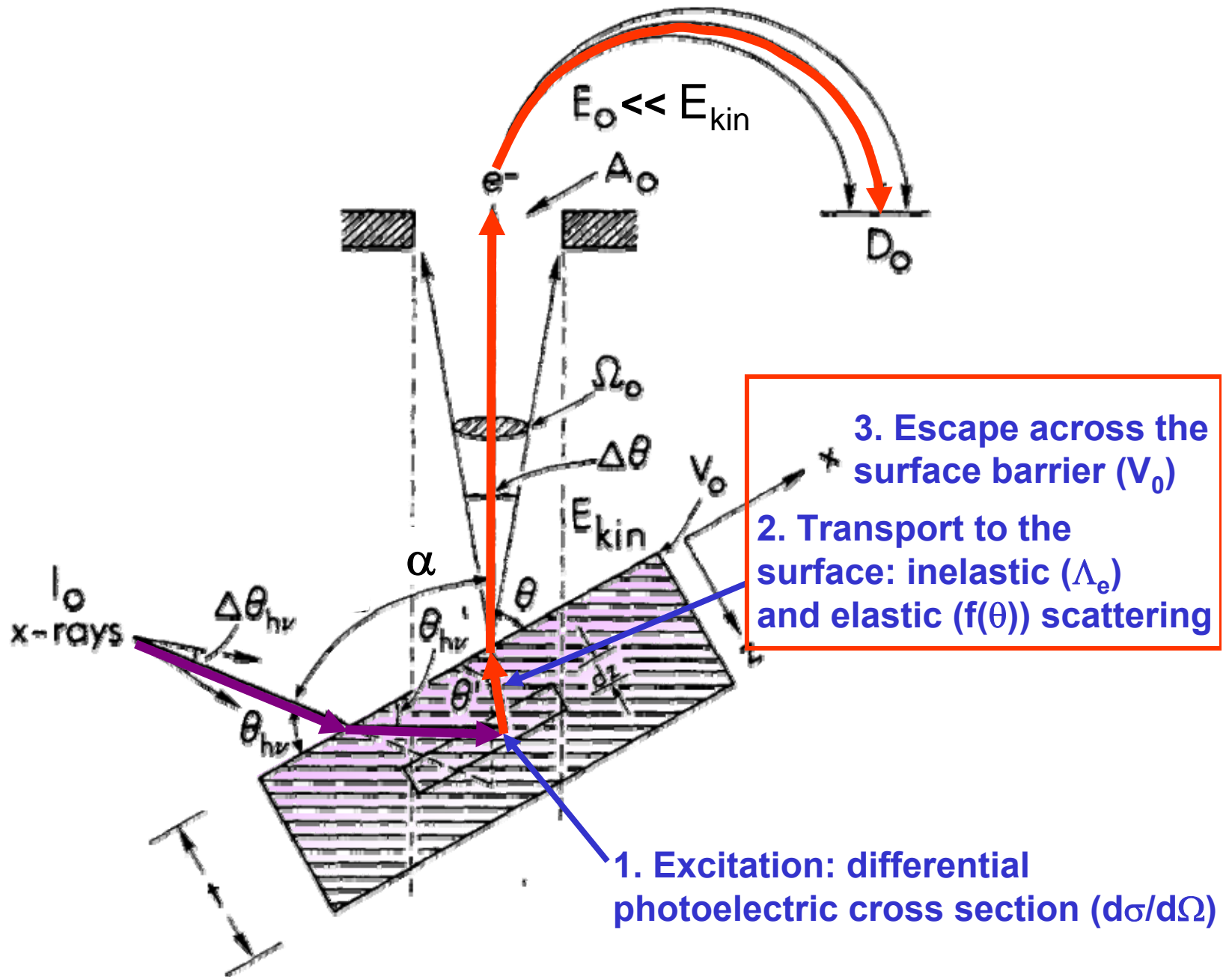


Intensity decreased by elastic scatt.

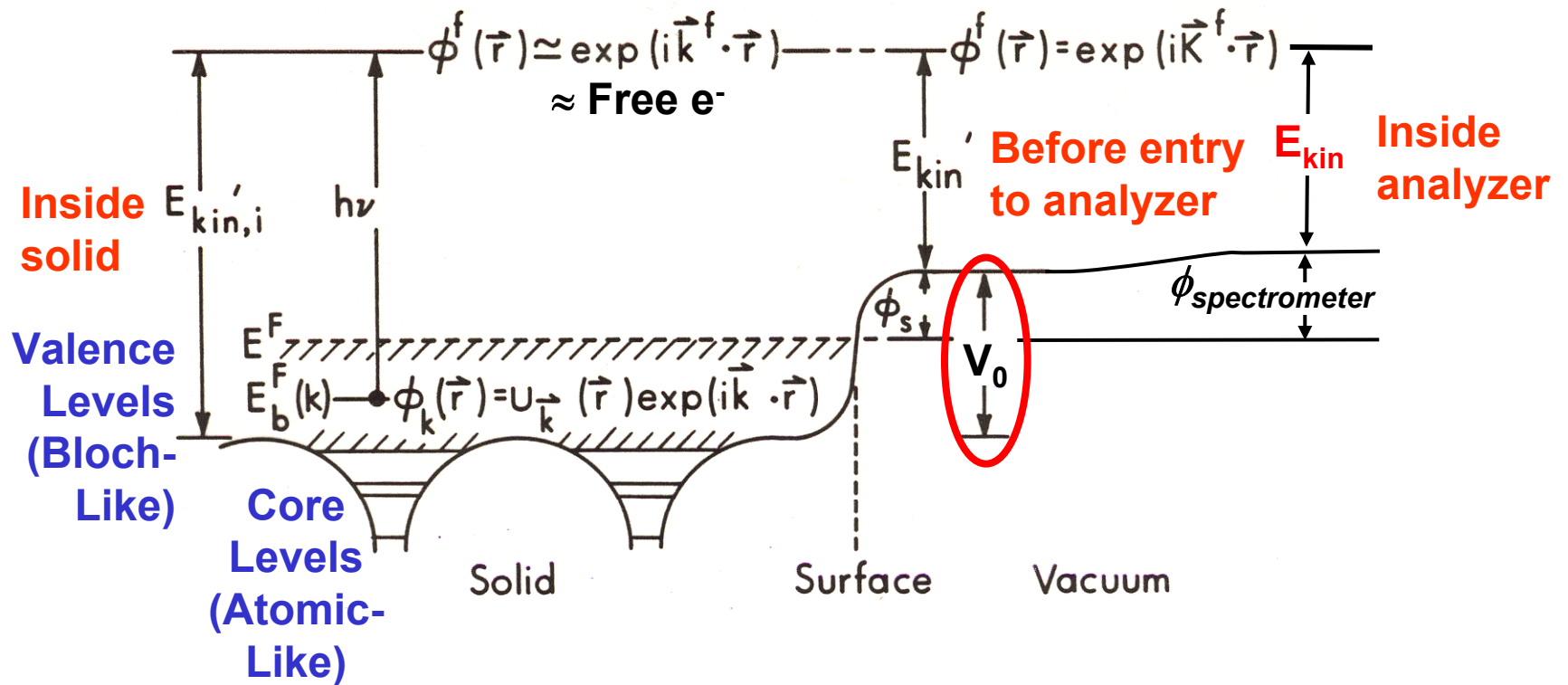




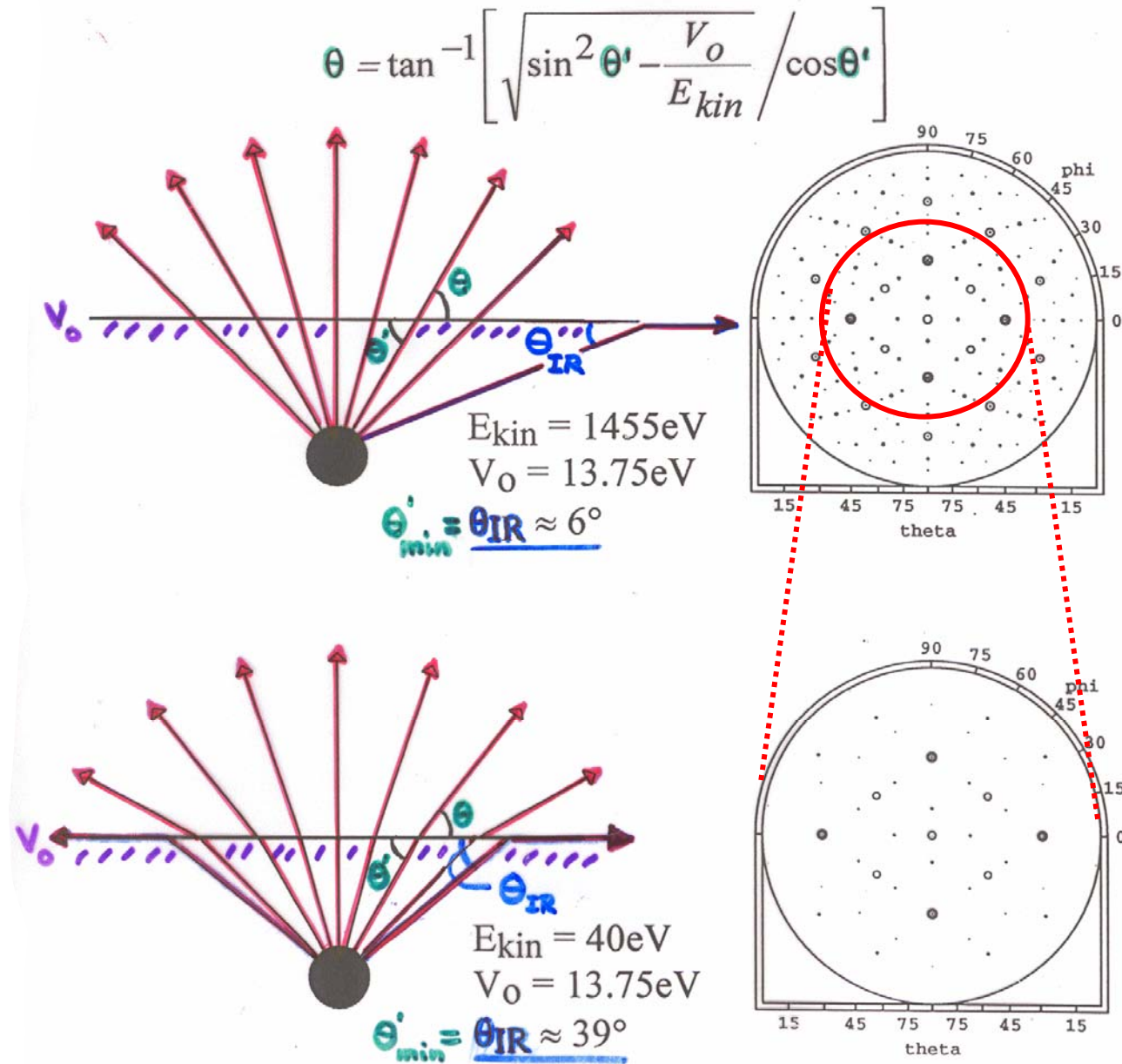
# PHOTOELECTRON INTENSITIES—THE 3-STEP MODEL



# One-Electron Picture of Photoemission from a Surface



# Electron Refraction at the Surface Due to the Inner Potential



**Observed  
 Low-Index  
 Directions  
 Above  
 W(110)**

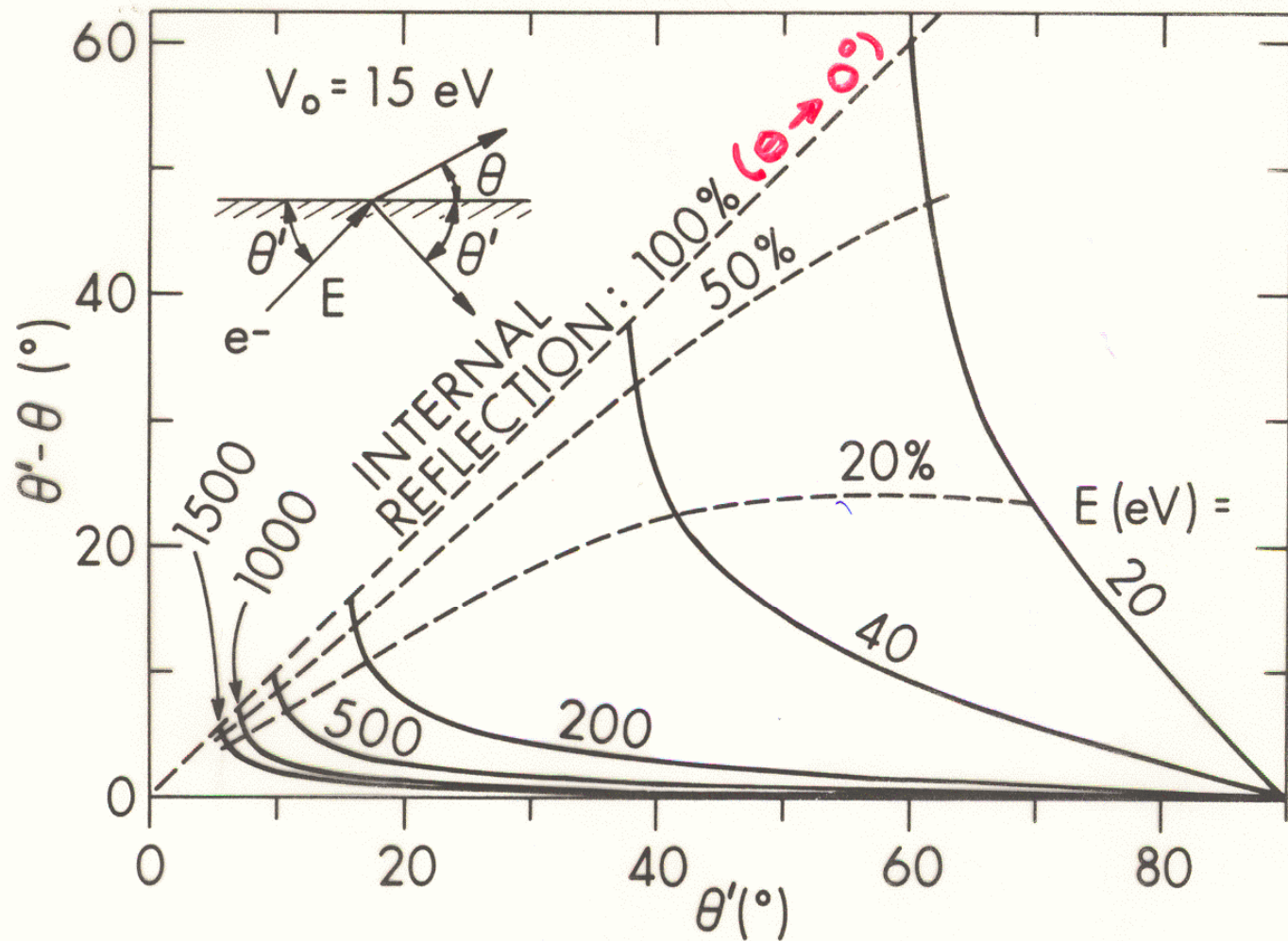


Fig. 14. Calculation of electron refraction effects for different electron kinetic energies and a typical  $V_0$  value of 15eV. The degree of refraction is indicated by the difference  $\theta'$  (internal)  $- \theta$  (external). Contours of equal probability of internal reflection are also shown. (From ref. (5).)

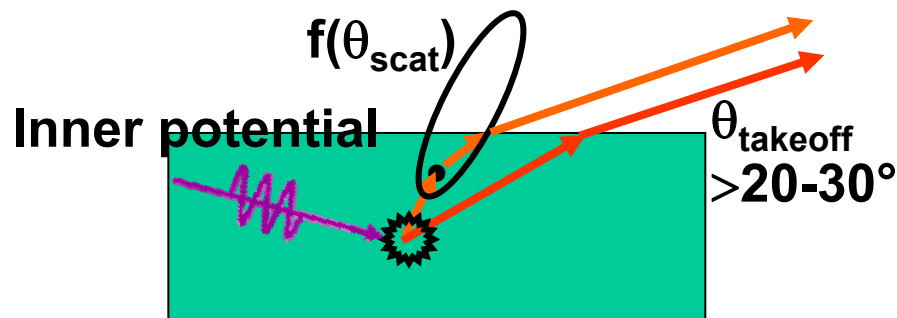
## Varying surface sensitivity for lower electron takeoff angles

Simplest interpretation:

$$\text{Average emission depth} = \Lambda_{\text{inelastic}} \sin \theta_{\text{takeoff}}$$

How valid?

$$E_{\text{kin}} \approx 500\text{-}1000 \text{ eV}$$



E.g.: A. Jablonski and C. J. Powell,  
J. Vac. Sci. Tech. A 21, 274 (2003):  
→ Mean Emission Depth (MED)  
more relevant than  $\Lambda_{\text{inelastic}}$

# Varying surface sensitivity for lower electron takeoff angles

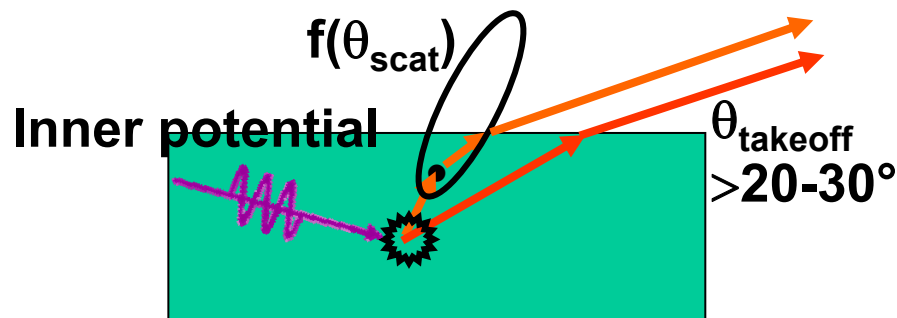
Simplest interpretation:

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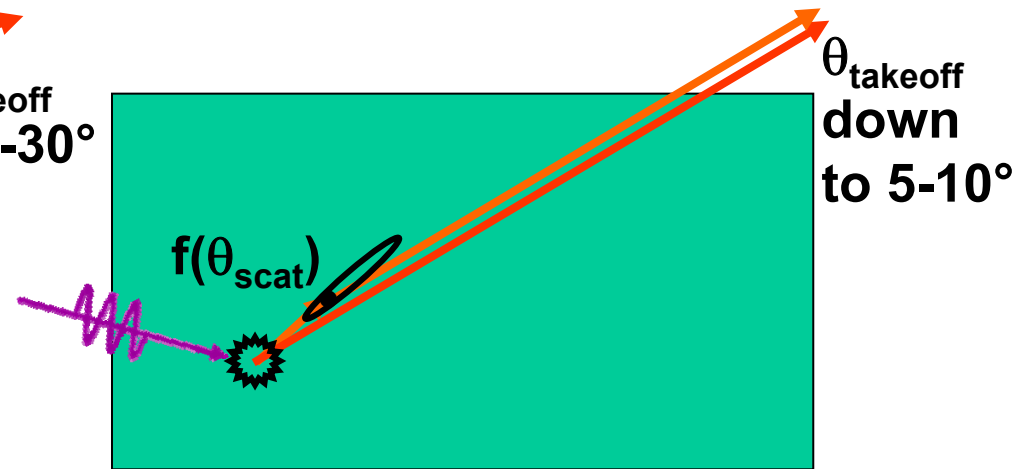
How valid?

$E_{\text{kin}} \approx 500-1000 \text{ eV}$

$E_{\text{kin}} \approx 10,000 \text{ eV}$



E.g.: A. Jablonski and C. J. Powell,  
J. Vac. Sci. Tech. A 21, 274 (2003):  
→ Mean Emission Depth (MED)  
more relevant than  $\Lambda_{\text{inelastic}}$

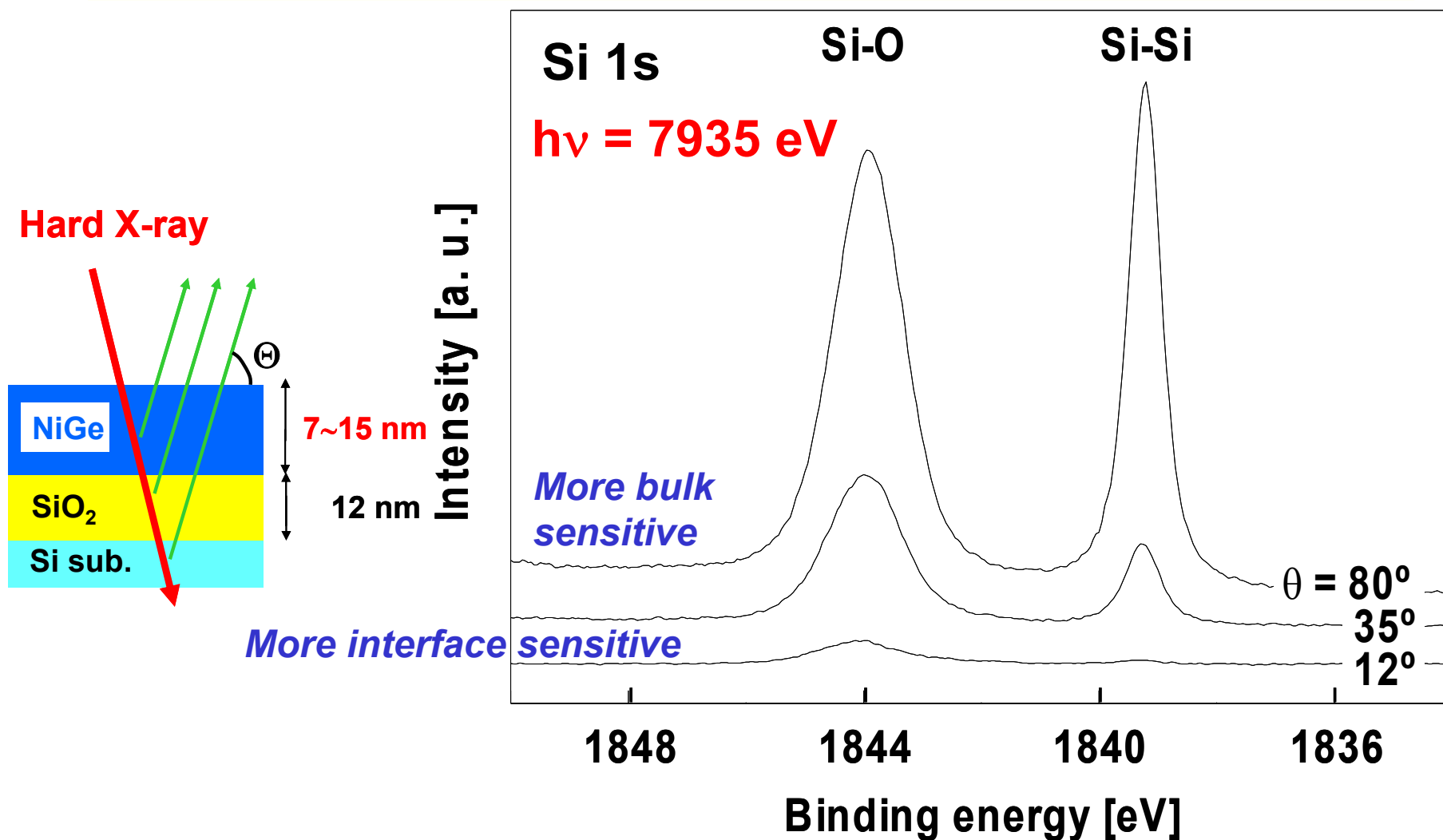


**Simpler analysis**

**Cleaner bulk & surface distinction**

C. J. Powell, W. Werner et al., priv. comm.;  
C.S.F., Nucl. Inst. & Meth. A 547, 24 (2005)

# Variable takeoff-angle Si 1s photoelectron spectra from NiGe(12-nm)/SiO<sub>2</sub>(12-nm)/Si(100)



T. Hattori et al., *Int. J. High Speed Electronics* 16 (2006) 353  
SPRING8-Japan

# Outline

**Surface, interface, and nanoscience—short introduction**

**Some surface concepts and techniques→photoemission**

**Synchrotron radiation: experimental aspects**

**Electronic structure—a brief review**

**The basic synchrotron radiation techniques  
+Instrumentation for PS and XES**

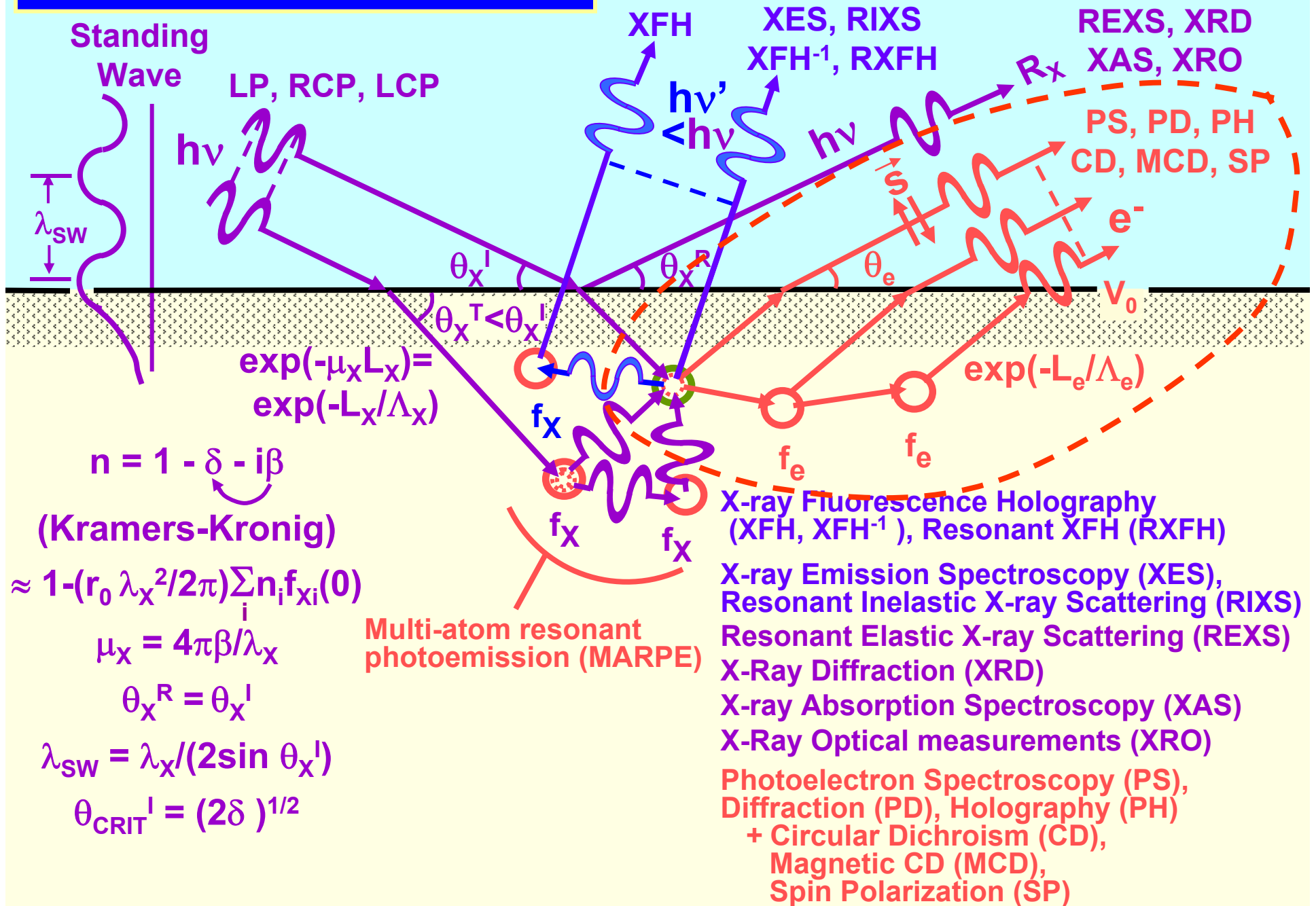
**→ Core-level photoemission:  
photoelectron diffraction**

**Valence-level photoemission**

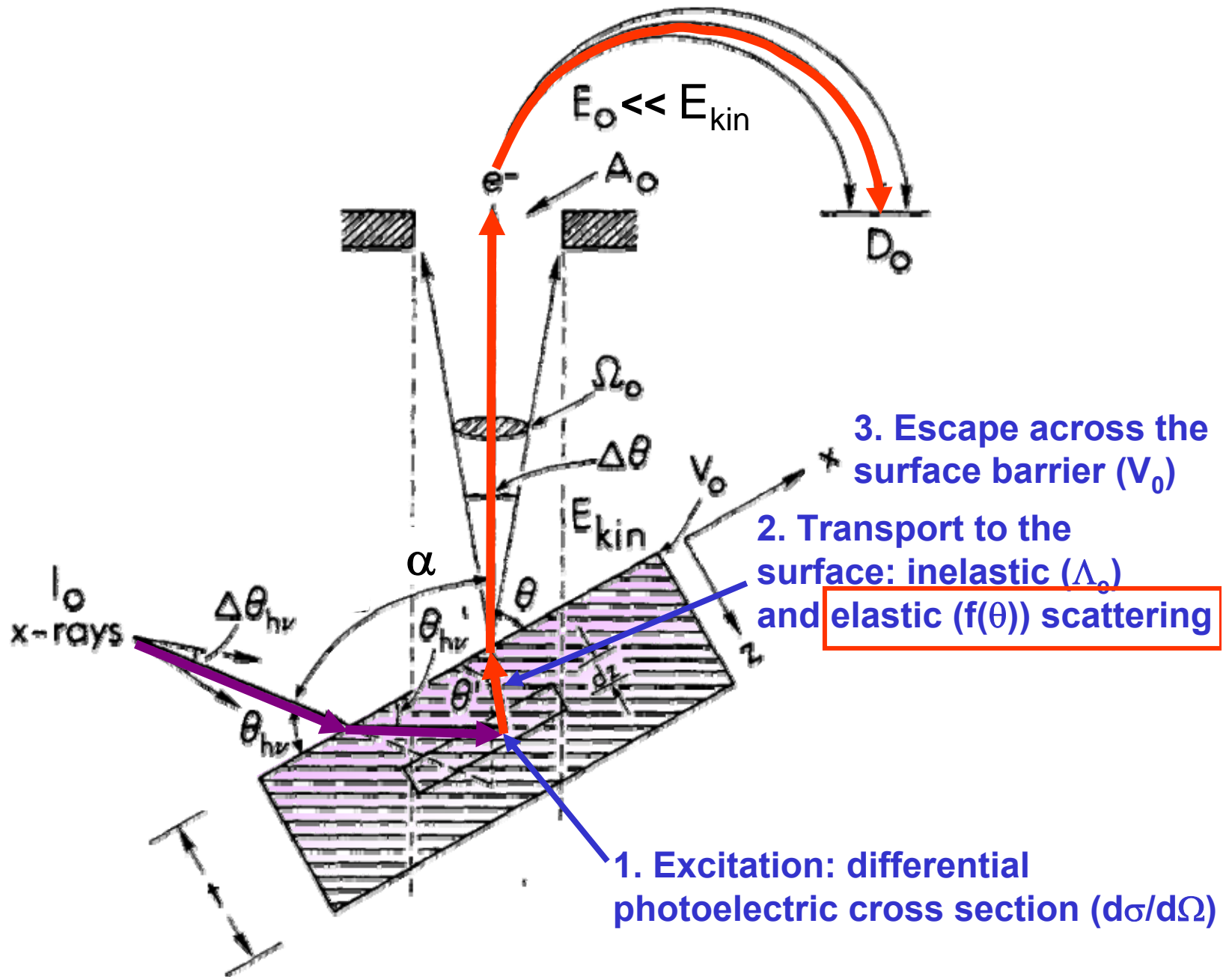
**Microscopy with photoemission**



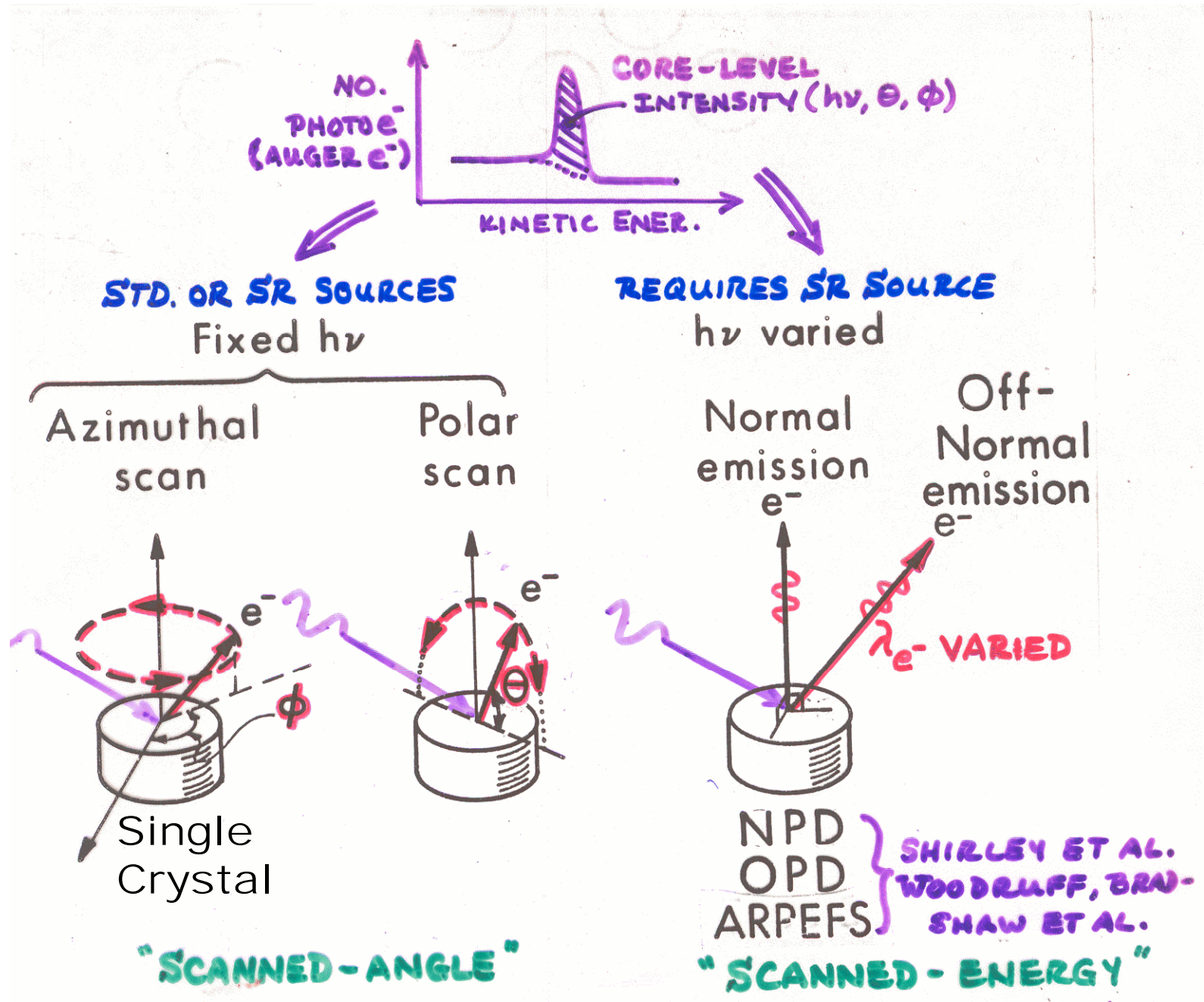
# Some basic measurements:



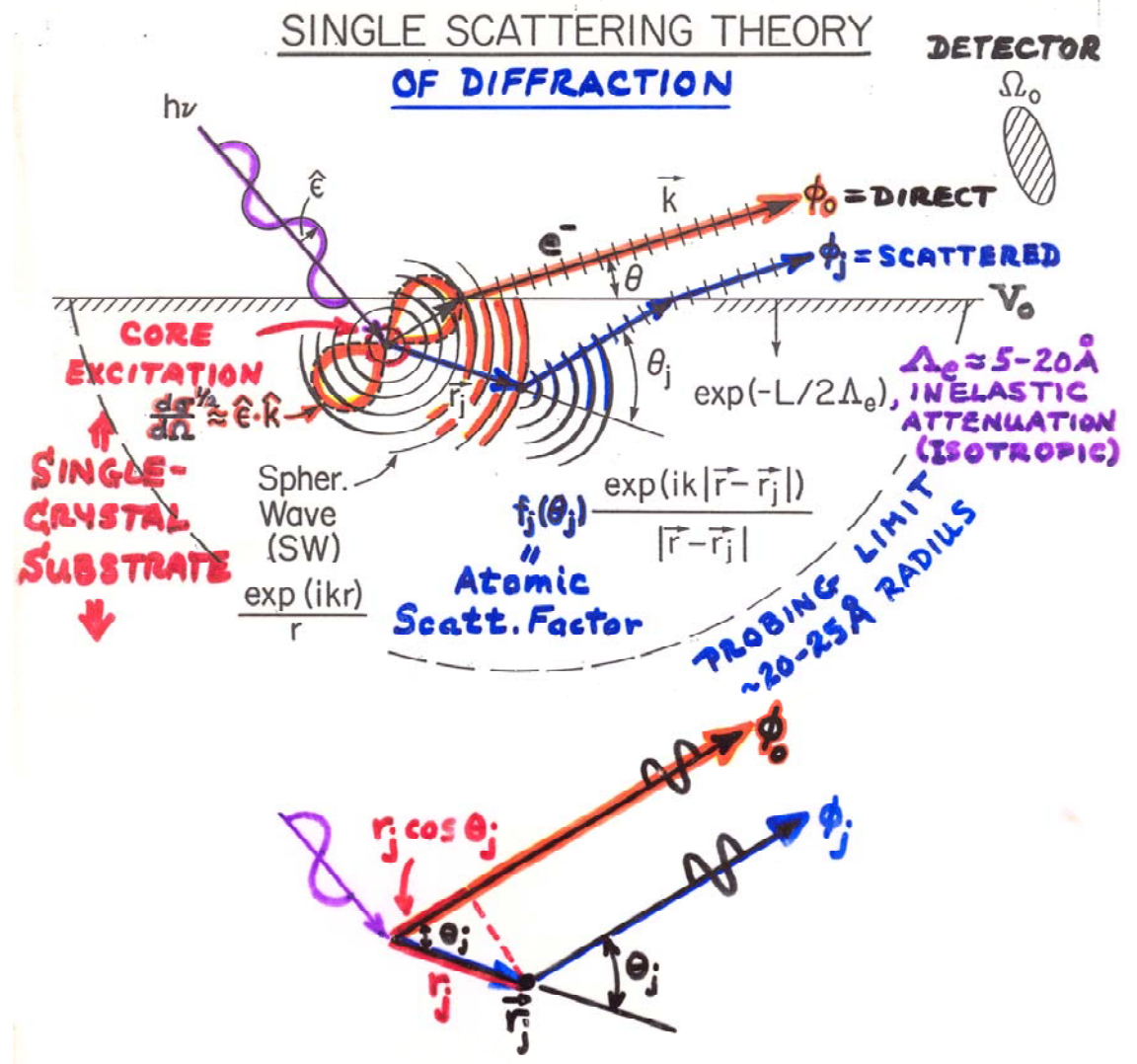
# PHOTOELECTRON INTENSITIES—THE 3-STEP MODEL



# PHOTOELECTRON DIFFRACTION AND HOLOGRAPHY



EFFECTS OF ELASTIC SCATTERING ON ANGULAR DISTRIBUTIONS: SINGLE-CRYSTAL SAMPLE → → PHOTOELECTRON DIFFRACTION And PHOTOELECTRON HOLOGRAPHY



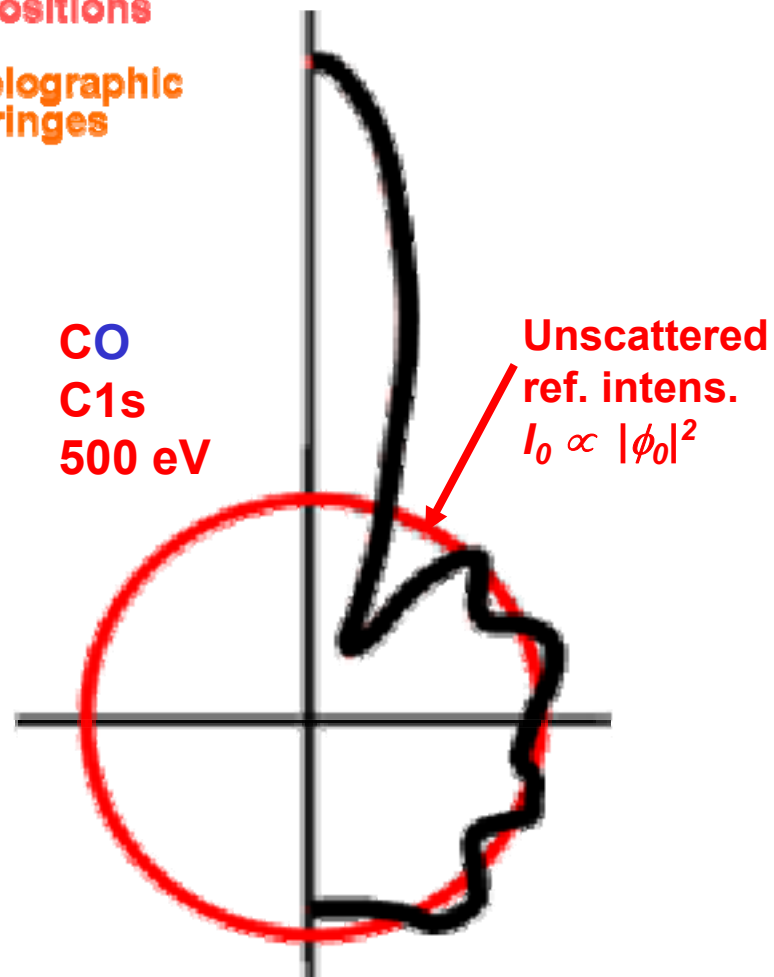
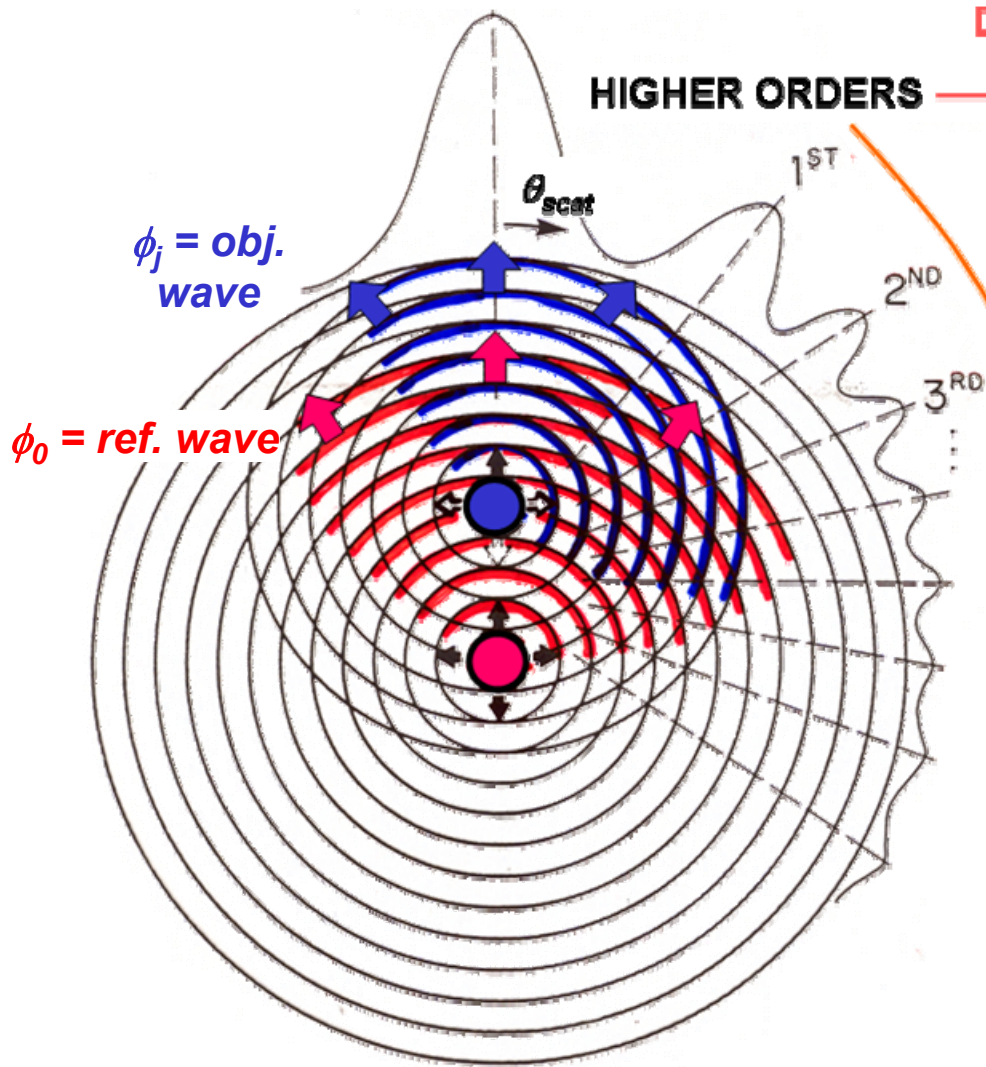
⇒ ALL BOND DISTANCE INFORMATION IN:  
 PATH LENGTH DIFFERENCE =  $r_j(1 - \cos \theta_j)$   
 ∴ PHASE DIFFERENCE =  $kr_j(1 - \cos \theta_j)$   
 =  $kr_j - \vec{k} \cdot \vec{r}_j$

“Study of Surface Structures...”  
 Figure 3

**FORWARD SCATT. = "0<sup>TH</sup> ORDER"** → **Bond & Low-Index Directions**

**HIGHER ORDERS** → **Bond Lengths & Atomic Positions**

→ **Holographic fringes**



**Photoelectron  
Diffraction**

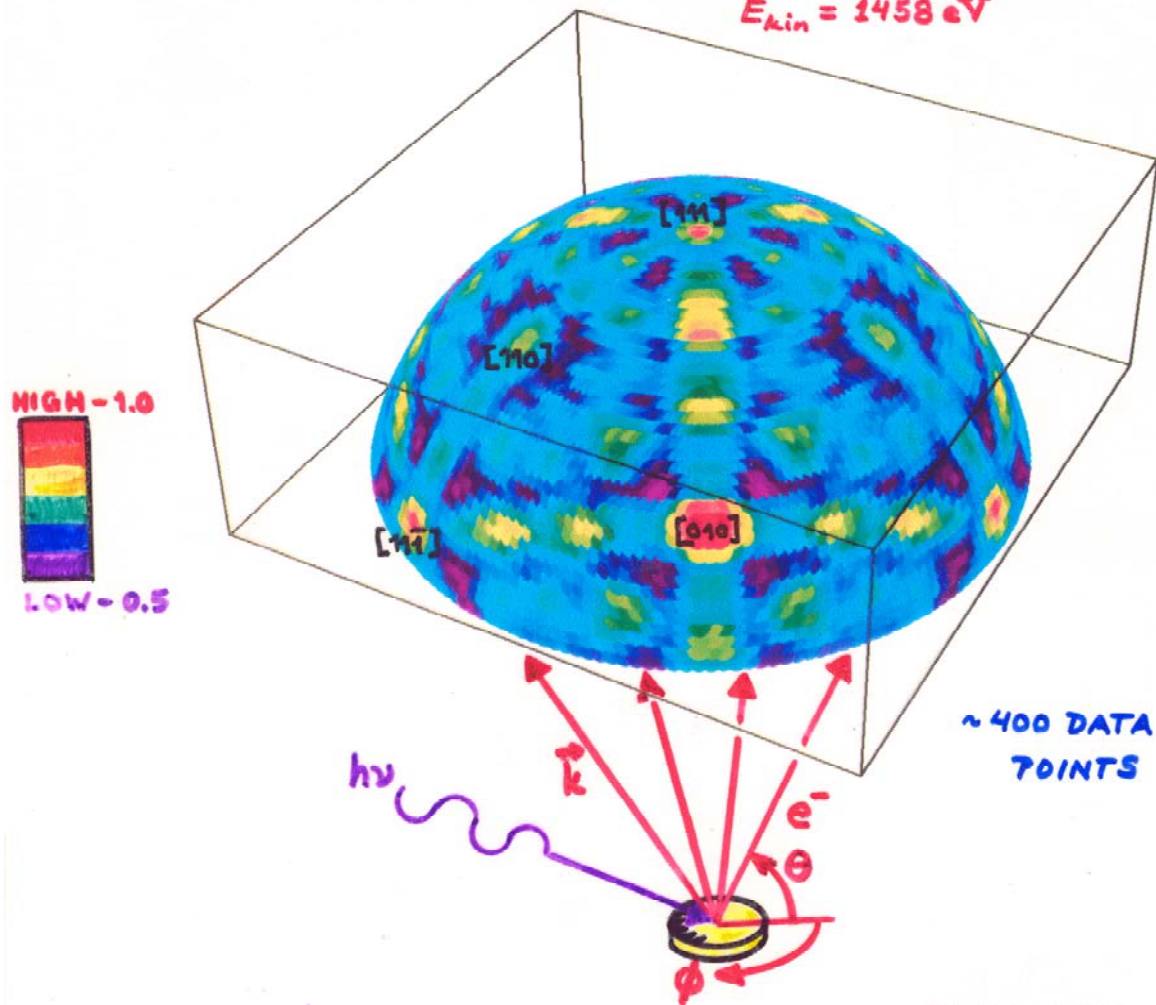
EDAC program: Javier Garcia de Abajo  
<http://maxwell.optica.csic.es/software/edac/index.html>

# SCANNED-ANGLE PHOTOELECTRON DIFFRACTION

Example:

Ge(111) - Ge3d Photoelectron Hologram

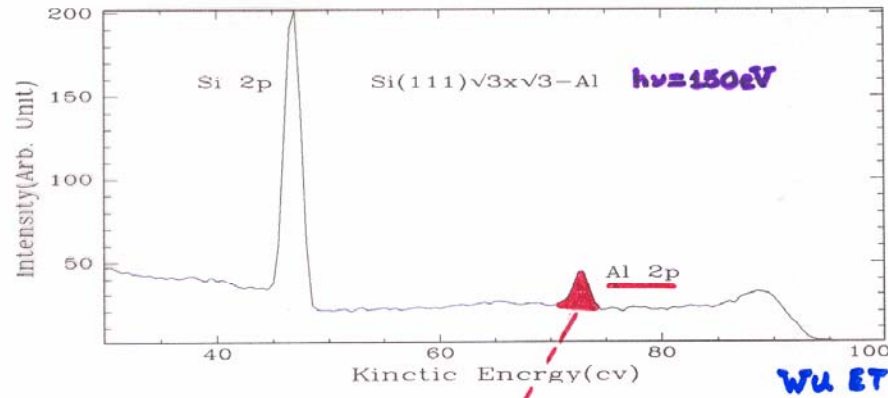
$E_{kin} = 1458 \text{ eV}$



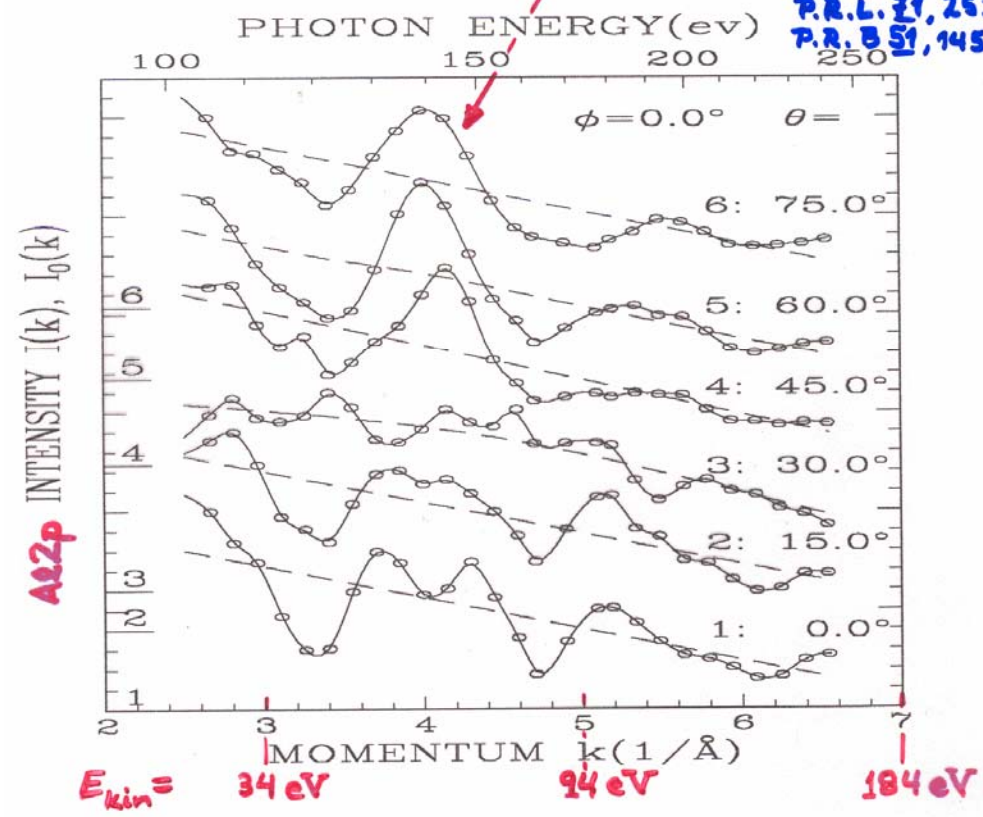
TRAN ET AL.,  
SURF. SCI. 281,  
270 ('93) +  
BUDGE, YINZUNZA

SCANNED-ENERGY PHOTOELECTRON DIFF.  
 $(\sqrt{3} \times \sqrt{3})$  AL ON Si(111)

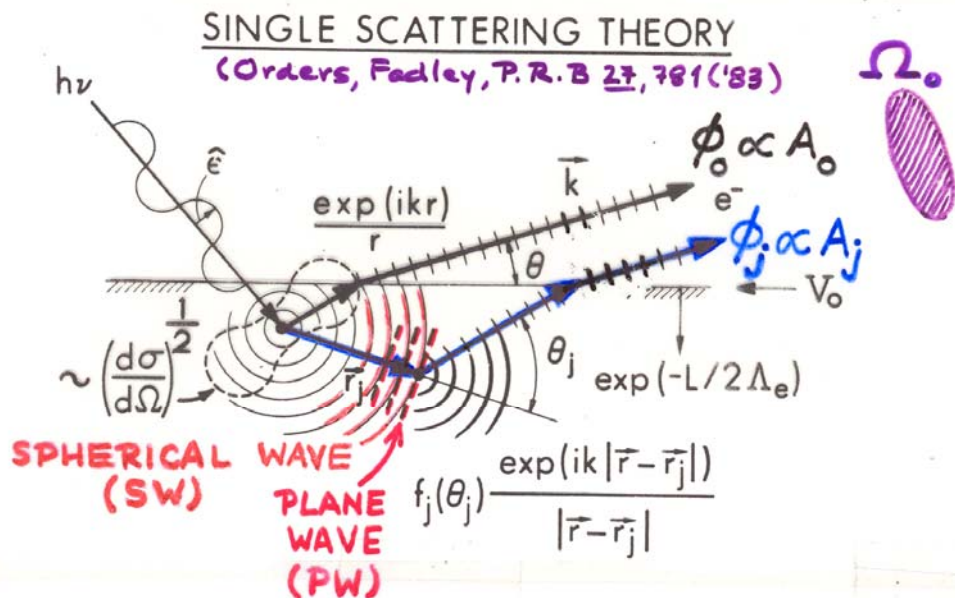
\* 41 diffraction curves  $\chi$  taken from Al 2p } ~1100 DATA POINTS  
 \*  $\theta = 0 \sim 70^\circ, \phi = 0 \sim 60^\circ$



WU ET AL.,  
 P.R.L. 31, 261 ('93)  
 P.R. B 51, 14549 ('95)



Photoelectron diffraction:  
Simple single-scattering theory for s-subshell emission



$$\chi(E \text{ or } \vec{k}) \propto \sum_j \frac{F_j(k)}{F_0} \cos \left[ \underbrace{kr_j(1 - \cos \theta_j)}_{\text{PATH LENGTH DIFFERENCE (P.L.D.)}} + \underbrace{\psi_j(\theta_j, k)}_{\text{SCATTERING PHASE SHIFT}} \right]$$

(CLUSTER) ELASTIC e<sup>-</sup>-ATOM SCATTERING DEBYE-WALLER SCATTERING INELASTIC e<sup>-</sup>-e<sup>-</sup> SCATTERING

$$F_j(k) = (\hat{\epsilon} \cdot \hat{r}_j) \frac{|f_j(\theta_j, k)|}{r_j} W_j(\theta_j, k) \exp(-L_j/2\Lambda_e)$$

= amplitude of scattered wave

$$F_0 = (\hat{\epsilon} \cdot \hat{k}) \exp(-L_0/2\Lambda_e)$$

= amplitude of direct wave

“Study of Surface Structures...”  
Figure 3



FROM SINGLE-SCATTERING THEORY:

(E.G., P.R. B 22, 6085 ('80); P.R. B 27, 781 ('83))

$$I(\vec{k}) \propto \left| \phi_0 + \sum_j \phi_j \right|^2, \quad \sum_j \text{ ON FINITE CLUSTER,}$$

$$\propto |\phi_0|^2 + \sum_j (\phi_0^* \phi_j + \phi_0 \phi_j^*) + \sum_j \sum_{j'} \phi_j^* \phi_{j'}$$

IF  $\phi_j \phi_{j'}$  SMALL W.R.T  $\phi_0^* \phi_j + \phi_0 \phi_j^*$ , A NECESSARY CONDITION FOR SIMPLE HOLOGRAPHY:

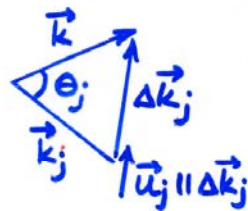
$$I(\vec{k}) \propto \underbrace{F_0^2}_{I_0} + 2F_0 \sum_j |F_j(\theta_j)| \underbrace{\cos[kr_j(1 - \cos\theta_j)]}_{\text{PATH LENGTH DIFFERENCE}} + \underbrace{\psi_j(\theta_j, k)}_{\text{SCATTERING PHASE}}$$

$$\chi(\vec{k}) = \frac{I(\vec{k}) - I_0}{I_0^{1/2}} \propto \left\{ \sum_j |F_j(\theta_j)| \cos[kr_j(1 - \cos\theta_j)] + \psi_j(\theta_j, k) \right\}$$

WITH:  $F_0 = (\hat{E} \cdot \hat{k}) \exp(-L_0/2\Delta_e)$   
 = amplitude of direct wave =  $I_0^{1/2}$

$$|F_j(\theta_j)| = (\hat{E} \cdot \hat{r}_j) \frac{|f_j(\theta_j)|}{r_j} W_j(\theta_j) \exp(-L_j/2\Delta_e)$$

= amplitude of scattered wave



$$W_j = \exp(-\Delta k_j^2 u_j^2)$$

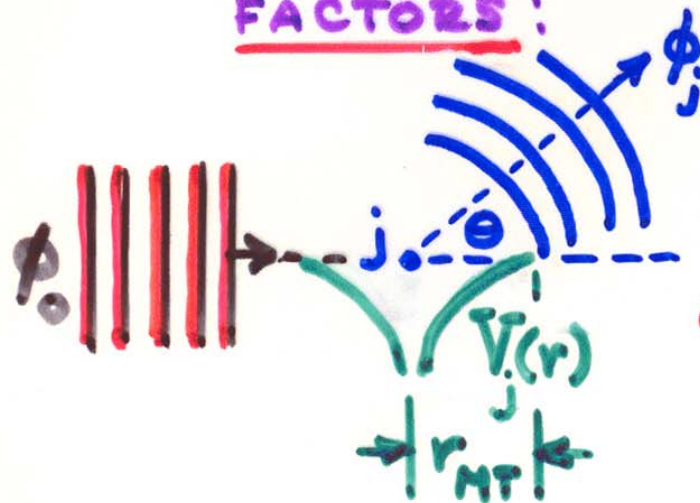
$$= \exp(-2k^2(1 - \cos\theta_j)u_j^2)$$

LIKE EXAFS/SEXAFS, BUT THERE:

- ADD CENTRAL ATOM PHASE SHIFT  $\delta_1$
- $\psi_j \Rightarrow \pi$  FOR ALL SCATTERERS
- $\cos \Rightarrow \sin$  IN ANGLE INTEGRATION
- $\hat{E} \cdot \hat{r}_j / r_j \Rightarrow \hat{E} \cdot \hat{v}_j / r_j^2$  IN OUT/BACK PATHS

## CALCULATION OF $e^-$ -ATOM SCATTERING

FACTORS:



PLANE-WAVE SCATTERING:

PARTIAL-WAVE METHOD†

$$\bullet \overset{\text{PW}}{f_j(\theta)} = \frac{1}{k} \sum_{l=0}^{l_{\max}} (2l+1) e^{i\delta_l} \sin \delta_l P_l(\cos \theta)$$

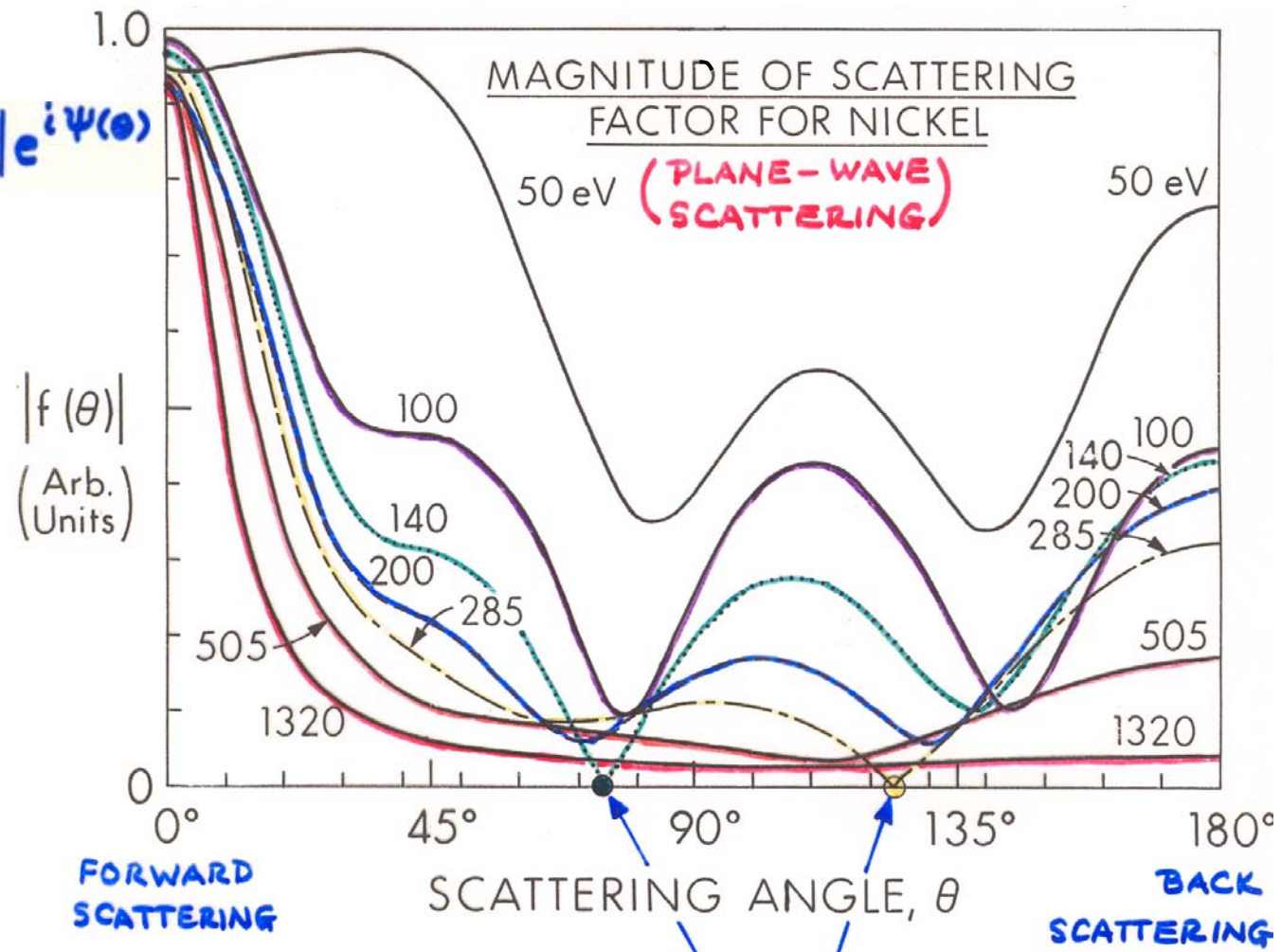
PHASE SHIFT

$$l_{\max} \approx k r_{MT}$$

† ANY TEXTBOOK ON SCATTERING

# ENERGY DEPENDENCE OF ELECTRON ELASTIC SCATTERING

$$f(\theta) = |f(\theta)| e^{i\psi(\theta)}$$

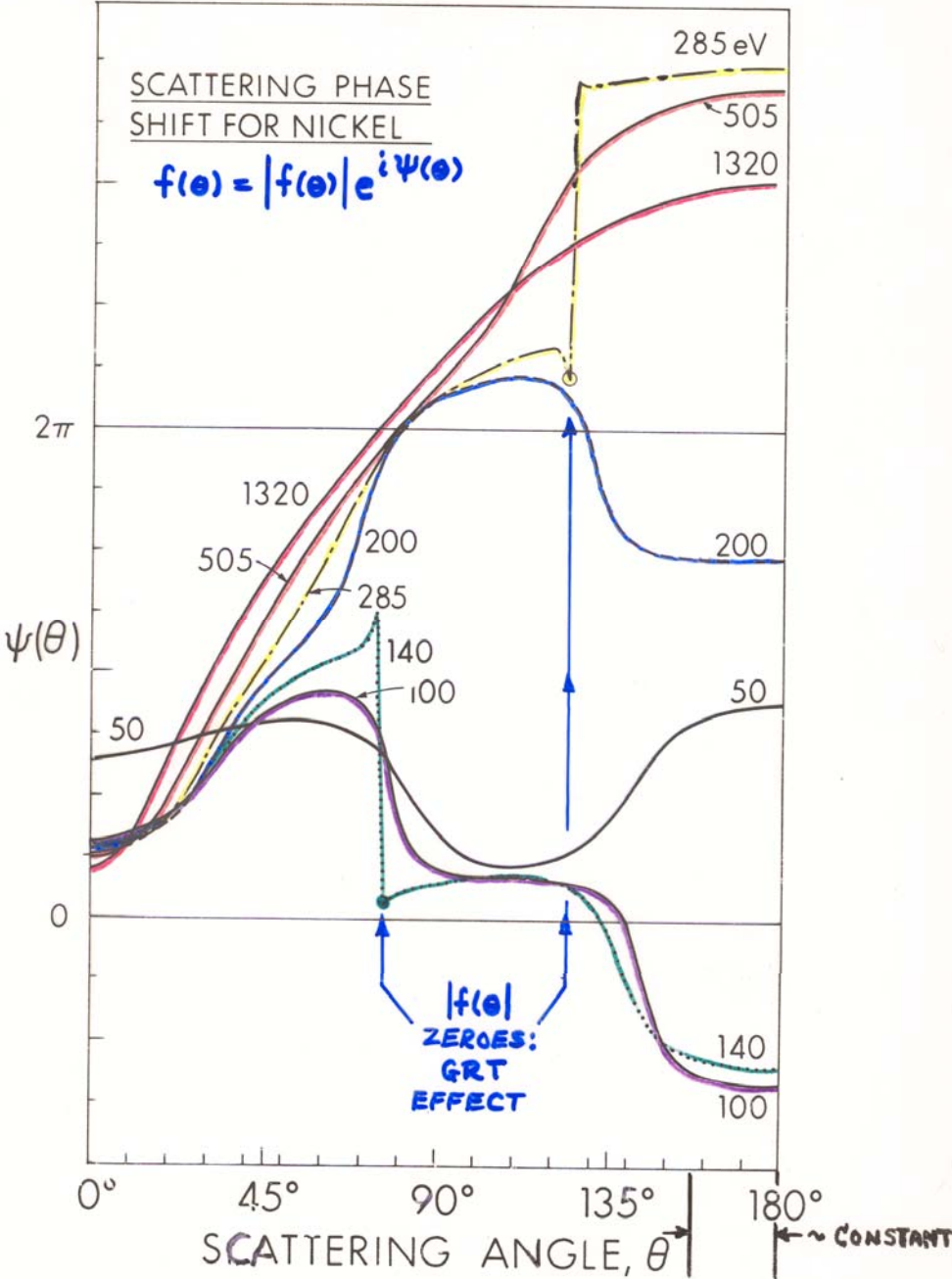


(M. SAGURTON ET AL.,  
SURF. SCI. 182, 287 ('87))

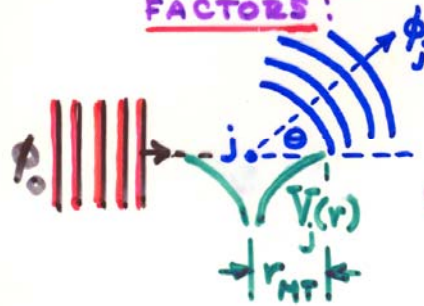
ZEROS,  
"GENERALIZED  
RAMSAUER-  
TOWNSEND  
EFFECT"

"Study of Surface Structures..."  
Figure 2

# ENERGY DEPENDENCE OF ELECTRON ELASTIC SCATTERING



CALCULATION OF  $e^-$ -ATOM SCATTERING FACTORS:

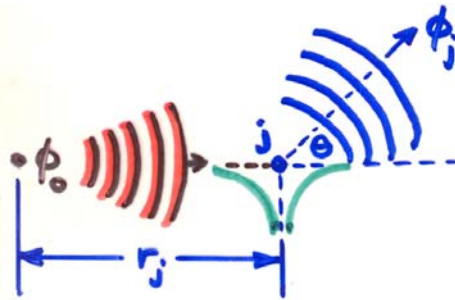


PLANE-WAVE SCATTERING:  
PARTIAL-WAVE METHOD†

•  $f_j^{PW}(\theta) = \frac{1}{k} \sum_{l=0}^{l_{max}} (2l+1) e^{i\delta_l} \sin \delta_l P_l(\cos \theta)$  ← PHASE SHIFT

$l_{max} \approx kr_{MT}$

† ANY TEXTBOOK ON SCATTERING



SPHERICAL-WAVE SCATTERING:  
REHR-ALBERS METHOD\*

•  $f_j^{SW}(\theta) = \frac{1}{k} \sum_{l=0}^{l_{max}} \left\{ (2l+1) e^{i\delta_l} \sin \delta_l P_l(\cos \theta) \right\} \cdot$

$$\frac{[(l+1)C_{l+1}(kr_j) + lC_{l-1}(kr_j)]}{2l+1}$$

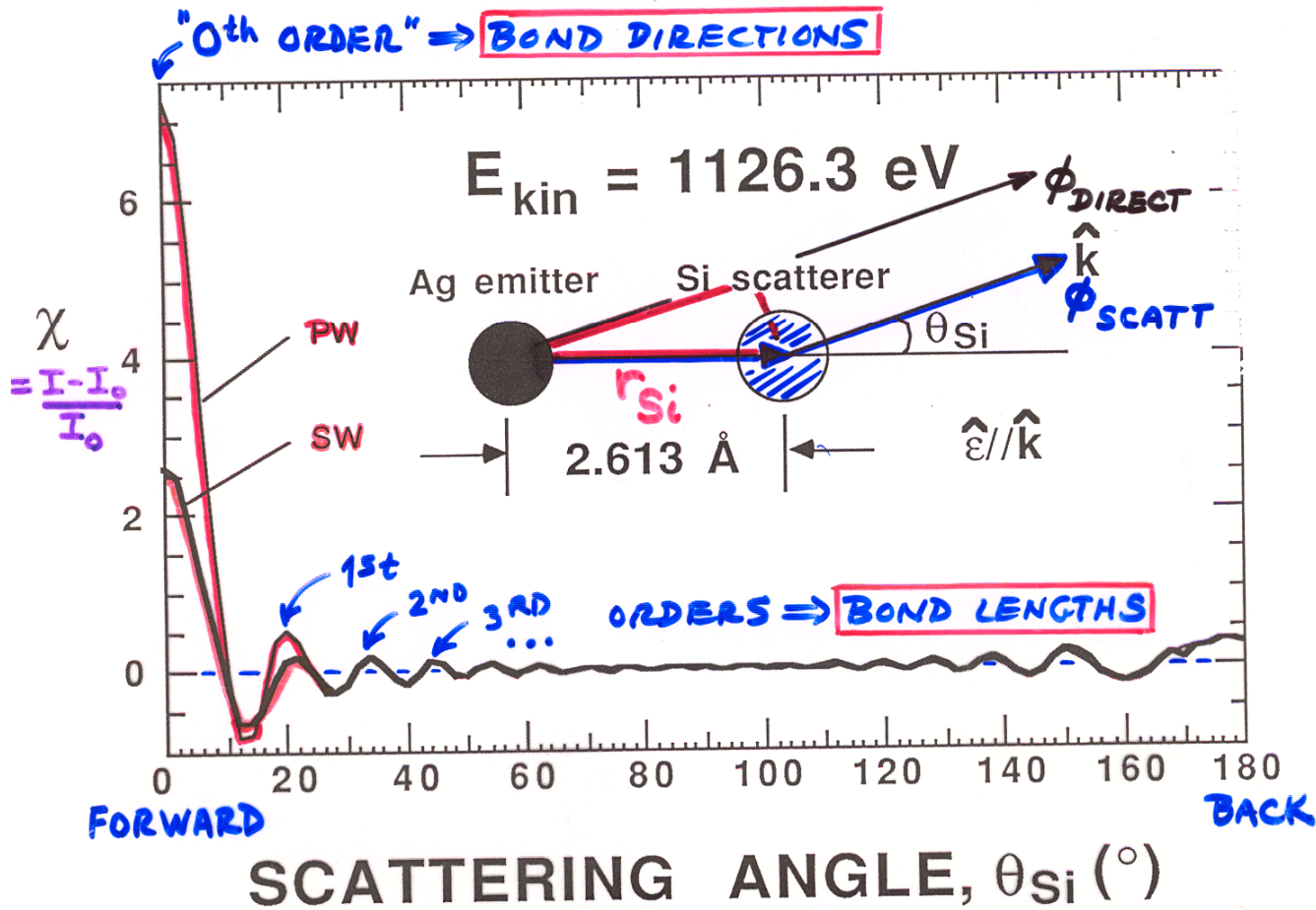
WITH:

$$C_l(kr_j) = \left[ 1 + \frac{l(l+1)}{2(kr_j)^2} \right] e^{\frac{i2l(l+1)}{2kr_j}}$$

\* MUSTRE DE LEON ET AL.,  
PHYS. REV. B 39, 5632 ('89)

- AND MORE ACCURATE MATRIX METHODS IN REHR, ALBERS, PHYS. REV. B 41, 8139 (1990) + FRIEDMAN, FADLEY, J. ELECT. SPECT. 51, 689 (1990)

# PW vs. SW scattering



PATH LENGTH DIFFERENCE =

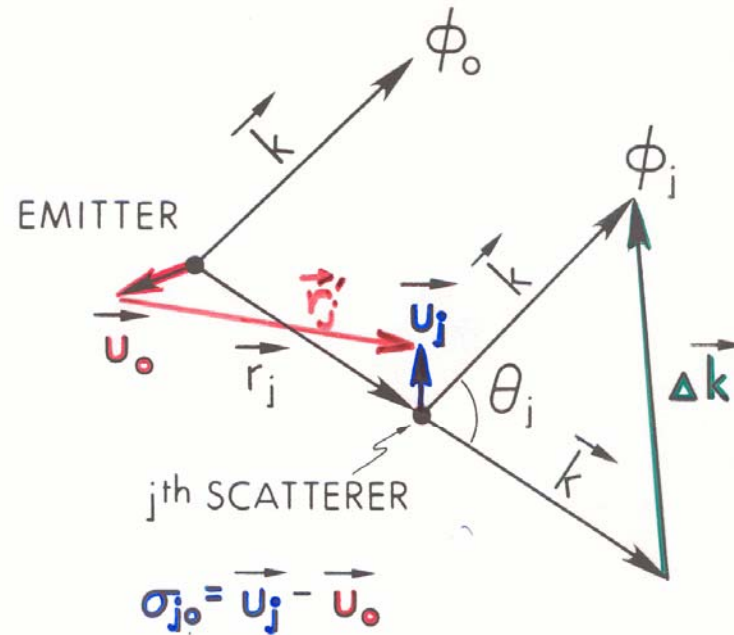
$$r_{Si}(1 - \cos \theta_{Si})$$

ORDERS:

$$2\pi n = [k r_{Si}(1 - \cos \theta_{Si}) + \psi_{Si}^{\downarrow}(\theta)]$$

SCATTERING  
PHASE SHIFT

# Vibrational effects on diffraction



- DW FACTOR =  $e^{-\frac{1}{2} \overline{(\Delta \vec{k} \cdot \vec{\sigma}_{j0})}^2} = e^{-\frac{1}{2} \Delta k^2 \overline{\sigma_{j0,||}^2}}$

- $\vec{U}_j, \vec{U}_0$  UNCORRELATED:

$$DW = e^{-\frac{1}{2} \overline{(\Delta \vec{k} \cdot \vec{u}_j)^2}} e^{-\frac{1}{2} \overline{(\Delta \vec{k} \cdot \vec{u}_0)^2}}$$

- $\vec{U}_j \approx \vec{U}_0$  IN DISTRIBUTION:

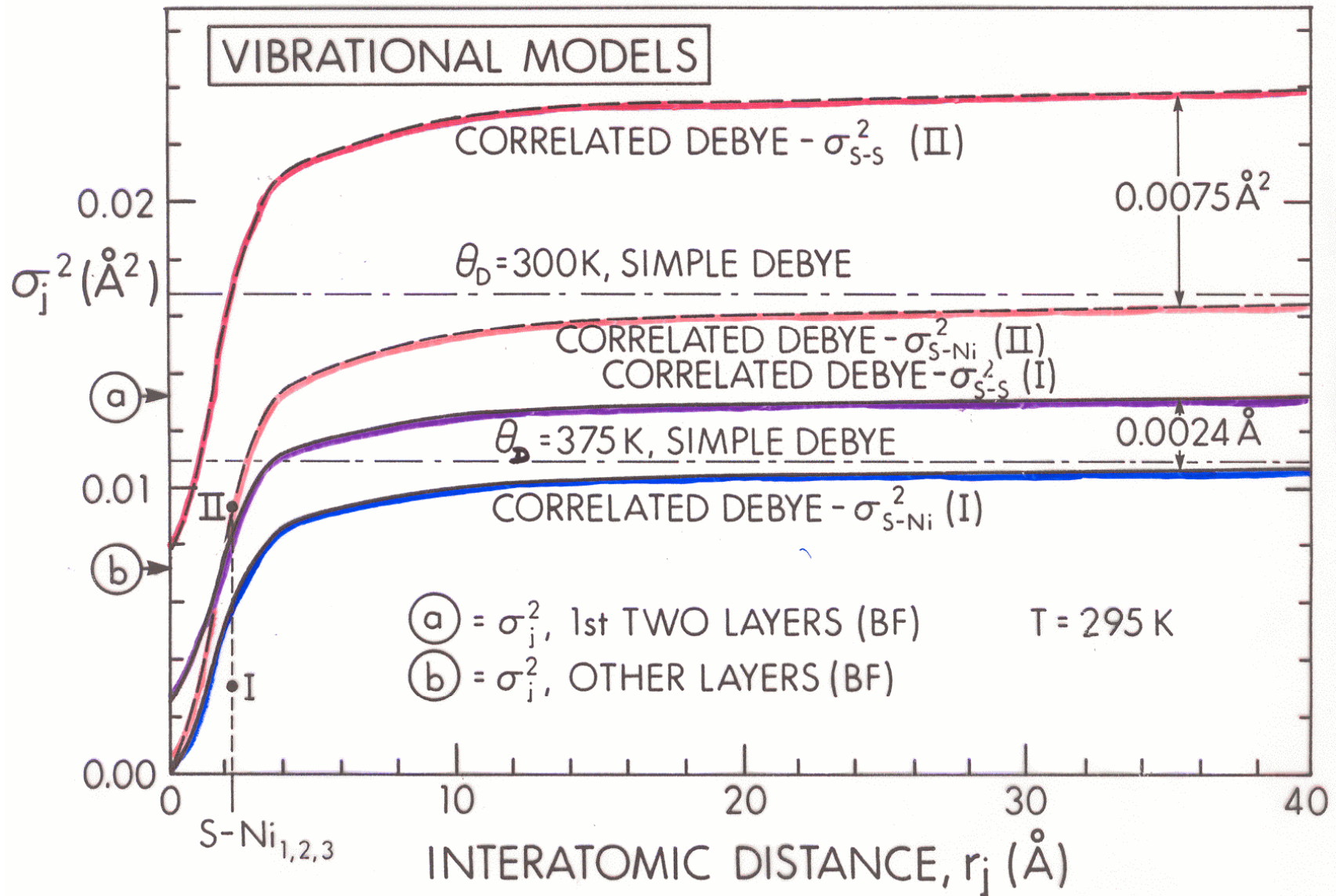
$$DW = e^{-\overline{(\Delta \vec{k} \cdot \vec{u}_j)^2}}$$

- $\vec{U}_j$  ISOTROPIC:

$$DW = e^{-\Delta k^2 \overline{u_j^2}} = e^{-2k^2(1 - \cos \theta_j) \overline{u_j^2}} \leftarrow \text{USUAL LEVEL}$$

DECREASING ACCURACY

↑ CORRELATED? ↓



[ SAGURTON, BULLOCK, FADLEY, SURF. SCI. ]  
 182, 287 (1987)

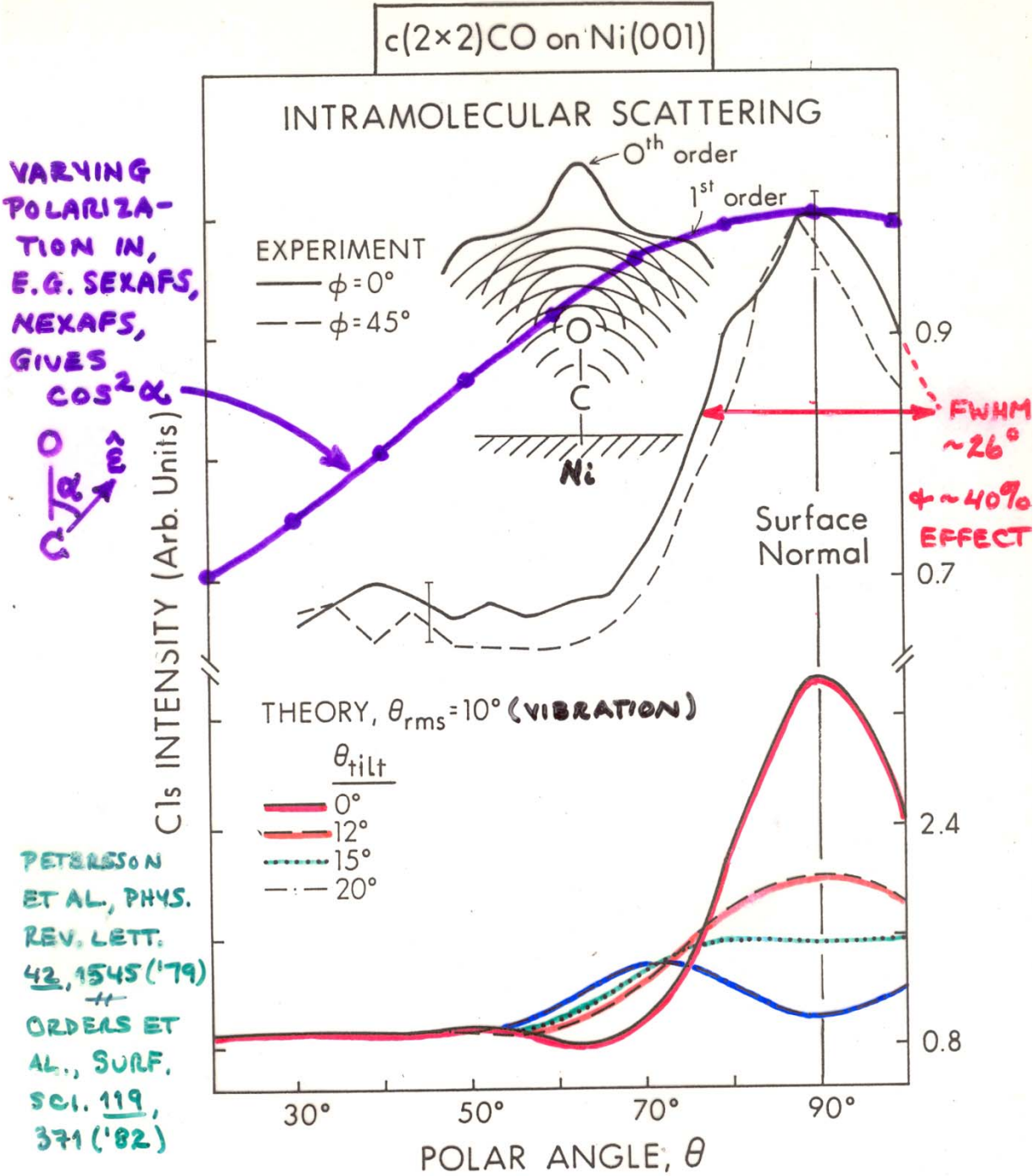


Table 1 Debye temperature and thermal conductivity<sup>a</sup>

Li	Be											B	C	N	O	F	Ne	
344	1440												2230					75
0.85	2.00											0.27	1.29					
Na	Mg											Al	Si	P	S	Cl	Ar	
158	400	Low temperature limit of $\theta$ , in Kelvin										428	645					92
1.41	1.56	Thermal conductivity at 300 K, in $W\ cm^{-1}K^{-1}$										2.37	1.48					
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr	
91	230	360.	420	380	630	410	470	445	450	343	327	320	374	282	90		72	
1.02		0.16	0.22	0.31	0.94	0.08	0.80	1.00	0.91	4.01	1.16	0.41	0.60	0.50	0.02			
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn <sub>w</sub>	Sb	Te	I	Xe	
56	147	280	291	275	450		600	480	274	225	209	108	200	211	153		64	
0.58		0.17	0.23	0.54	1.38	0.51	1.17	1.50	0.72	4.29	0.97	0.82	0.67	0.24	0.02			
Cs	Ba	La $\beta$	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn	
38	110	142	252	240	400	430	500	420	240	165	71.9	78.5	105	119				
0.36		0.14	0.23	0.58	1.74	0.48	0.88	1.47	0.72	3.17		0.46	0.35	0.08				
Fr	Ra	Ac																
			Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu		
									200		210				120	210		
			0.11	0.12	0.16		0.13		0.11	0.11	0.11	0.16	0.14	0.17	0.35	0.16		
			Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr		
			163		207													
			0.54		0.28	0.06	0.07											

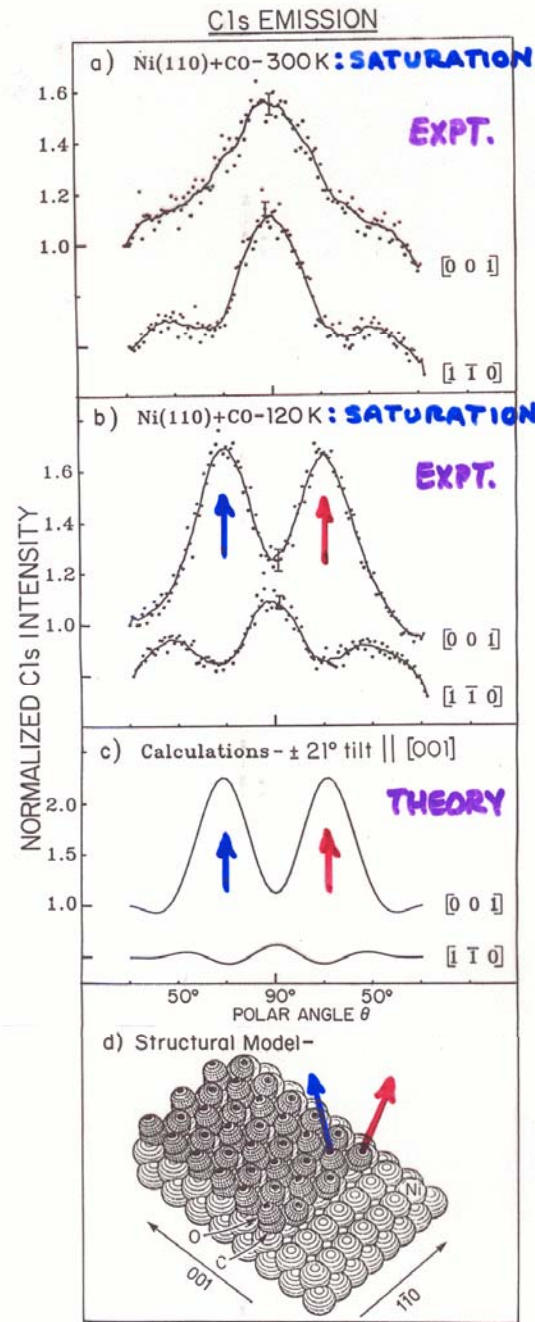
<sup>a</sup>Most of the  $\theta$  values were supplied by N. Pearlman; references are given the *A.I.P. Handbook*, 3rd ed; the thermal conductivity values are from R. W. Powell and Y. S. Touloukian, *Science* **181**, 999 (1973).

**Case study:  
Determining  
the orientation of  
an adsorbed  
molecule from  
photoelectron  
diffraction at about  
1 keV energy**



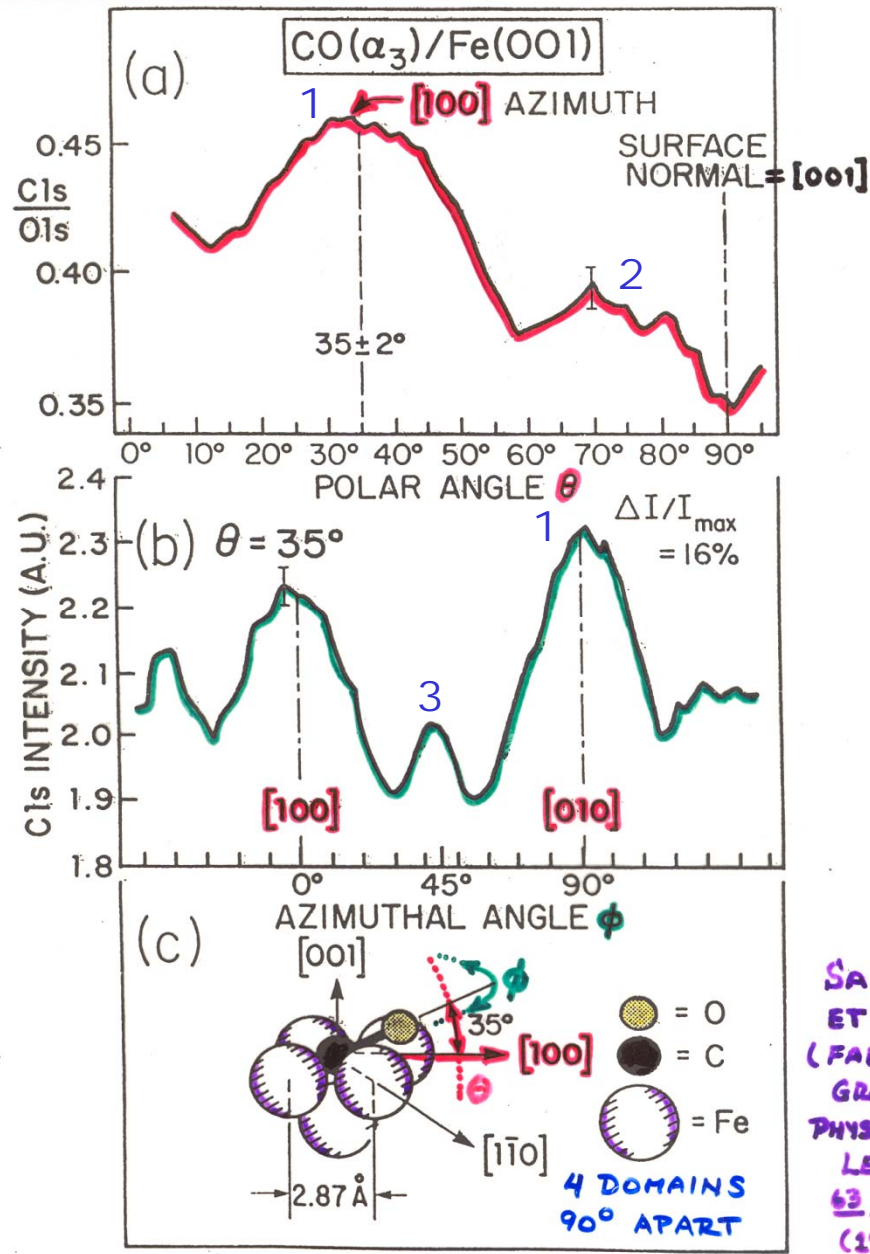
“Study of Surface Structures...”  
Figure 8

TEMPERATURE-  
DEPENDENT  
ADSORBATE  
ORIENTATION



“Study of Surface Structures...”  
Figure 12

ORIENTATION OF A HIGHLY TILTED MOLEC. ON SURFACE

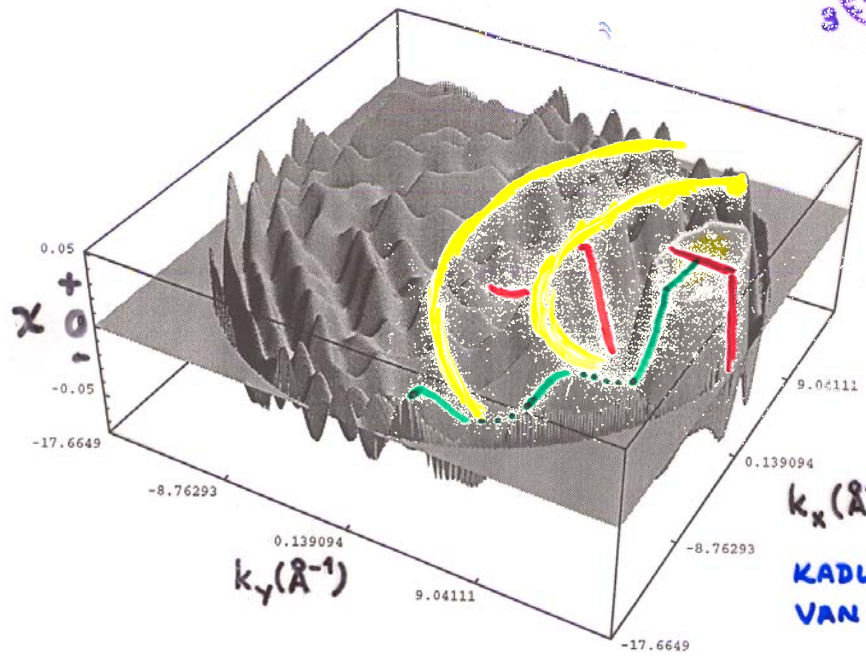
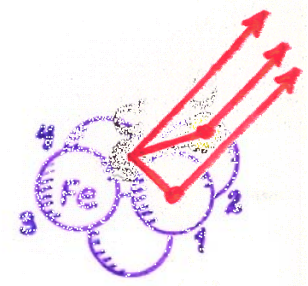
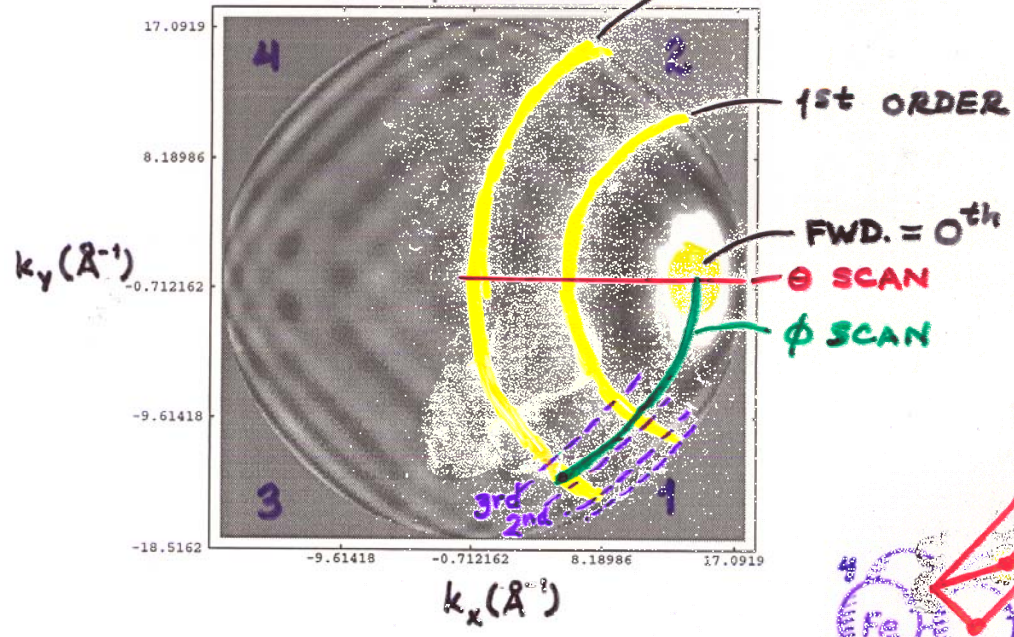


SAIKI  
 ET AL.  
 (FADLEY  
 GROUP)  
 PHYS. REV.  
 LETT.  
 63, 283  
 (1989)

“Study of Surface Structures...”  
 Figure 9

CALCULATED 2<sup>nd</sup> INTENSITY

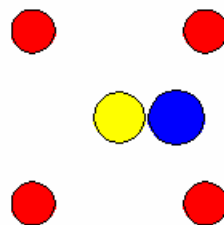
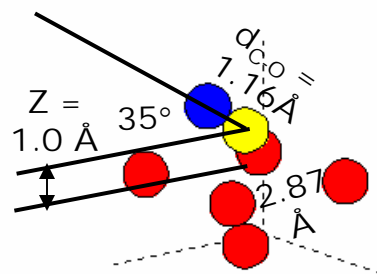
CO( $\alpha_3$ )/Fe(001) 2<sup>nd</sup> ORDER



KADUWELA, BUDGE,  
VAN HOVE, FADLEY

Online calculation of photoelectron diffraction patterns:

7 atoms:



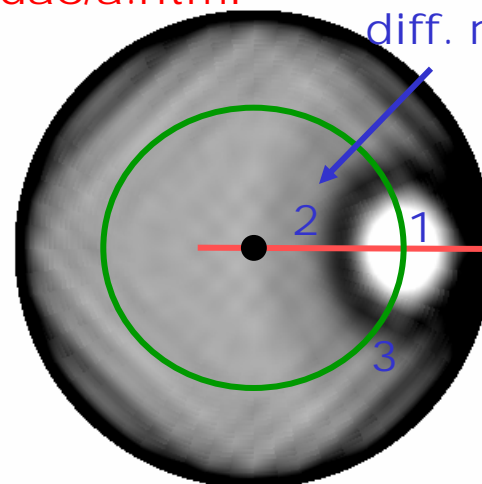
# EDAC output for CO/Fe(001)



Click on the figure to download data.

<http://csic.sw.ehu.es/jga/software/edac/a.html>

Oxygen  
1<sup>st</sup> order  
diff. ring



**Left:** representation of the cluster rocking around a line parallel to the  $z$  direction and passing by the **emitter (yellow atom)**. The dashed lines stand for the  $xyz$  axes. **Right:** top view of the cluster, where the  $x/y$  direction (not plotted) runs along the horizontal/vertical screen direction. Different atomic species have been assigned the colors **O**, **Fe**.

**Polar scan of photoemission intensity** (logarithmic scale). White/black regions correspond to high/low intensity. The orientation is the same as in the top-view of the cluster. The distance to the center of the figure is proportional to the polar angle  $\theta$ . The polar angle range is (0.0, 89.0) (in degrees).

### Parameters used in the calculation:

$N=7$  atoms  
Iteration order=4  
 $l_{\max}=25$   
 $V_0=10.5$  eV  
Photoelectron energy=1202 eV  
p-polarized light  
 $z_0=1.435$  Å  
Recursion iteration method

X 4 domains  
rotated by 90°

# Electron Diffraction in Atomic Clusters

## for Core Level Photoelectron Diffraction Simulations



Created by [F. Javier García de Abajo](#) (CSIC and DIPC, San Sebastian, Spain)  
in collaboration with [M. A. Van Hove](#) and [C. S. Fadley](#) (LBNL, Berkeley, and UCD, Davis, California)

This site allows performing on-line photoelectron diffraction calculations. Multiple scattering (MS) of the photoelectron is carried out for a cluster representing a solid or molecule. Select the corresponding parameters and click on the "Calculate" button below to perform the actual calculation and to produce a plot of the calculated data (a separate window pops out to display it). A numerical data table can be downloaded by clicking on the resulting plot. Click on the different parameter names in blue to see fuller explanations. Click on the "Preview Cluster" button to display the currently selected atomic cluster (but without performing a MS calculation) or the button "Download Cluster" to download the currently selected cluster. Notice that the scattering phase shifts and excitation radial matrix elements are calculated internally for each cluster configuration, so that the user does not have to provide them. Please, read the [terms of use](#) and the [restrictions on input parameters](#) before using this site for the first time.

### Terms and conditions of use

[Terms of use](#)

[Restrictions on input parameters](#)

Password:

A password is only necessary for large computation times (click [here](#) for more details). Leave it blank otherwise.

Title (optional):

### Cluster definition

The cluster and the list of emitters are defined by a list of commands with the following format (click [here](#) or on the items of this list for further details):

atom symbol  $x y z$       layer symbol  $x y z a b \alpha_1 \alpha_2$

surface symbol  $x y z a$  type      emitter  $x y z$

Fill in the text box with these commands according to the cluster specifications that you need. [Some examples are provided by clicking here](#) (you may cut and paste them to this page and modify them further).

```

atom O 0.95 0 1.66
atom C 0 0 1.0
surface Fe 1.435 1.435 0 2.87 bcc100
emitter 0 0 1.0
end

```

The cluster consists of a maximum of  atoms. (Warning: a finite number of atoms generally introduces symmetry breaking.)

The size of the cluster is determined by the distance  $d_{\max} =$  Å and the reference point  $x_0 =$  Å,  $y_0 =$  Å,  $z_0 =$  Å.

See [cluster shape](#) for more details.

- Plot cluster on output?  Yes  No
- Cluster shape:  Parabolic  Spherical

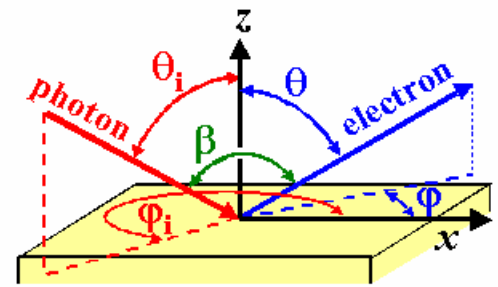
## Geometry of beam and analyzer

**Incoming beam parameters** (see figure)

Polar angle  $\theta_1 =$  degrees

Azimuthal angle  $\varphi_1 =$  degrees

- Polarization:**
- p-polarization
  - s-polarization
  - RCP
  - LCP



**Schematic representation of the geometry**

- Mobility of cluster beam, and sample** (click here for details):
- Only the sample moves with constant  $\beta =$  degrees
  - Only the analyzer moves
  - Both the sample and the analyzer move



## Energy and angle scanning parameters (see figure above)

The following entries will select the range of photoelectron energies and angles of emission.

Energy scans for a given emission angle can be chosen by selecting more than one energy of emission and only one polar angle and one azimuthal angle (the value of each angle is then taken as the lower limit of the selected angular range, and the value of the upper limits are disregarded). In this case, the output is a 1D plot with the photoelectron intensity as a function of photoelectron energy.

Electron energy range:  equally-spaced value(s) of the electron energy from  eV to  eV  
Polar angle:  equally-spaced value(s) of the polar angle  $\theta$  from  degrees to  degrees  
Azimuthal angle:  equally-spaced value(s) of the azimuthal angle  $\phi$  from  degrees to  degrees  
Type of 2D angular representation:  Linear scale  Logarithmic scale  
Type of azimuthal of polar angular representation:  Cartesian  Polar

Photoelectron detector half-width acceptance angle =  degrees. The photoelectron intensities are angle-averaged over a cone with half aperture given by this parameter.

## Multiple scattering parameters

**Internal code parameters**  
Maximum orbital quantum number  $l_{\max} =$    
Scattering order =   
Iteration method:  Jacobi (regular MS)  Recursion

**Additional solid parameters**  
Inner potential  $V_0 =$   eV  
Electronic edge  $z_0 =$   Å

**8.1 eV from band struct.  
+ work function = 4.3 eV  
= 12.4 eV**

Inelastic mean free path: either choose a fixed value =  Å  
or (if that last entry is <0) use the **TPP-2M formula**  
with parameters  $\rho =$   g/cm<sup>3</sup>,  $N_v =$  ,  $E_p =$   eV, and  $E_g =$   eV  
Temperature (K) =  and Debye temperature (K) =



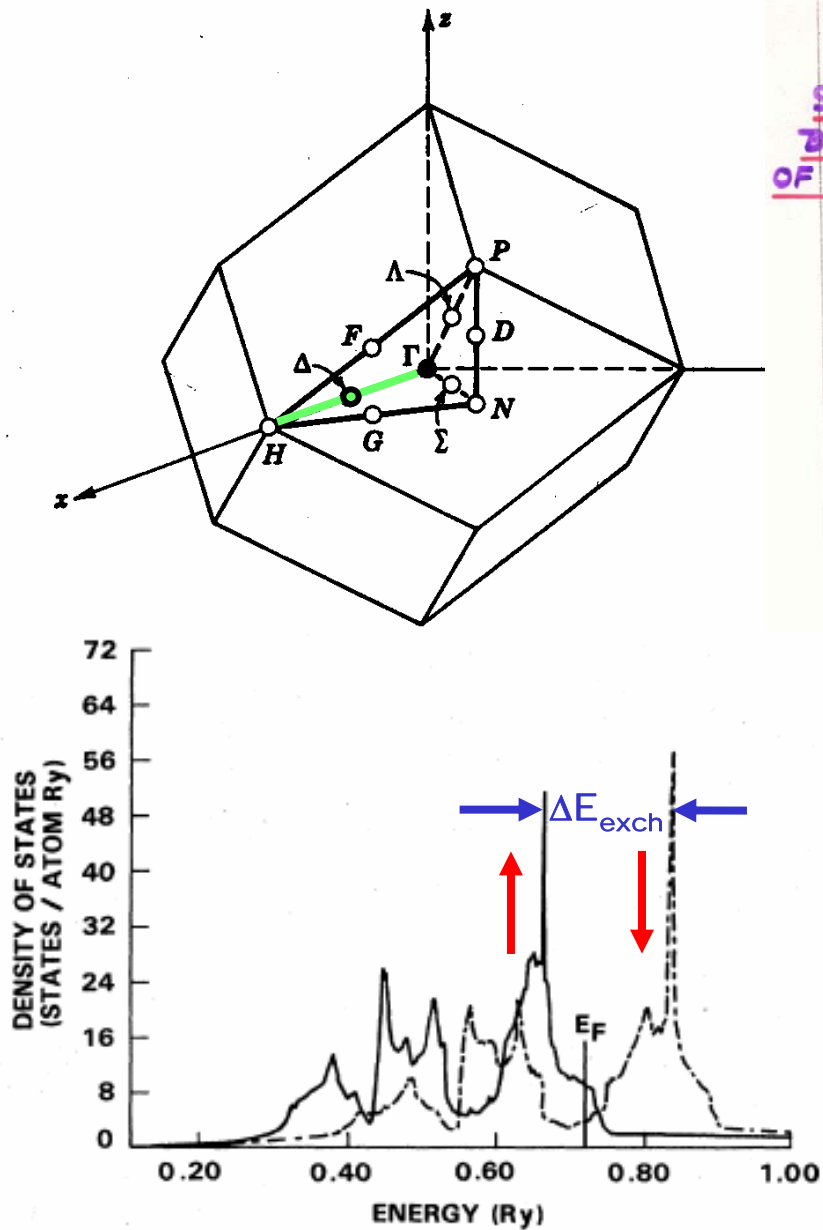
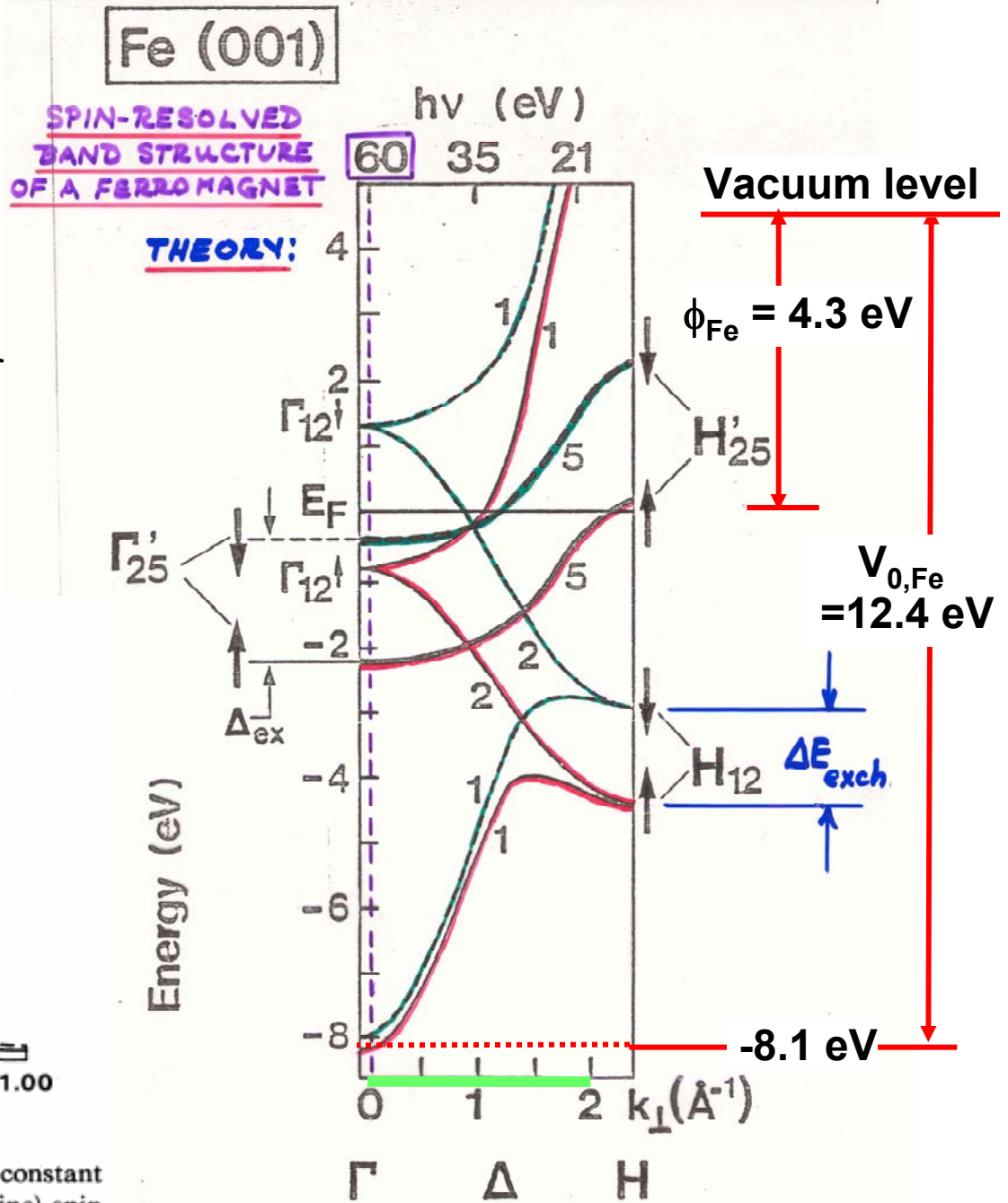


FIG. 4. Density of states at the equilibrium lattice constant of Fe for majority- (solid line) and minority- (broken line) spin states.

Hathaway et al., Phys. Rev. B 31, 7603 ('85)



E. KISKER ET AL., PHYS. REV. B  
31, 329 (1985)

### Initial core-state quantum numbers

Radial matrix elements:  Automatic: core level (e.g. 1s, 2s, 2p, etc.) =   
 Manual:  $l_0 =$  $, R_{l_0+1} =$  $, \delta_{l_0+1} =$  $, R_{l_0-1} =$  $, \delta_{l_0-1} =$

Calculate\*

Download Input File\*\*

Reset\*\*\*

**COMPUTATION TIME:** the CPU time needed for the calculation using the default cluster and input parameters (use Reset to recover default input) is 1.24 seconds on a Pentium III @ 733 MHz. This gives a time scale to estimate the computation time for other input parameters, keeping in mind that it scales like  $\sim (n_{\text{scat}} - 1) N^2 (l_{\text{max}} + 1)^3$ , where  $N$  is the number of atoms in the cluster and  $n_{\text{scat}}$  is the scattering order. For reference, the default values are  $N=48$ ,  $l_{\text{max}}=6$ , and  $n_{\text{scat}}=2$ , for which the above number is  $7.9 \cdot 10^5$ .

**IMPORTANT: READ THESE LINES BEFORE RUNNING THE CODE FOR THE FIRST TIME.**

**\*The results will be plotted on a separate window.**

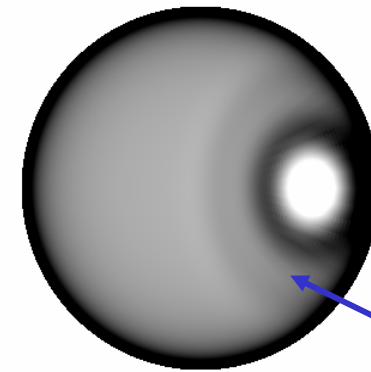
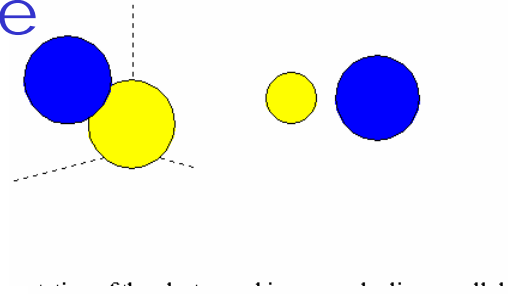
**\*\*The input file can be used to run the code locally, for which a copy of the code is needed. This can be obtained from F. Javier García de Abajo. An online version of the input-file manual is also available [here](#).**

**\*\*\*Reset all input values (including cluster specification) to the original settings.**

For comments/questions/suggestions, please contact F. Javier García de Abajo at [jga@sw.ehu.es](mailto:jga@sw.ehu.es)

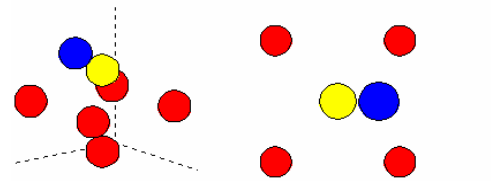
# CO/Fe(001)—Effect of CO height $z$ above first Fe plane

2 atoms:  $Z = \infty$

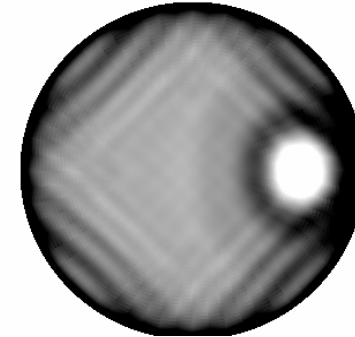
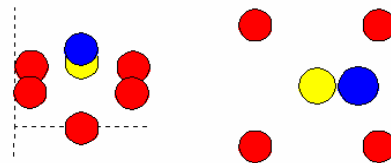


Oxygen-1<sup>st</sup> order diff. ring

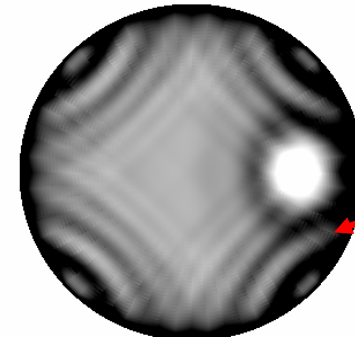
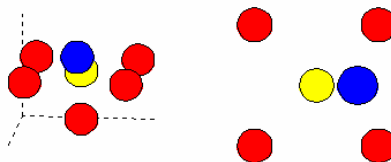
7 atoms: 1.0 Å



0.5 Å

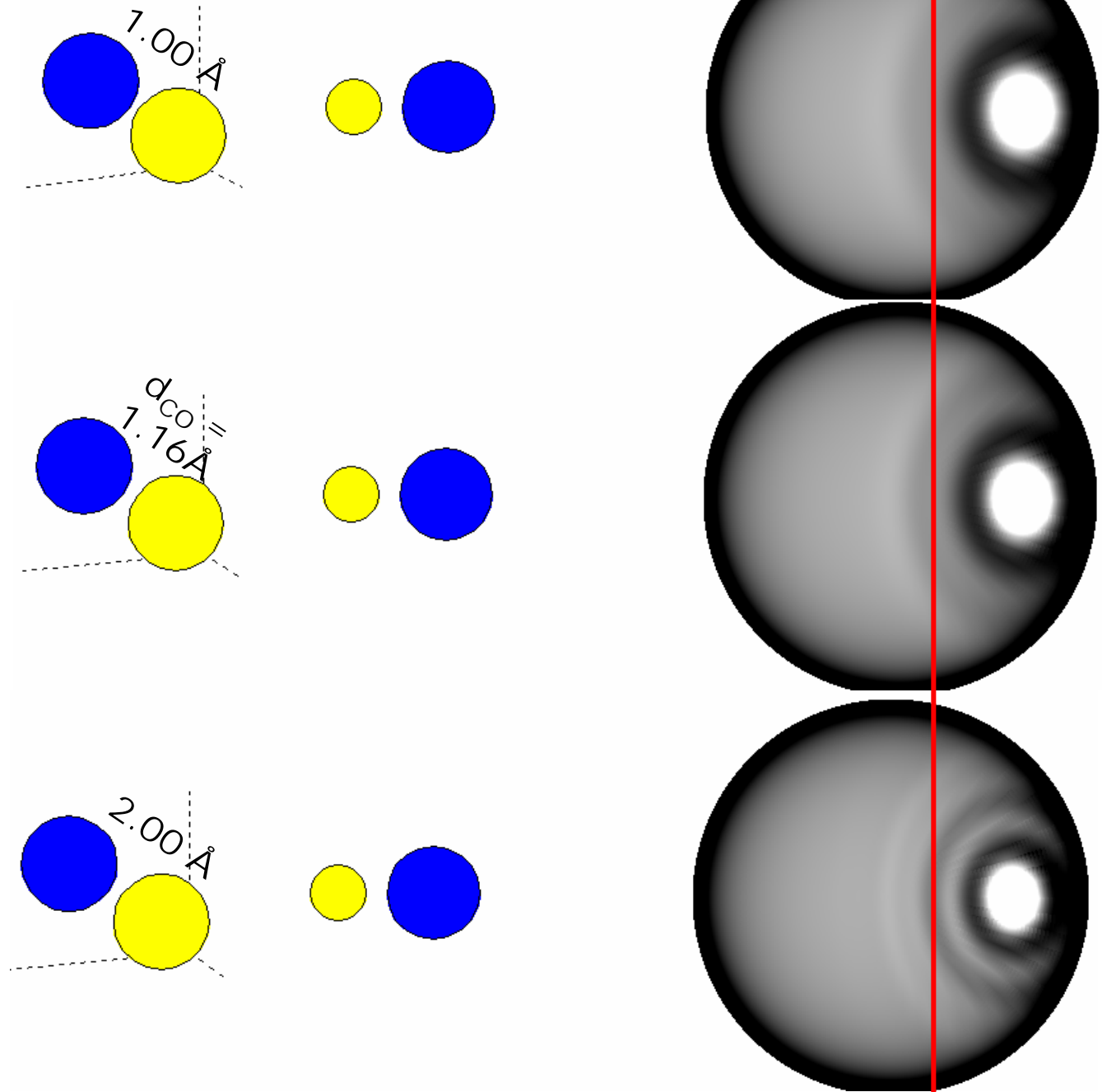


0.0 Å



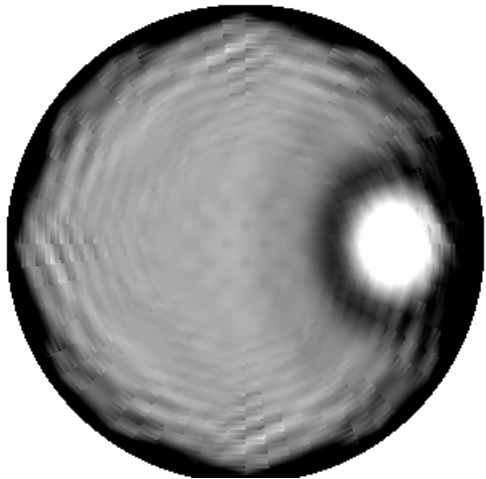
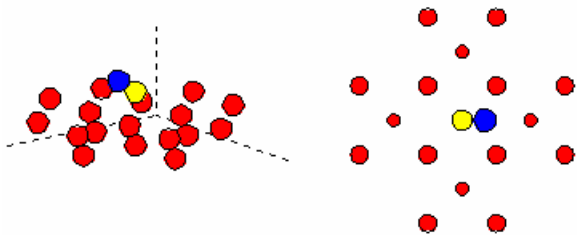
Iron-1<sup>st</sup> order diff. ring

CO/Fe(001)—Effect of CO bond dist.

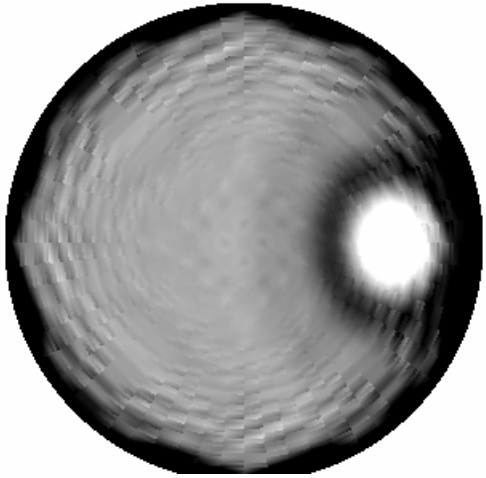
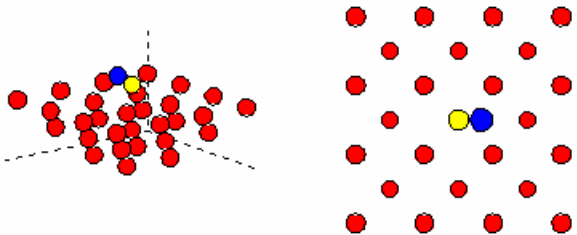


# CO/Fe(001)—Effect of cluster size

19 atoms:



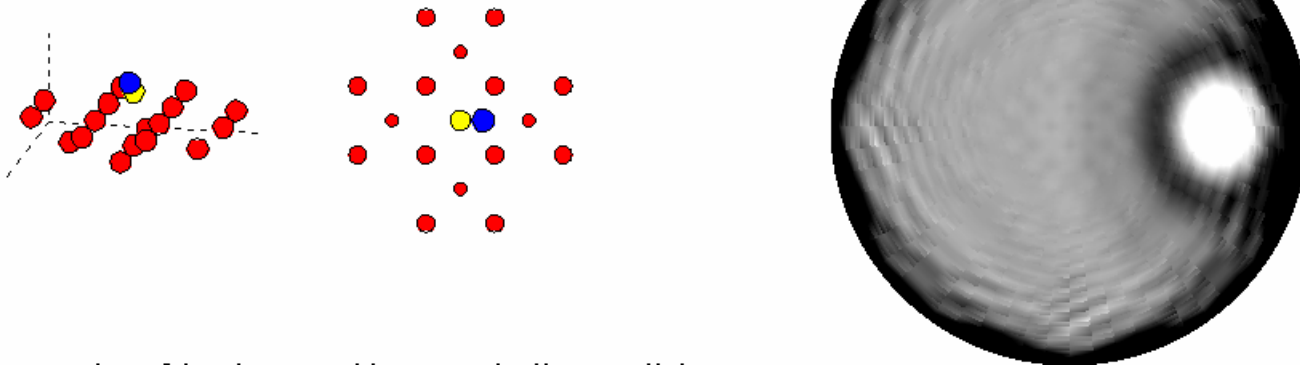
31 atoms:



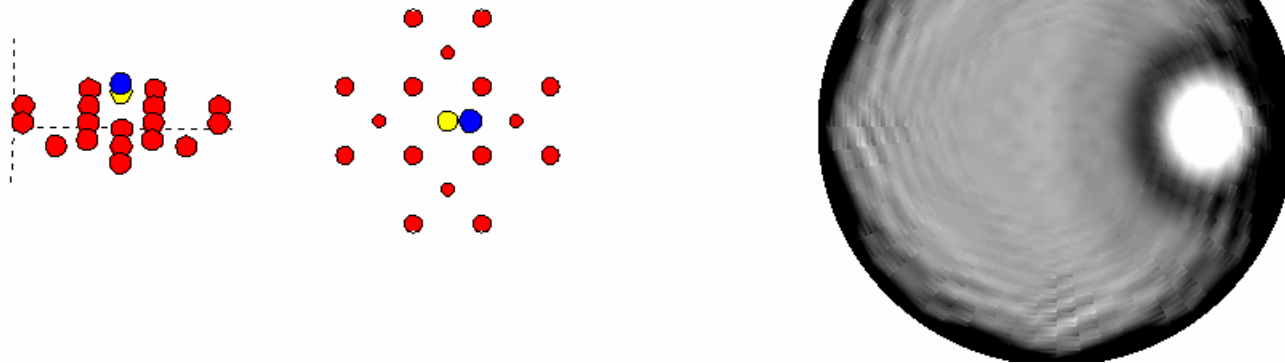
19  $\approx$  31, AND SO "CONVERGED" AT 19 OR LESS

# CO/Fe(001)—Effect of scattering order

Single scattering:



Fourth order scattering:



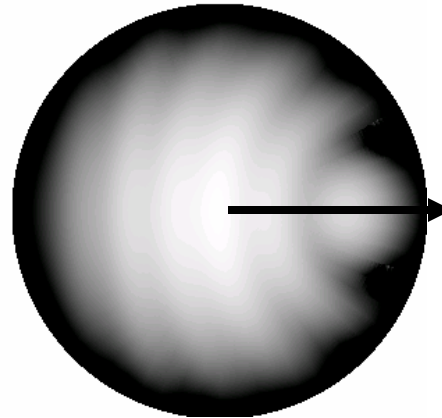
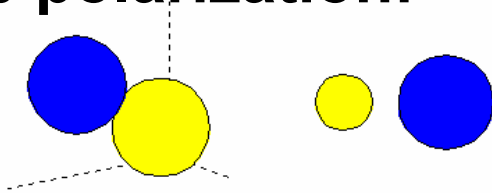
APPROX. CONVERGED AT SINGLE—FOR THIS PARTICULAR PROBLEM ONLY!



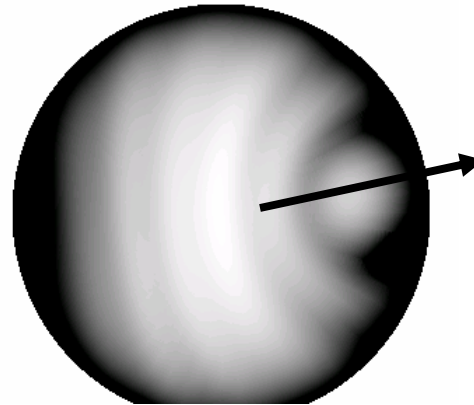
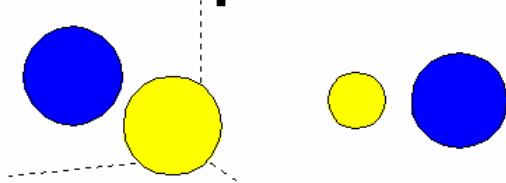
# Effect of varying the polarization?: C 1s emission from CO

$E_{\text{kin}} = 200 \text{ eV}$

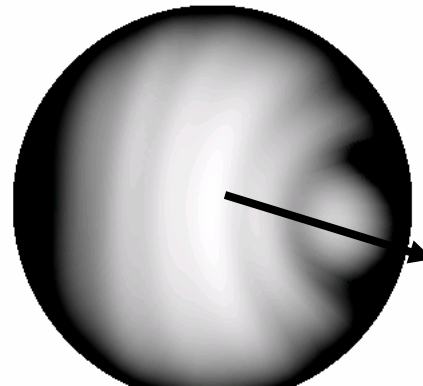
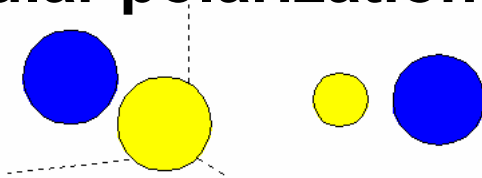
Linear p polarization:



Right circular polarization:

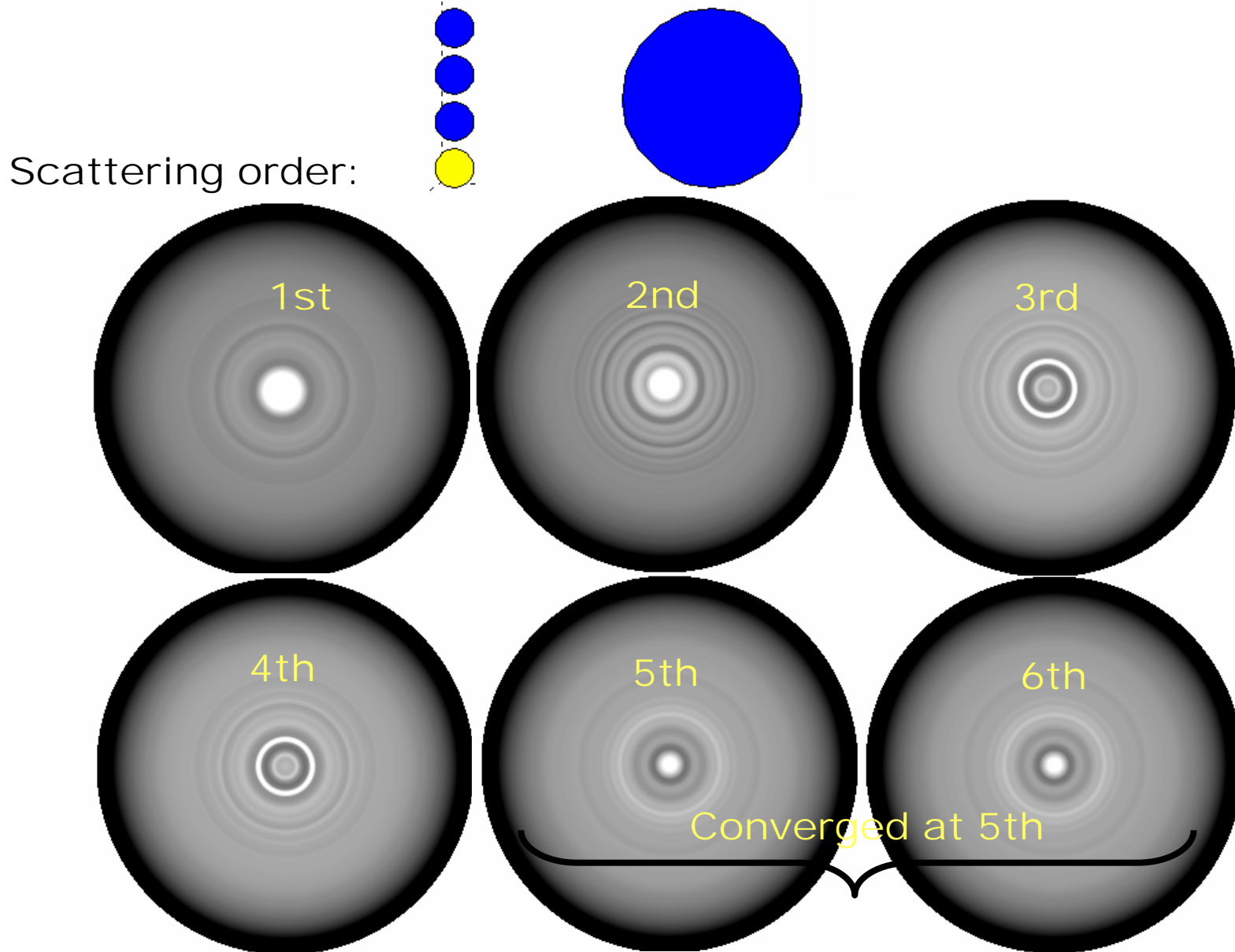


Left circular polarization:

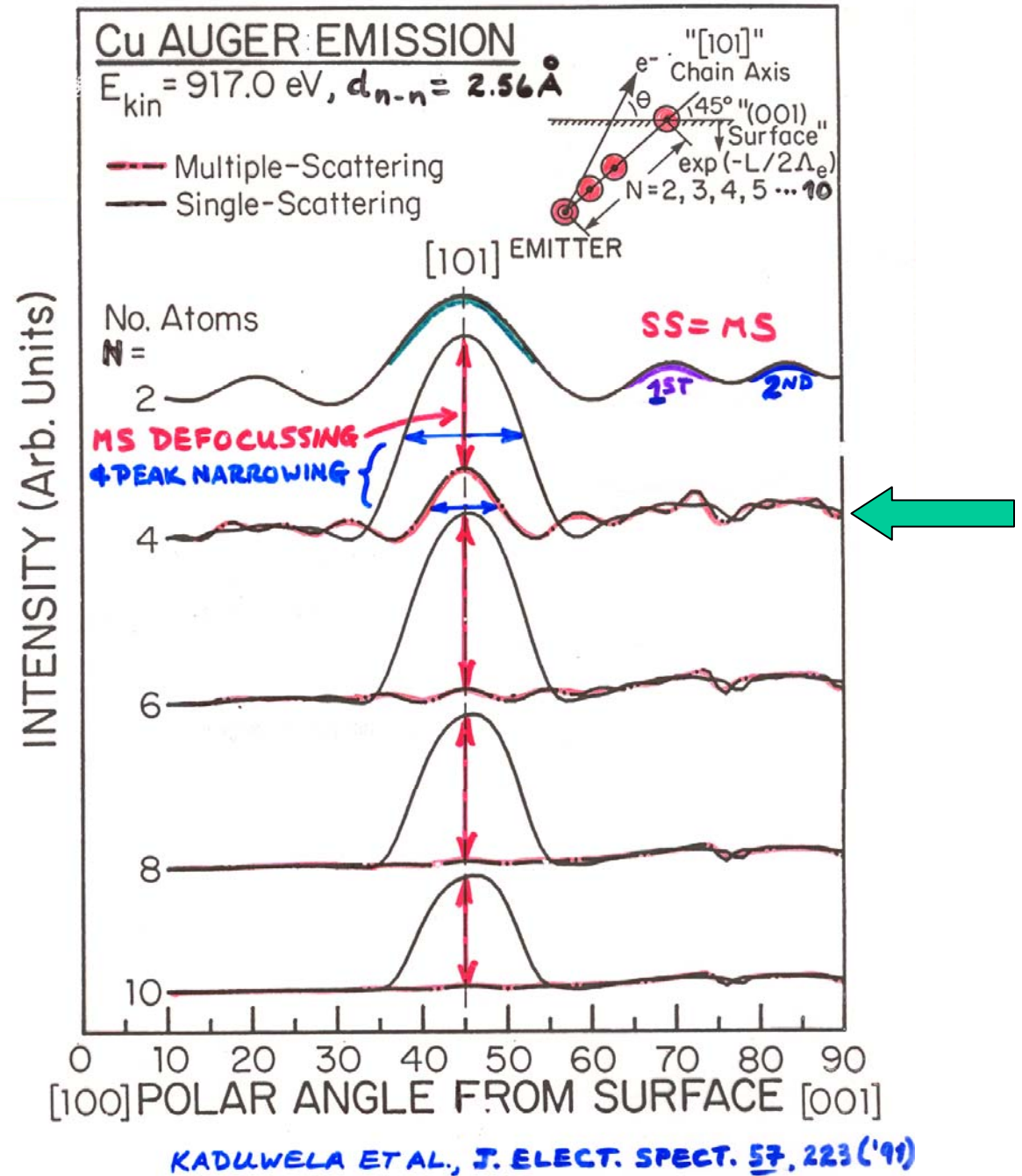


Circular dichroism in angular distributions (CDAD)—more later

# 4-atom Fe nearest-neighbor chain along [110]— Effect of scattering order



Cu nearest-neighbor chains along [110]—  
Effect of scattering order

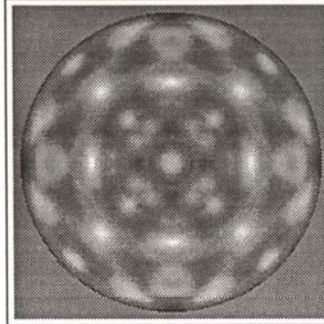


Plus cf. Figs. 6 and 7 in C.F., "The  
Study of Surface Structures by  
Photoelectron Diffraction and Auger  
Electron Diffraction"

Photoelectron Intensities From Different Surfaces  
(Stereographic Projection)

Ni(001):Ni 2p at 636 eV

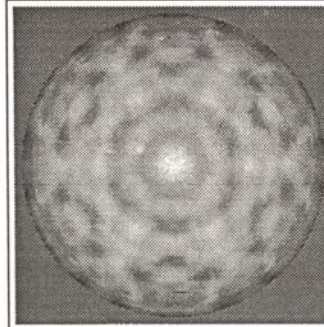
fcc  
(001)



THEVUTHASAN  
ET AL.

Ru(0001):Ru 3d at 1206 eV

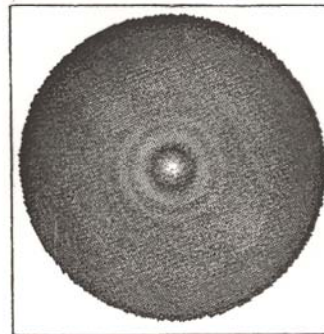
hcp  
(0001)



THEVUTHASAN  
ET AL.

HOPG:Graphite (0001): C 1s at 946 eV

textured

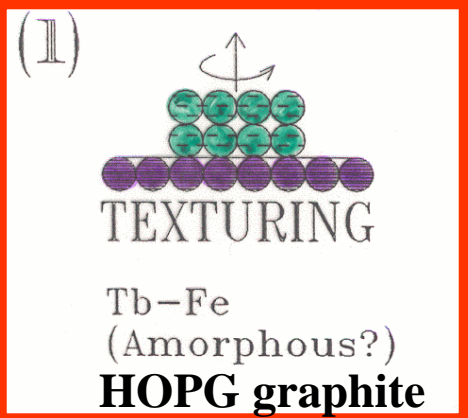
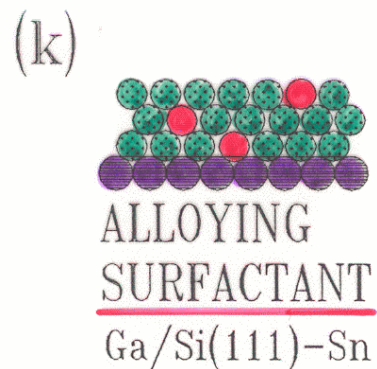
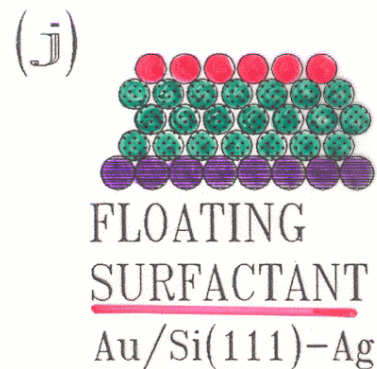
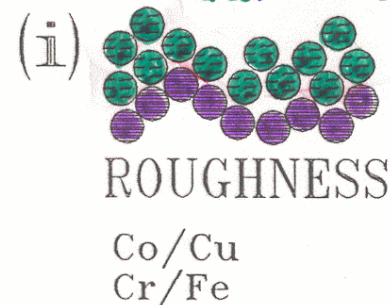
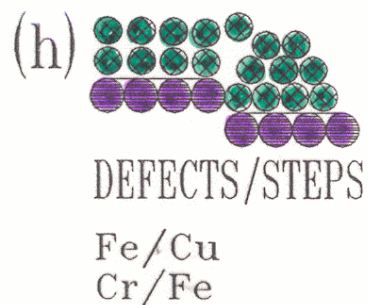
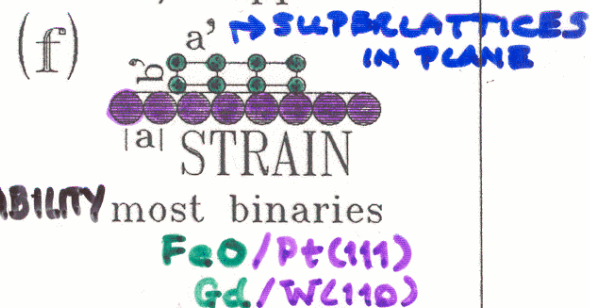
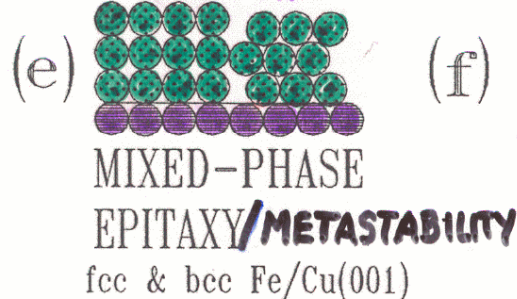
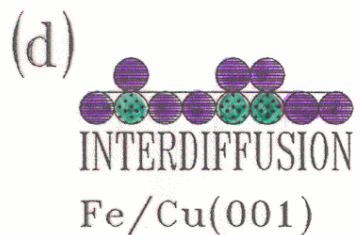
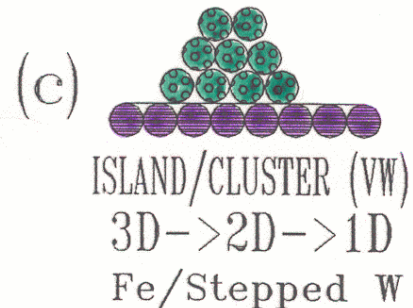
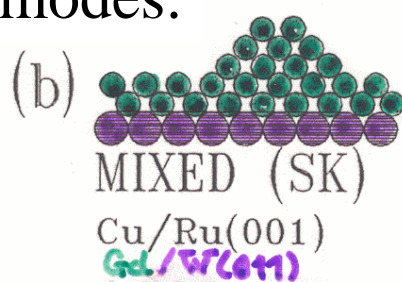
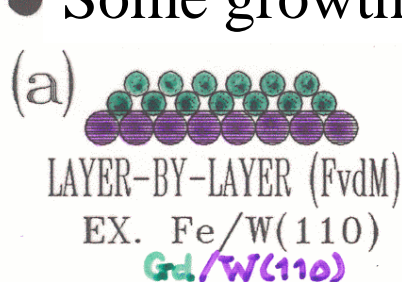


OSTERWALDER  
ET AL.

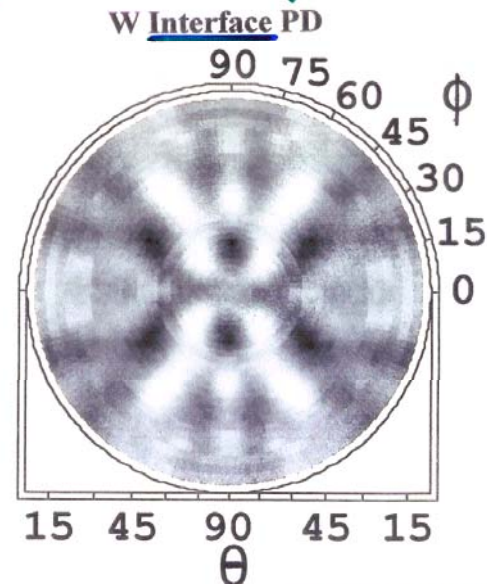
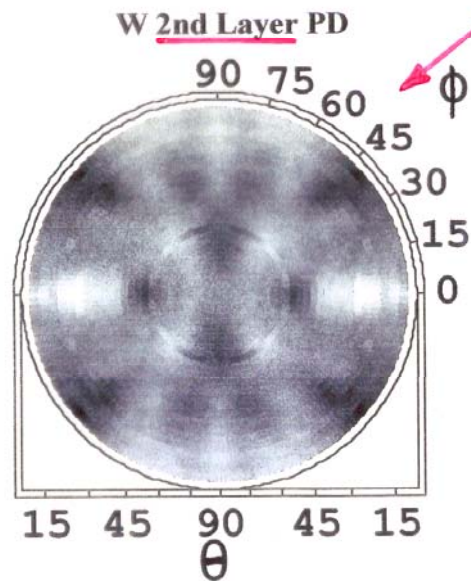
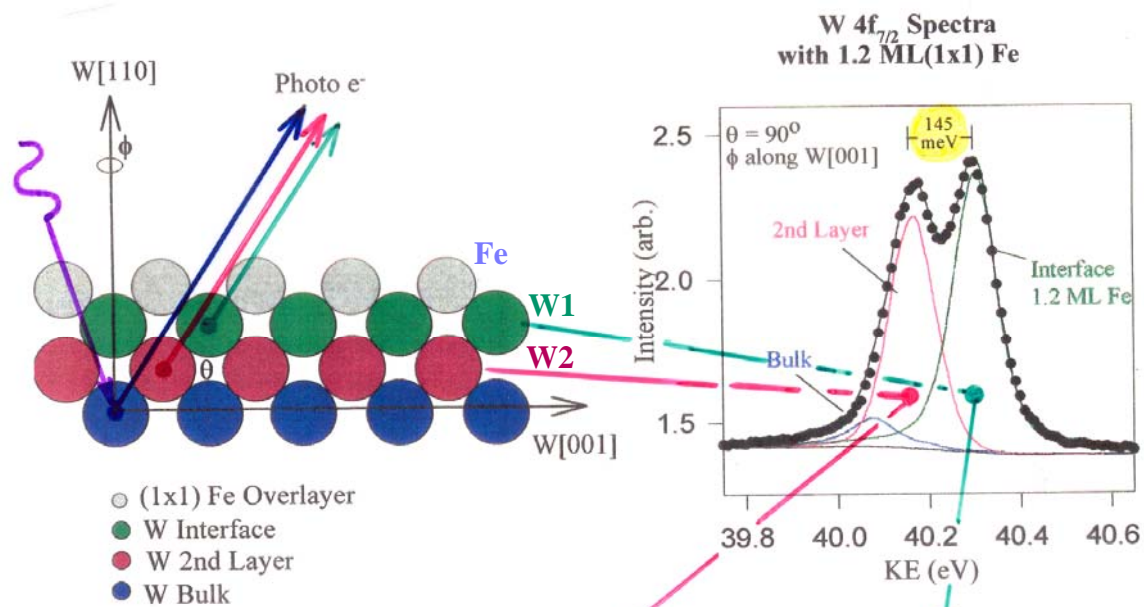


Fingerprint  
identification  
of short-range  
atomic  
structure  
and symmetry

● Some growth modes:

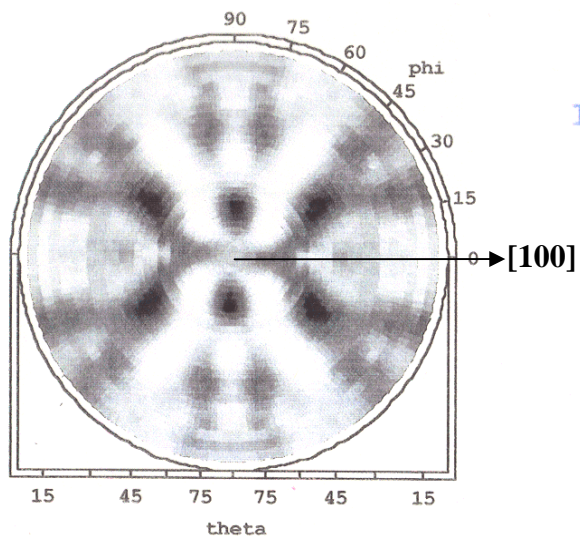


# Photoelectron diffraction from W(110) interface atoms beneath an Fe overlayer



TOBER ET AL.  
 P.R.L.,  
 79, 2085 ('93)

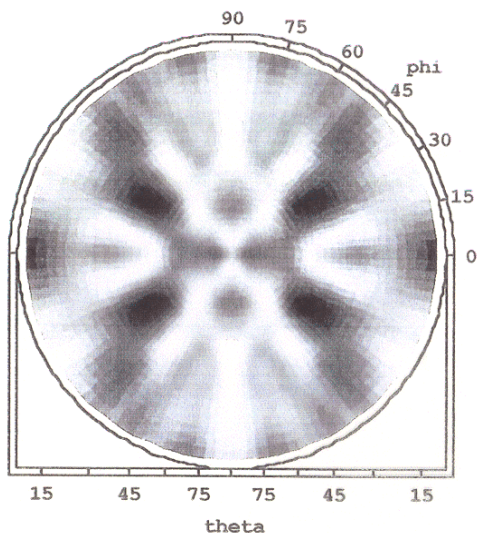
# Fe on W(110): Determination of structure by expt./theory comparison



W 4f<sub>7/2</sub>  
Interface Diffraction

Experiment

$h\nu = 70 \text{ eV}$   
 $E_{\text{kin}} = 40 \text{ eV}$



W 4f<sub>7/2</sub>  
Interface Diffraction

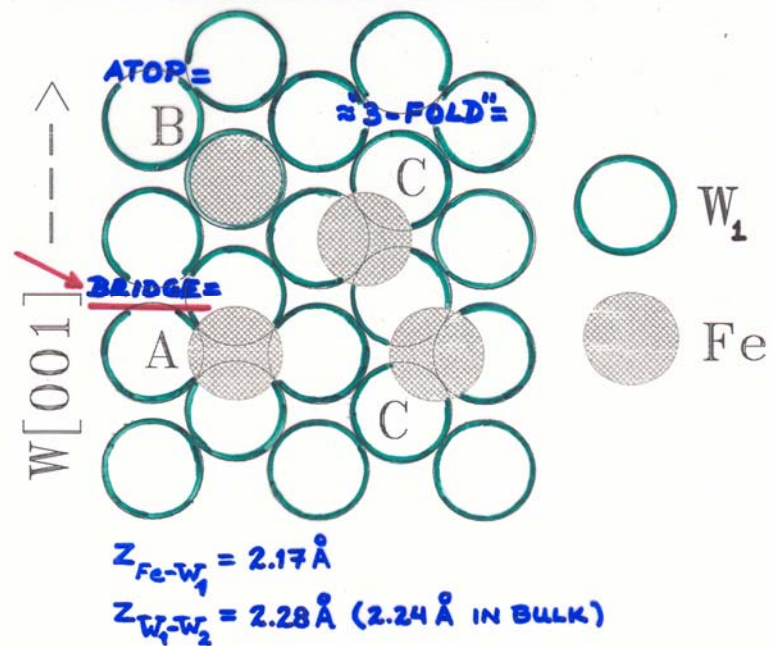
Multiple Scattering  
Theory  
(110 atom cluster)

$E_{\text{kin}} = 40 \text{ eV}$   
 $Z_{\text{Fe}} = 2.165 \text{ \AA}$

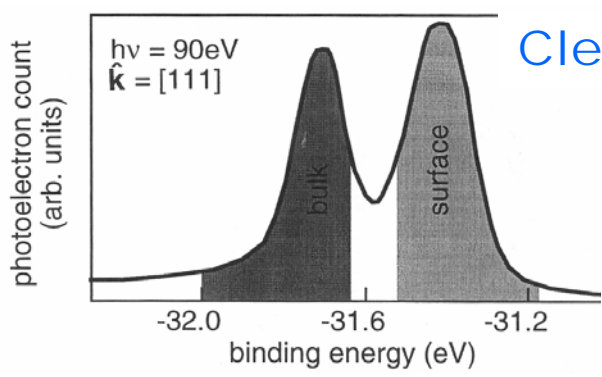
(Bridge Site)

↳ CONTINUES BULK  
W STRUCTURE

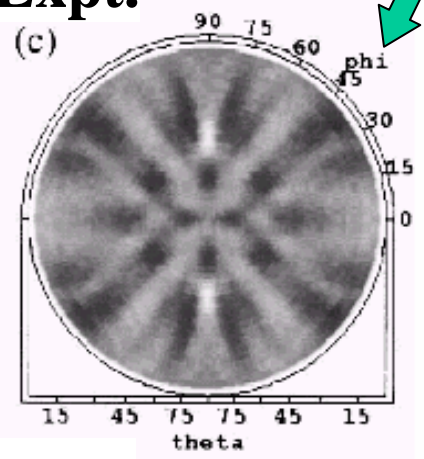
STRUCTURE DETERMINATION:



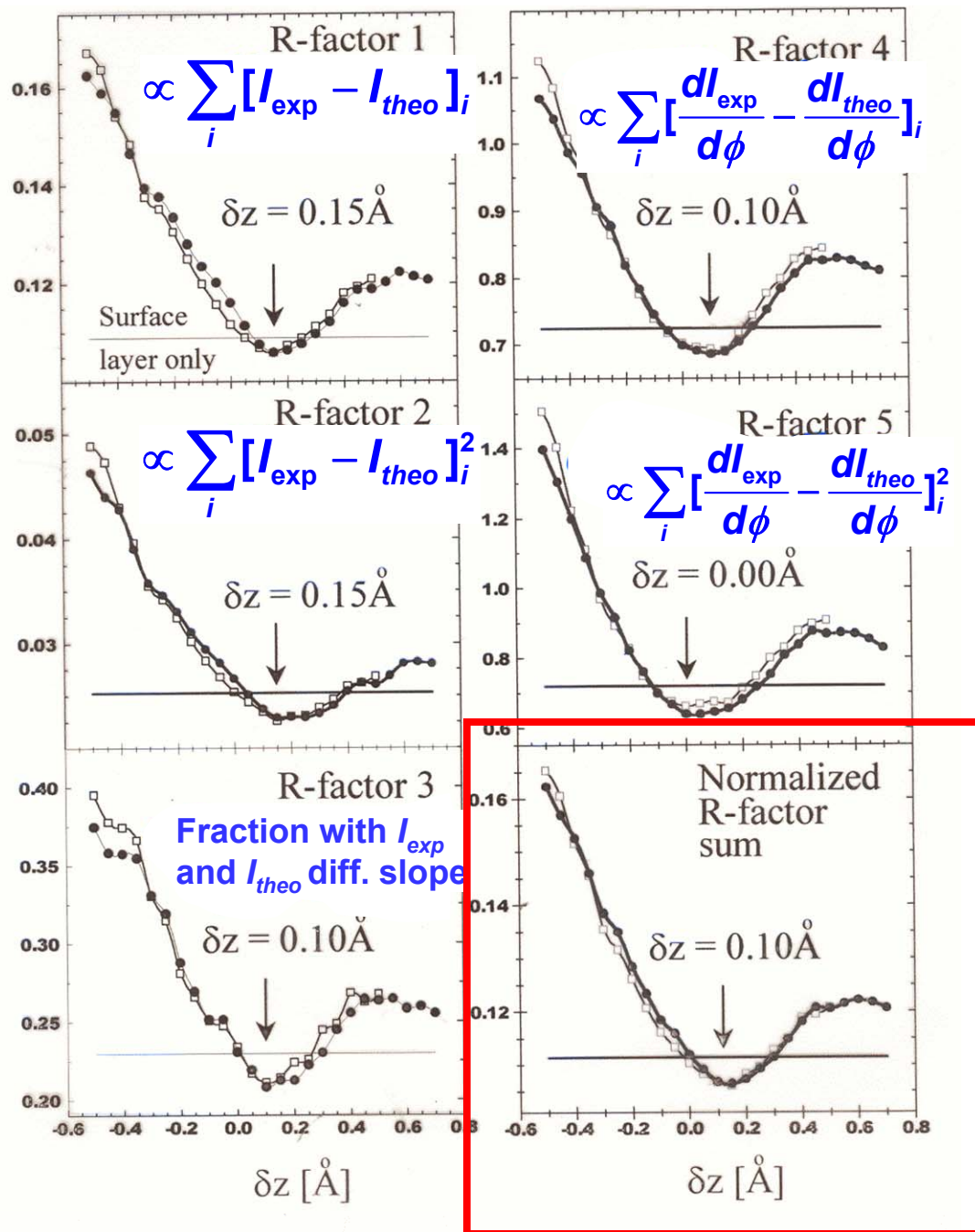
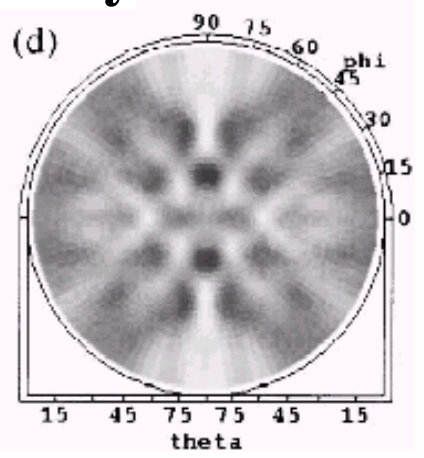
# Clean W(110) 4f Surface Peak: R-Factor Analysis



**Expt.**



**Theory**

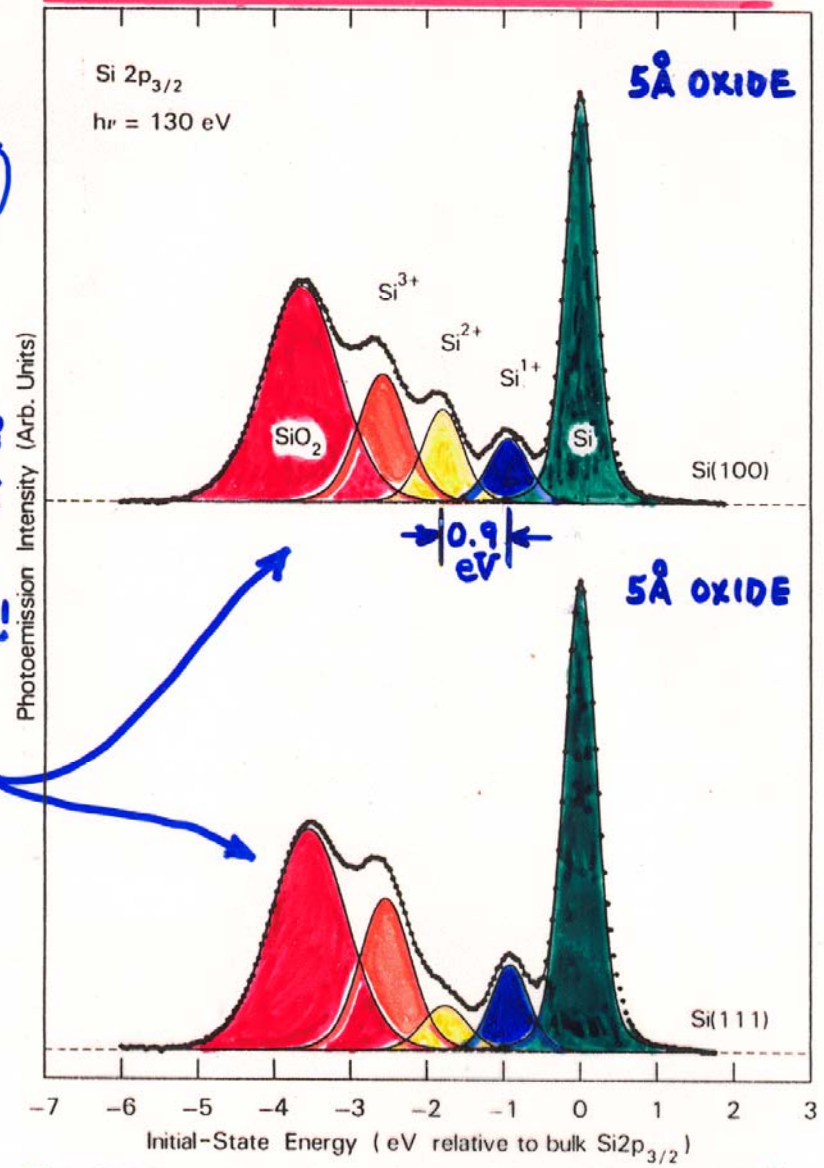




**PHOTOELECTRON SPECTRA**  
**OXIDIZED SILICON**  
**CHEMICAL SHIFTS OF CORE LEVELS**

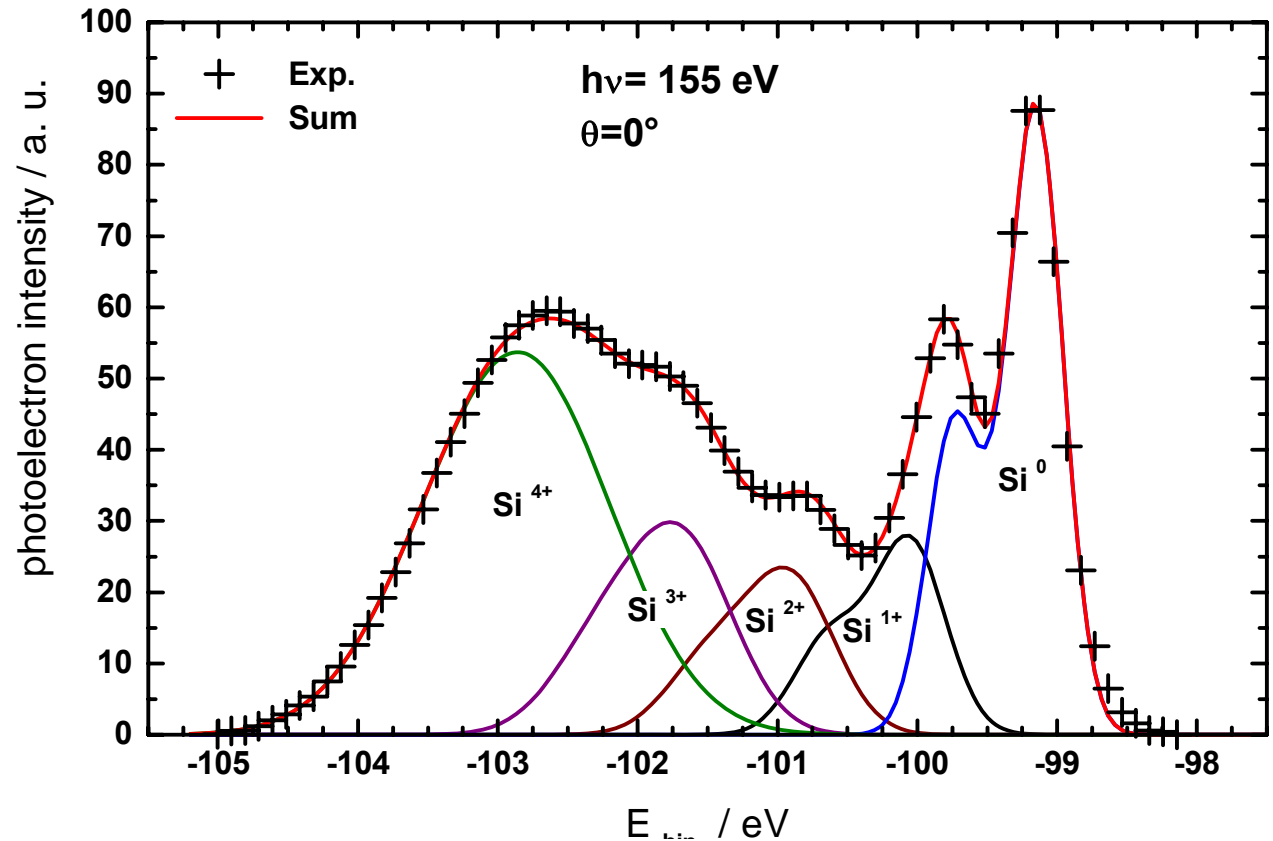


EXACTLY  
 WHAT IS  
 STRUCTURE  
 OF INTERFACE?  
 NEED STATE-  
 SPECIFIC  
 STRUCTURAL  
 INFORMATION!



HIMPSEL ET AL., PHYS. REV. B, 38, 6084 ('90)

Case study:  
Interface  
structure of  
 $\text{SiO}_x/\text{SiO}_2$   
(Westphal et al.)



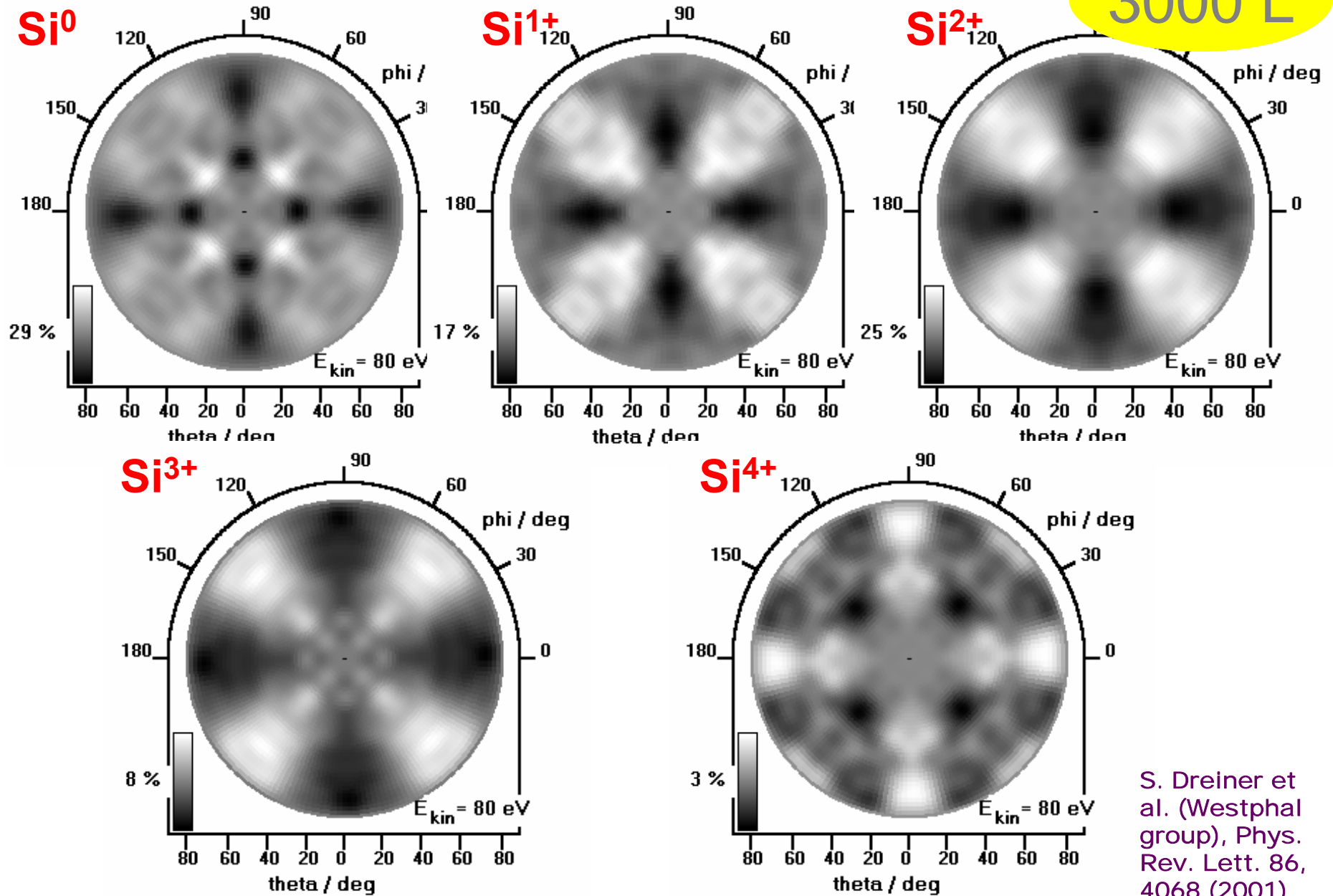
<b>Spin-orbit-splitting</b>	<b>0.58 eV</b>
<b><math>\text{Si}^0</math> width</b>	<b>0.48 eV</b>
<b><math>\text{Si}^{1+}</math> shift / width</b>	<b>0.9 / 0.59 eV</b>
<b><math>\text{Si}^{2+}</math> shift / width</b>	<b>1.74 / 0.72 eV</b>
<b><math>\text{Si}^{3+}</math> shift / width</b>	<b>2.46 / 0.84 eV</b>
<b><math>\text{Si}^{4+}</math> shift / width</b>	<b>3.54 / 1.42 eV</b>

F.J. Himpsel et al, Phys. Rev. B 38 (1988) 6084

S. Dreiner et al. (Westphal group), Phys. Rev. Lett. 86, 4068 (2001)

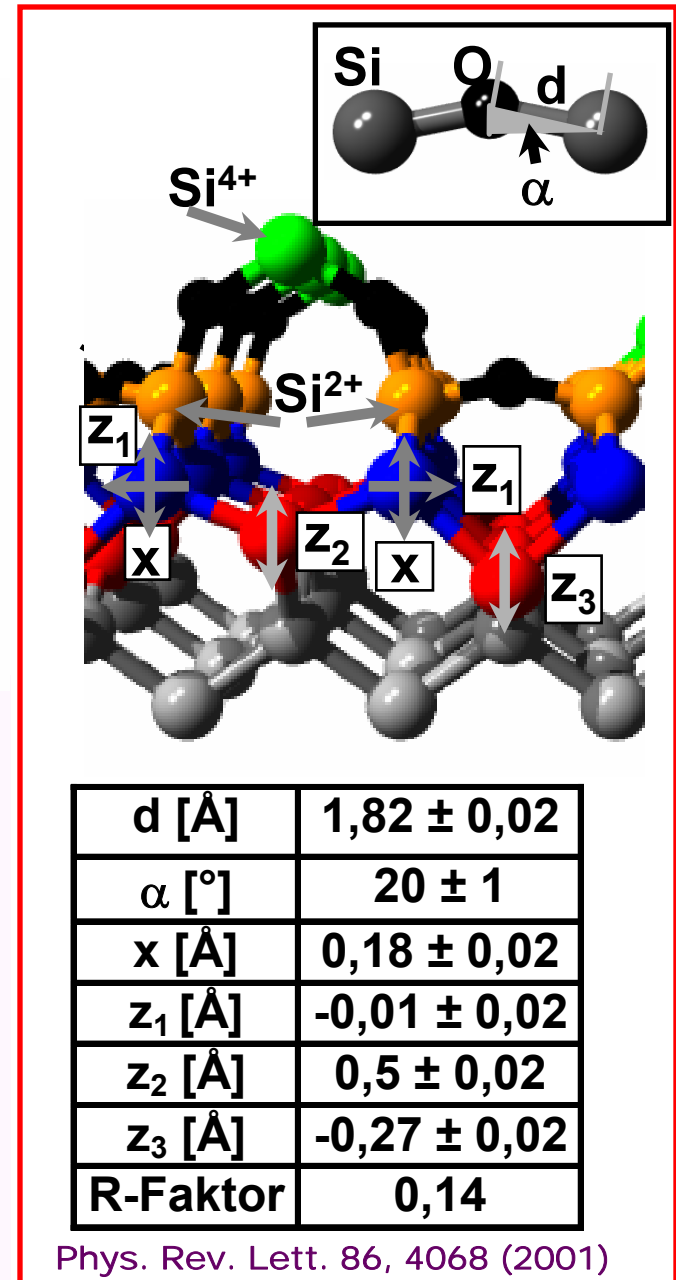
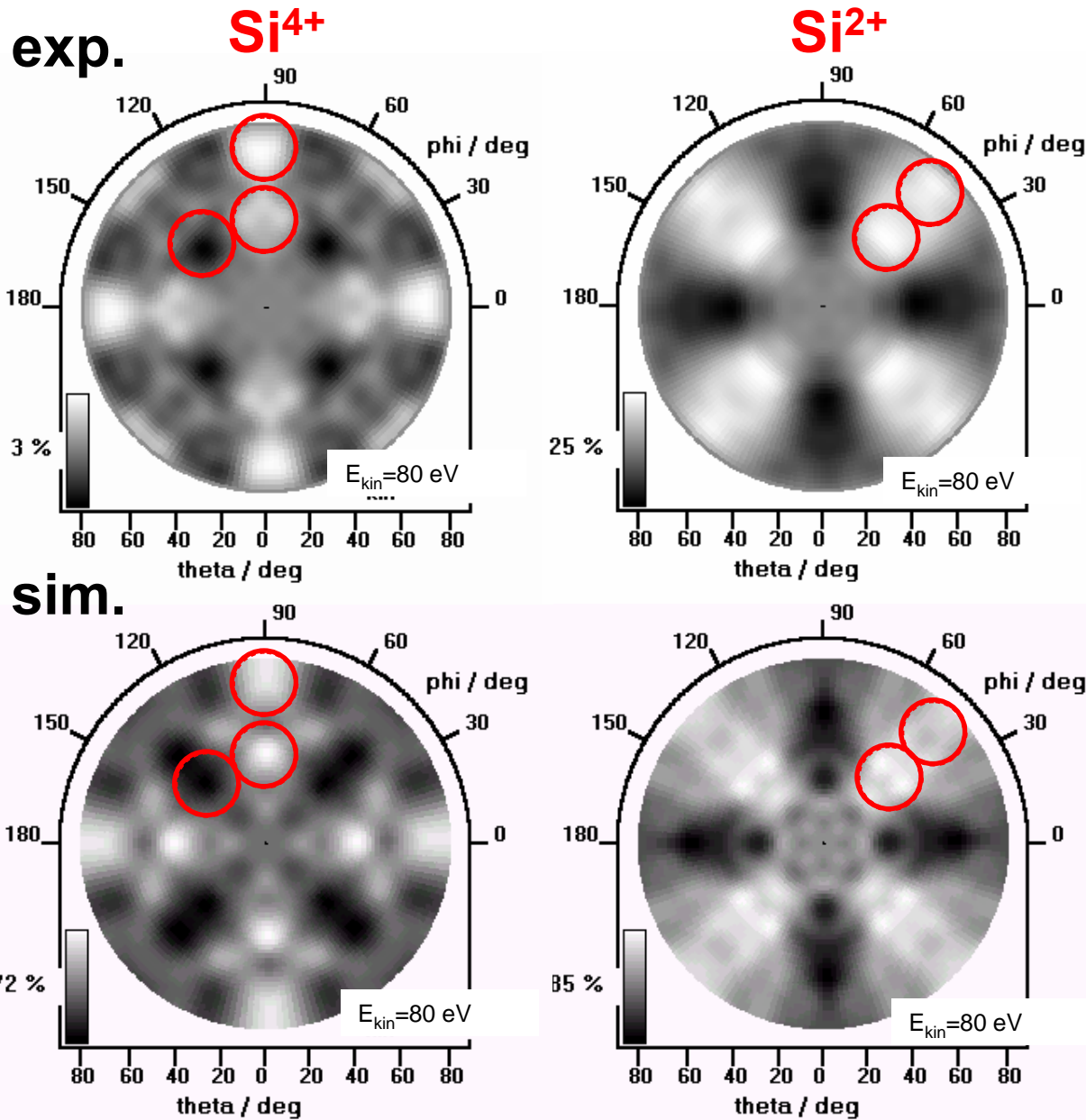
# Experimental diffraction patterns for SiO<sub>2</sub>/Si(100)

3000 L

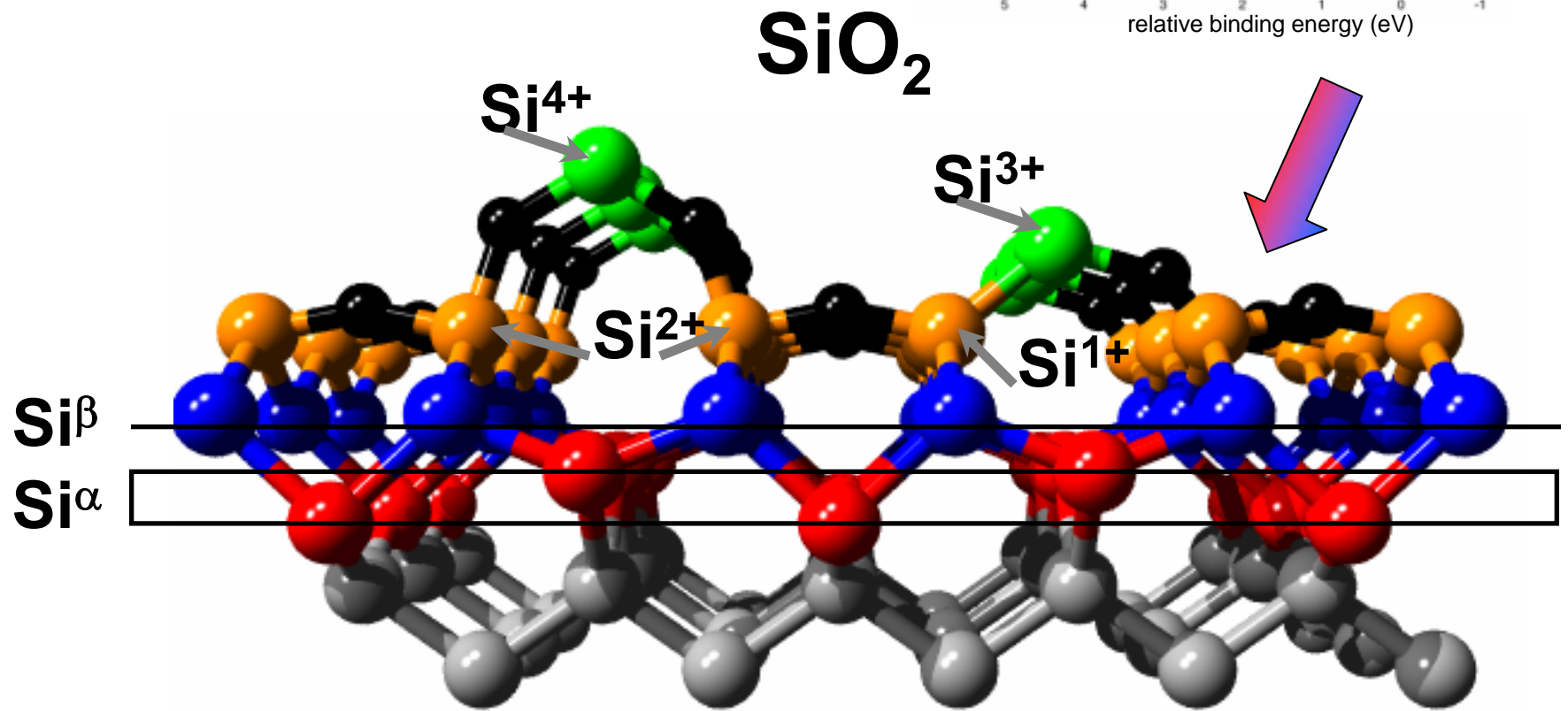
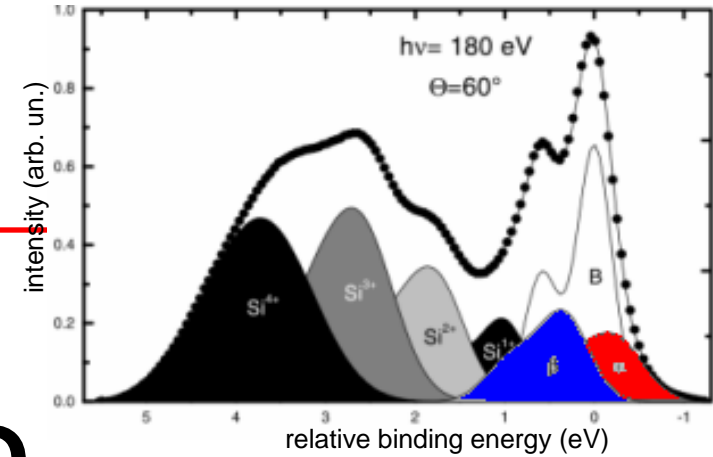
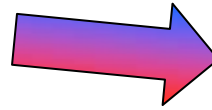


S. Dreiner et al. (Westphal group), Phys. Rev. Lett. 86, 4068 (2001)

# Structure determination by R-factor analysis: SiO<sub>x</sub>/Si(100)



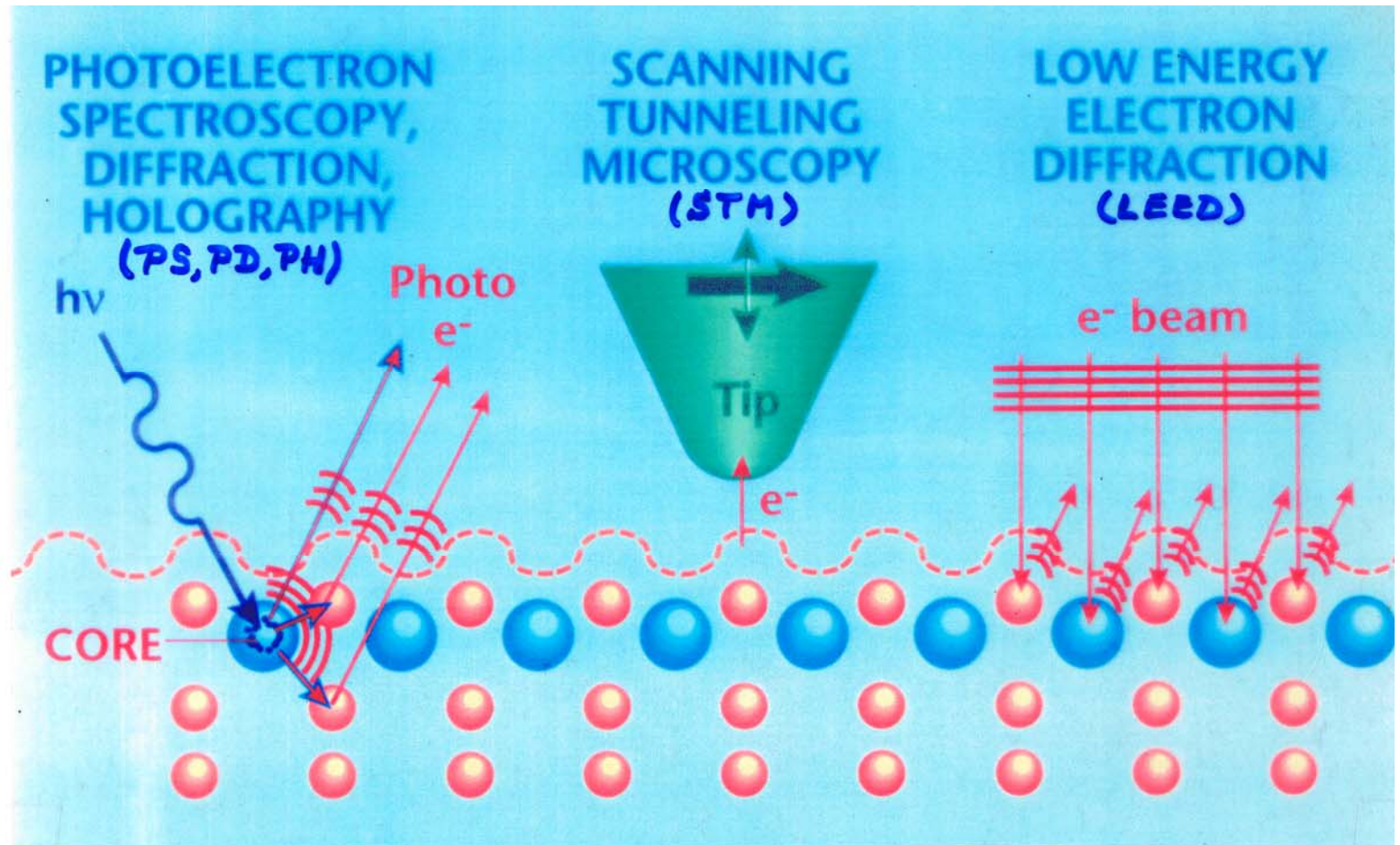
+ Assignment of additional  $\text{Si}^\alpha$ - and  $\text{Si}^\beta$ -components



**Si-bulk**

S. Dreiner et al. (Westphal group)

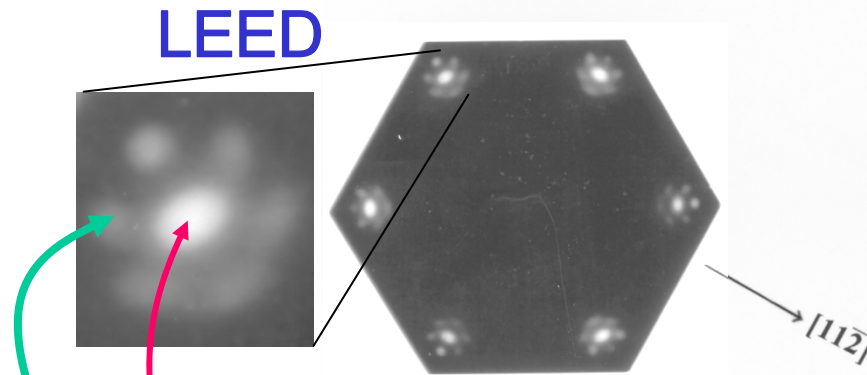
# Some Complementary Surface Structure Probes



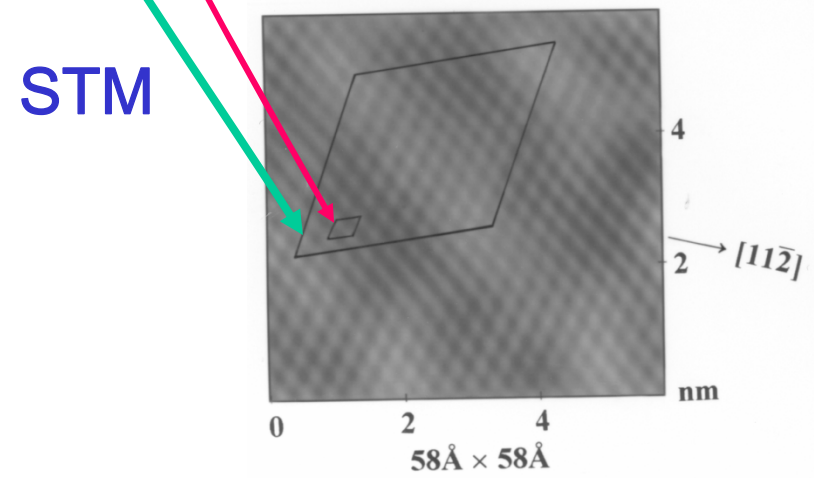
	Short ( $< 10\text{\AA}$ )	Short, long and disorder	Long ( $> 100\text{\AA}$ )
- <u>Type of order:</u>	Short ( $< 10\text{\AA}$ )	Short, long and disorder	Long ( $> 100\text{\AA}$ )
- <u>Atom &amp; site specific:</u>	Yes	No	No
- <u>Sensing depth:</u>	5-40 $\text{\AA}$	Mostly surface D.O.S.	5-20 $\text{\AA}$
- <u>Lateral resolution:</u>	1 mm <sup>2</sup> to (300 $\text{\AA}$ ) <sup>2</sup>	Single atom	1 mm <sup>2</sup> to 1 micron <sup>2</sup>

**Case study:  
1 ML of FeO  
on Pt(111):  
A combined  
LEED, STM,  
XPD study**

(a) Low energy electron diffraction

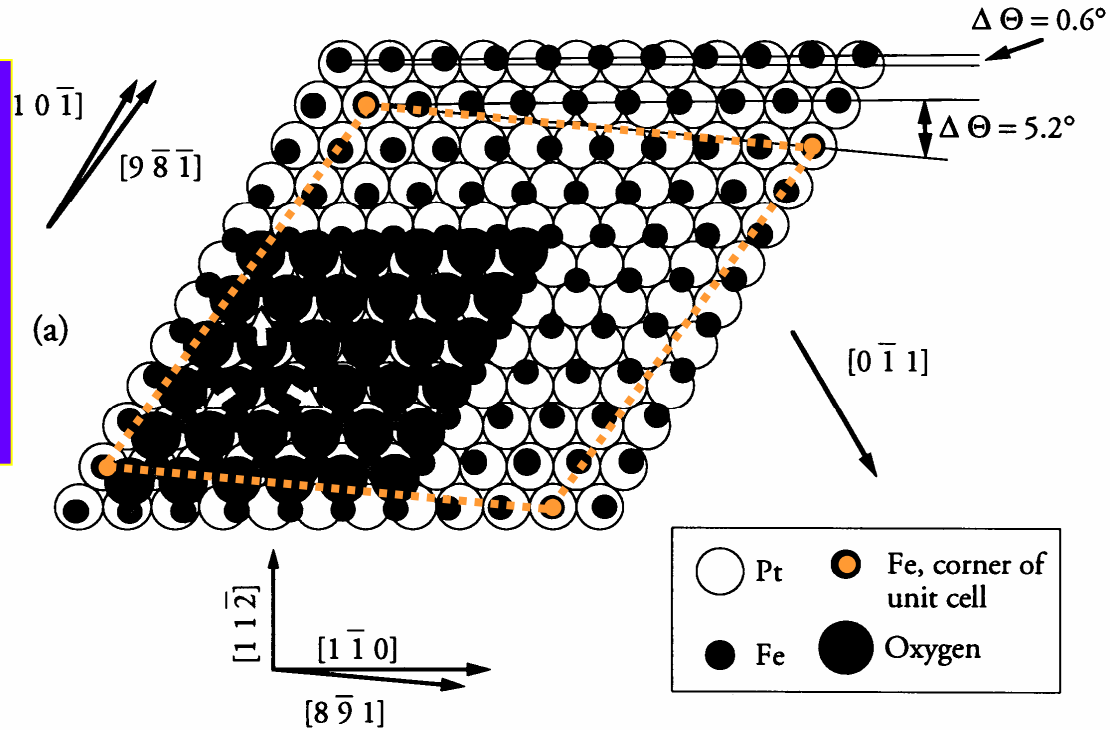


(b) Scanning tunneling microscopy



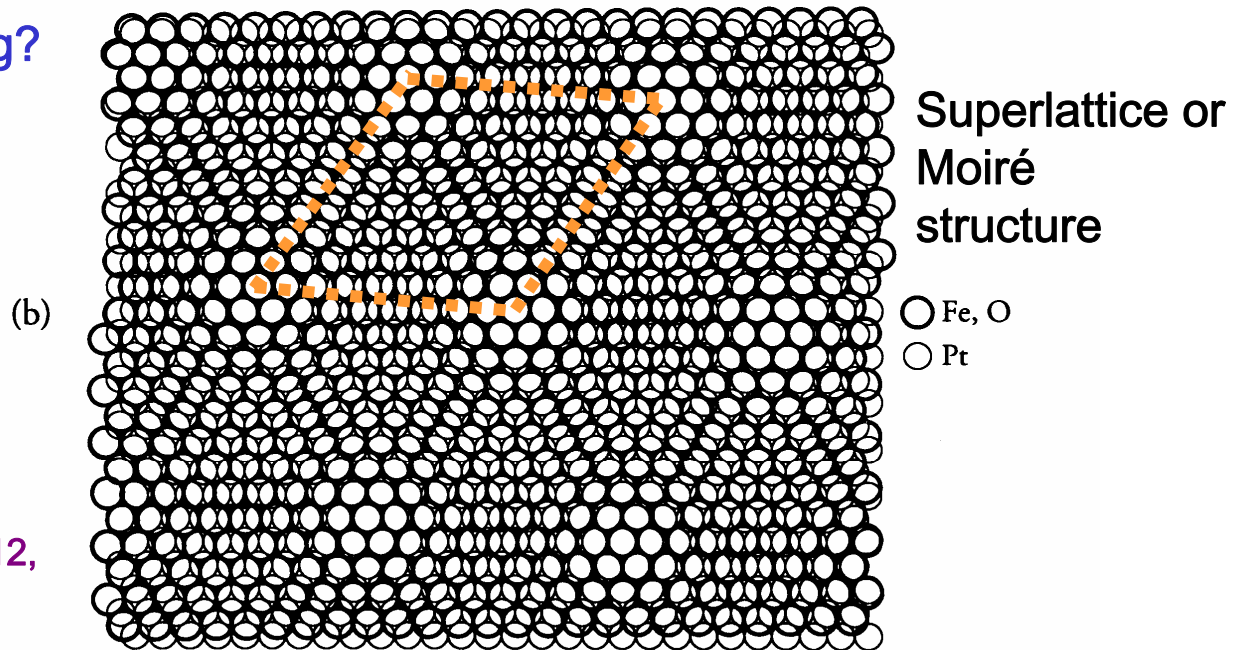
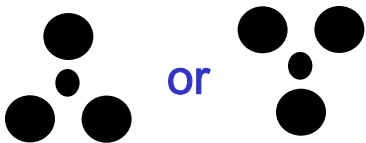
Galloway et al., Surf. Sci. 198, 127 ('93);  
J. Vac. Sci. Tech. A12, 2302 ('94).  
Y.J. Kim et al.,  
Phys. Rev. B 55, R 13448 ('97);  
Surf. Sci. 416, 68 ('98)

1 ML of FeO  
on Pt(111):  
Structural model  
from  
LEED and STM



Remaining Questions:

- Is Fe or O on top?
- Fe-O interlayer spacing?
- Fe-O orientation?

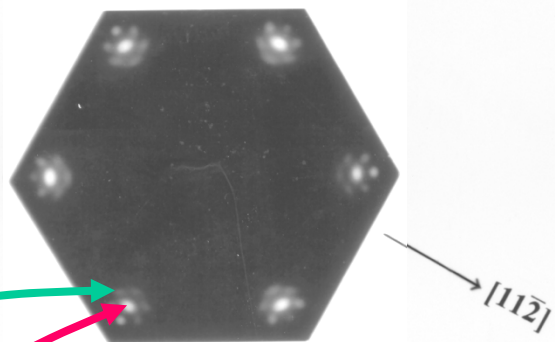


Galloway et al., Surf. Sci. 198, 127 ('93); J. Vac. Sci. Tech. A12, 2302 ('94).



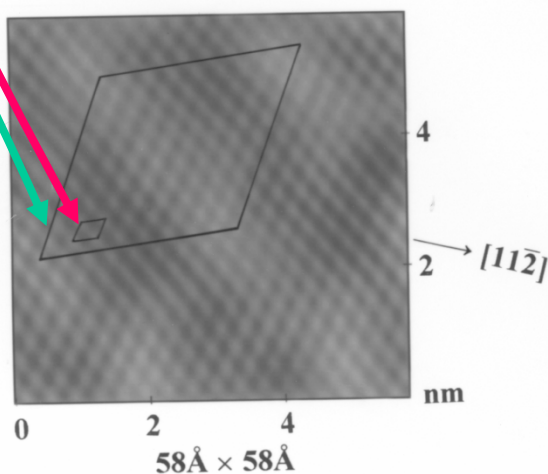
(a) Low energy electron diffraction

LEED

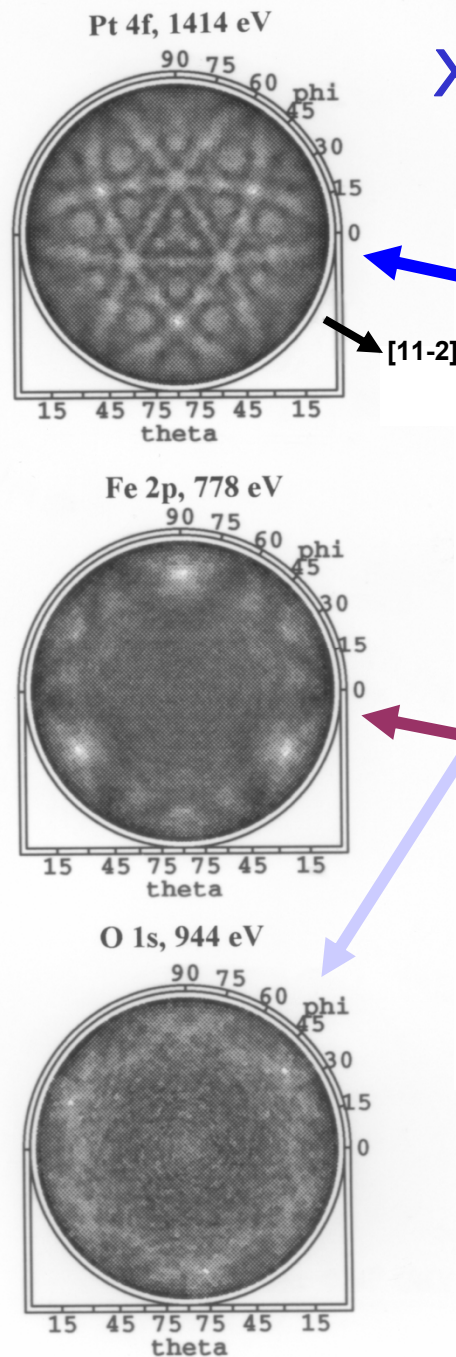


(b) Scanning tunneling microscopy

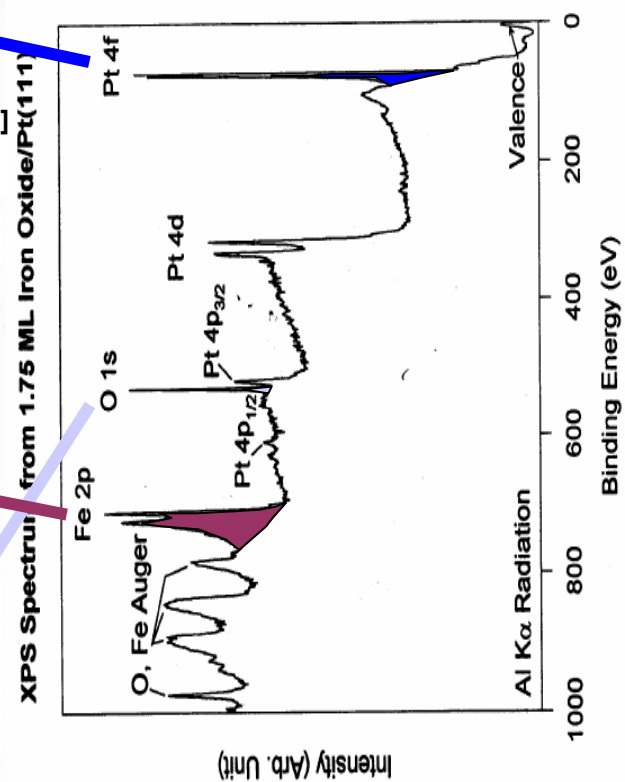
STM



(c) Photoelectron diffraction



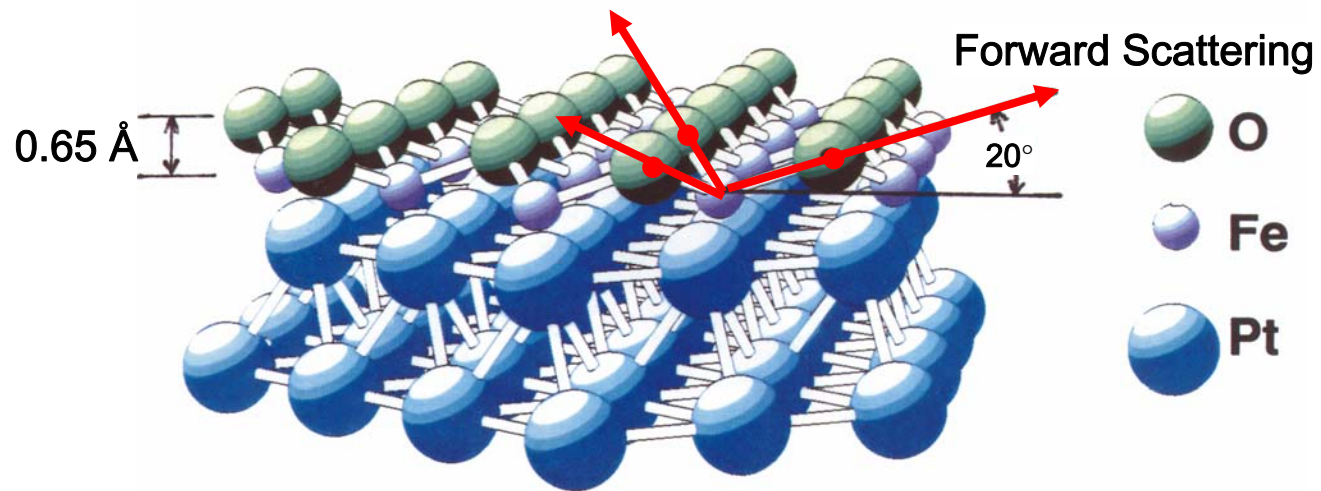
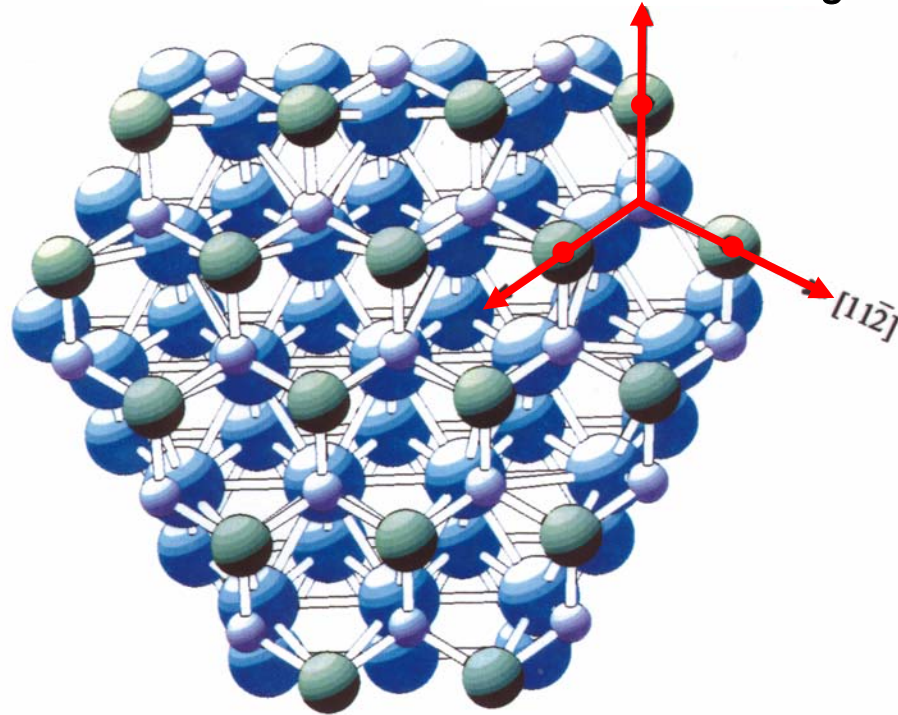
XPD



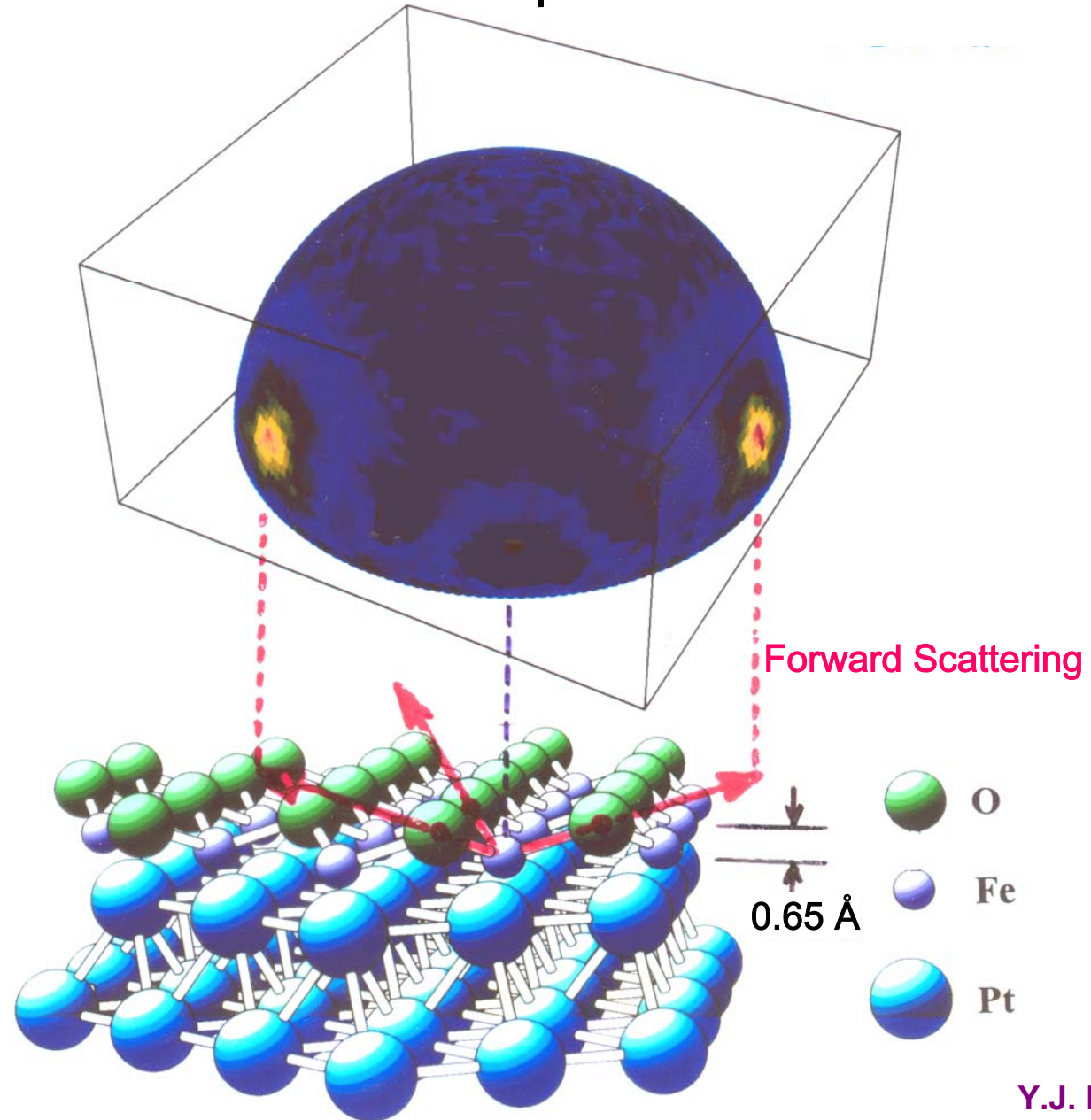
Y.J. Kim et al.,  
Phys. Rev. B 55, R 13448 ('97);  
Surf. Sci. 416, 68 ('98)

# FeO/Pt(111)

Forward Scattering



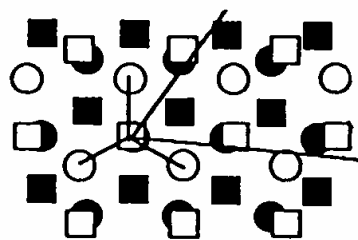
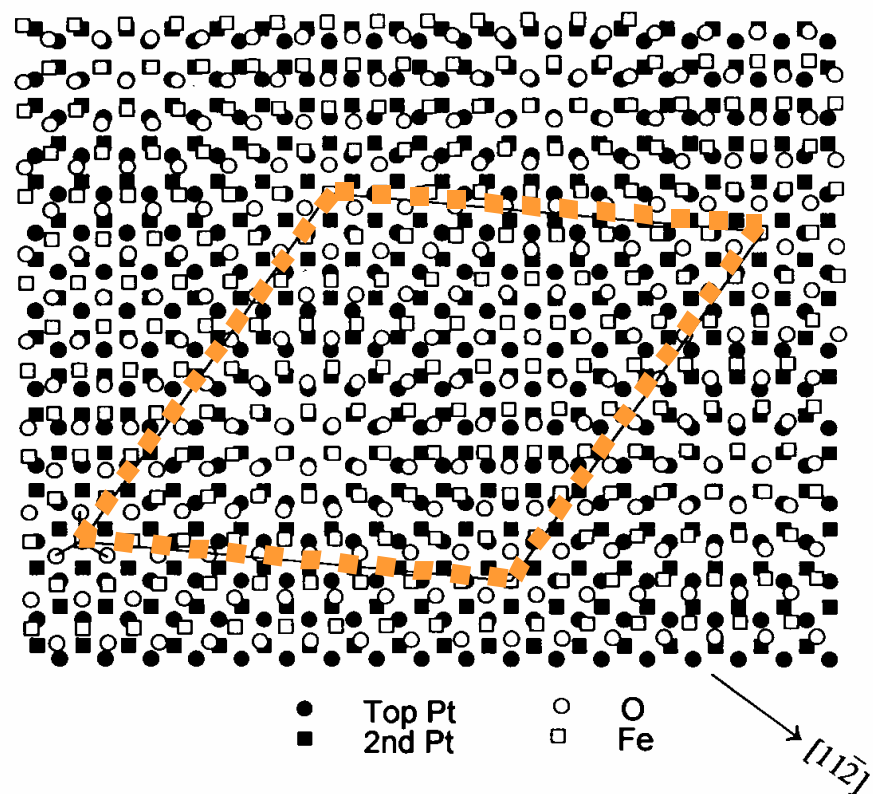
# X-ray Photoelectron Diffraction: Fe 2p from 1ML FeO on Pt(111)



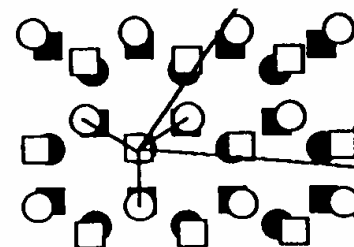
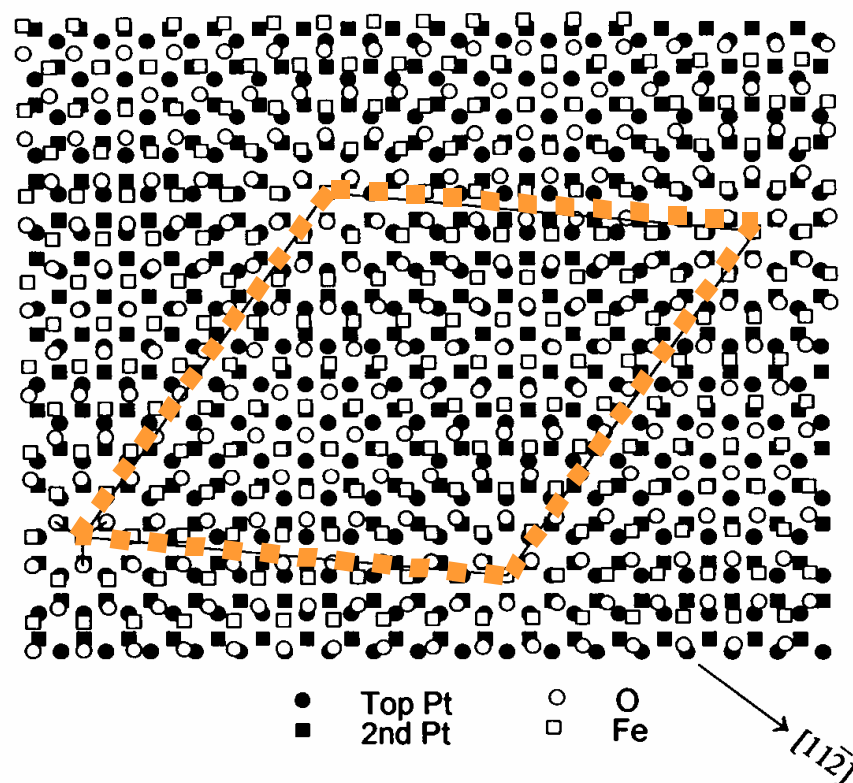
Y.J. Kim et al.  
Phys. Rev. B 55, R 13448 ('97)

# Permits selecting favored domain of growth—2<sup>nd</sup> layer Pt effect

(a) FeO/Pt(111) - Favored

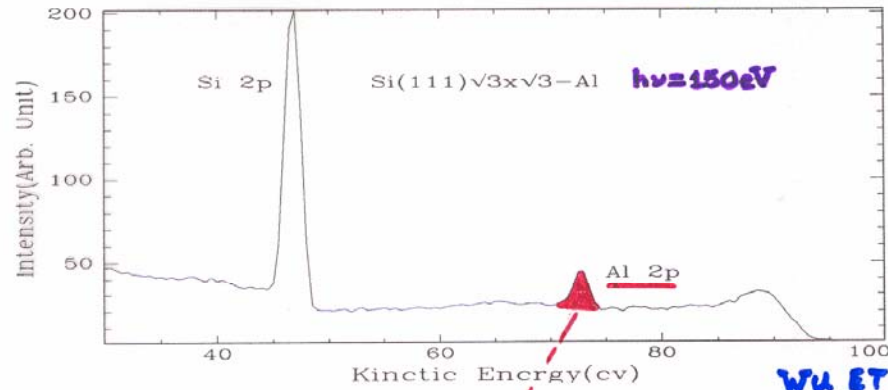


(b) FeO/Pt(111) - Unfavored

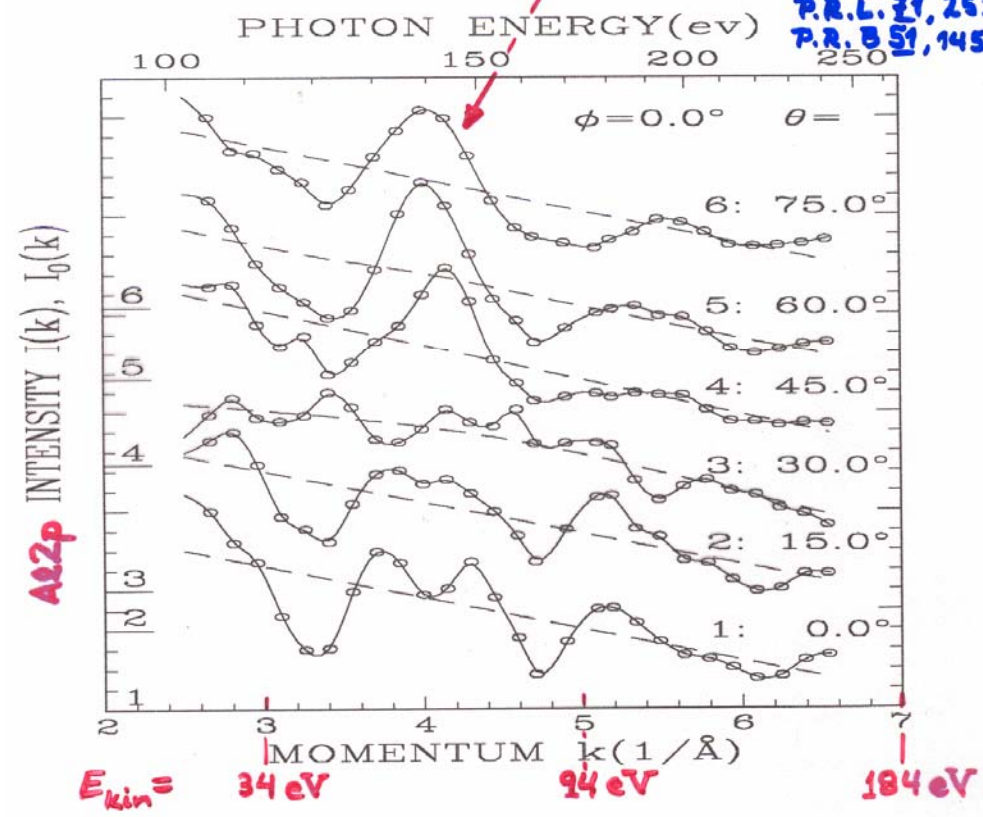


SCANNED-ENERGY PHOTOELECTRON DIFF.  
 $(\sqrt{3} \times \sqrt{3})$  Al on Si(111)

\* 41 diffraction curves  $\chi$  taken from Al 2p } ~1100 DATA POINTS  
 \*  $\theta = 0 \sim 70^\circ, \phi = 0 \sim 60^\circ$

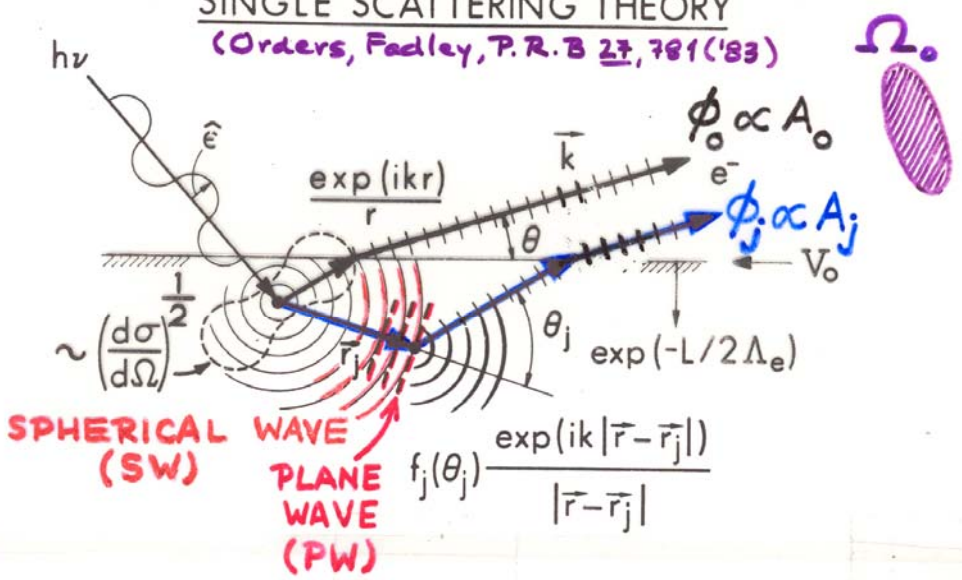


WU ET AL.,  
 P.R.L. 31, 261 ('93)  
 P.R. B 51, 14549 ('95)



**Photoelectron diffraction:  
Simple single-scattering theory for s-subshell emission**

SINGLE SCATTERING THEORY  
(Orders, Fadley, P. R. B 27, 781 ('83))



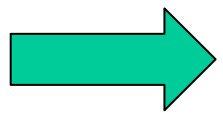
$$\chi(E \text{ or } \vec{k}) \propto \sum_j \frac{F_j(k)}{F_0} \cos \left[ \underbrace{kr_j(1 - \cos \theta_j)}_{\text{PATH LENGTH DIFFERENCE (P.L.D.)}} + \underbrace{\psi_j(\theta_j, k)}_{\text{SCATTERING PHASE SHIFT}} \right]$$

$$F_j(k) = (\hat{\epsilon} \cdot \hat{r}_j) \frac{|f_j(\theta_j, k)|}{r_j} \underbrace{W_j(\theta_j, k)}_{\text{DEBYE-WALLER}} \exp(-L_j/2\Lambda_e) \underbrace{\exp(-L_j/2\Lambda_e)}_{\text{INELASTIC SCATTERING}}$$

= amplitude of scattered wave

$$F_0 = (\hat{\epsilon} \cdot \hat{k}) \exp(-L_0/2\Lambda_e)$$

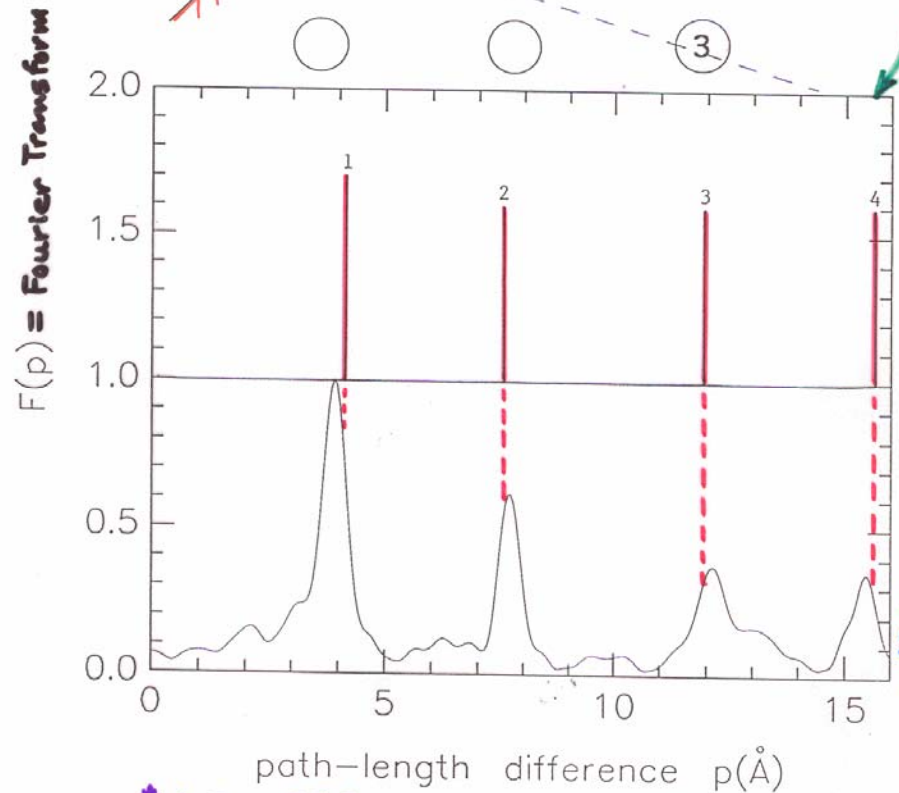
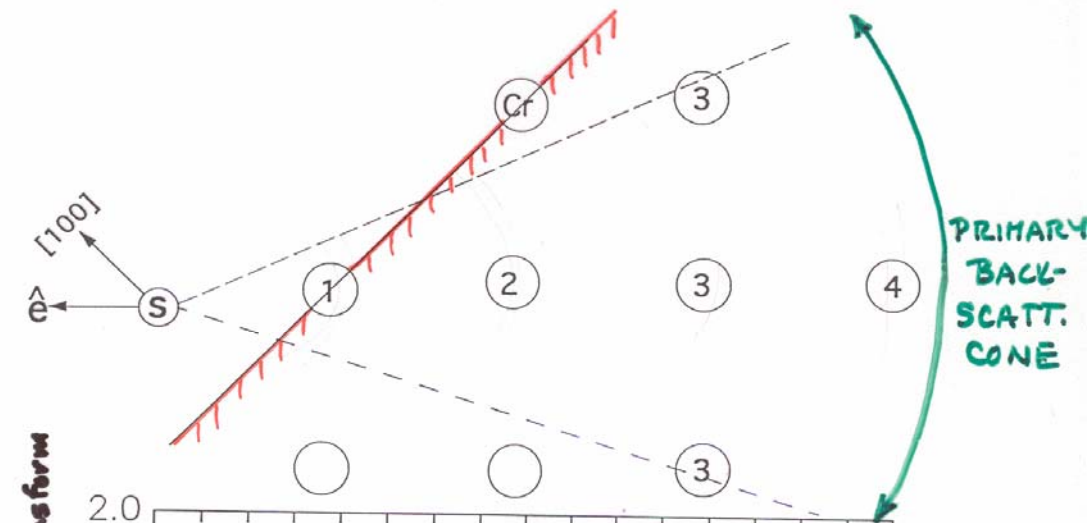
= amplitude of direct wave



∴ FOURIER TRANSFORM OF  $\chi(k) \Rightarrow$   
PEAKS AT  $\sim \text{P.L.D.} = r_j(1 - \cos \theta_j)$

PATH-LENGTH DIFF'S. FROM FOURIER TRANSFORMS\*

c(2x2)S/Cr(001): 45° off normal



ZHENG,  
SHIRLEY  
(1993)

\* AUTO-REGRESSIVE DATA EXTENSION

# Outline

**Surface, interface, and nanoscience—short introduction**

**Some surface concepts and techniques→photoemission**

**Synchrotron radiation: experimental aspects**

**Electronic structure—a brief review**

**The basic synchrotron radiation techniques:  
more experimental and theoretical details**

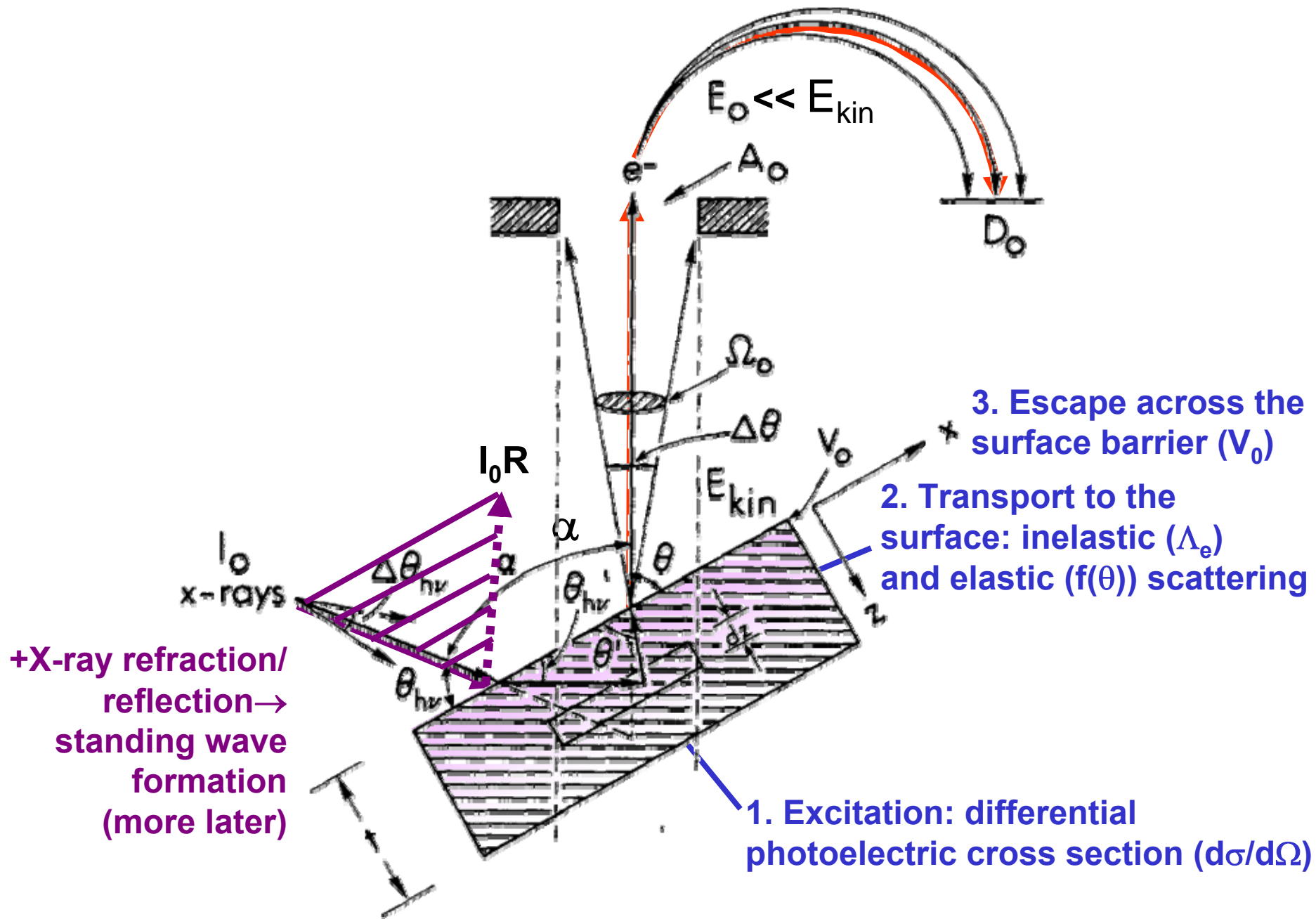
 **Core-level photoemission:  
X-ray optical effects on intensities**

**Valence-level photoemission**

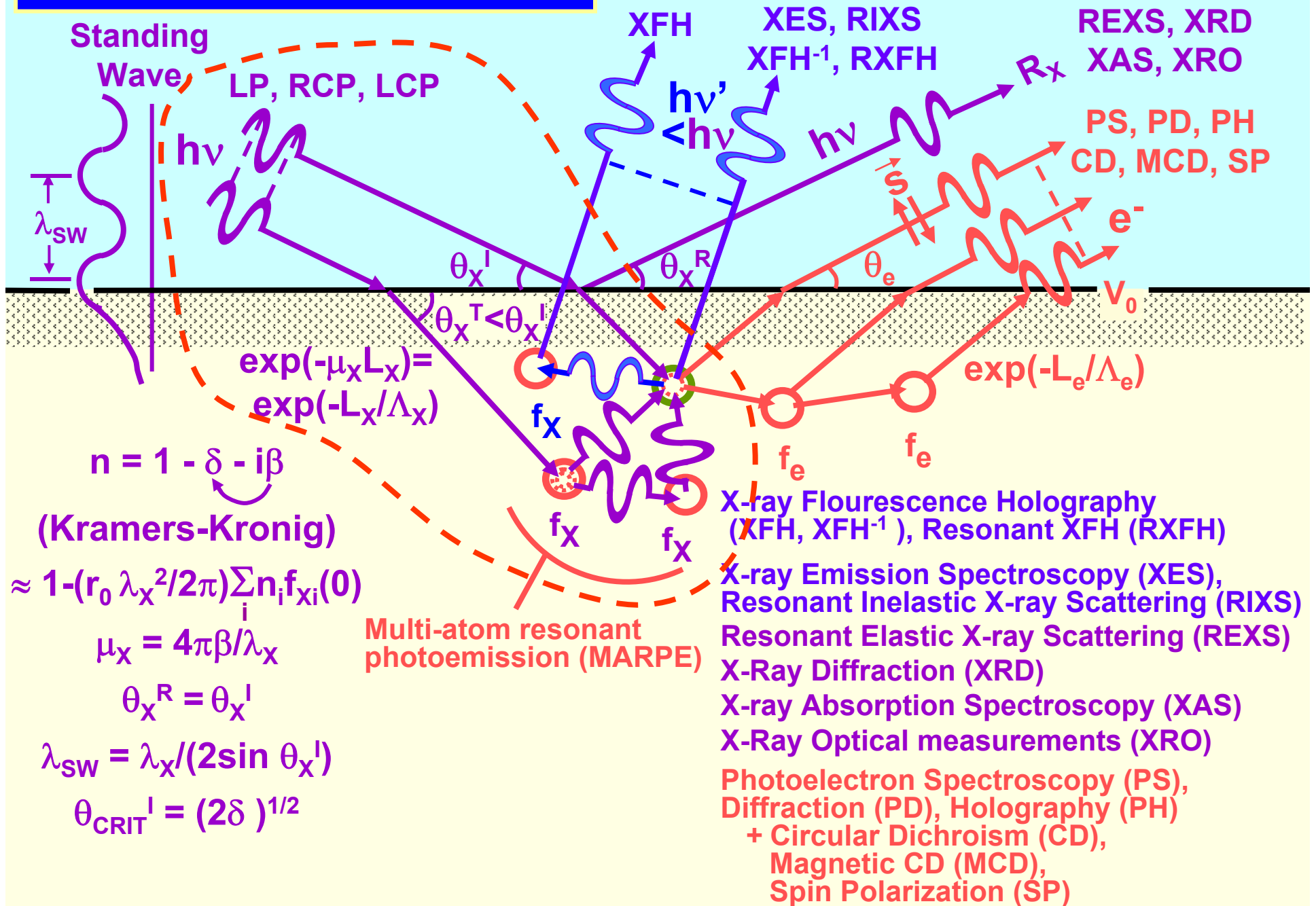
**Microscopy with photoemission**



# PHOTOELECTRON INTENSITIES—THE 3-STEP MODEL



# Some basic measurements:



# A LITTLE X-RAY OPTICS

(E.G. See pp. 1-38, 1-44, 5-18-5-19 in X-Ray Data Booklet)

$$\text{Index of refraction} = n = 1 - \delta - i\beta$$

$\delta = + \text{no.} = \text{refractive decrement} \ll 1$  (Sometimes negative through absorption resonances)

$\beta = + \text{no.} = \text{absorptive decrement} \ll 1$

$\delta$  and  $\beta$  linked by Kramers-Kronig transform

$$n \text{ also} = 1 - (r_e/2\pi)\lambda_{hv}^2 \sum n_i f_i (0=\text{fwd. scatt.})$$

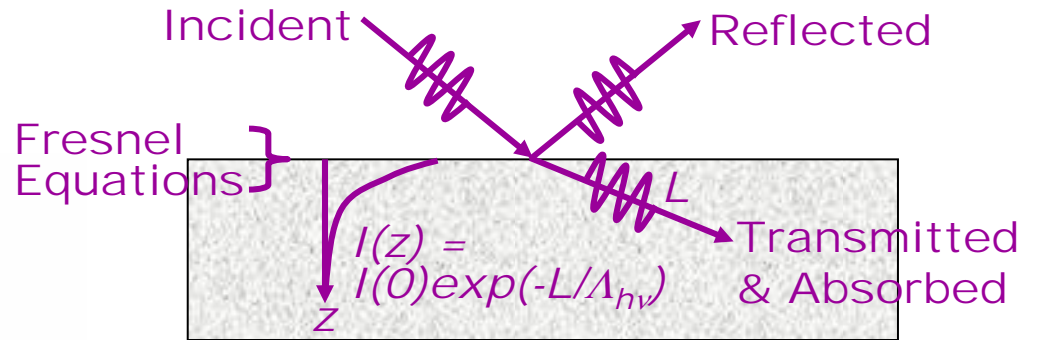
$$\begin{aligned} r_e &= \text{classical electron radius} \\ &= e^2/4\pi\epsilon_0 m_e e^2 = 2.817 \times 10^{-15} \text{ m} \\ \lambda_{hv} &= \text{x-ray wavelength} \end{aligned}$$

$n_i = \text{no. } i \text{ atoms per unit volume}$

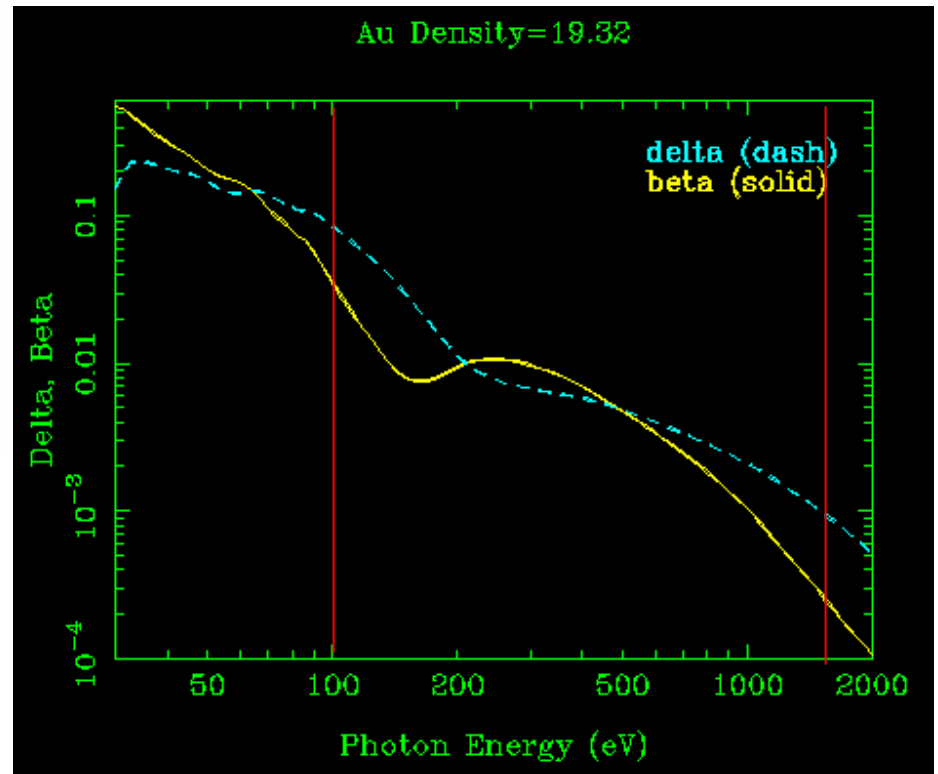
$f_i = \text{x-ray scattering factor for } i\text{th type of atom, in forward direction}$

$$\text{Exponential absorption length} = l_{\text{abs}} = \lambda_{hv}/(4\pi\beta) = \Lambda_{hv}$$

$$\begin{aligned} \theta_{\text{CRIT}} &= \text{critical grazing angle at} \\ &\text{which reflectivity begins (} R \approx 0.20 \text{)} \\ &= [2\delta]^{0.5} \end{aligned}$$



Online data and calculations at:  
[http://www-cxro.lbl.gov/optical\\_constants/](http://www-cxro.lbl.gov/optical_constants/)



X-ray scattering factor:  
 $f_i = \text{Re}f_i + i(\text{Im}f_i)$

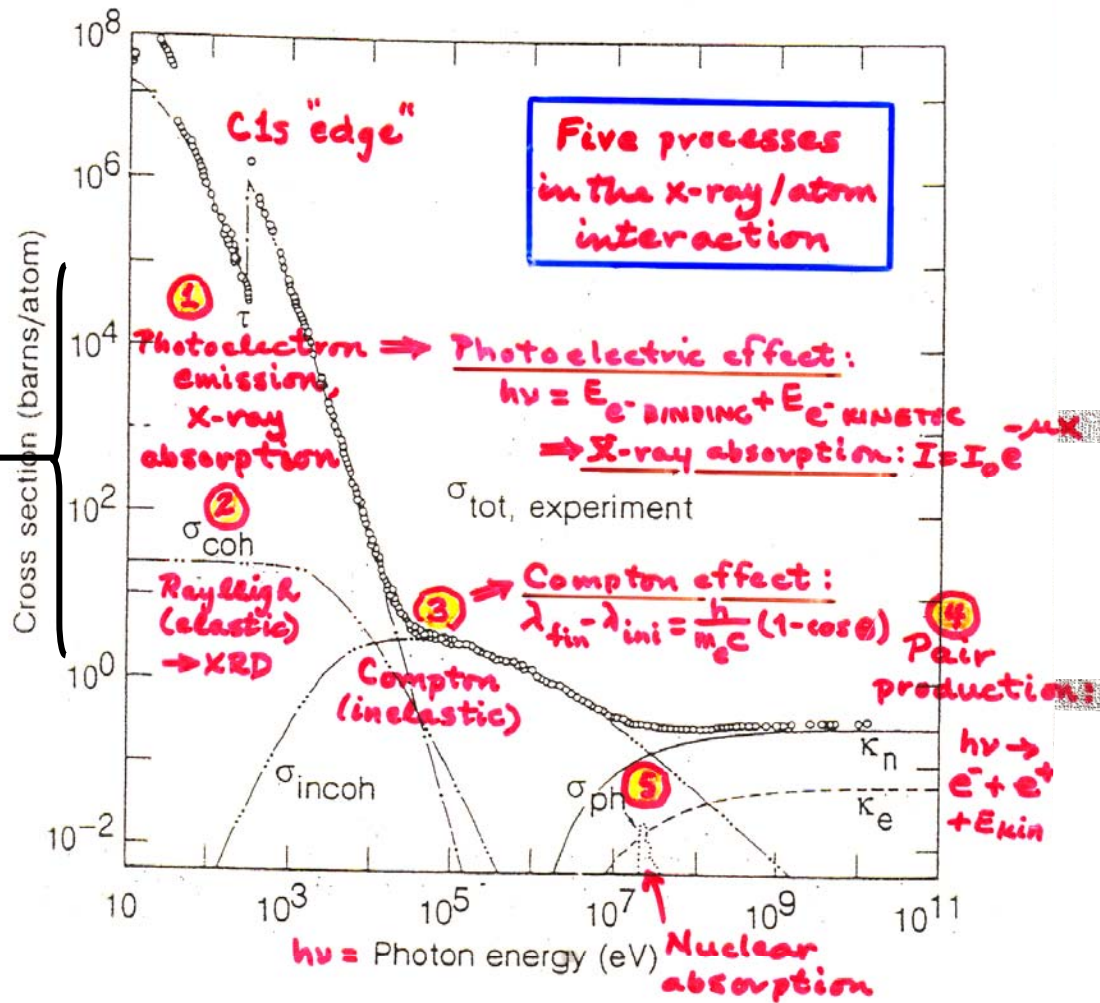


Fig. 3-1. Total photon cross section  $\sigma_{\text{tot}}$  in carbon, as a function of energy, showing the contributions of different processes:  $\tau$ , atomic photo-effect (electron ejection, photon absorption);  $\sigma_{\text{coh}}$ , coherent scattering (Rayleigh scattering—atom neither ionized nor excited);  $\sigma_{\text{incoh}}$ , incoherent scattering (Compton scattering off an electron);  $\kappa_n$ , pair production, nuclear field;  $\kappa_e$ , pair production, electron field;  $\sigma_{\text{ph}}$ , photonuclear absorption (nuclear absorption usually followed by emission of a neutron or other particle). (From Ref. 3; figure courtesy of J. H. Hubbell.)

## X-Ray Interactions with Matter



### Contents

- [Introduction](#)
- Access the [atomic scattering factor](#) files.
- Look up [x-ray properties of the elements](#).
- The [index of refraction](#) for a compound material.
- The x-ray [attenuation length](#) of a solid.
- X-ray transmission
  - Of a [solid](#).
  - Of a [gas](#).
- X-ray reflectivity
  - Of a [thick mirror](#).
  - Of a [single layer](#).
  - Of a [bilayer](#).
  - Of a [multilayer](#).
- The diffraction efficiency of a [transmission grating](#).
- Related calculations:
  - Synchrotron [bend magnet radiation](#).

#### **NEW!** [What's New?](#)

#### [Other x-ray web resources](#).

These pages utilize *JavaScript*, but the [decaffeinated versions](#) are still available.

### Reference

B.L. Henke, E.M. Gullikson, and J.C. Davis. *X-ray interactions: photoabsorption, scattering, transmission, and reflection at E=50-30000 eV, Z=1-92*, Atomic Data and Nuclear Data Tables Vol. **54** (no.2), 181-342 (July 1993).

| [CXRO](#) | [ALS](#) |

By Eric Gullikson. Please direct any comments to [EMGullikson@lbl.gov](mailto:EMGullikson@lbl.gov)  
[Server Statistics](#) © 1995-2001

Website

# ENHANCED SURFACE SENSITIVITY @ GRAZING INCIDENCE

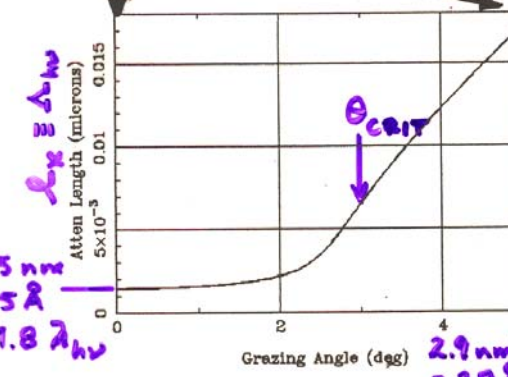
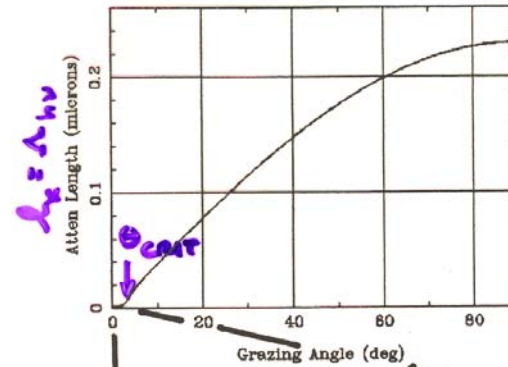
SOME X-RAY OPTICAL EFFECTS: REDUCED PENETRATION DEPTHS AND INCREASED REFLECTIVITY AT GRAZING INCIDENCE ANGLES

$\theta_{CRIT}$  = Grazing angle at which reflectivity begins ( $R \approx 0.20$ )  
 $= [2\delta]^{0.5}$



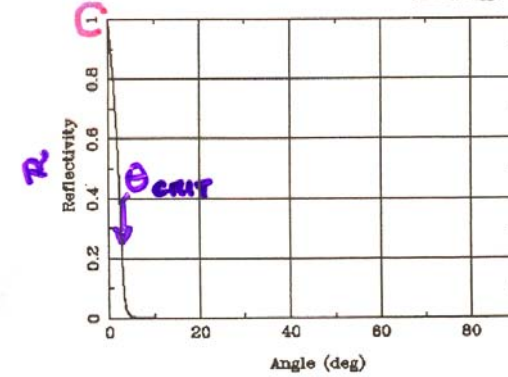
X-Ray Attenuation Length

Au Density=19.32, Energy=1487.eV



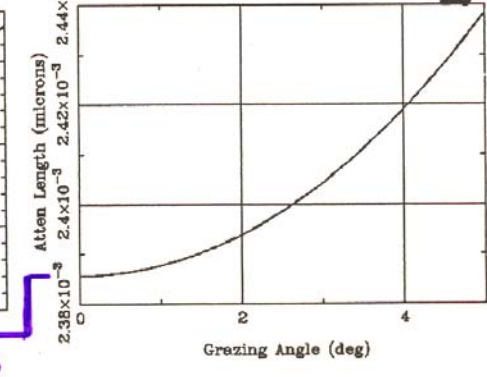
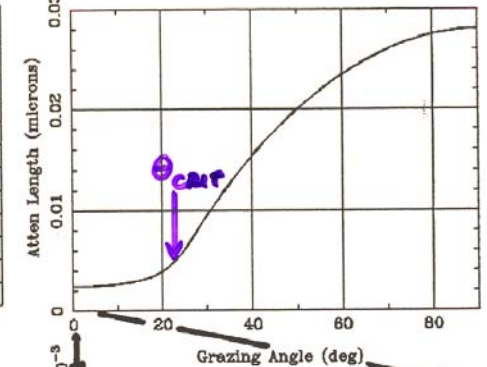
Mirror Reflectivity

Au Rho=19.32, Sig=0.nm, P=-1., E=1487.eV



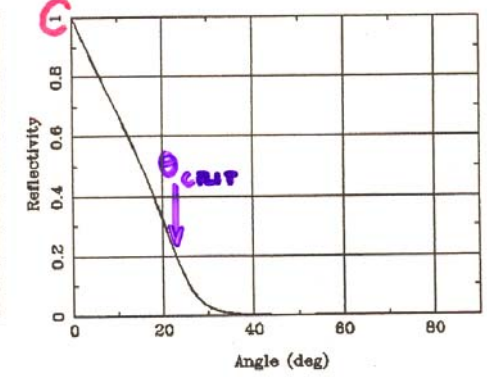
X-Ray Attenuation Length

Au Density=19.32, Energy=100.eV

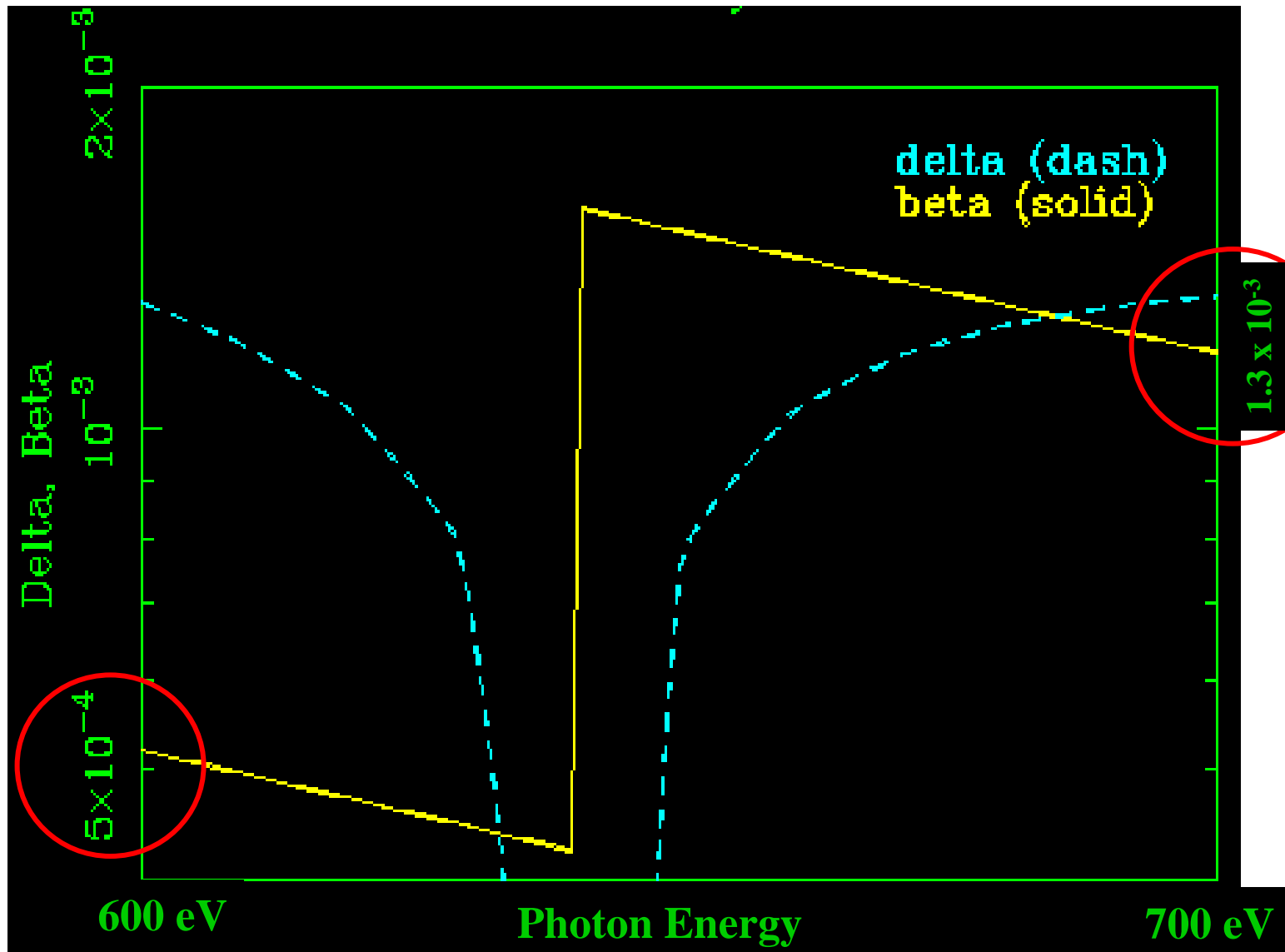


Mirror Reflectivity

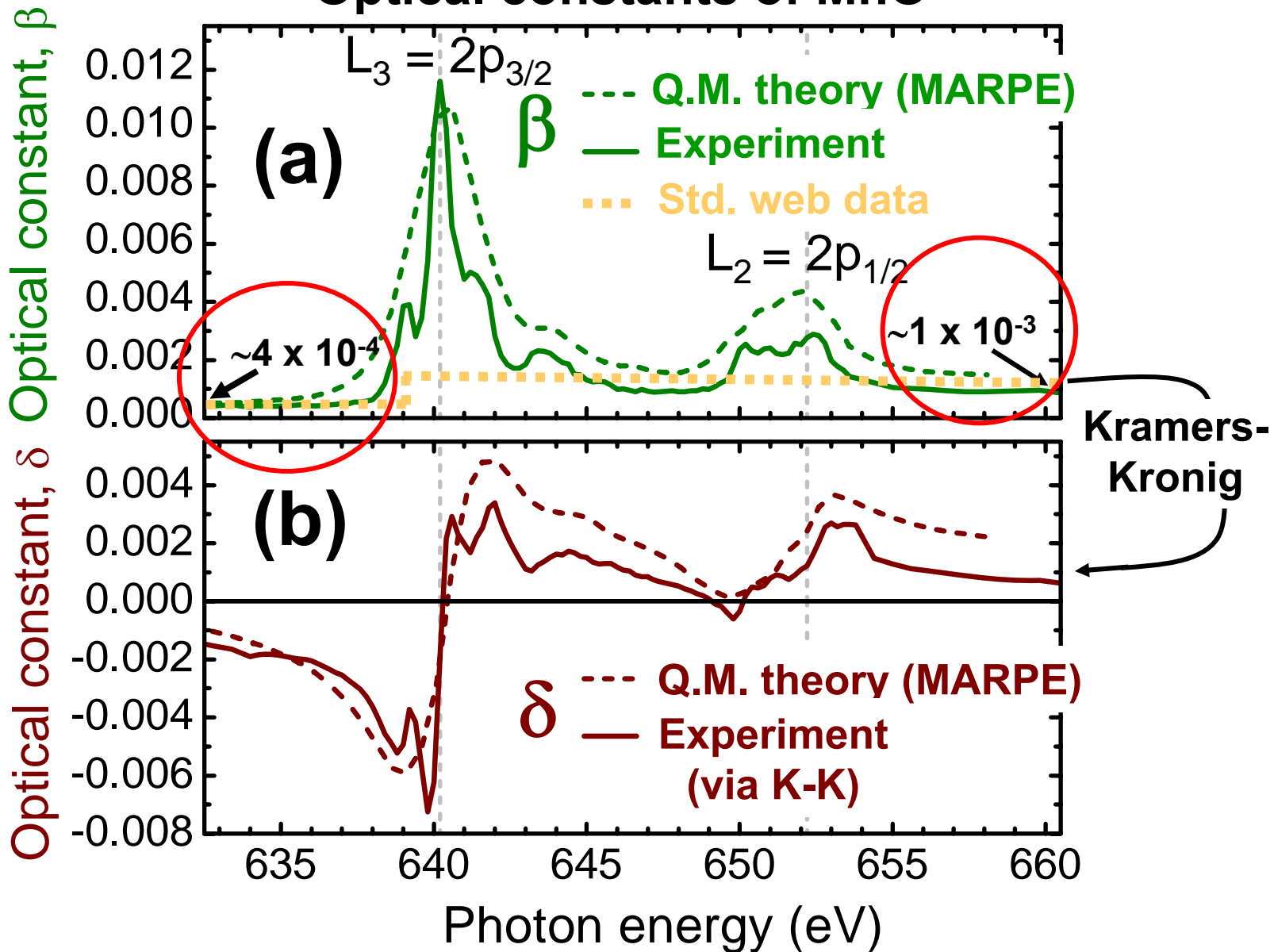
Au Rho=19.32, Sig=0.nm, P=-1., E=100.eV



Optical constants through Mn 2p edges of MnO—  
Web data without absorption peaks



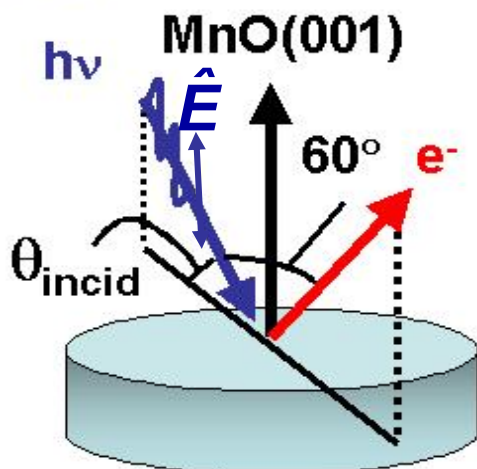
# Optical constants of MnO



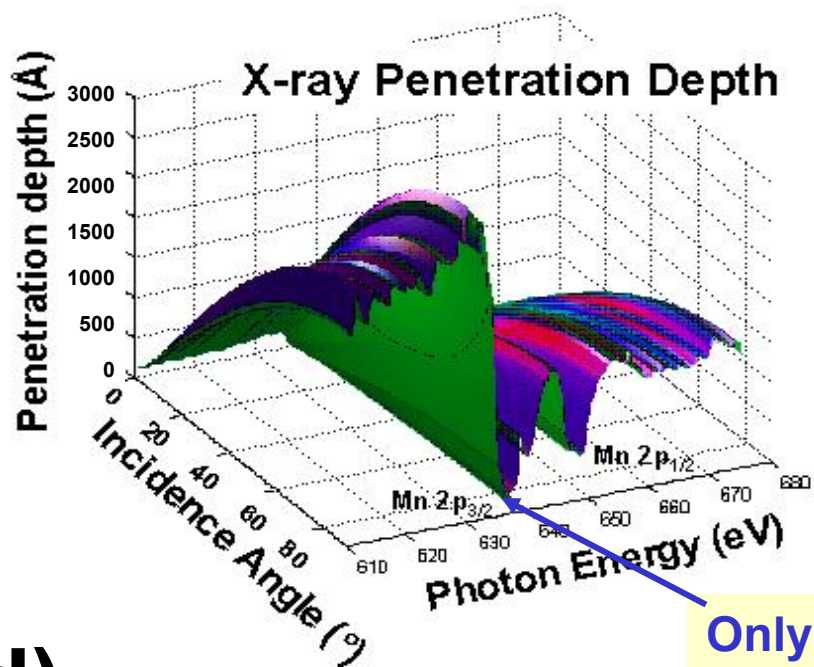


# X-ray optical effects through core resonances:

(a)

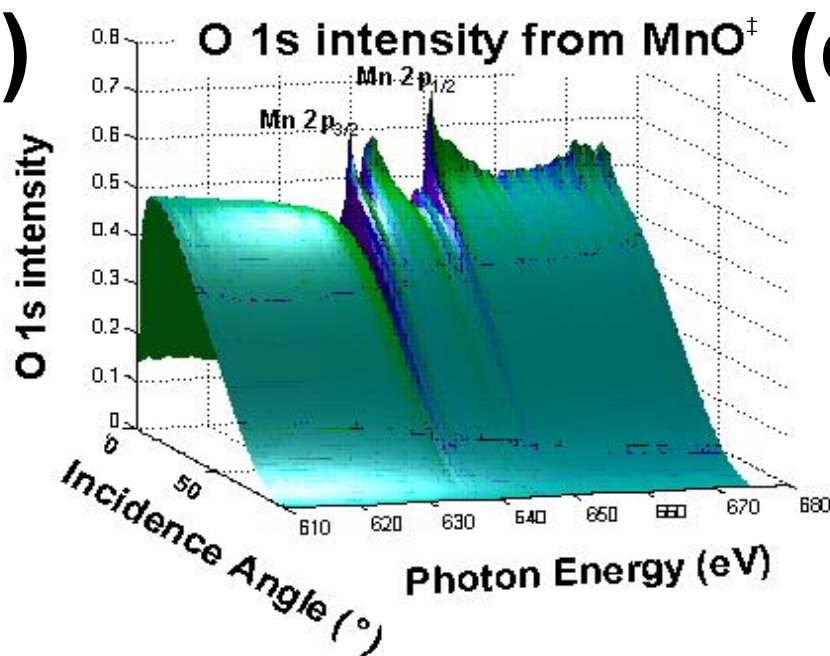


(b)

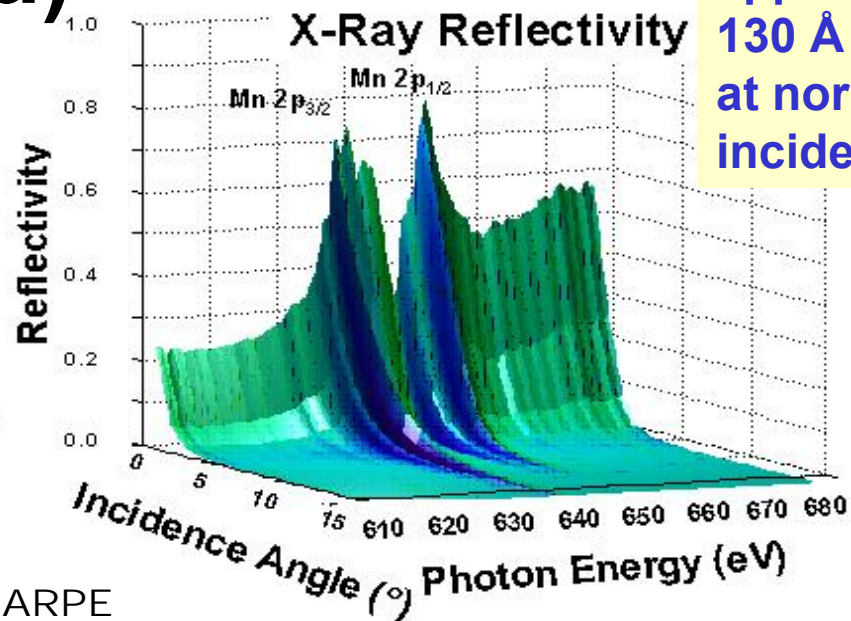


Only approx. 130 Å at normal incidence

(c)



(d)



†Aka Multi-Atom Resonant Photoemission = MARPE

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**Core-level photoemission**

**X-ray optical effects on emission→**

 **Use of standing waves to probe buried interfaces**

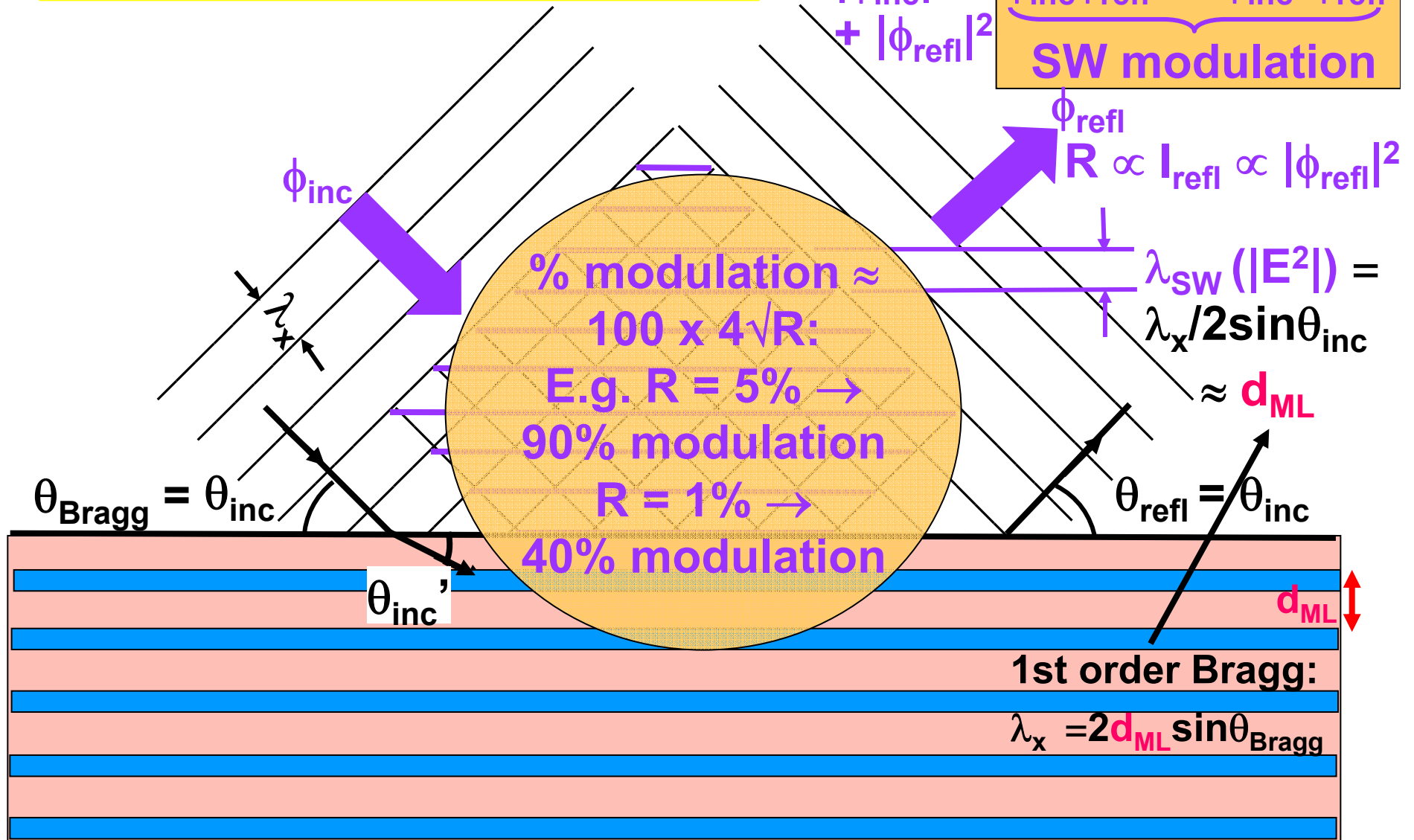
**Valence-level photoemission**

**Microscopy with photoemission**

# Standing wave formation:

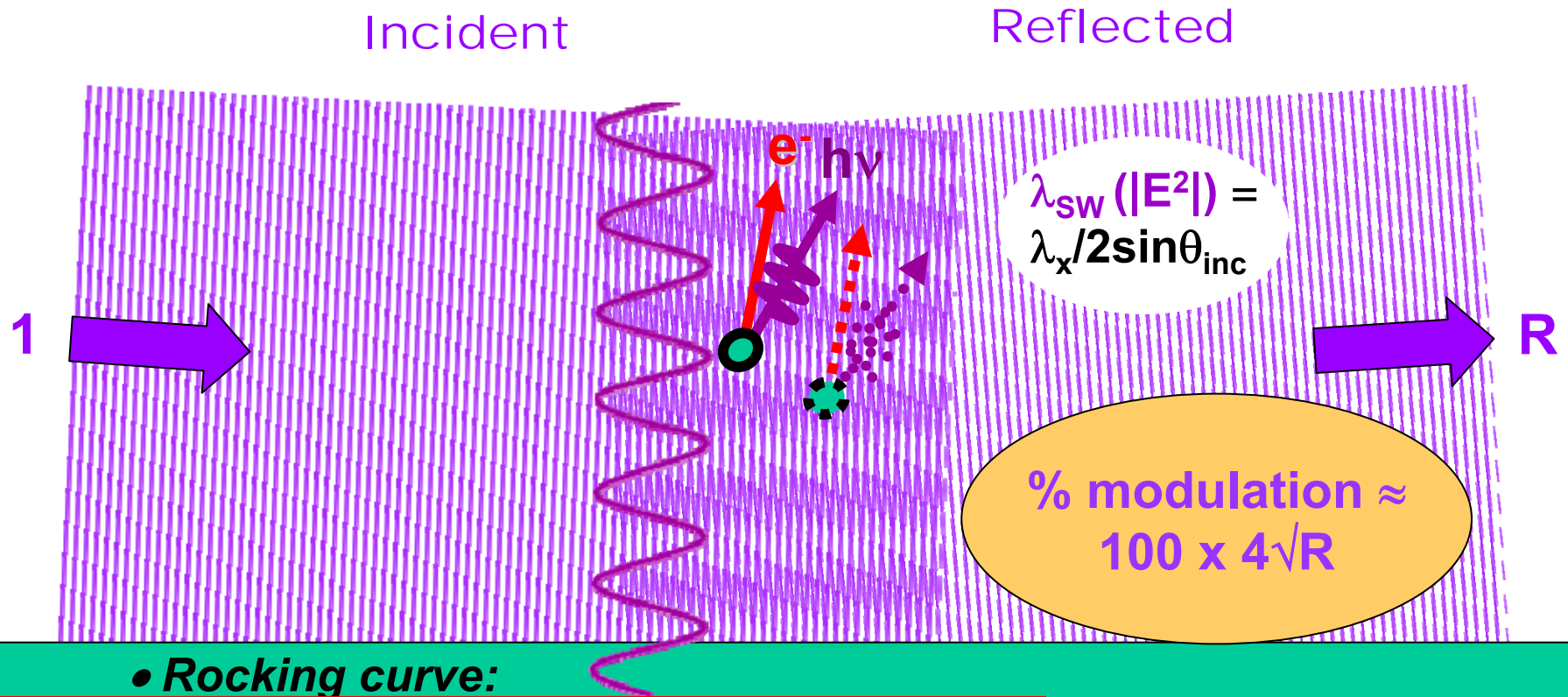
$$I_{sw} (|E^2|) \propto |\phi_{inc} + \phi_{refl}|^2$$

$$= |\phi_{inc}|^2 + \underbrace{\phi_{inc}\phi_{refl}^* + \phi_{inc}^*\phi_{refl}}_{\text{SW modulation}} + |\phi_{refl}|^2$$



Periodic atomic planes:  $d_{ML} \leq \sim 5 \text{ \AA}$  -- Si(111) --  $\leq 3.74 \text{ \AA}$ ,  $\text{LaB}_{66}(001)$  --  $\leq 23.52 \text{ \AA} \rightarrow 5.88 \text{ \AA}$ , mica --  $10.0 \text{ \AA}$ ; or Synthetic multilayers:  $d_{ML} \approx \sim 20-40 \text{ \AA}$

# Standing wave formation in reflection from a surface, or single-crystal Bragg planes<sup>+</sup>, or a multilayer mirror



- **Rocking curve:**

$$I(\theta_{inc}) \propto 1 + R(\theta_{inc}) + 2\sqrt{R(\theta_{inc})} f \cos[\varphi(\theta_{inc}) - 2\pi P]$$

- **Energy scan:**

$$I(h\nu) \propto 1 + R(h\nu) + 2\sqrt{R(h\nu)} f \cos[\varphi(h\nu) - 2\pi P]$$

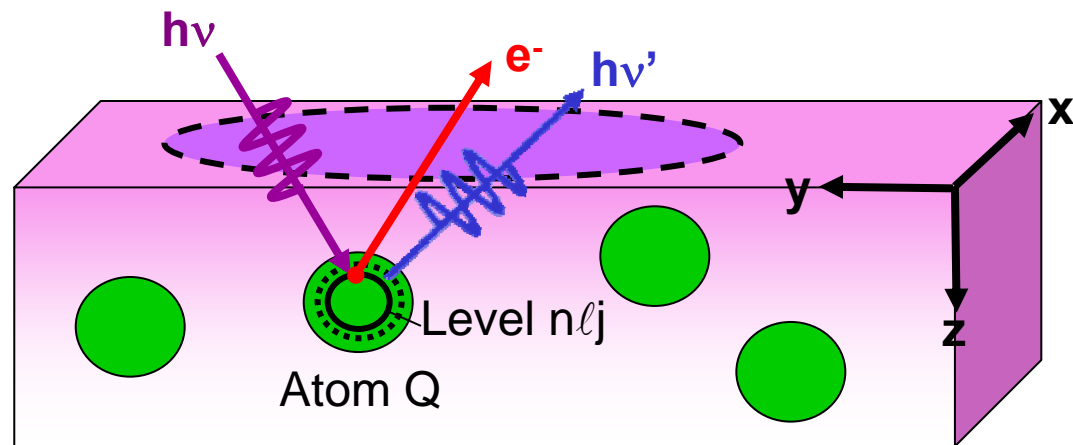
with:  $f$  = coherent fraction of atoms,  $P$  = phase of coherent-atom position

- **Phase scan with wedge-shaped sample ("Swedge" method):**

XMCD—Kim, Kortright,  
PRL 86, 1347 (2001)

<sup>+</sup>Standing waves via Bragg reflection of hard x-rays: Batterman, Phys. Rev A 133, 759 (1964)

# PHOTOELECTRON (OR X-RAY EMISSION) INTENSITIES AND COMPOSITION



$I(Qn\ell j) =$

$$C \int_0^{\infty} |\vec{E}(x,y,z)|^2 \rho_Q(x,y,z) \frac{d\sigma_{Qn\ell j}(h\nu)}{d\Omega} \exp\left[-\frac{z}{\Lambda_{e(x)} \sin\theta}\right] \Omega(h\nu, x, y) dx dy dz$$

$|\vec{E}(x,y,z)|^2 =$  *x-ray intensity, incl. standing wave modulation*

$\rho_Q(x,y,z) =$  *density of atoms Q → quantitative analysis*

$\frac{d\sigma_{Qn\ell j}(h\nu)}{d\Omega} =$  *differential photoelectric (or x – ray emission)*

*cross section for subshell Qnℓ j*

$\Lambda_{e(x)} =$  *inelastic attenuation length for electrons or x – rays*

$\Omega(h\nu, x, y) =$  *spectrometer acceptance solid angle*

**X-ray Optical Calculations :**

**Calculating XRO effects on spectroscopy--Yang**

- $n(h\nu) = 1 - \delta(h\nu) + i\beta(h\nu)$
- variable polarization
- multiple reflection/refraction
- exact treatment of interlayer intermixing a/o roughness
- electric field at  $i$ -th layer:

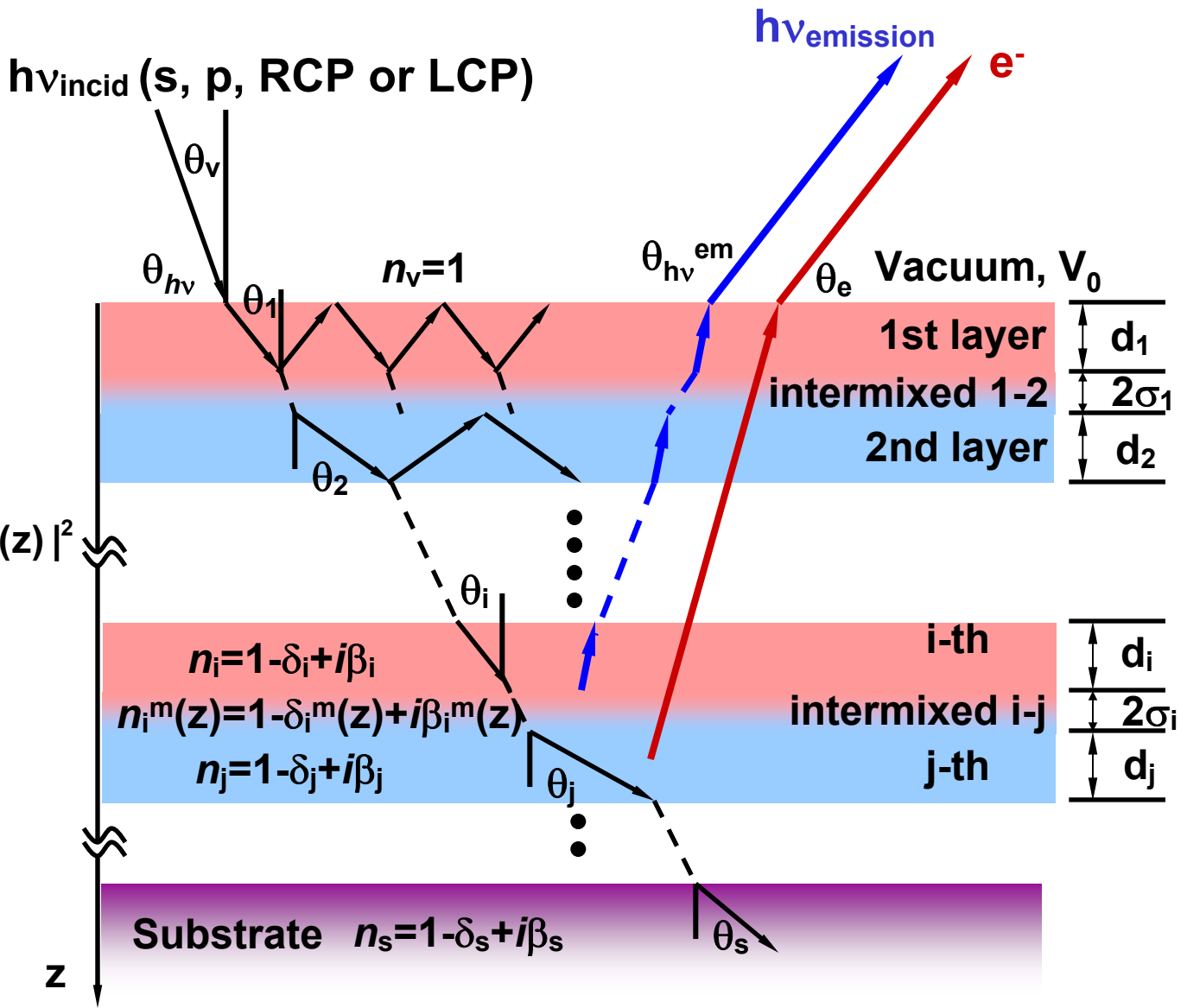
$$|E_{sw,i}(z)|^2 = |E_i^+(z) + E_i^-(z)|^2$$

**Photoemission:**

- differential cross section
- inelastic attenuation
- surface refraction

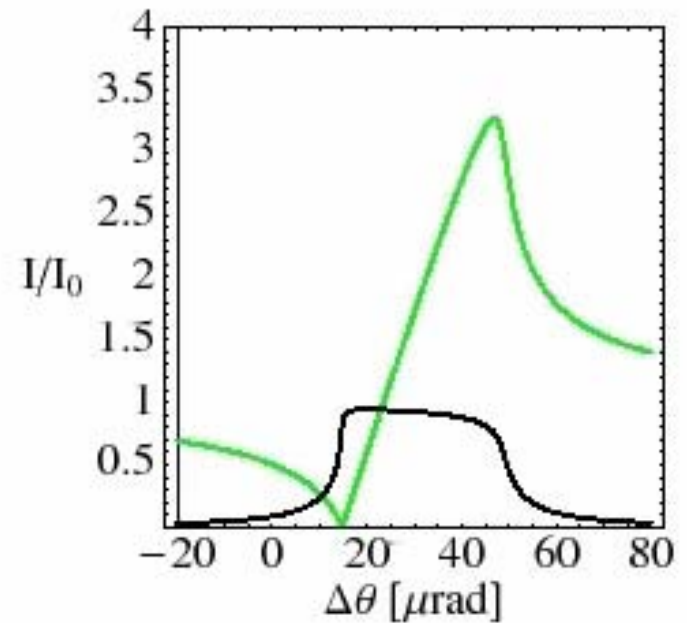
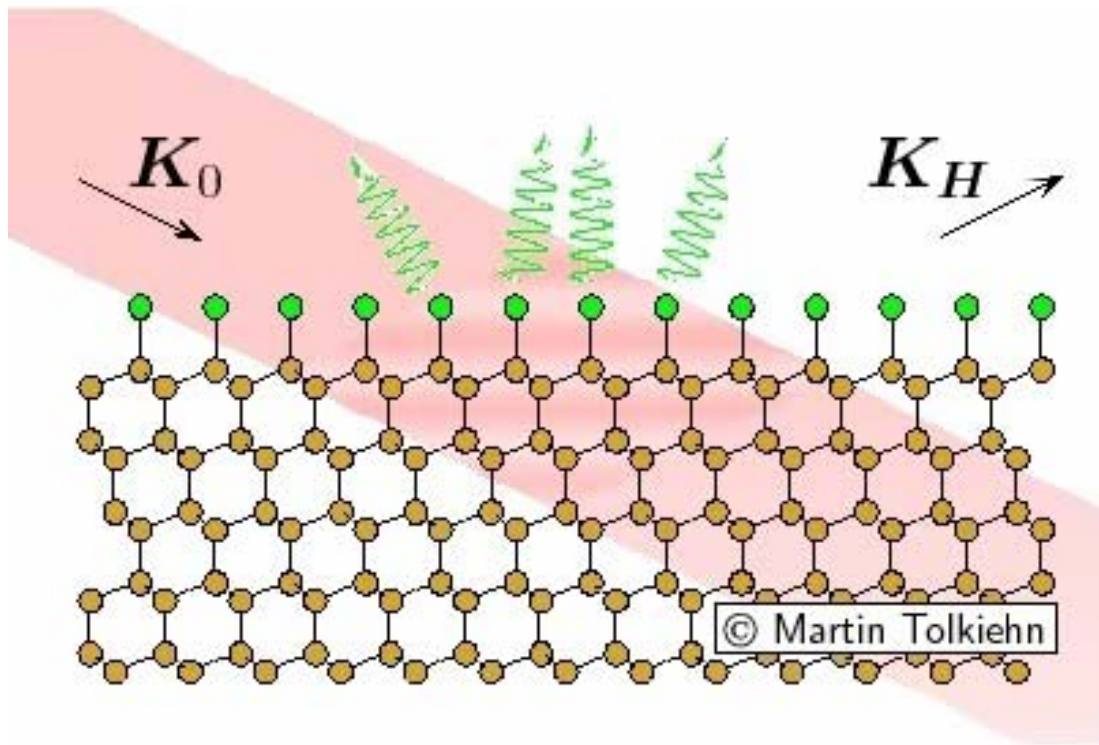
**X-ray emission:**

- fluorescence yield



# Standing Wave Behavior During a Rocking Curve Scan— Emission Intensity from a Surface Atom/Nanolayer

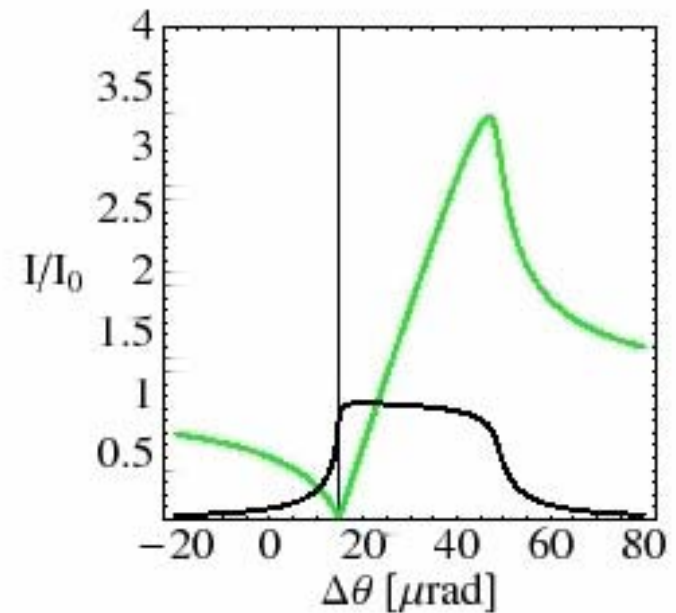
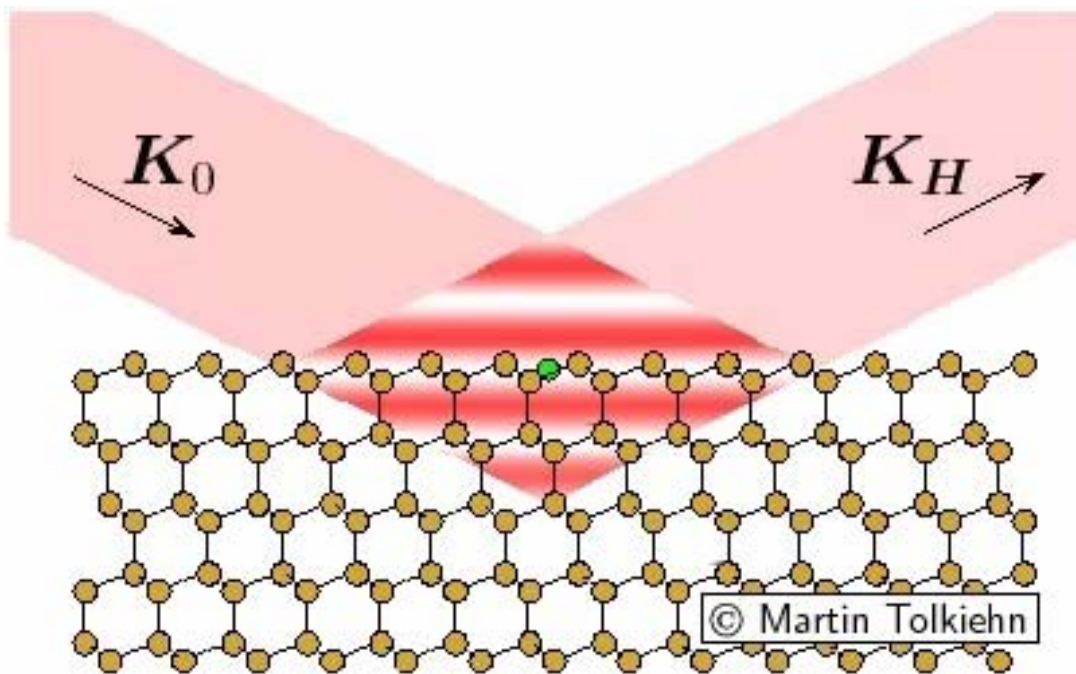
— Reflectivity  
— Emission Intensity



With thanks to Martin Tolkiehn, Diamond  
Dimitri Novikov, Hasylab

# Various Forms of Rocking Curves— Vertical Shift of Emitter/Nanolayer Position

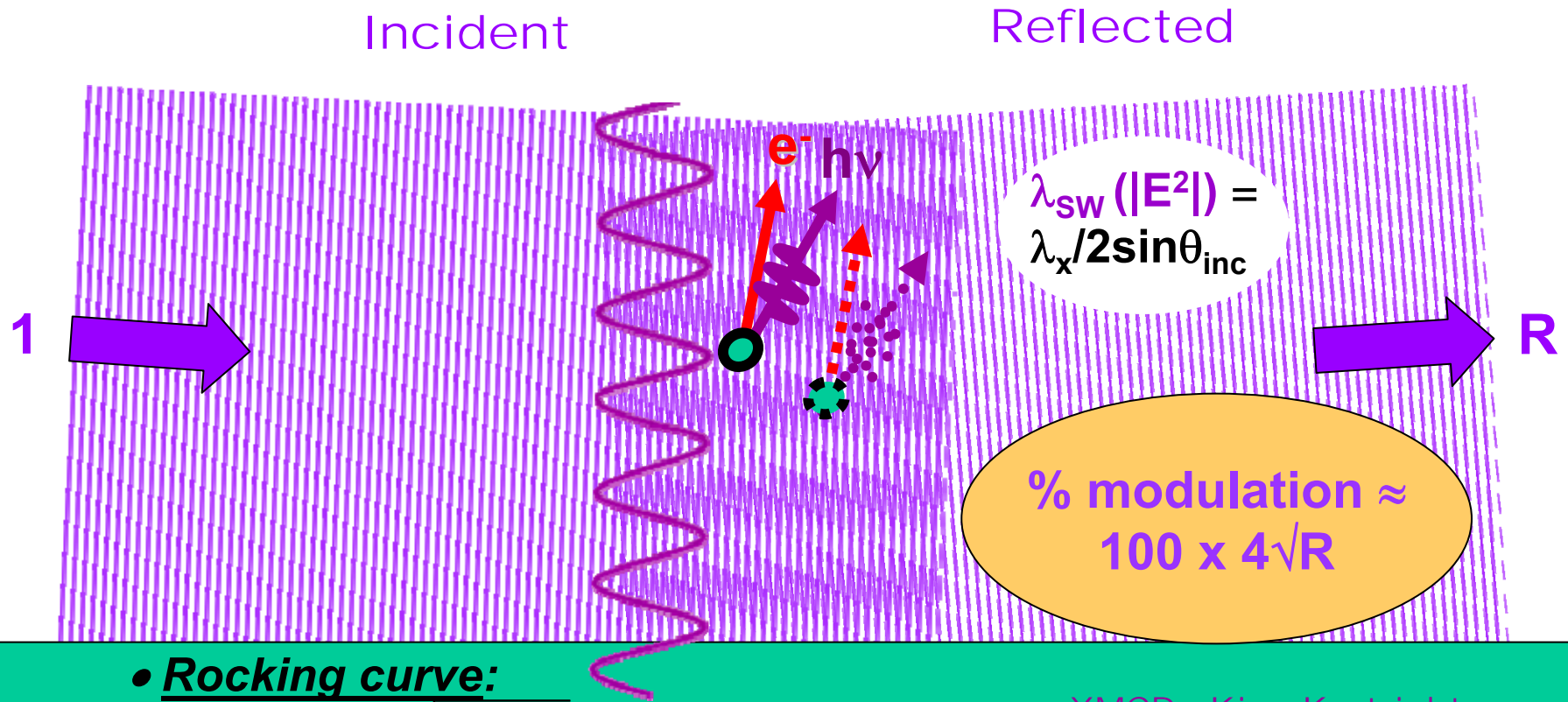
— Reflectivity  
— Emission intensity profile at different vertical heights



With thanks to Martin Tolkieln, Diamond  
Dimitri Novikov, HasyLab



# Standing wave formation in reflection from a surface, or single-crystal Bragg planes<sup>+</sup>, or a multilayer mirror



- Rocking curve:

$$I(\theta_{inc}) \propto 1 + R(\theta_{inc}) + 2\sqrt{R(\theta_{inc})} f \cos[\varphi(\theta_{inc}) - 2\pi P]$$

- Energy scan:

$$I(h\nu) \propto 1 + R(h\nu) + 2\sqrt{R(h\nu)} f \cos[\varphi(h\nu) - 2\pi P]$$

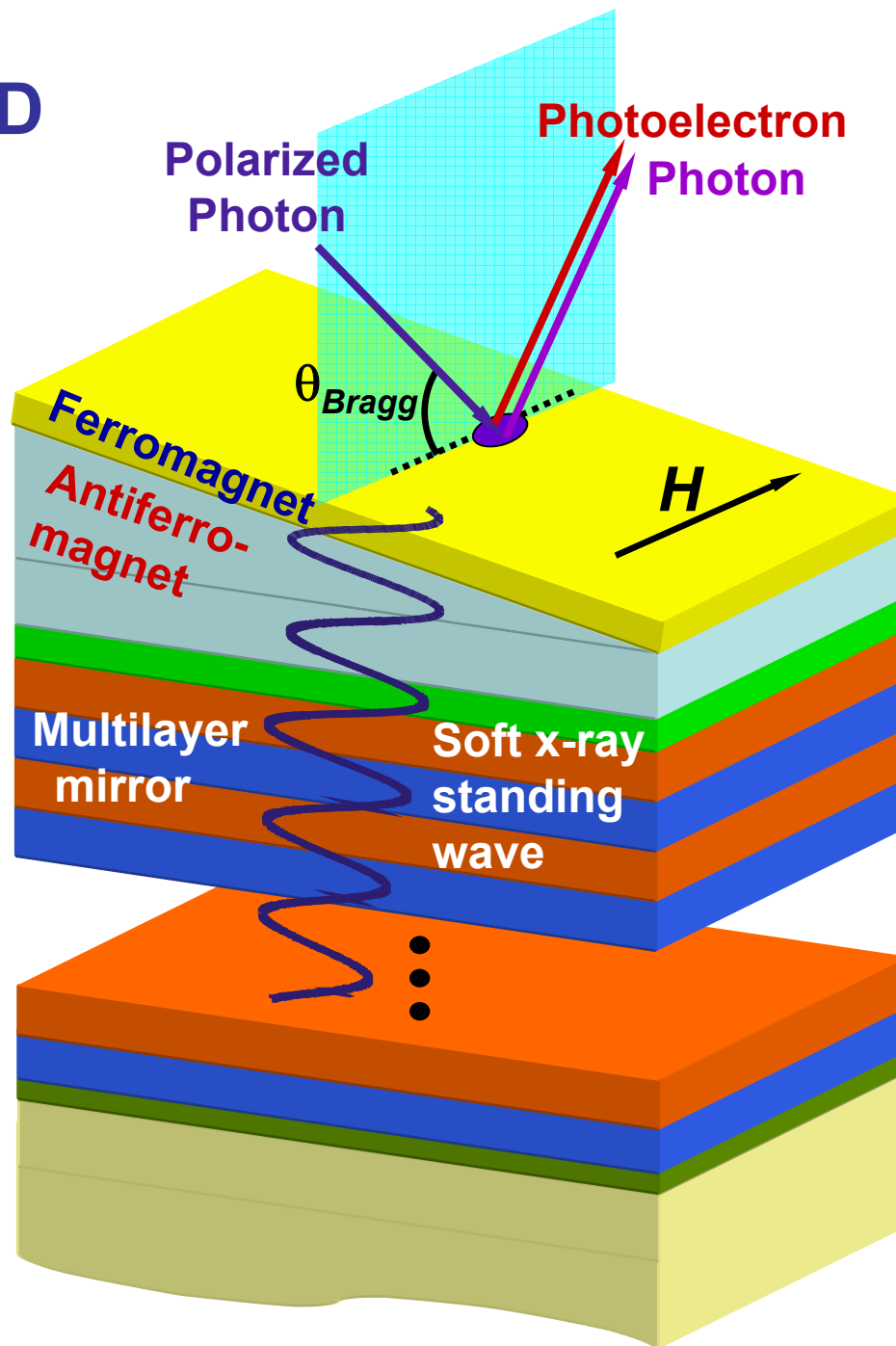
with:  $f$  = coherent fraction of atoms,  $P$  = phase of coherent-atom position

➔ Phase scan with wedge-shaped sample ("Swedge" method):

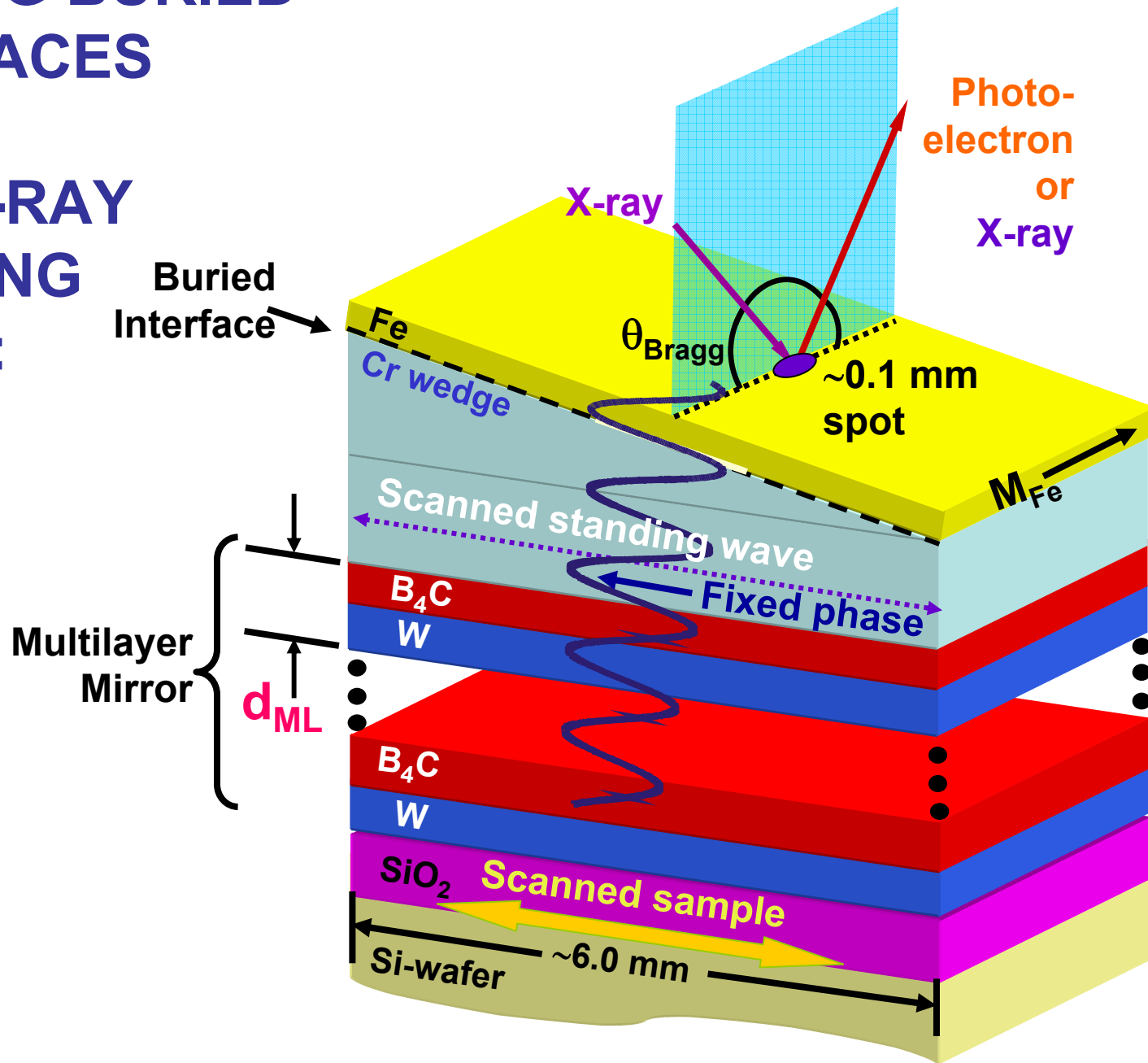
XMCD—Kim, Kortright,  
PRL 86, 1347 (2001)

<sup>+</sup>Standing waves via Bragg reflection of hard x-rays: Batterman, Phys. Rev A 133, 759 (1964)

# PROBING BURIED INTERFACES WITH SOFT X-RAY STANDING WAVES:

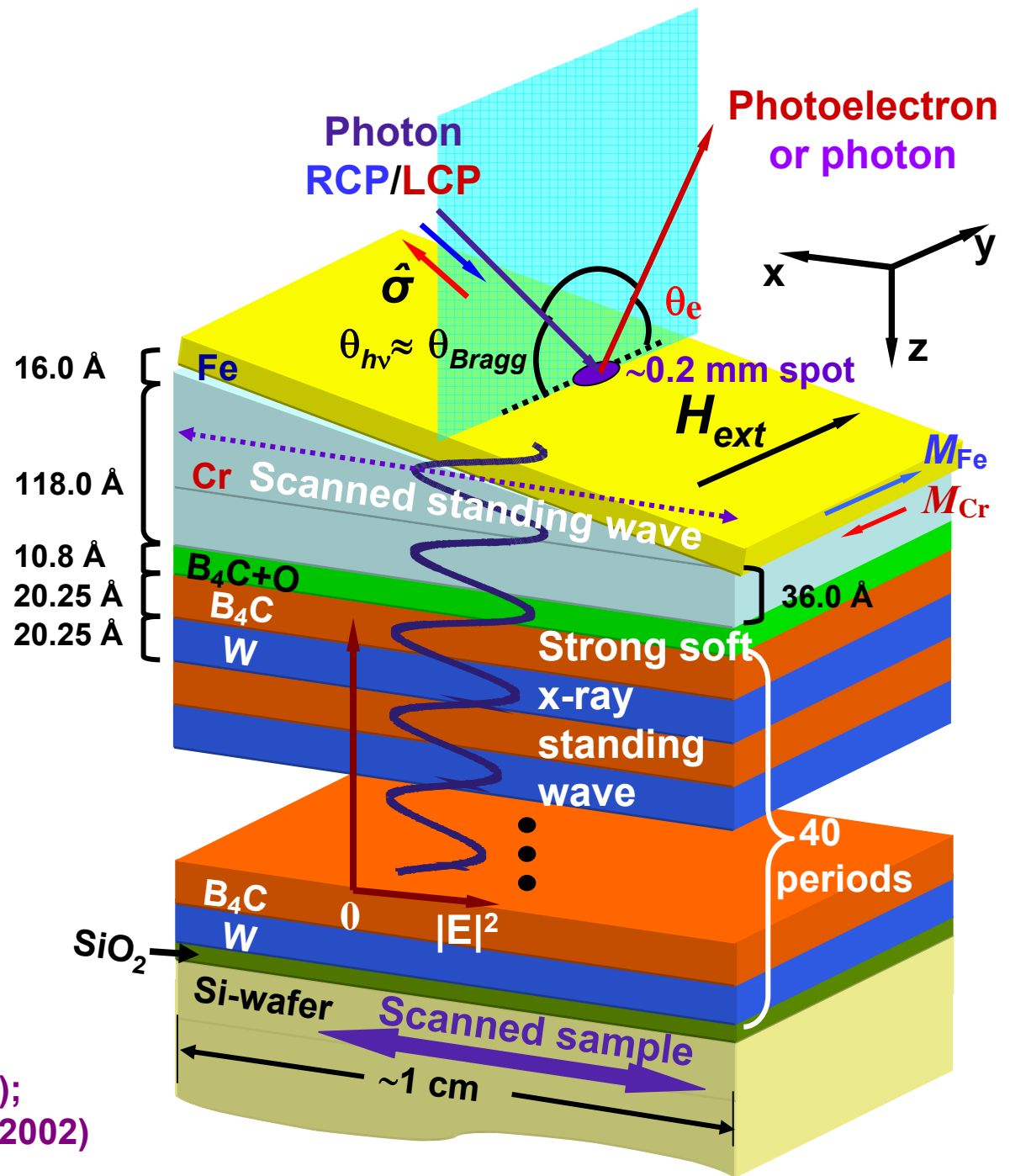


# PROBING BURIED INTERFACES WITH SOFT X-RAY STANDING WAVES:



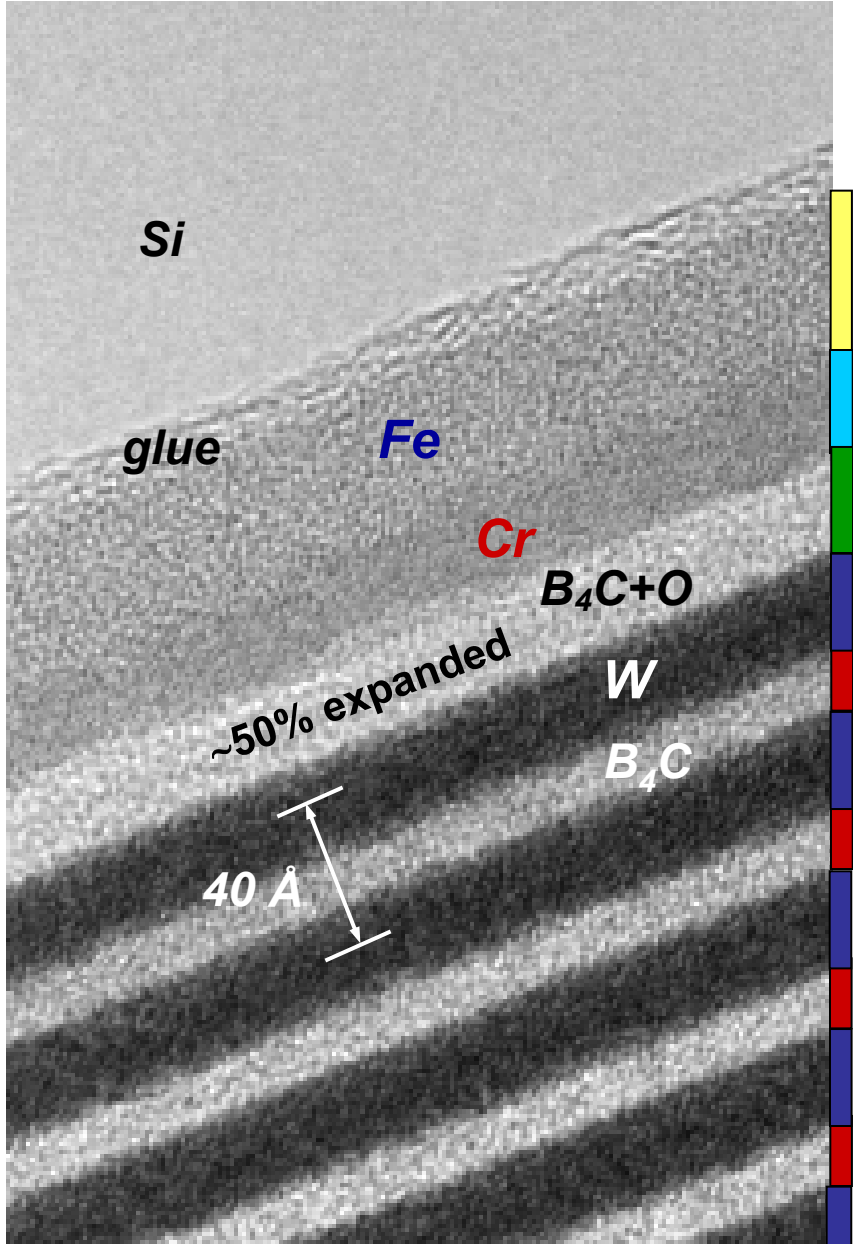
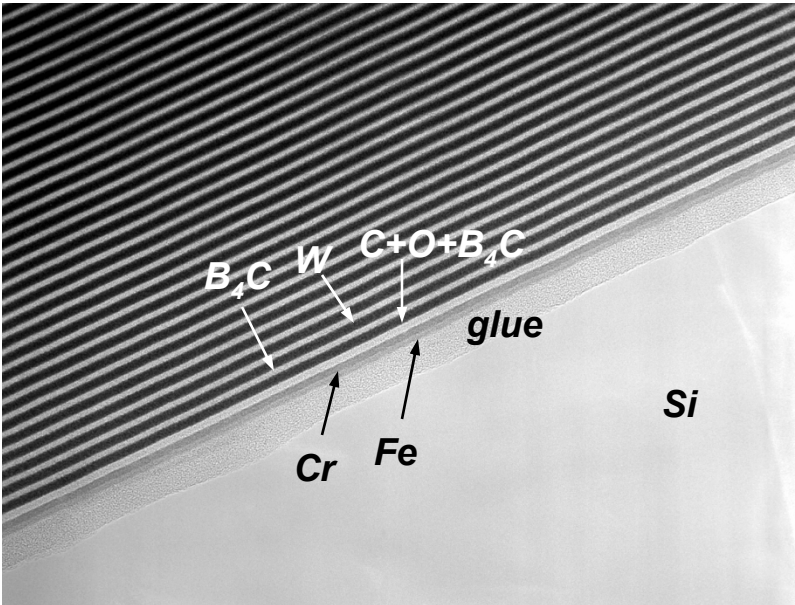
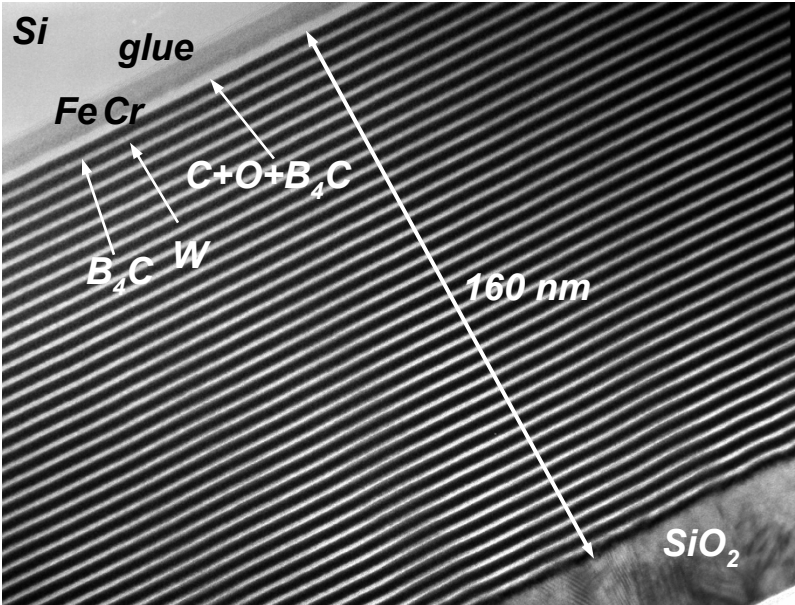
**PROBING  
BURIED  
INTERFACES  
WITH  
SOFT X-RAY  
STANDING  
WAVES:**

40.50 Å  
period =  
standing  
wave  
period

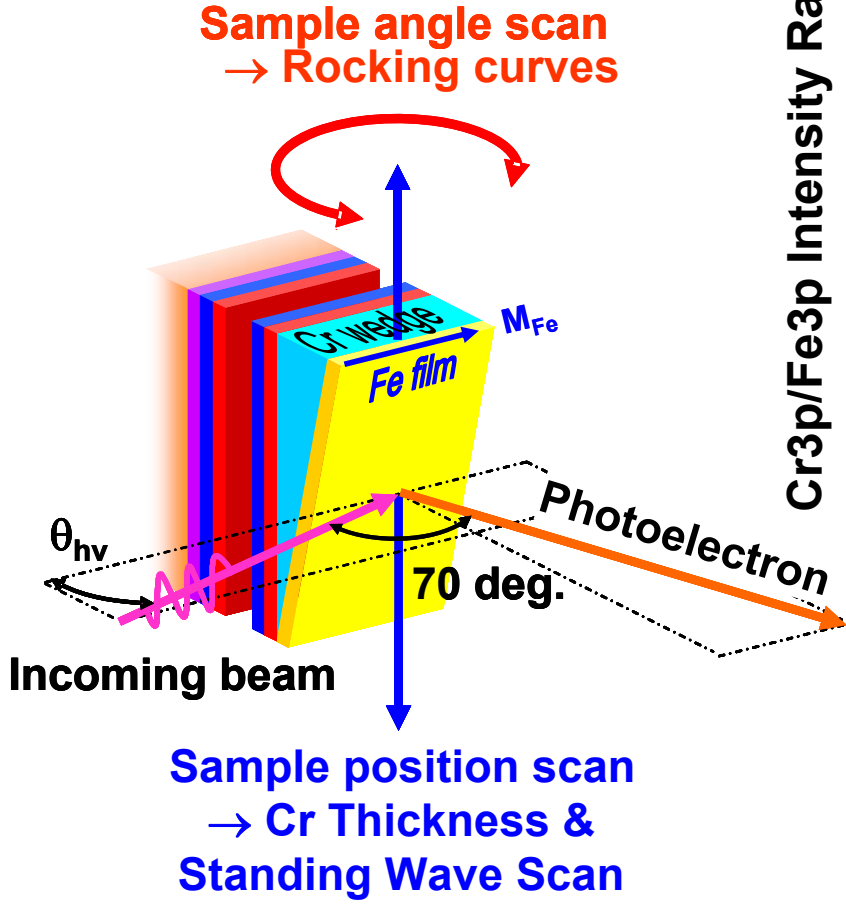


S.-H. Yang. B.S. Mun et al.,  
Surf. Sci. Lett. 461, L557 (2000);  
J. Phys. Cond. Matt. 14, L406 (2002)

**TRANSMISSION ELECTRON MICROSCOPY IMAGE FOR Fe/Cr/MULTILAYER SWG**  
**(Synthesis-CXRO, and Imaging-NCEM, LBNL)**

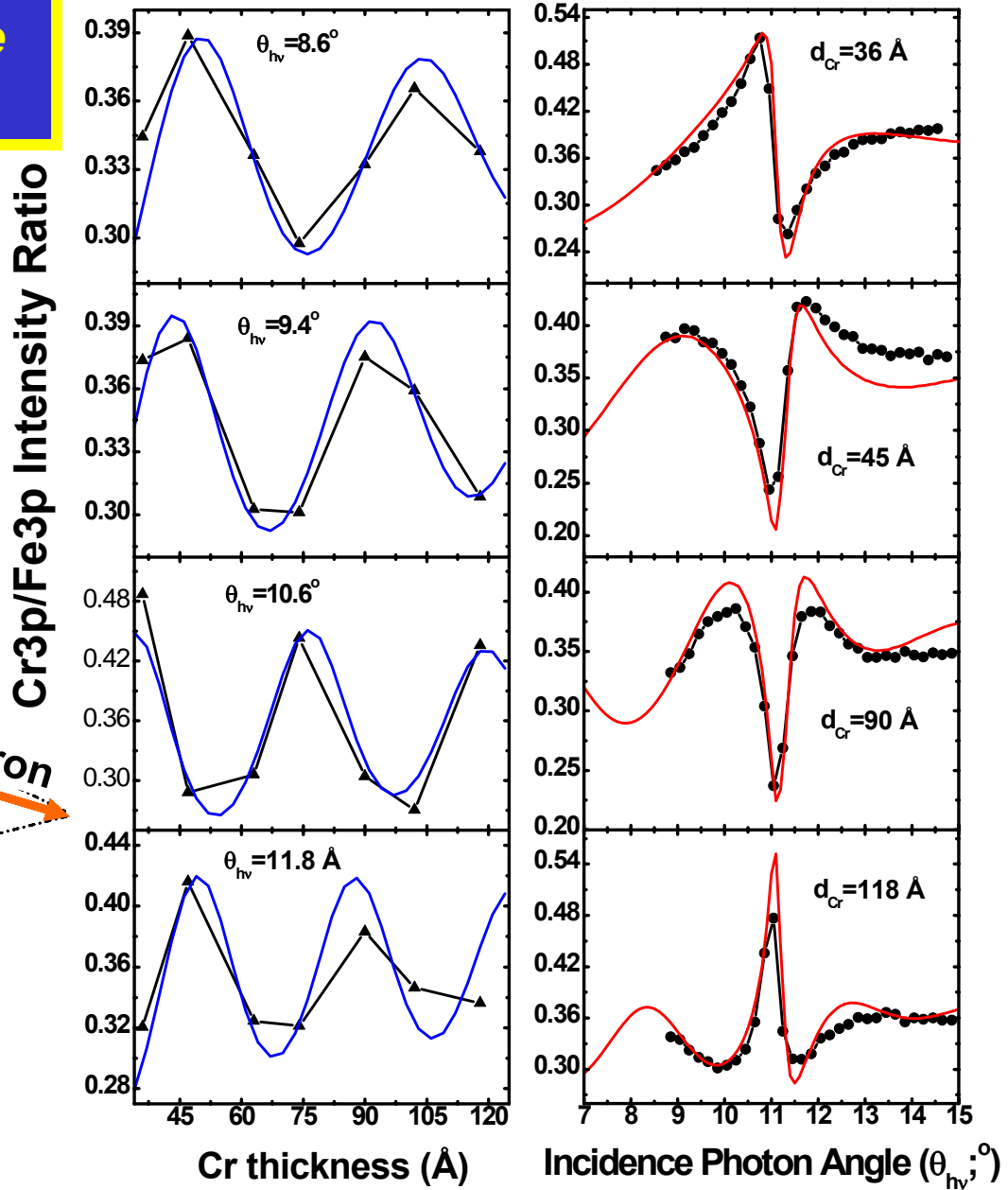


**Experimental + Calculated Photoemission Yield Ratio  $I(\text{Fe } 3p)/I(\text{Cr } 3p)$  from Fe/Cr wedge on standing-wave multilayer**



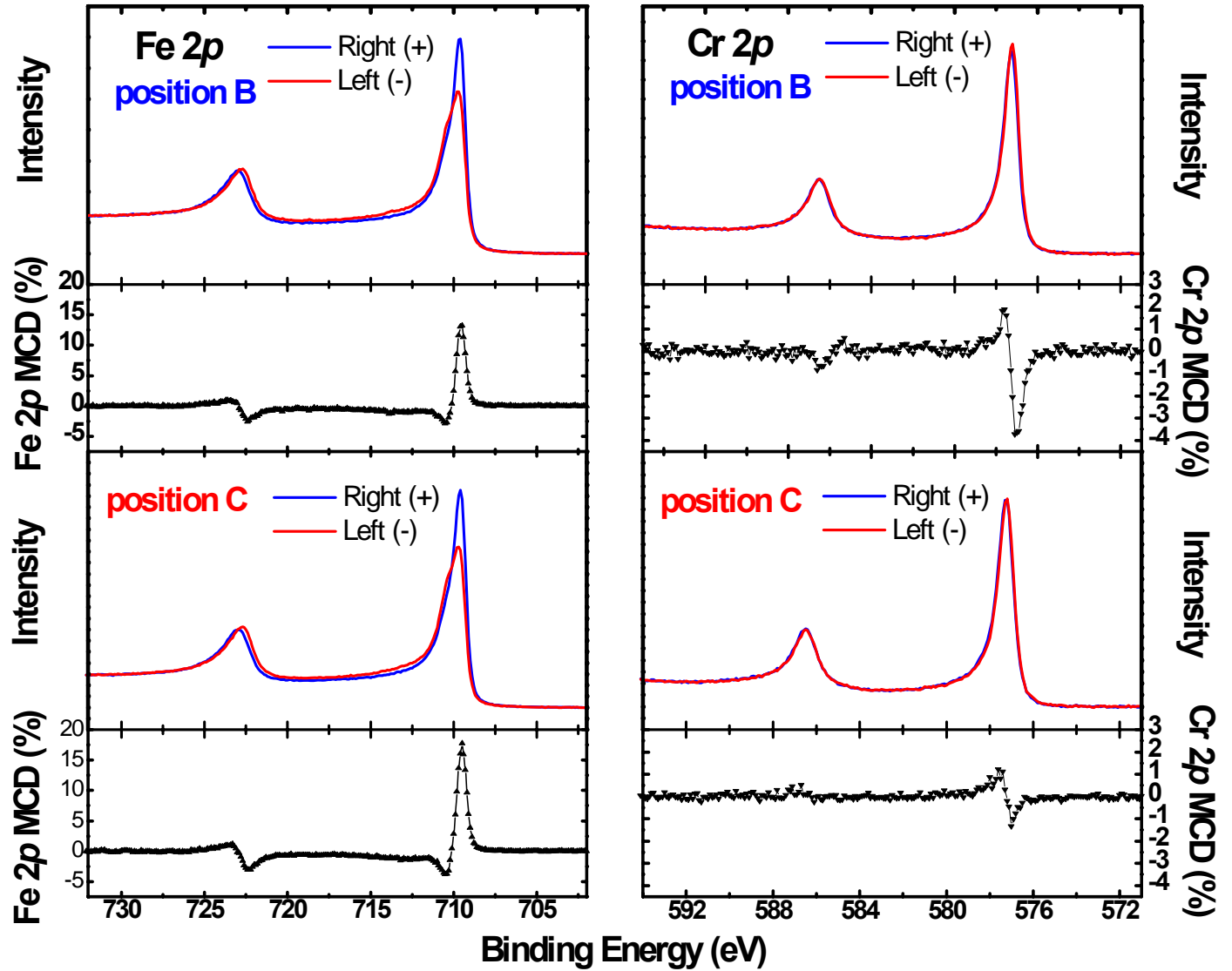
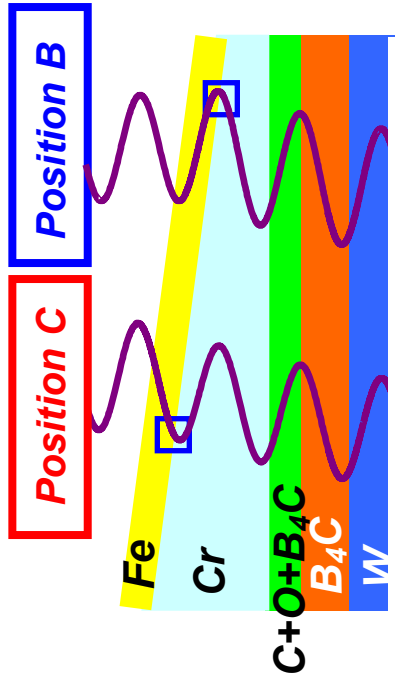
**Sample pos'n. scan-- Standing wave scan**

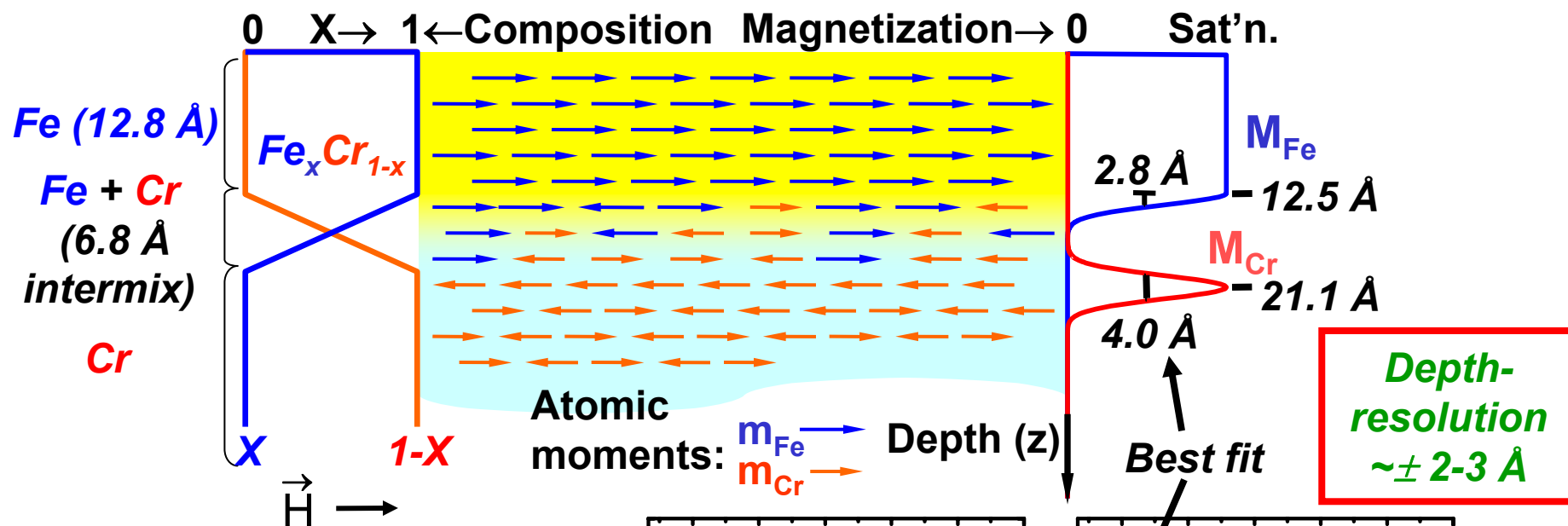
**Sample angle scan-- Rocking curves**



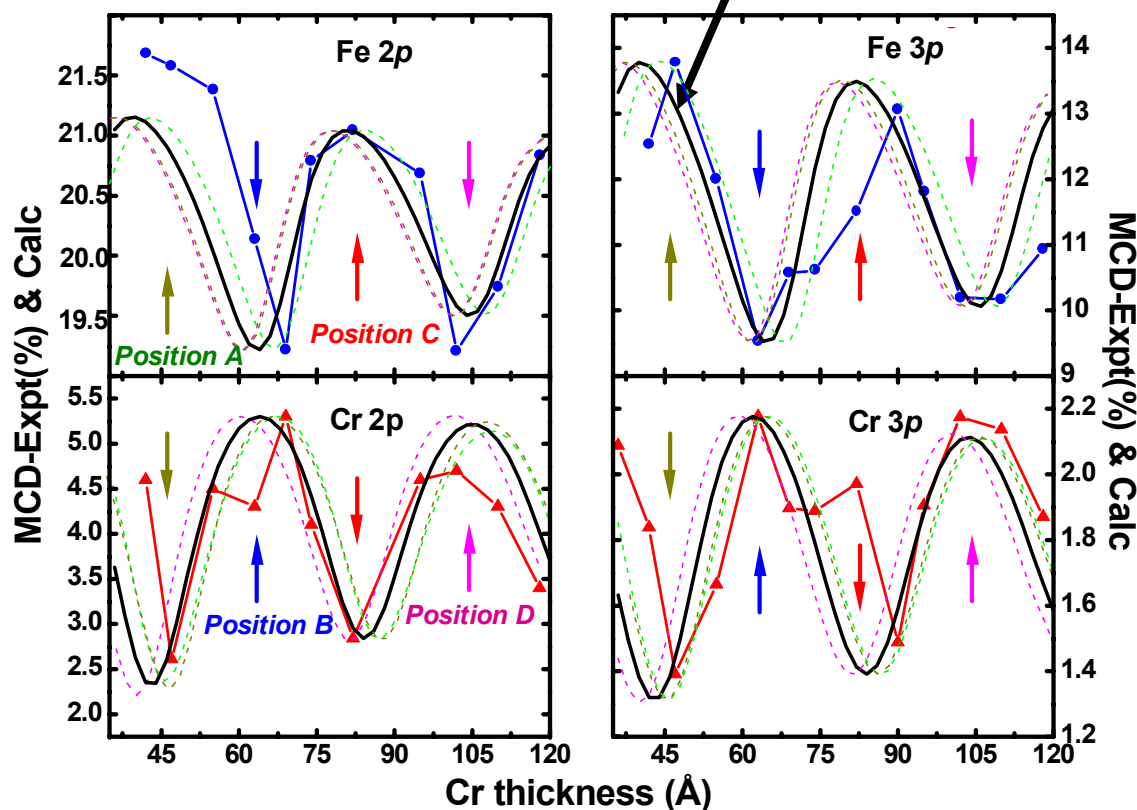
**Fe & Cr 2p MCD Data from wedge (Fe/Cr)+SWG**

**Cr magnetization is antiparallel to Fe; systematic variation of MCD strengths vs  $d_{cr}$**





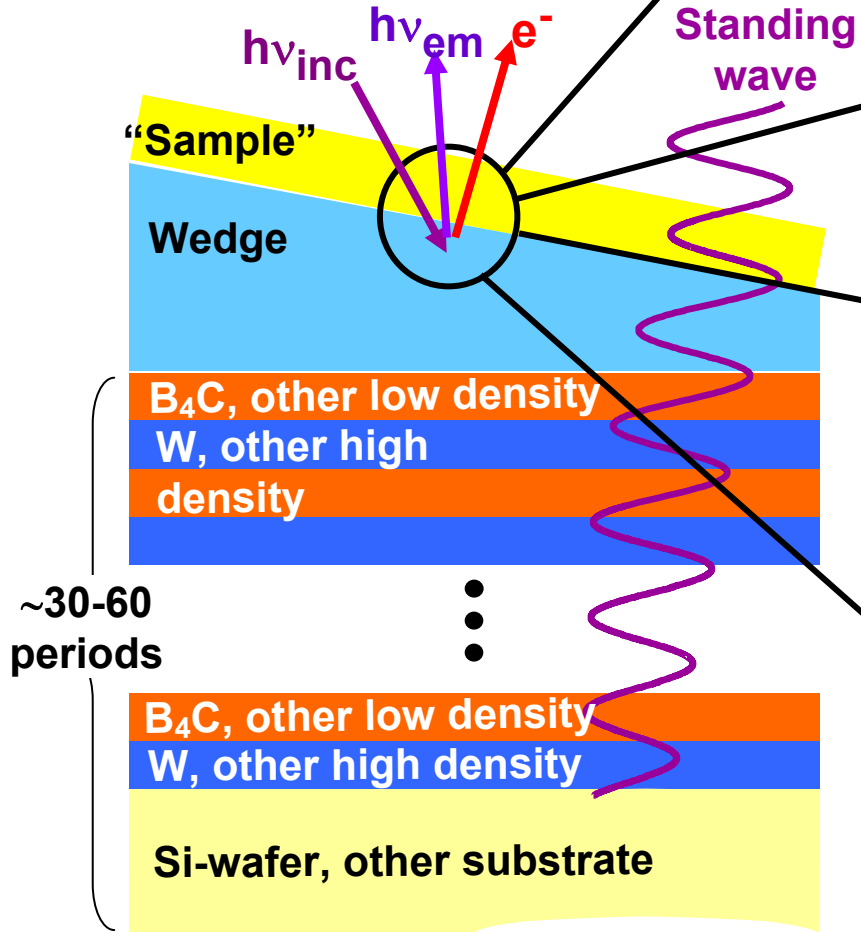
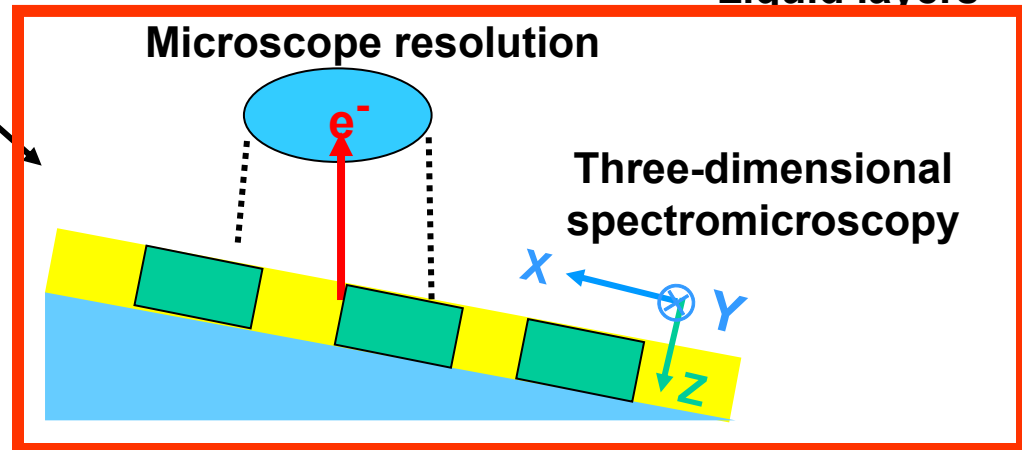
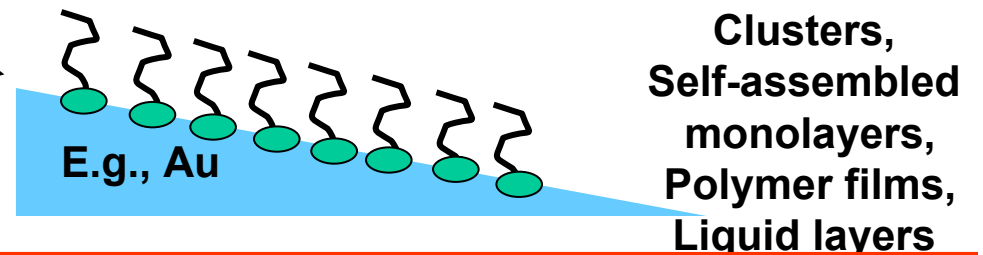
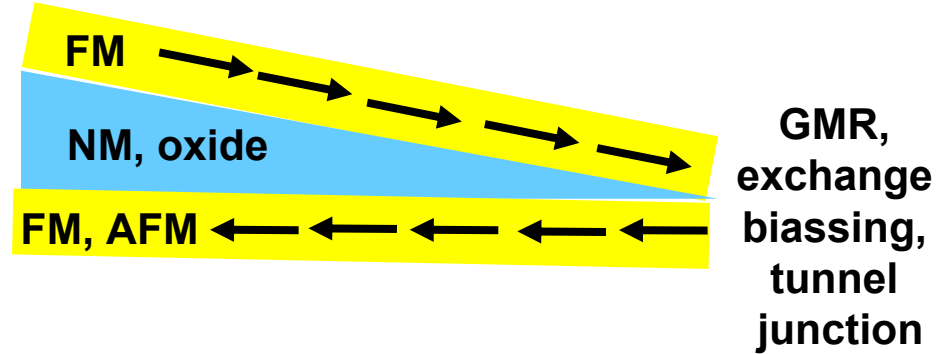
Non-destructive, depth-resolved det'n. of composition and magnetization profiles from standing-wave excited photoemission





# Standing-Wave Excited Spectroscopy--Future Possibilities

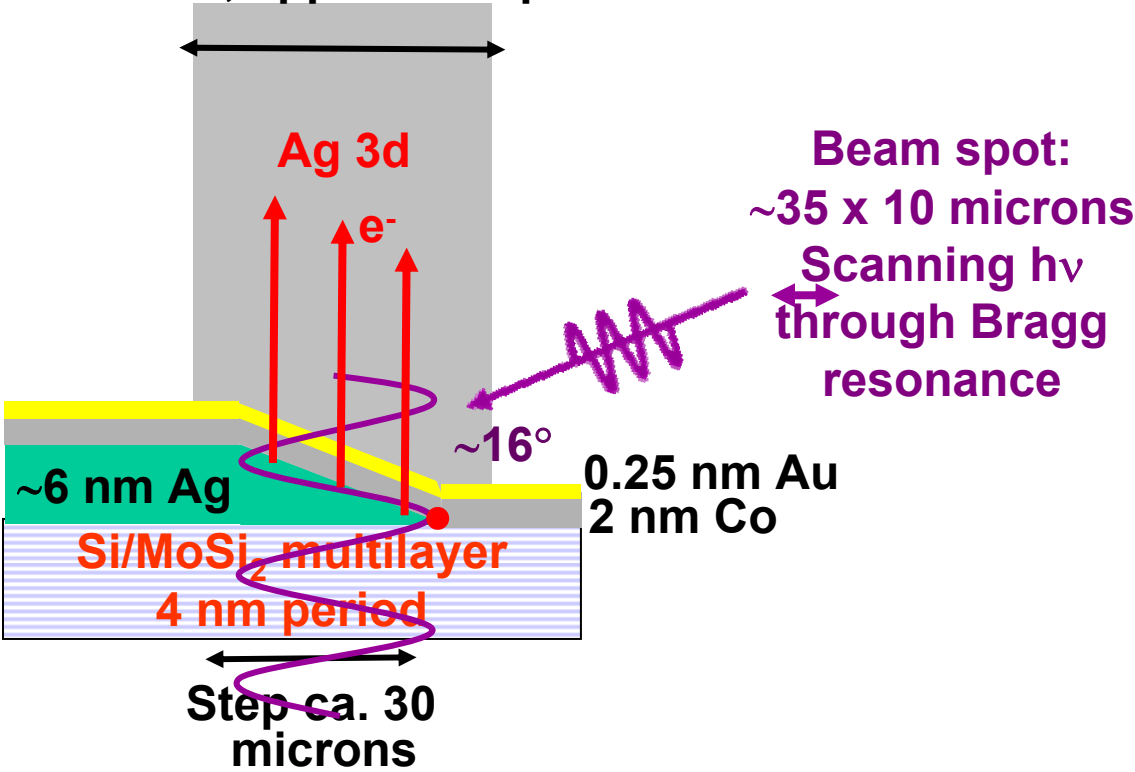
- Other material pairs in multilayer ( $B_4C/W$ ,  $Al_2O_3/Pt$ ,...) + epitaxial multilayers → epitaxial samples
- Smaller periods (to ~25-30 Å) → smaller SW period, better resolution
- Lower  $h\nu_{inc}$  → higher Bragg angles → perpend. component of M
- X-ray emission → deeper layers, more sensitivity to SW position



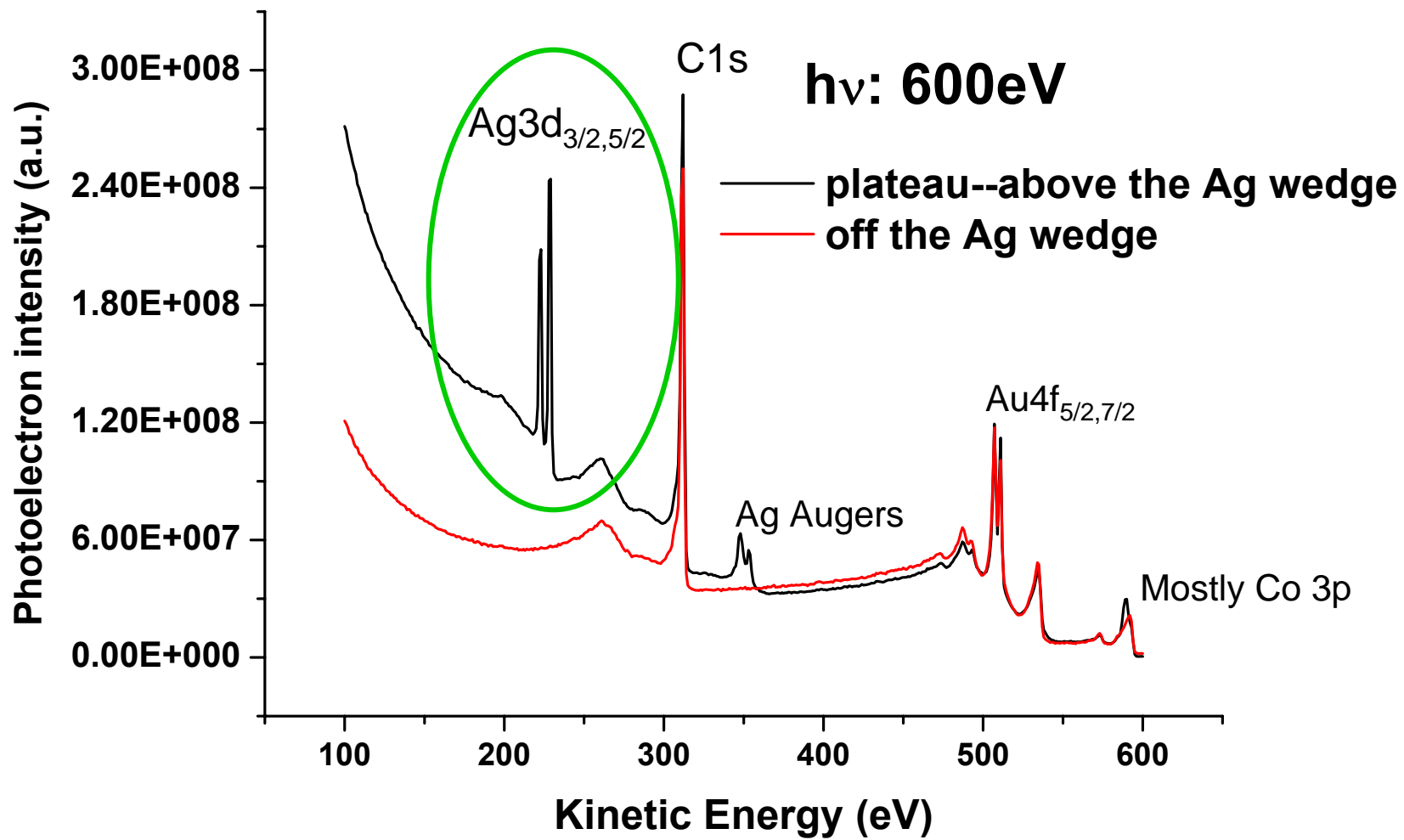
# First observation of standing wave effects in a photoelectron microscope

Elmitec SP-PEEM—BESSY, Berlin

Microscope field of view  
~50 microns, approx. 1-2 periods

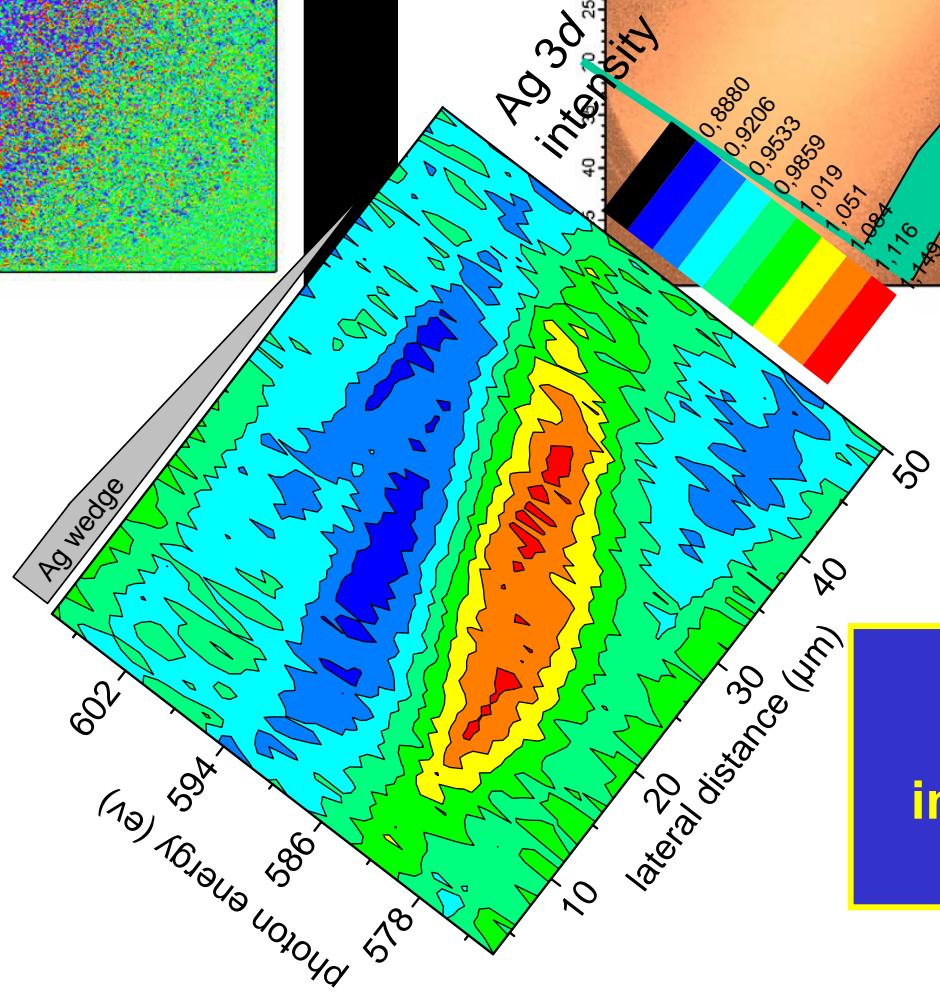
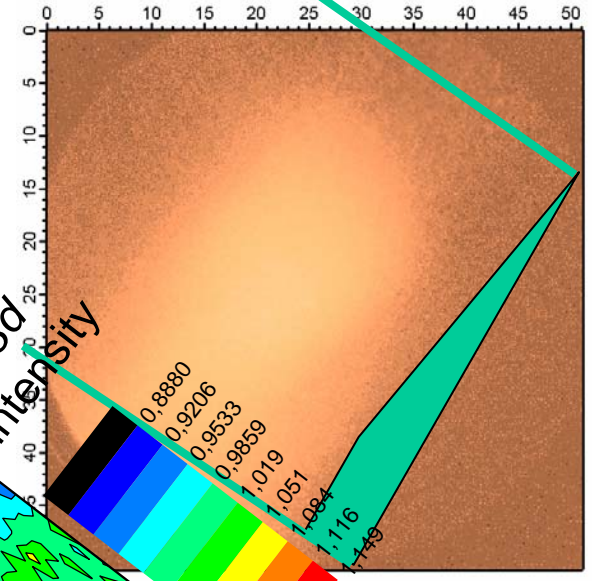
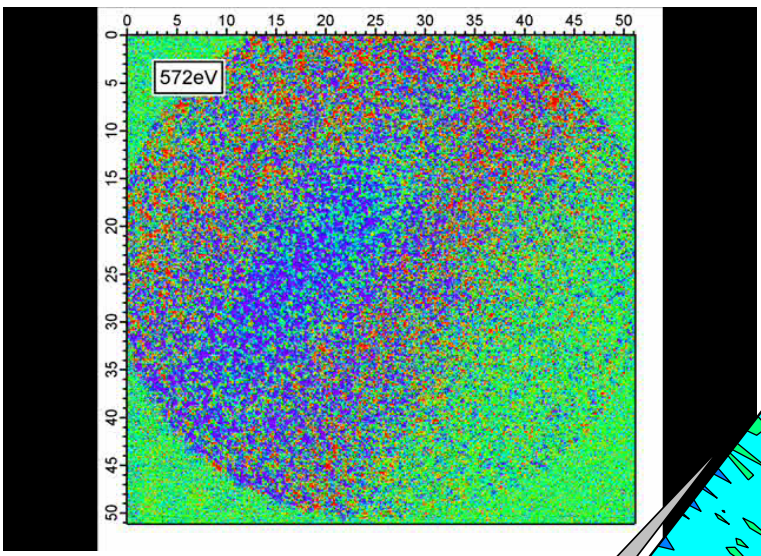


F. Kronast, H. Dürr, BESSY  
D. Buergler, R. Scheiber, C. Schneider, Jülich  
CF



Movie:  
Ag 3d intensity moving along the wedge  
while scanning over the Bragg energy

PEEM image of the Ag wedge  
(normalized Ag 3d intensity)



**Standing wave effects  
in a photoelectron  
microscope**

# Outline

**Surface, interface, and nanoscience—short introduction**

**Some surface concepts and techniques→photoemission**

**Synchrotron radiation: experimental aspects**

**Electronic structure—a brief review**

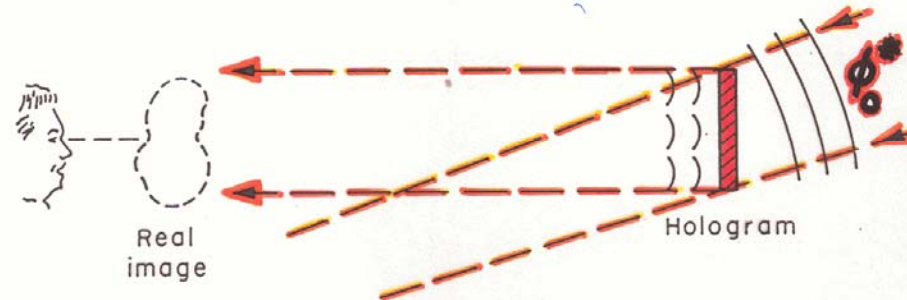
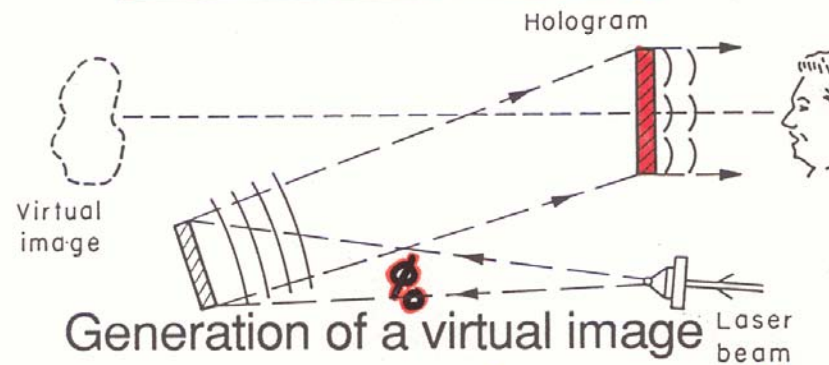
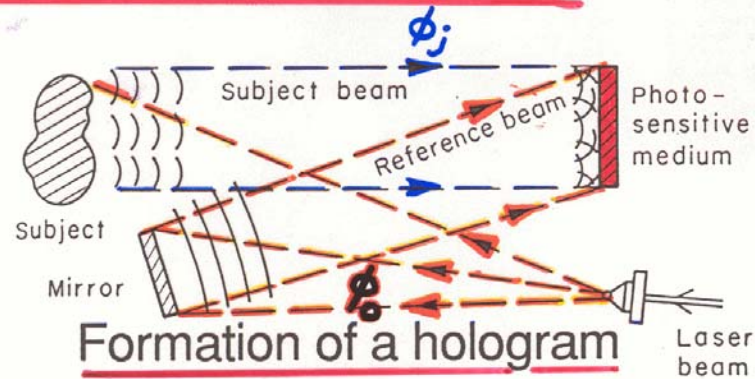
**The basic synchrotron radiation techniques:  
more experimental and theoretical details**

 **Core-level photoemission:  
photoelectron (and x-ray fluorescence) holography**

**Valence-level photoemission**

**Microscopy with photoemission**

## CLASSIC OPTICAL HOLOGRAPHY:



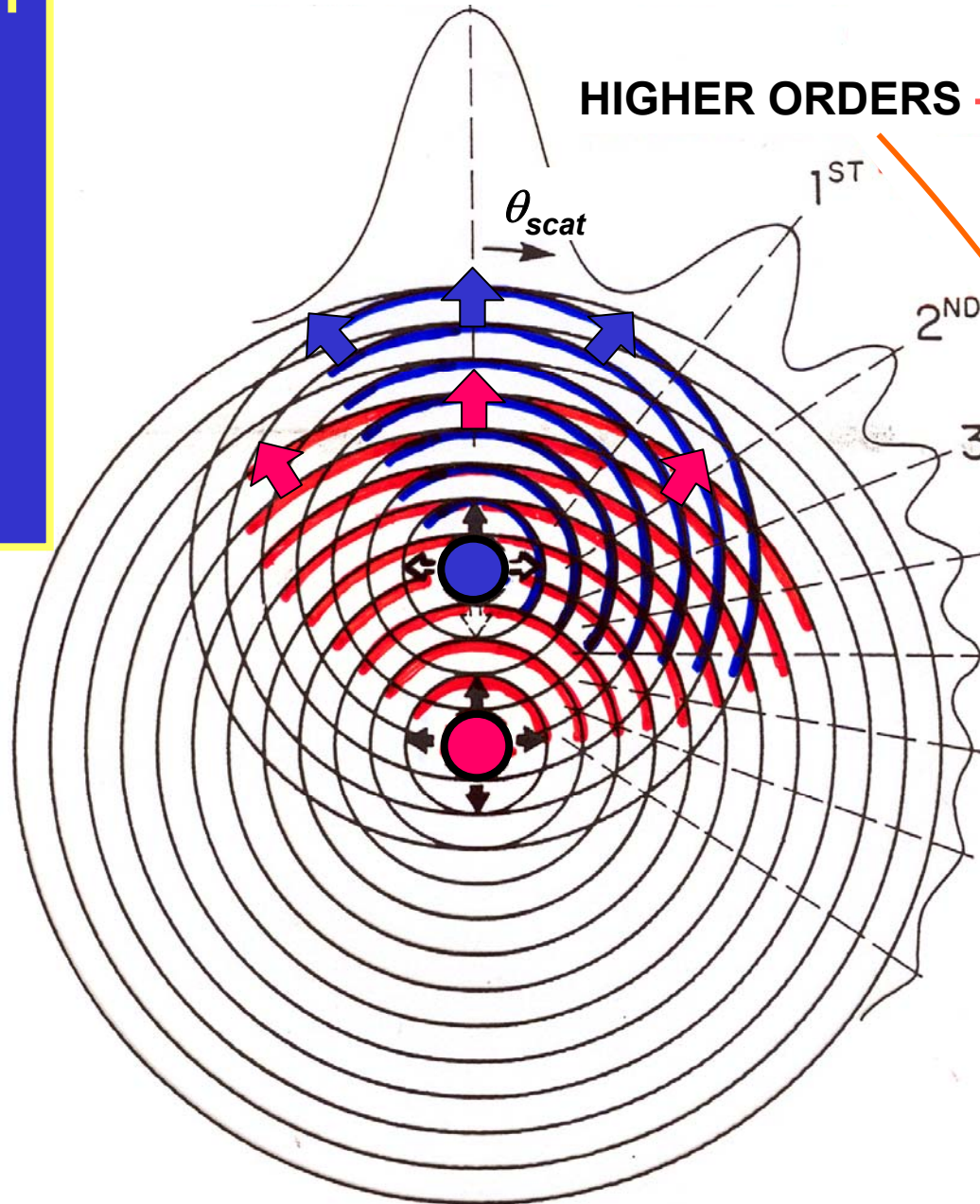
In electron emission holography, reference is outgoing spherical & conjugate is incoming spherical

Photoelectron  
diffraction →  
holography:  
Element-  
specific  
short-range  
atomic  
structure

FORWARD SCATT. = "0<sup>TH</sup> ORDER" → Bond & Low-Index  
Directions

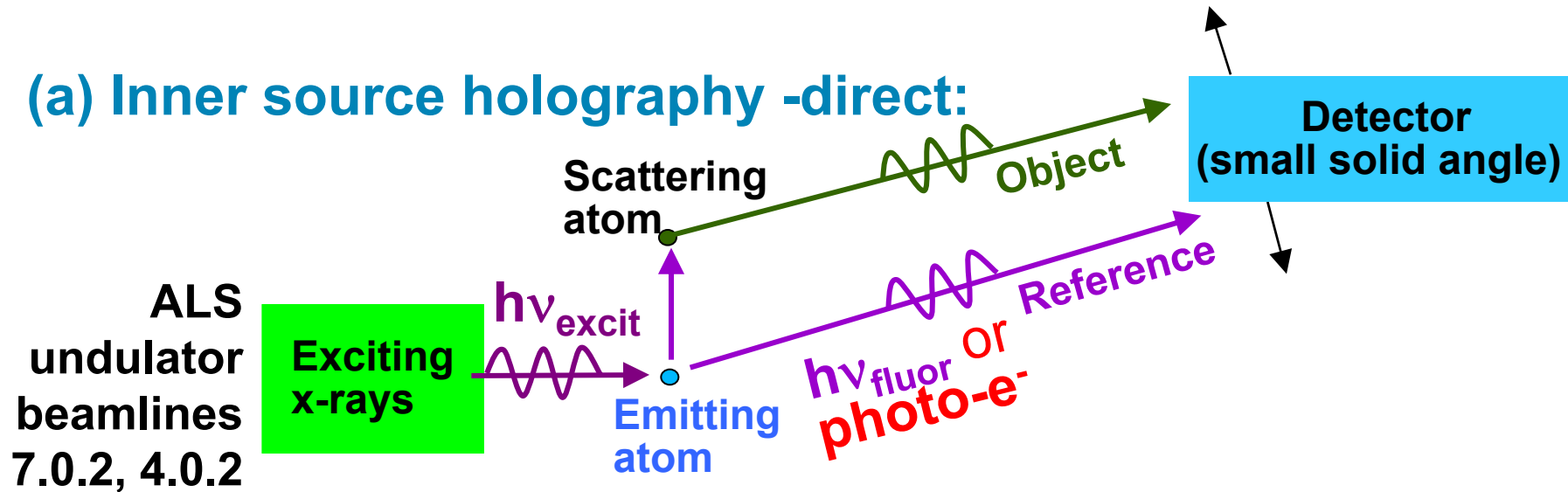
HIGHER ORDERS → Bond Lengths  
&  
Atomic  
Positions

→ Holographic  
fringes



Principles of **photoelectron** and **x-ray fluorescence** holography:

(a) Inner source holography -direct:



Recent overviews:

G. Faigel and M. Tegze, Rep. Prog. Phys. 62, 355 (1999)

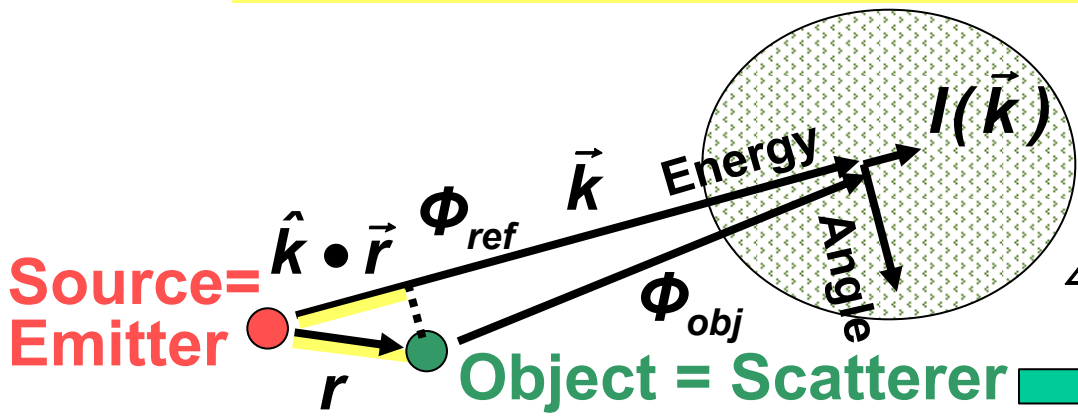
Adams et al., Phys. Stat. Sol. (b) 215, 757 (1999)

C.S.F., M.A Van Hove, et al., J. Phys. B Cond. Matt. 13, 10517 (2001)



# The basic imaging ideas

(Gabor; Helmholtz-Kirchoff; Wolf; Szöke; Barton-Tong)



$k = 2\pi/\lambda$   
 3D sampled region:  
 $\Delta k_x \times \Delta k_y \times \Delta k_z$

**Resolution:**  
 $\Delta x \approx 1/\Delta k_x$   
 $\Delta y \approx 1/\Delta k_y$   
 $\Delta z \approx 1/\Delta k_z$

Phase difference between  $\Phi_{ref}$  and  $\Phi_{obj} = \vec{k} \cdot \vec{r} - kr$

$$I(\vec{k}) = |\Phi_{ref}(\vec{k}) + \Phi_{obj}(\vec{k})|^2$$

**Holographic interference**

$$= |\Phi_{ref}(\vec{k})|^2 + \Phi_{ref}^*(\vec{k})\Phi_{obj}(\vec{k}) + \Phi_{ref}(\vec{k})\Phi_{obj}^*(\vec{k}) + |\Phi_{obj}(\vec{k})|^2$$

**Hologram:**  $\chi(\vec{k}) = \frac{I(\vec{k}) - I_0}{I_0} = \frac{I(\vec{k}) - |\Phi_{ref}(\vec{k})|^2}{|\Phi_{ref}(\vec{k})|^2}$

**Weak, ~isotropic scattering, no phase shift**

**Holographic image:**

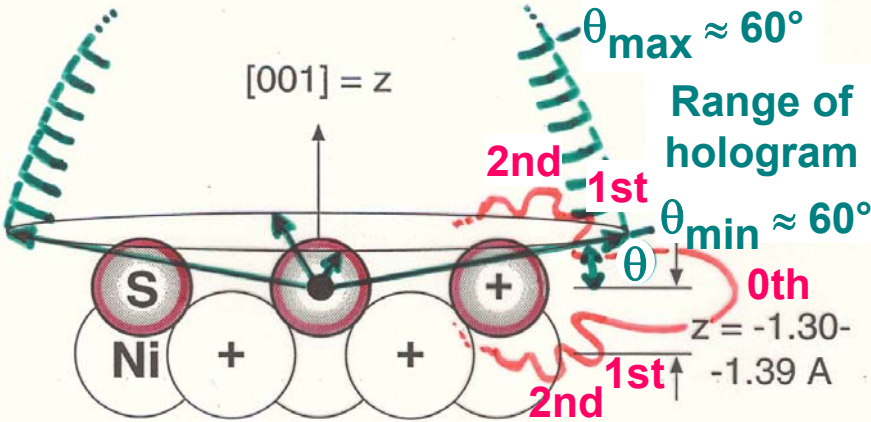
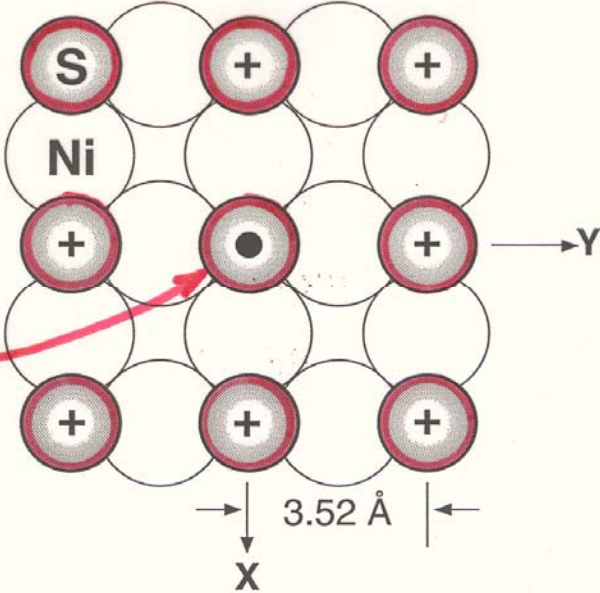
$$U(\vec{r}) = \left| \iiint \chi(\vec{k}) \exp[i\vec{k} \cdot \vec{r} - ikr] d^3k \right|$$

**(Usual phase problem)**

**Inside-source PH-  
first adsorbate:  
S/Ni(100)**

c(2x2)S on Ni(001)  
A Well-Defined Test Case

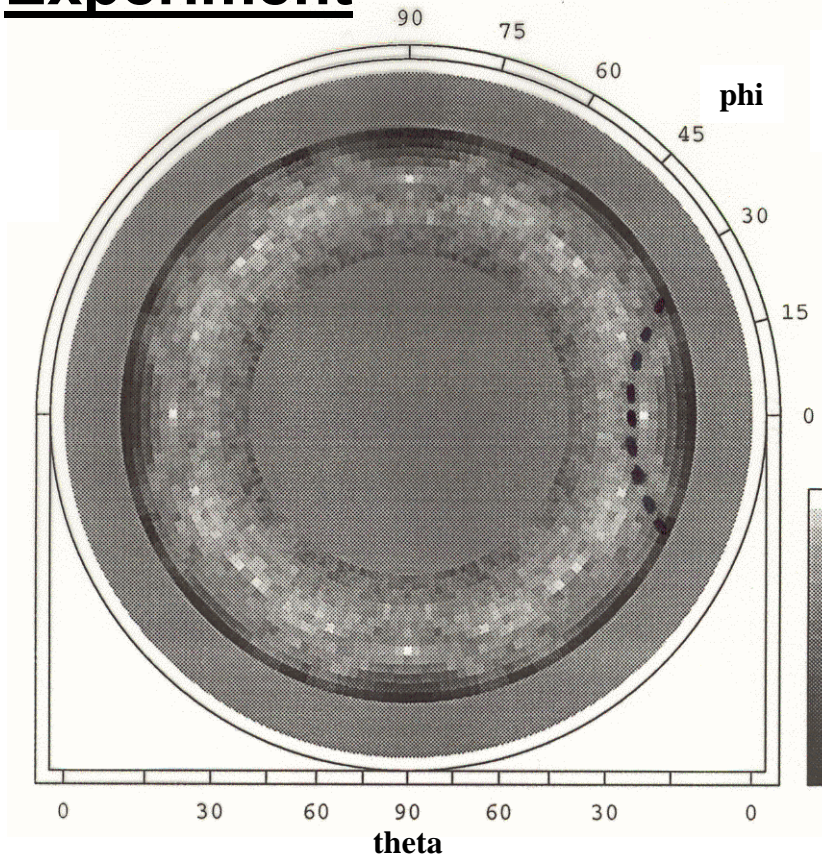
Typical S emitter  
 $h\nu = 1486.6 \text{ eV} \rightarrow$   
 $E_{\text{kin}} = 1327 \text{ eV}$



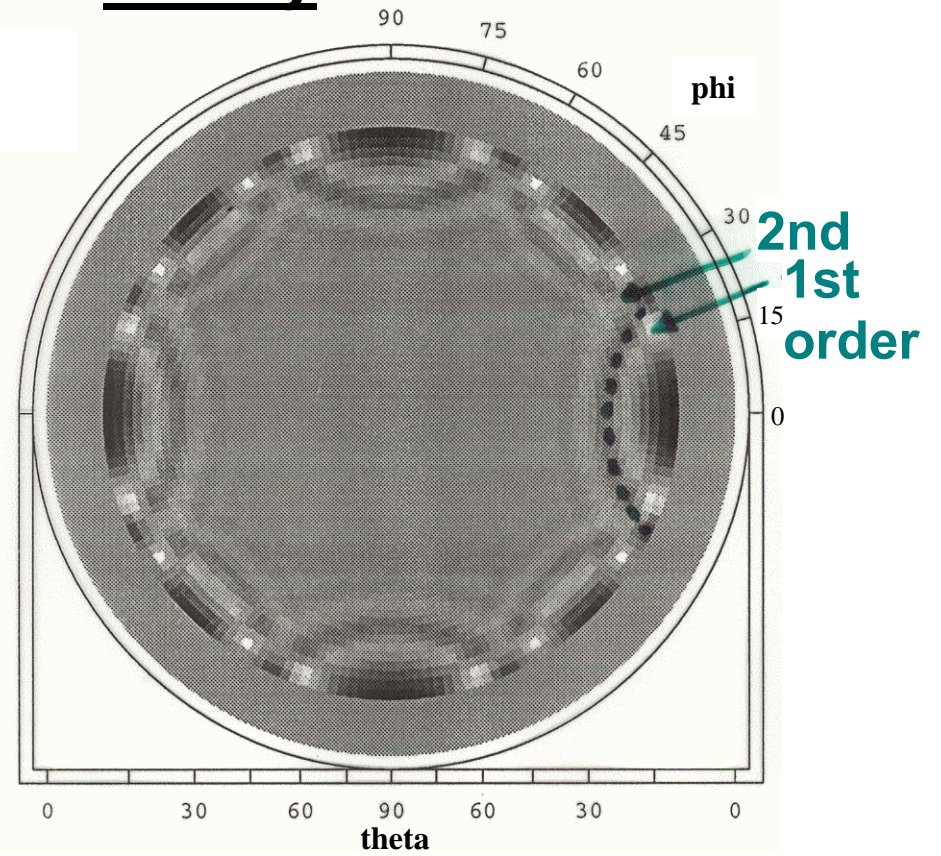
Thevuthasan et al.,  
 Phys. Rev. Lett. 70, 595 ('93)

# Holograms: S/Ni(001)

**Experiment**

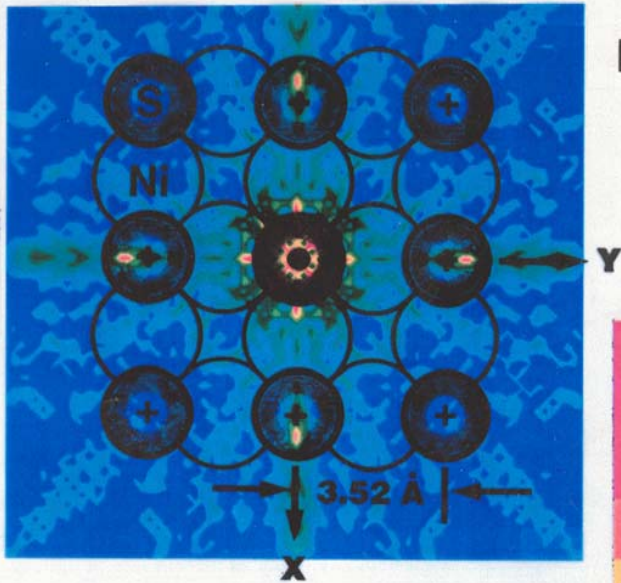


**Theory**

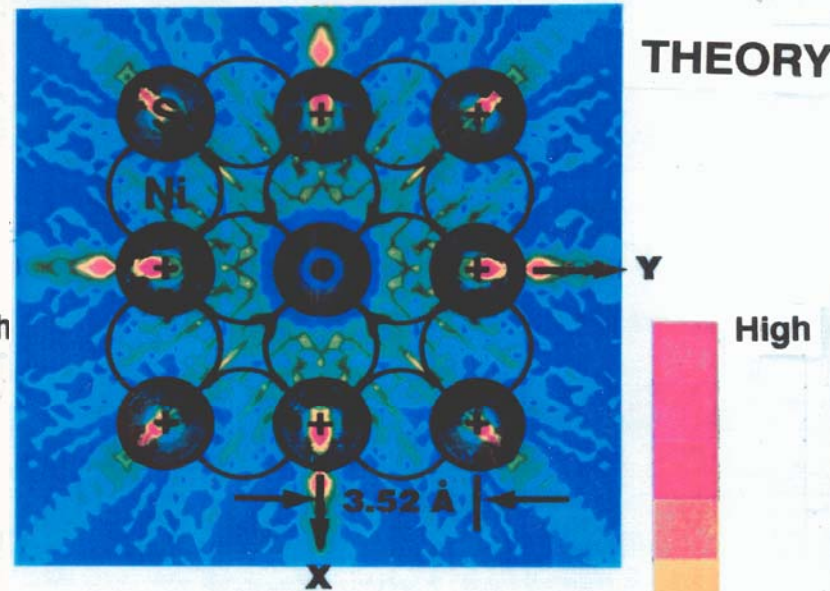


# Holographic Images: S/Ni(001)

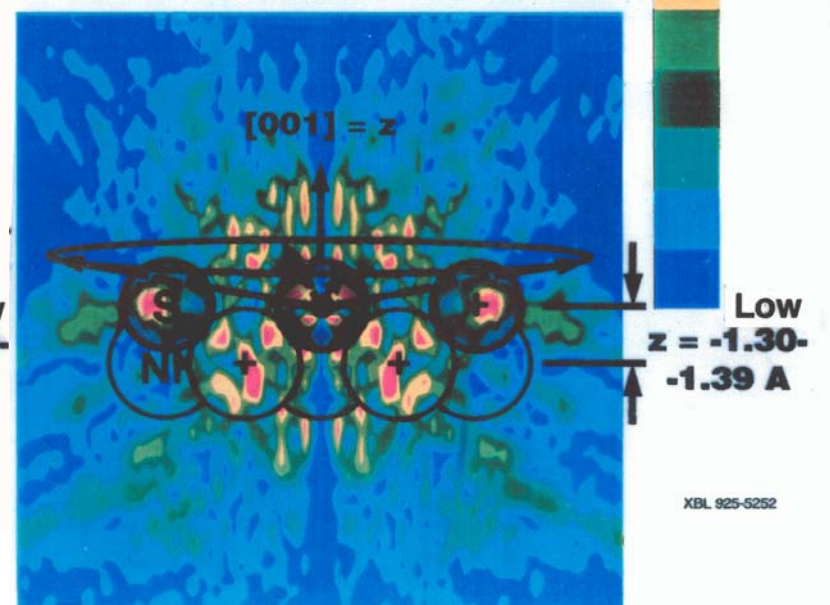
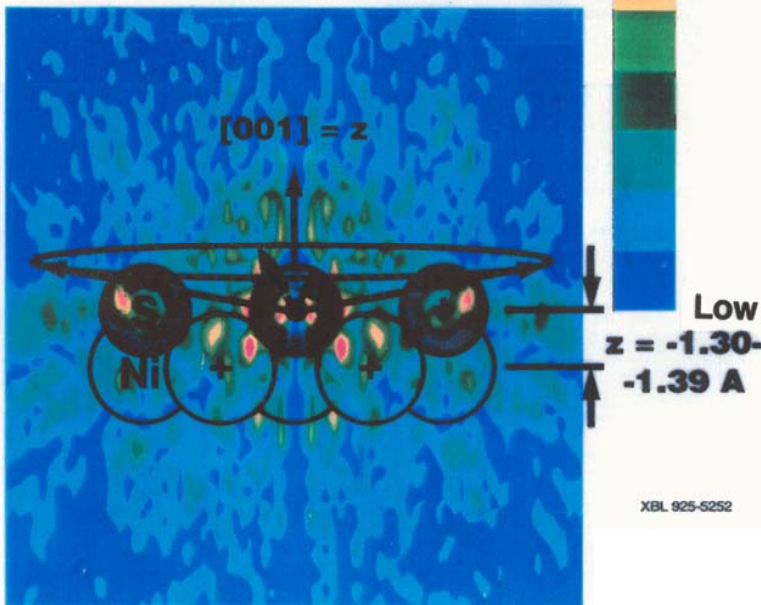
Fourier transform  
with scatt.  
wave correc.  
in sulfur(xy)  
plane



THEORY



Fourier transform  
with scatt.  
wave correc.  
in yz  
plane



Thevuthasan et al., Phys. Rev. Lett. 70, 595 ('93)

# Derivative photoelectron holography: As and Si emission from As/Si(111):

$$U(\vec{r}) = \left| \iiint \chi(\vec{k}) \exp[i\vec{k} \cdot \vec{r} - ikr] d^3 k \right|$$

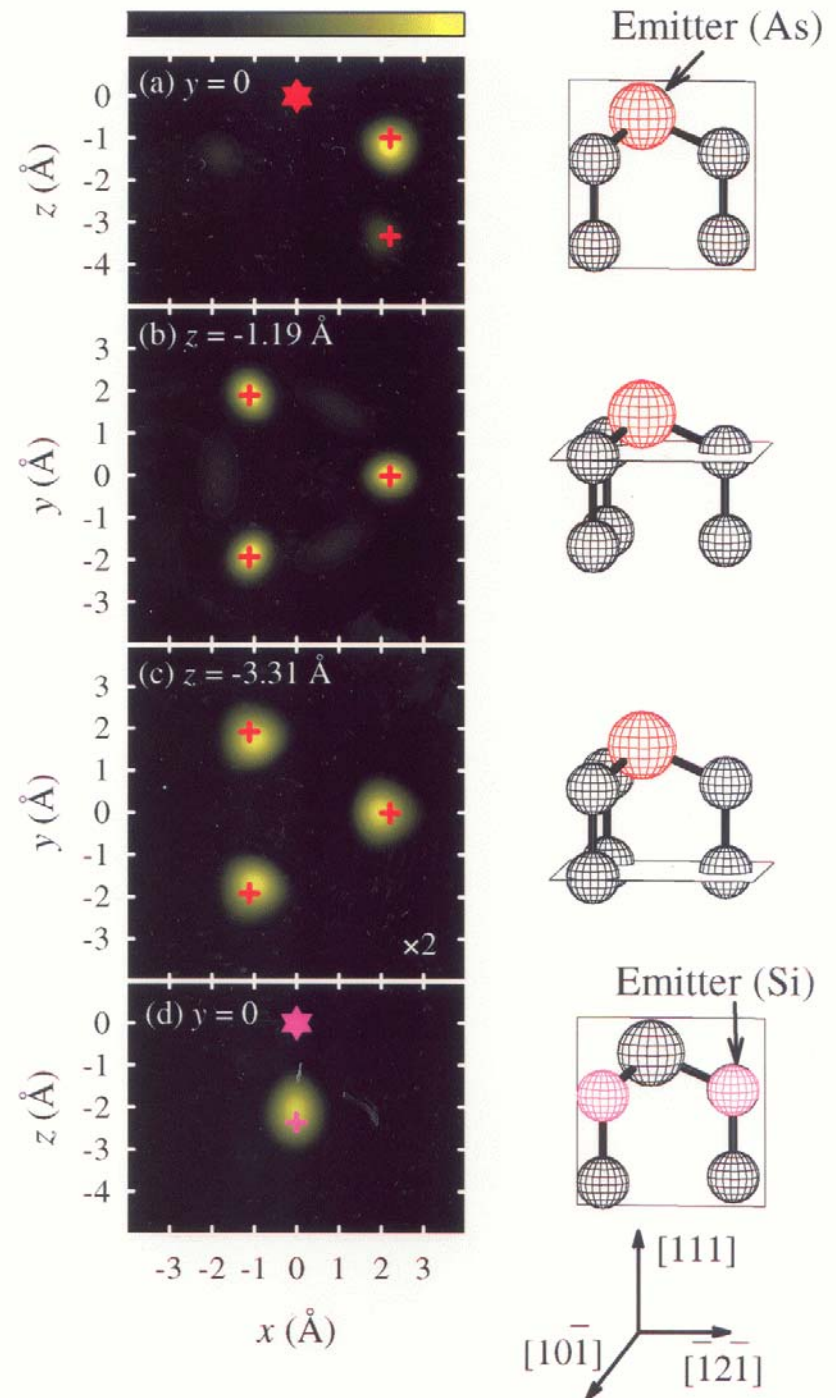
with  $\chi = \frac{I(\vec{k}) - I_0}{I_0}$

and  $I(\vec{k})$  from integration of log arithmetic derivative

$$L(h\nu, \hat{k}) = \frac{I(h\nu + \delta, \hat{k}) - I(h\nu - \delta, \hat{k})}{[I(h\nu + \delta, \hat{k}) + I(h\nu - \delta, \hat{k})] \delta}$$

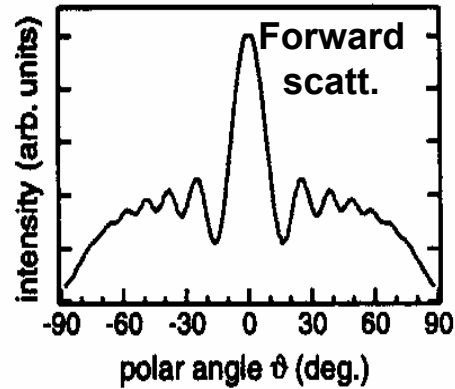
$$I(\vec{k}) \equiv I(k, \hat{k}) = A \int L(h\nu, \hat{k}) d^3 k$$

Luh, Miller, Chiang, PRL  
81, 4160 (1998)

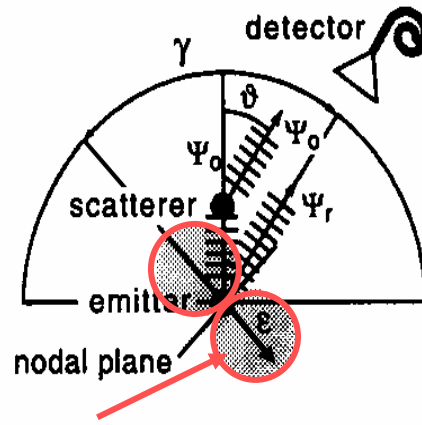
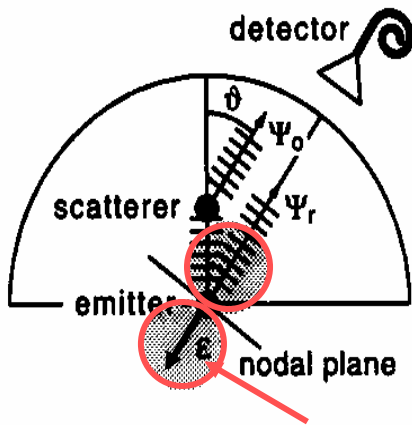
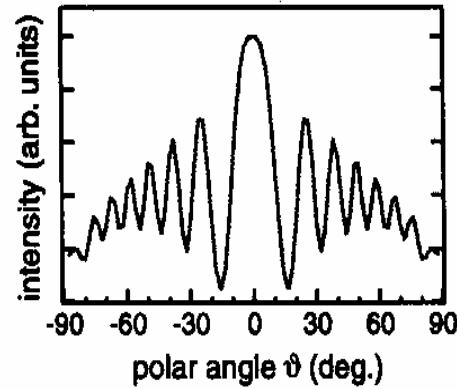


# Single-atom holograms

a) far node geometry ( $\gamma = 0^\circ$ )



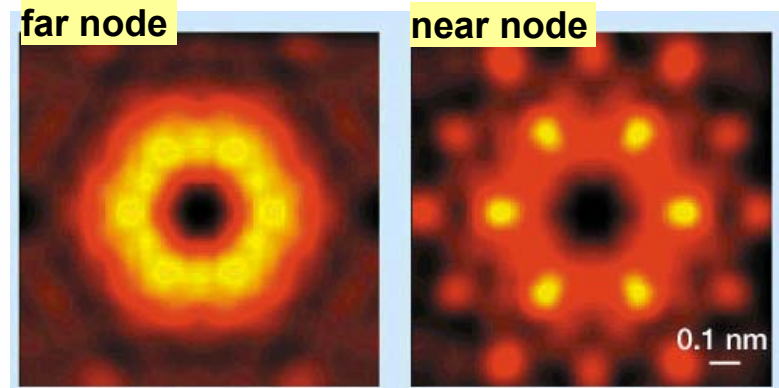
b) near node geometry ( $\gamma = 80^\circ$ )



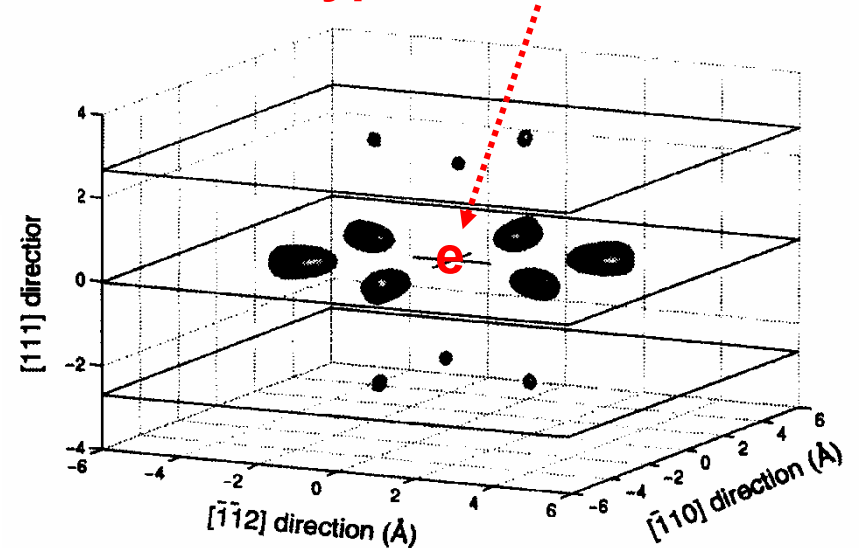
$$M(\vec{k}, \vec{r}) \propto \sqrt{\text{photoe}^- \text{ cross sec.}} \\ = \hat{\epsilon} \cdot \hat{k}$$

Wider et al. PRL  
86, 2337 (2001)

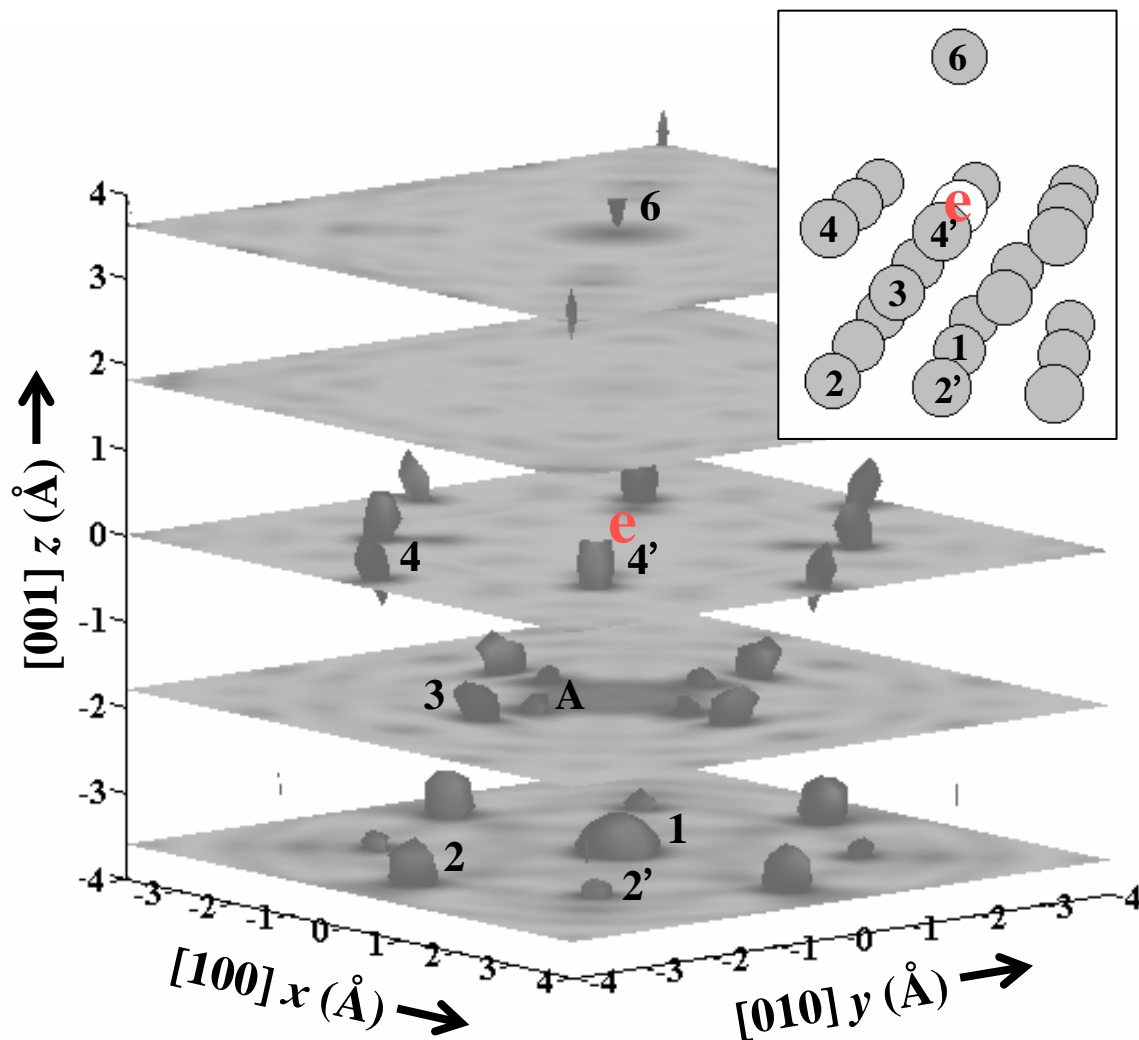
# Near-node photoelectron holography: Al 2s emission from Al(111)



Images around typical Al emitter



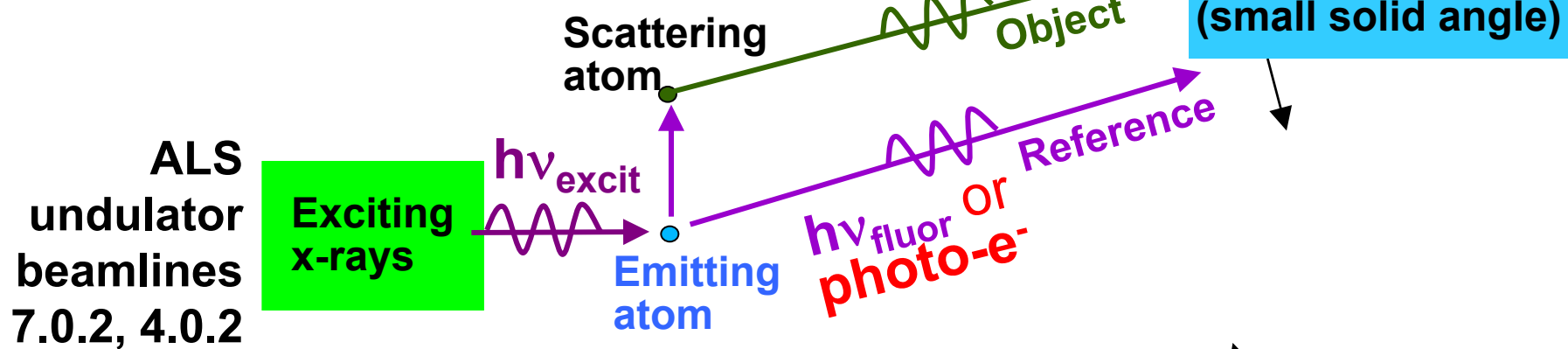
**Cu 3p-Cu(001)--  
differential  
photoelectron  
holography**



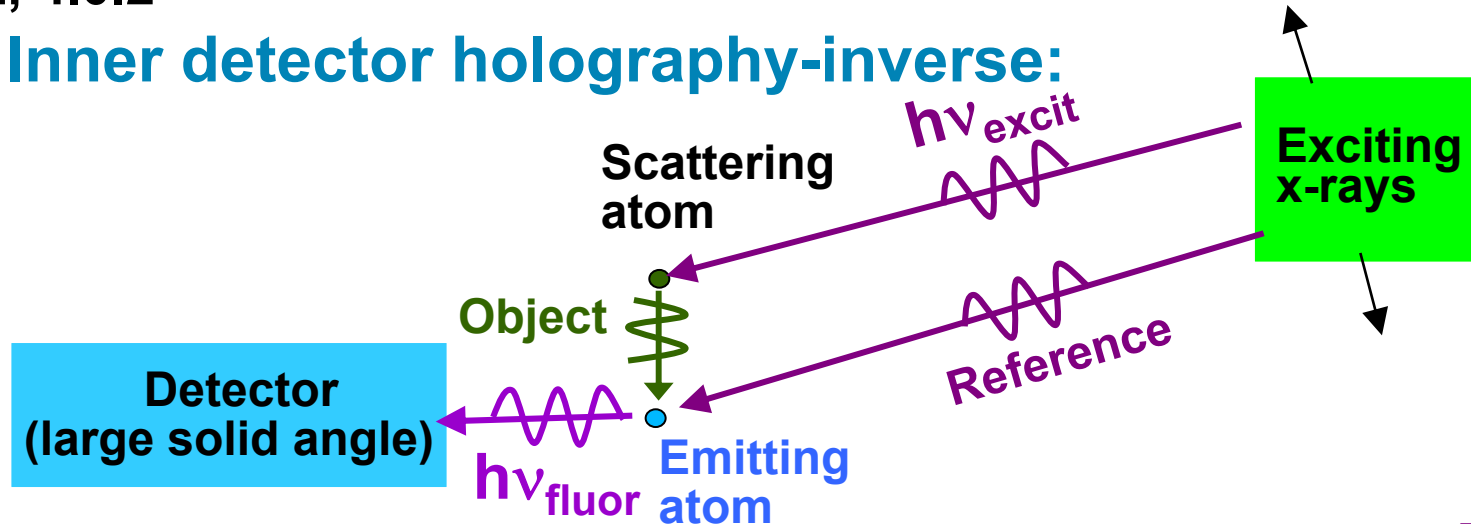
Imaging of back, side, (and fwd.) scattering atoms  
(Omori et al., PRL 88, 055504 ('02) and  
animations at <http://electron.lbl.gov/marchesini/dph>)

Principles of **photoelectron** and **x-ray fluorescence** holography:

**(a) Inner source holography -direct:**



**(b) Inner detector holography-inverse:**



Recent overviews:

G. Faigel and M. Tegze, Rep. Prog. Phys. 62, 355 (1999)

Adams et al., Phys. Stat. Sol. (b) 215, 757 (1999)

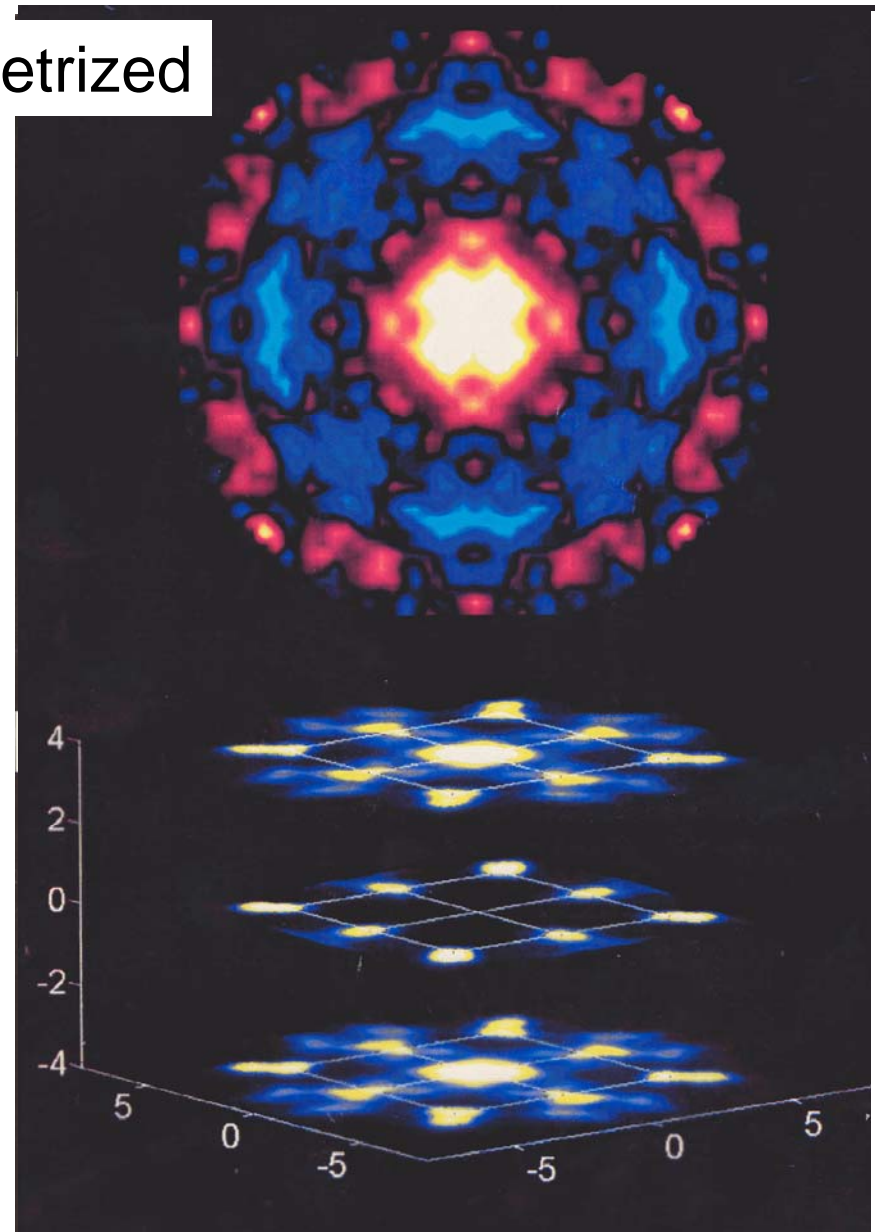
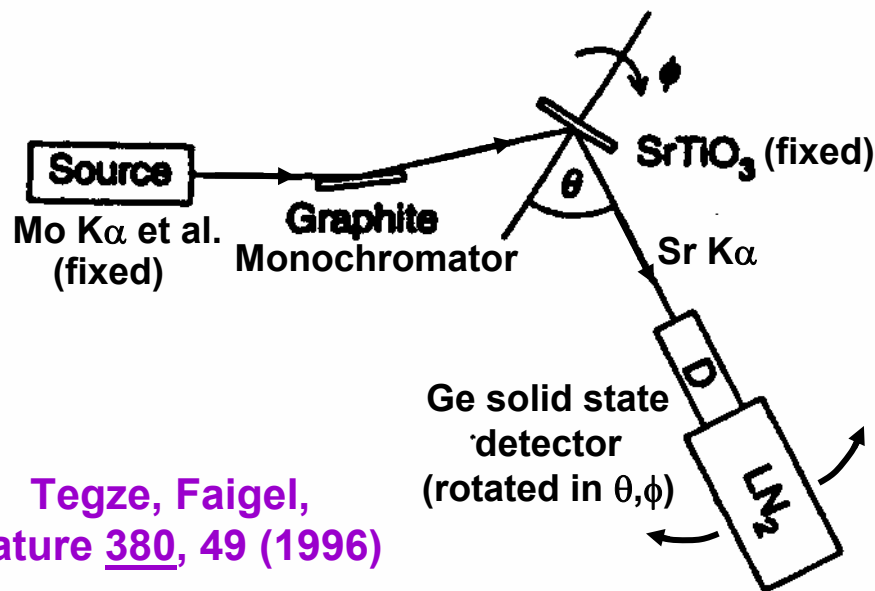
C.S.F., M.A Van Hove, et al., J. Phys. B Cond. Matt. 13, 10517 (2001)



# Inside-source XFH--the first experiment:

SrTiO<sub>3</sub> (100) sample  
Mo x-ray tube  
Excitation of Sr K $\alpha$   
@ 14.1 keV with  
Mo K $\alpha$  @ 17.4 keV  
Approx. 2 months  
data accumulation  
10<sup>10</sup> photons counted  
over 2400 pixels in  $\theta$ ,  $\phi$

Symmetrized



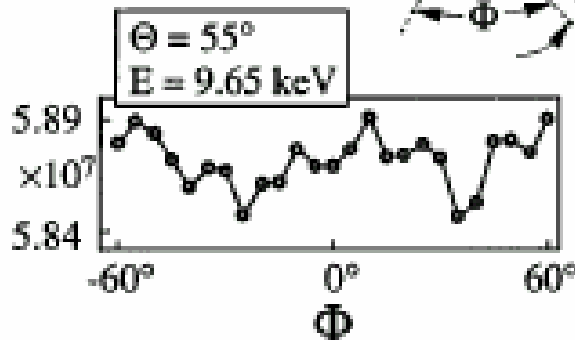
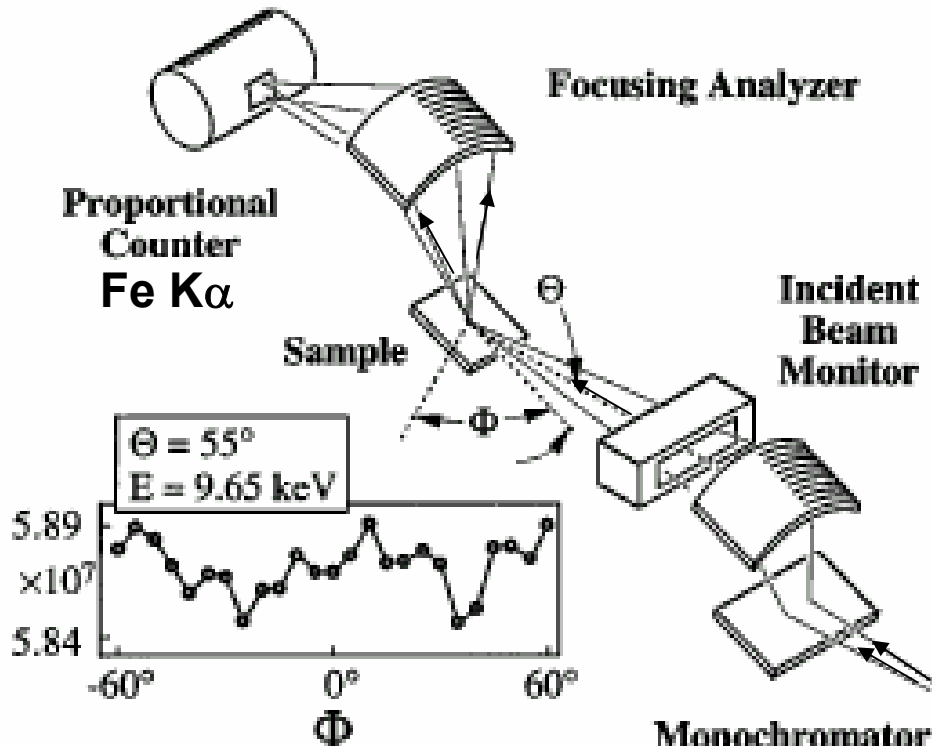
Tegze, Faigel,  
Nature 380, 49 (1996)

# Inside-detector XFH--the first experiment:

Can be multi-energy →  
“MEXH”

Resolution much worse  
in perpendicular plane:

$$\Delta k_x = \Delta k_y \gg \Delta k_z$$

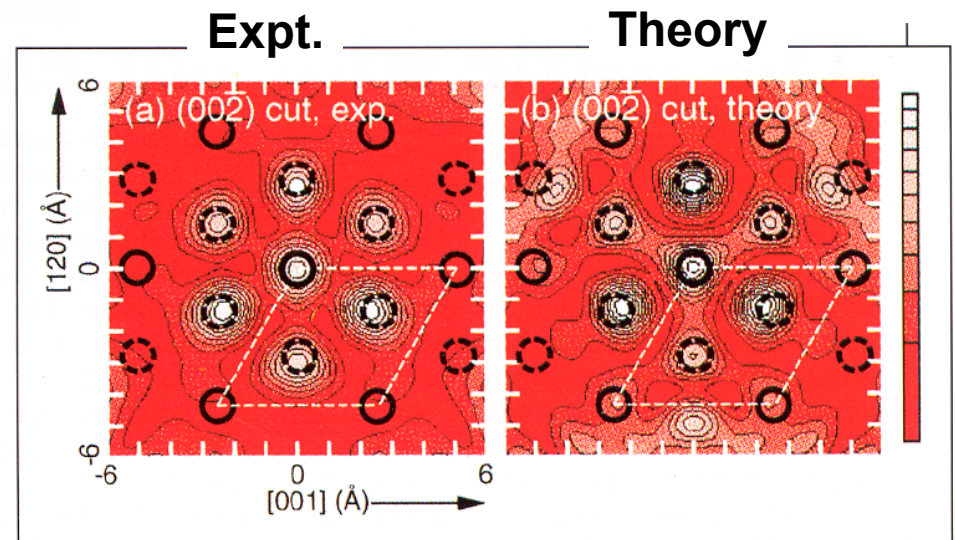


$$\frac{\Delta I}{I_0} \approx 0.5\%$$

Monochromator  
3 energies

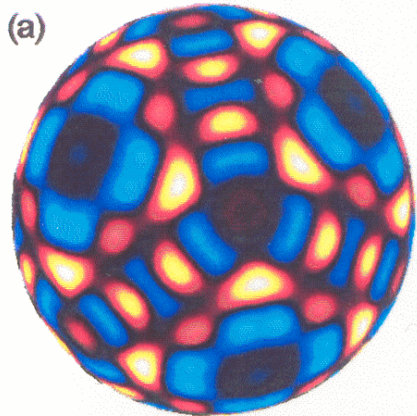
Images  
of  $\text{Fe}_2\text{O}_3$

Gog et al. PRL  
76, 3132 (1996)

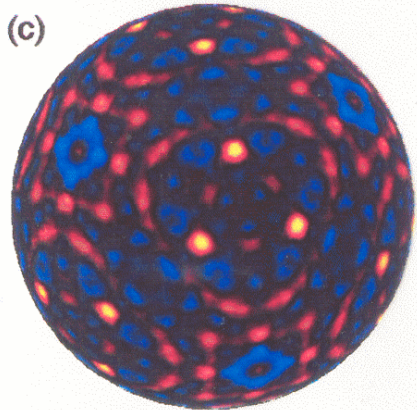
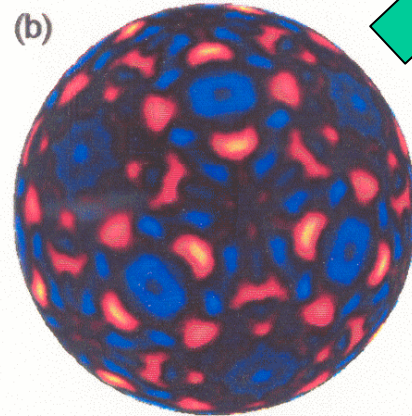


# XFH at ESRF: CoO(111)

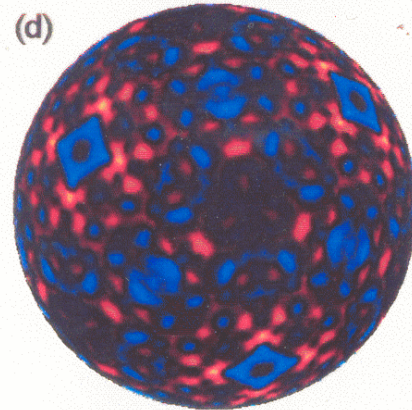
Inside source:  
 $h\nu = 6.92 \text{ keV}$



Inside detector:  
 $h\nu = 13.86 \text{ keV}$

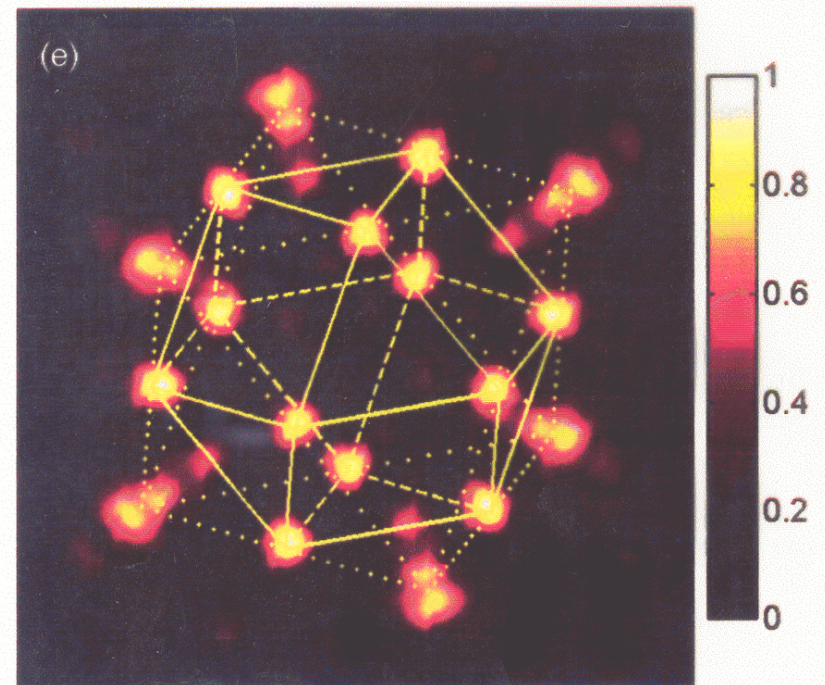


Inside detector:  
 $h\nu = 17.44 \text{ keV}$



Inside detector:  
 $h\nu = 18.92 \text{ keV}$

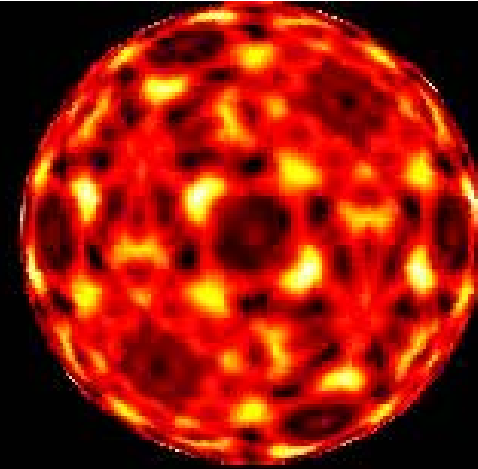
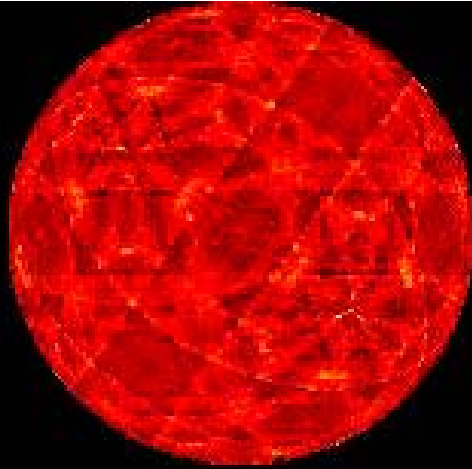
Multi-energy  
transform



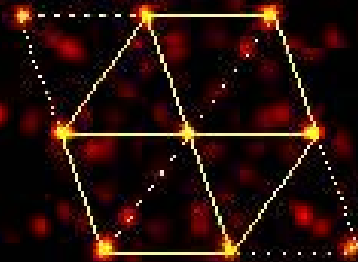
Tegze, Faigel, Marchesini et al.,  
Phys. Rev. Lett. 82, 4847 ('99)

# Multi-Energy Inside-Detector X-Ray Holography of NiO

Full hologram  
with Kossel lines



Smoothed hologram  
→ short-range structure



Ni and weaker O images

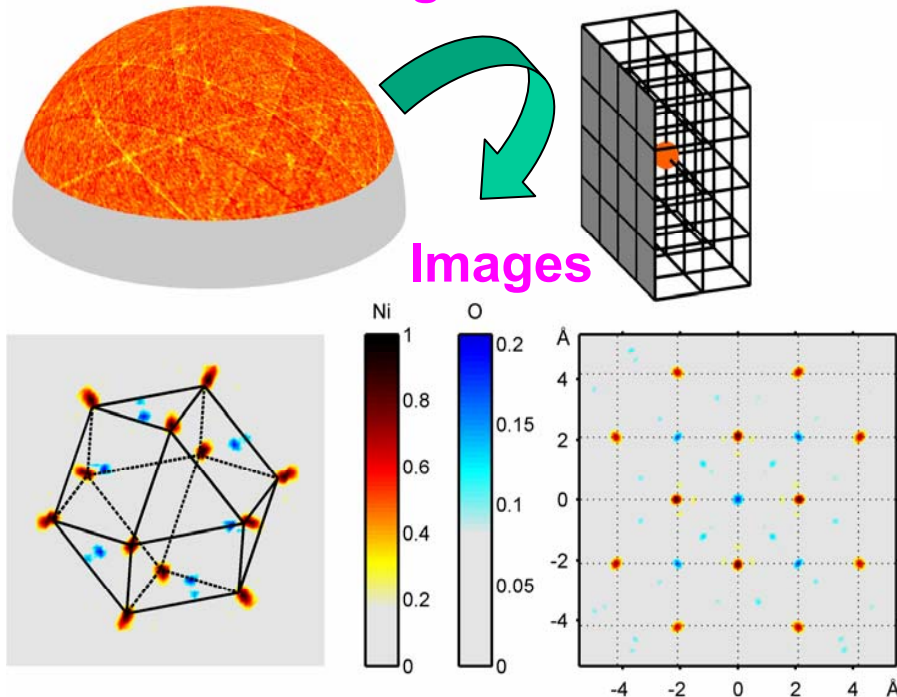
Marchesini et al.,  
Nature 407, 38 (2000)

# XFH at ESRF: some highlights

## Imaging light atoms: Nature 407, 38 (2000)

- O around Ni in NiO
- ~150 O and Ni atoms imaged

Inside detector-  
Ni  $K\alpha$  Hologram



## Imaging a quasicrystal: Phys. Rev. Lett. 85, 4723 (2000)

- method works without true periodicity
- neighbors around Mn in MnAlPd
- image of average atomic distribution

Inside detector-  
Mn  $K\alpha$  Hologram

